

# DUNE: Nuclear Reactor Point Kinetics Simulator

Comprehensive Technical Report and Code Analysis

An Educational Tool for University 1st Year Nuclear Engineering Students

**Course Code: NE-3206**

**Group Members:**

Hridoy Kabiraj (Roll: 14)

Aishik Chowdhury (Roll: 17)

Abrar Abdullah Diam (Roll: 56)

**Department of Nuclear Engineering**

**University of Dhaka**

GitHub Repository: <https://github.com/Hridoy-Kabiraj/DUNE>

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### **Abstract**

This comprehensive technical report presents a detailed analysis of the DUNE (Demonstrable Utility for Nuclear Education) project—a nuclear reactor point kinetics simulation system with an interactive GUI frontend and optional Arduino-driven 3D printed physical model integration. The project was developed as an educational tool to introduce University 1st year students to nuclear engineering concepts through hands-on simulation and visualization. This document provides an in-depth exploration of the theoretical foundations of reactor kinetics, detailed code walkthroughs with line-by-line annotations, architectural analysis, and implementation details. The simulation implements the six-group delayed neutron point kinetics equations coupled with thermal-hydraulic feedback and control rod dynamics, offering real-time visualization of reactor behavior including power transients, temperature evolution, and safety systems such as SCRAM protection. The Arduino integration provides tangible physical feedback through servo-controlled control rods and LED power indicators, bridging the gap between abstract nuclear physics concepts and observable physical phenomena.

# Contents

<b>1</b>	<b>Introduction</b>	<b>7</b>
1.1	Project Context and Motivation . . . . .	7
1.2	Problem Statement . . . . .	7
1.3	Intended Audience and Use Cases . . . . .	7
1.4	Key Features and Capabilities . . . . .	8
1.5	Document Organization . . . . .	8
<b>2</b>	<b>Repository Exploration</b>	<b>9</b>
2.1	Repository Structure Overview . . . . .	9
2.2	Core Python Modules . . . . .	9
2.2.1	reactorPhysics.py . . . . .	9
2.2.2	reactor.py . . . . .	10
2.2.3	legoReactor.py . . . . .	10
2.2.4	guiTemplate.py . . . . .	11
2.3	Arduino Integration . . . . .	11
2.3.1	reactorSketch.ino . . . . .	11
2.4	Package Configuration . . . . .	11
2.4.1	setup.py . . . . .	11
2.5	Documentation . . . . .	12
2.5.1	README.md . . . . .	12
<b>3</b>	<b>Theoretical Background: Nuclear Reactor Point Kinetics</b>	<b>12</b>
3.1	Introduction to Reactor Kinetics . . . . .	12
3.2	Neutron Population Dynamics . . . . .	12
3.2.1	The Neutron Life Cycle . . . . .	12
3.2.2	The Point Kinetics Approximation . . . . .	12
3.3	Point Kinetics Equations with Delayed Neutrons . . . . .	13
3.3.1	Physical Interpretation . . . . .	13
3.4	Delayed Neutron Data for U-235 . . . . .	13
3.5	Reactivity and Its Components . . . . .	14
3.5.1	Reactivity Units . . . . .	14
3.5.2	Reactivity Components in DUNE . . . . .	14
3.6	Thermal-Hydraulic Coupling . . . . .	15
3.6.1	Fuel Temperature . . . . .	15
3.6.2	Coolant Temperature . . . . .	15
3.6.3	Power Calculation . . . . .	15
3.7	Control Rod Dynamics . . . . .	16
3.8	Reactor SCRAM . . . . .	16
3.9	Xenon-135 Poisoning Dynamics . . . . .	16
3.9.1	Production and Removal Pathways . . . . .	16
3.9.2	Iodine-135 Balance Equation . . . . .	16
3.9.3	Xenon-135 Balance Equation . . . . .	17
3.9.4	Xenon Reactivity Contribution . . . . .	17
3.9.5	Total Reactivity with Xenon . . . . .	17
3.9.6	Physical Phenomena Modeled . . . . .	17
3.10	Samarium-149 Poisoning Dynamics . . . . .	18
3.10.1	Production and Removal Pathways . . . . .	18

