

PROJECT #3

Comp 482

Hrag Ayvazian

12/14/17

Hrag Ayvazian

```

/*****isStronglyConnected*****/
public boolean isStronglyConnected() {
    int[] p = new int[nVertices];
    for(int i = 0; i < nVertices; i++) {
        for(int j = 0; j < nVertices; j++) {
            p[j] = -1;
        }
        dfs(i,p);
        for(int j = 0; j < nVertices; j++) {
            if(p[j] == -1) {
                return false;
            }
        }
    }
    return true;
}

private void dfs(int s, int[] p) {
    for(int i = 0; i < adjList[s].size(); i++) {
        if(p[adjList[s].get(i).vertex2] == -1) {
            p[adjList[s].get(i).vertex2] = s;
            dfs(adjList[s].get(i).vertex2, p);
        }
    }
}
}

```

For my isStronglyConnected I got a runtime analysis of $O(|V|^2 + |V| |E|)$. The way I got this runtime was by starting off at the isStronglyConnected method. Then looking at the next step in the isStronglyConnected method we see a for loop that loops the number of vertices which gives us a big O of $|V|$. After that we see another for loop that is nested inside the loop before giving us a time complexity of big $O(|V|^2)$. Once that nested for loop is done I choose to use Depth First Search (DFS) and so I branch to the DFS method. In the DFS method I had a for loop that checks the number of edges on each vertex so the time complexity of this will be big $O(|V| |E|)$. However, when we merge it back with the isStronglyConnected method we will get $V O(|V| |E|)$ and so when you distribute the V you'll get $O(|V|^2 + |V| |E|)$. After the DFS is done we have another for loop that loops around the number of vertices that will give us a time complexity of $O(|V|^2)$. Then we are done with the isStronglyConnected but we have to evaluate all of the time complexities we have and since we have $O(|V|^2)$ and $O(|V|^2 + |V| |E|)$ and since $O(|V|^2)$ is in $O(|V|^2 + |V| |E|)$ we have an overall time complexity of $O(|V|^2 + |V| |E|)$.

Graph.java

```
/*
 * Name: Hrag Ayvazian
 * Date: 12/7/2017
 * COMP 482
 * Project #3
 * */
import java.io.File;
import java.io.FileNotFoundException;
import java.util.*;

public class Graph {
    //-----
    private ArrayList<EdgeNode>[] adjList;
    private int nVertices;
    private int nEdges;
    private String fileName;

    public static void main (String[] args)
    {
        //A
        System.out.println("Instructor Testcase A");
        System.out.println("\nDijkstra Shortest Paths");
        Graph g1 = new Graph("inputA.txt");
        g1.printGraph();
        int start = 1;

        SPPacket spp = g1.dijkstraShortestPaths(start);
        System.out.println("\nPrint shortest paths from start
vertex = " + start);
        g1.printShortestPaths( spp );

        if( g1.isStronglyConnected())
            System.out.println( "\nGraph is strongly
connected");
        else
            System.out.println( "\nGraph is not strongly
connected");

        //B
        System.out.println("Instructor Testcase B");
        System.out.println("\nBellman Ford Shortest Paths");
        g1 = new Graph("inputB.txt");
        g1.printGraph();
    }
}
```

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        start = 0;

        spp = g1.bellmanFordShortestPaths(start);
        if( spp != null)
        {
            System.out.println("\nPrint shortest paths from
start vertex = " + start);
            g1.printShortestPaths( spp );
        }
        else
            System.out.println("Graph has a negative cycle");

        //C
        System.out.println("Instructor Testcase C");
        System.out.println("\nBFS Shortest paths Shortest
Paths");
        g1 = new Graph("inputC.txt");
        g1.printGraph();
        start = 5;

        spp = g1.bfsShortestPaths(start);
        System.out.println("\nPrint shortest paths from start
vertex = " + start);
        g1.printShortestPaths( spp );

        //D
        System.out.println("Instructor Testcase D");
        System.out.println("\nBellman Ford Shortest Paths");
        g1 = new Graph("inputD.txt");
        g1.printGraph();
        start = 0;

        spp = g1.bellmanFordShortestPaths(start);
        if( spp != null)
        {
            System.out.println("\nPrint shortest paths from
start vertex = " + start);
            g1.printShortestPaths( spp );
        }
        else
            System.out.println("\nGraph has a negative cycle");

        if( g1.isStronglyConnected())
            System.out.println( "\nGraph is strongly
connected");
        else
```

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```
        System.out.println( "\nGraph is not strongly
connected");

    } //end main

    /*****Constructor*****/
    public Graph(String inputFileName) {
        fileName = inputFileName;
        try {
            Scanner input = new Scanner(new File(fileName));
            nVertices = input.nextInt();
            adjList = new ArrayList[nVertices];
            nEdges = 0;
            for(int i = 0; i < nVertices; i++) {
                adjList[i] = new ArrayList<EdgeNode>();
            }
            while(input.hasNextInt()) {
                int v1 = input.nextInt();
                adjList[v1].add(new
EdgeNode(v1,input.nextInt(),input.nextInt()));
                nEdges++;
            }
        }
        catch(FileNotFoundException e) {}
    }

    /*****Print graph method*****/

    public void printGraph() {
        System.out.println("Graph: nVertices = " + nVertices + "
nEdges = " + nEdges);
        System.out.println("Adjacency Lists");
        for(int i = 0; i < nVertices; i++) {
            System.out.print("v = " + i + " ");
            System.out.println(adjList[i]);
        }
    }

    /*****BFS Shortest paths*****/
    public SPPacket bfsShortestPaths(int start) {
        int[] parent = new int[nVertices];
        int[] distance = new int[nVertices];
        boolean[] visited = new boolean[nVertices];
        int l = 0;
        Queue<Integer> visit = new PriorityQueue<>();
        for(int i = 0; i < nVertices; i++) {
```

```
        parent[i] = -1;
        distance[i] = Integer.MAX_VALUE;
        visited[i] = false;
    }
    visited[start] = true;
    distance[start] = 1;
    visit.add(start);
    while(!visit.isEmpty()) {
        int current = visit.remove();
        int numAdj = adjList[current].size();
        for(int i = 0; i < numAdj; i++) {
            int dest = adjList[current].get(i).vertex2;
            if(!visited[dest]) {
                visit.add(dest);
                visited[dest] = true;
                distance[dest] = distance[current] + 1;
                parent[dest] = current;
            }
        }
    }
    return new SPPacket(start, distance, parent);
}
```

```
    *****Dijkstra's Shortest Path
    Algorithm*****
    public SPPacket dijkstraShortestPaths(int start) {
        int[] parent = new int[nVertices];
        int[] distance = new int[nVertices];
        boolean[] visited = new boolean[nVertices];
        Queue<Integer> visit = new PriorityQueue<>();
        for(int i = 0; i < nVertices; i++) {
            parent[i] = -1;
            distance[i] = Integer.MAX_VALUE;
            visited[i] = false;
        }
        visited[start] = true;
        distance[start] = 0;
        visit.add(start);
        while(!visit.isEmpty()) {
            int current = visit.remove();
            int numAdj = adjList[current].size();
            for(int i = 0; i < numAdj; i++) {
                int dest = adjList[current].get(i).vertex2;
                if(!visited[dest]) {
                    visit.add(dest);
                    visited[dest] = true;
                }
            }
        }
    }
}
```

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        }
        if(distance[current] +
adjList[current].get(i).weight < distance[dest]) {
            distance[dest] = distance[current] +
adjList[current].get(i).weight;
            parent[dest] = current;
        }
    }
}
return new SPPacket(start, distance, parent);
}

/*****Bellman Ford Shortest
Paths*****/
public SPPacket bellmanFordShortestPaths(int start){
    int[] p = new int[nVertices];
    int[] d = new int[nVertices];
    EdgeNode[] edges = new EdgeNode[nEdges];
    int k = 0;
    for(int i = 0; i < nVertices; i++) {
        p[i] = -1;
        d[i] = Integer.MAX_VALUE;
        for(int j = 0; j < adjList[i].size(); j++) {
            edges[k] = adjList[i].get(j);
            k++;
        }
    }
    d[start] = 0;
    for(int i = 0; i < nVertices - 1; i++) {
        for(int j = 0; j < nEdges; j++) {
            if(d[edges[j].vertex1] + edges[j].weight <
d[edges[j].vertex2]) {
                d[edges[j].vertex2] = d[edges[j].vertex1] +
edges[j].weight;
                p[edges[j].vertex2] = edges[j].vertex1;
            }
        }
    }
    for(int j = 0; j < nEdges; j++) {
        if((long)d[edges[j].vertex1] + edges[j].weight <
(long)d[edges[j].vertex2]) {
            return null;
        }
    }
    return new SPPacket(start, d, p);
}
```

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```

    /*******Prints shortest
    paths*****/
    public void printShortestPaths(SPPacket spp) {
        System.out.println(spp);
    }

    /*******isStronglyConnected*****/
    /
    public boolean isStronglyConnected() {
        int[] p = new int[nVertices];
        for(int i = 0; i < nVertices; i++) {
            for(int j = 0; j < nVertices; j++) {
                p[j] = -1;
            }
            dfs(i,p);
            for(int j = 0; j < nVertices; j++) {
                if(p[j] == -1) {
                    return false;
                }
            }
        }
        return true;
    }

    private void dfs(int s, int[] p) {
        for(int i = 0; i < adjList[s].size(); i++) {
            if(p[adjList[s].get(i).vertex2] == -1) {
                p[adjList[s].get(i).vertex2] = s;
                dfs(adjList[s].get(i).vertex2, p);
            }
        }
    }
}
} //end Graph class

/***/
class EdgeNode {
    int vertex1;
    int vertex2;
    int weight;
    public EdgeNode(int v1, int v2, int w) {
        vertex1 = v1;
        vertex2 = v2;
        weight = w;
    }
}
```


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```
        public String toString() {
            return "(" + vertex1 + "," + vertex2 + "," + weight +
        ");";
        }

    }

}

/*****
class SPPacket {
    int[] d;//distance array
    int[] parent;//parent path array
    int source;//source vertex
    public SPPacket(int start, int[] dist, int[] pp) {
        source = start;
        d = dist;
        parent = pp;
    }
    public int[] getDistance() {
        return d;
    }

    public int[] getParent() {
        return parent;
    }

    public int getSource() {
        return source;
    }
    public String toString() {
        String str = "";
        str += ("Shortest Paths from vertex " + source + " to
vertex\n");
        for(int i = 0; i < parent.length; i++) {
            str += (i + ": ");
            String s = "";
            int p = i;
            if(p != source) {
                while(parent[p] != -1) {
                    s = parent[p] + "," + s;
                    p = parent[p];
                }
            }
            str += s;
            str += i;
            str += ("] Path Weight = " + d[i] + "\n");
        }
    }
}
```

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```
        return str;  
    }  
}
```

Test Case

Instructor Testcase A

Dijkstra Shortest Paths

Graph: nVertices = 5 nEdges = 9

Adjacency Lists

v = 0 [(0,1,1), (0,2,1)]

v = 1 [(1,0,2), (1,3,5)]

v = 2 [(2,0,7), (2,4,3)]

v = 3 [(3,2,6), (3,4,4)]

v = 4 [(4,1,3)]

Print shortest paths from start vertex = 1

Shortest Paths from vertex 1 to vertex

0: [1,0] Path Weight = 2

1: [1] Path Weight = 0

2: [1,0,2] Path Weight = 3

3: [1,3] Path Weight = 5

4: [1,0,2,4] Path Weight = 6

Graph is strongly connected

Instructor Testcase B

Bellman Ford Shortest Paths

Graph: nVertices = 5 nEdges = 7

Adjacency Lists

v = 0 [(0,1,2), (0,4,4)]

v = 1 [(1,2,-1)]

v = 2 [(2,0,3), (2,3,1)]

v = 3 [(3,1,2)]

v = 4 [(4,3,-3)]

Print shortest paths from start vertex = 0

Shortest Paths from vertex 0 to vertex

0: [0] Path Weight = 0

1: [0,1] Path Weight = 2

2: [0,1,2] Path Weight = 1

3: [0,4,3] Path Weight = 1

4: [0,4] Path Weight = 4

Instructor Testcase C

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BFS Shortest paths Shortest Paths

Graph: nVertices = 6 nEdges = 10

Adjacency Lists

v = 0 [(0,1,1), (0,5,6)]

v = 1 [(1,2,1)]

v = 2 [(2,1,2), (2,4,1)]

v = 3 [(3,0,1), (3,4,1)]

v = 4 [(4,0,1), (4,5,4)]

v = 5 [(5,2,1)]

Print shortest paths from start vertex = 5

Shortest Paths from vertex 5 to vertex

0: [5,2,4,0] Path Weight = 3

1: [5,2,1] Path Weight = 2

2: [5,2] Path Weight = 1

3: [3] Path Weight = 2147483647

4: [5,2,4] Path Weight = 2

5: [5] Path Weight = 0

Instructor Testcase D

Bellman Ford Shortest Paths

Graph: nVertices = 6 nEdges = 7

Adjacency Lists

v = 0 [(0,5,-3)]

v = 1 [(1,2,2)]

v = 2 [(2,4,1), (2,0,1)]

v = 3 [(3,5,2)]

v = 4 [(4,0,-3)]

v = 5 [(5,1,1)]

Graph has a negative cycle

Graph is not strongly connected