3.10.2	Neodymium-149 Balance Equation	18
3.10.3	Promethium-149 Balance Equation	18
3.10.4	Samarium-149 Balance Equation	18
3.10.5	Samarium Reactivity Contribution	19
3.10.6	Total Reactivity with Both Poisons	19
3.10.7	Physical Phenomena Modeled	19
3.10.8	Comparison: Xenon-135 vs Samarium-149	19
3.11	Extended State Vector	19
3.12	Complete State Vector	19
<b>4</b>	<b>Detailed Code Walkthrough: reactorPhysics.py</b>	<b>20</b>
4.1	Module Header and Physical Constants	20
4.2	Reactivity Feedback Coefficient	21
4.3	Neutron Population Dynamics	22
4.4	Precursor Population Dynamics	22
4.5	Thermal Power Calculation	23
4.6	Fuel Temperature Dynamics	24
4.7	Coolant Temperature Dynamics	25
4.8	Control Rod Worth Functions	26
4.9	Total Reactivity Calculation	27
4.10	Complete Reactor System ODEs	27
<b>5</b>	<b>Reactor Control System: reactor.py</b>	<b>28</b>
5.1	LegoReactor Class Structure	28
5.2	Time Stepping and Integration	29
5.3	Pre-Step Control Logic	30
5.4	SCRAM Protection System	31
5.5	Manual Rod Control	31
5.6	PID Power Control	32
5.7	Coolant Flow Control	33
5.7.1	Dynamic Flow Rate Adjustment	33
5.7.2	Manual Coolant Control Mode	34
5.7.3	Gradual Flow Rate Ramping	34
5.8	Testing and Validation	35
<b>6</b>	<b>GUI Frontend: legoReactor.py</b>	<b>36</b>
6.1	GUI Architecture Overview	36
6.2	Main Application Class	36
6.3	Plot Initialization and Configuration	37
6.4	Real-Time Plotting	38
6.5	Event Handlers: User Interaction	39
6.6	Monitor Updates	40
6.7	CSV Data Logging System	41
6.7.1	CSV Initialization	41
6.7.2	Data Logging at Fixed Intervals	41
6.7.3	CSV File Closure on Exit	42
6.7.4	CSV Data Structure	42
6.8	Arduino Serial Communication	43
6.9	Serial Port Auto-Detection	44

6.10	Application Entry Point . . . . .	45
<b>7</b>	<b>Arduino Hardware Integration</b>	<b>46</b>
7.1	Arduino Sketch Overview . . . . .	46
7.1.1	Detailed Circuit Implementation with L298N Motor Driver . . . . .	47
7.2	Serial Command Processing . . . . .	47
7.2.1	Python-Arduino Communication for Coolant Control . . . . .	49
7.2.2	Integer Parsing from Serial . . . . .	49
7.3	Physical Model Integration . . . . .	50
<b>8</b>	<b>Mathematical Formulation and Numerical Methods</b>	<b>50</b>
8.1	System of ODEs . . . . .	50
8.2	Reactivity Functions . . . . .	51
8.2.1	Control Rod Worth . . . . .	51
8.2.2	Temperature Reactivity . . . . .	51
8.3	Numerical Integration Method . . . . .	51
8.3.1	LSODA Algorithm . . . . .	51
8.3.2	Why LSODA for Reactor Kinetics? . . . . .	52
8.4	Time Stepping Strategy . . . . .	52
8.5	Stability Analysis: Linearized System . . . . .	52
8.6	Power-Temperature Coupling . . . . .	53
8.6.1	Power Increase Scenario . . . . .	53
<b>9</b>	<b>Usage Examples and Operational Scenarios</b>	<b>53</b>
9.1	Installation and Setup . . . . .	53
9.1.1	Prerequisites . . . . .	53
9.1.2	Launching the Application . . . . .	53
9.2	Operational Scenarios . . . . .	54
9.2.1	Scenario 1: Reactor Startup from Cold Shutdown . . . . .	54
9.2.2	Scenario 2: Automatic Power Control . . . . .	54
9.2.3	Scenario 3: Reactivity-Initiated Accident (RIA) . . . . .	55
9.2.4	Scenario 4: Loss of Coolant Flow . . . . .	55
9.2.5	Scenario 5: Plot Zoom and Time History Analysis . . . . .	56
9.3	Arduino Hardware Demonstrations . . . . .	56
9.3.1	Visual Power Feedback . . . . .	56
9.3.2	Control Rod Motion . . . . .	56
9.3.3	SCRAM Indication . . . . .	56
9.3.4	Auditory Feedback from Coolant Pump . . . . .	56
9.4	Suggested Classroom Activities . . . . .	57
9.4.1	Activity 1: Find the Critical Rod Position . . . . .	57
9.4.2	Activity 2: Control System Challenge . . . . .	57
9.4.3	Activity 3: SCRAM Limit Investigation . . . . .	57
9.4.4	Activity 4: Transient Analysis . . . . .	57
<b>10</b>	<b>Conclusions and Future Enhancements</b>	<b>57</b>
10.1	Project Summary . . . . .	57
10.2	Key Accomplishments . . . . .	58
10.2.1	Technical Achievements . . . . .	58
10.2.2	Educational Impact . . . . .	58

10.3	Limitations of Current Implementation . . . . .	58
10.3.1	Physics Simplifications . . . . .	58
10.3.2	Control System Limitations . . . . .	59
10.4	Future Enhancement Opportunities . . . . .	59
10.4.1	Physics Improvements . . . . .	59
10.4.2	Software Enhancements . . . . .	60
10.4.3	Hardware Expansions . . . . .	61
10.4.4	Educational Curriculum Development . . . . .	61
10.5	Broader Impact . . . . .	61
10.5.1	STEM Education . . . . .	61
10.5.2	Cyber-Physical Systems in Engineering Education . . . . .	62
10.5.3	Public Understanding of Nuclear Energy . . . . .	62
10.5.4	Open-Source Community . . . . .	62
10.6	Project Heritage and Attribution . . . . .	62
10.7	Final Remarks . . . . .	63
	<b>Acknowledgements</b>	<b>63</b>
<b>A</b>	<b>Reactor Physics Equations Reference</b>	<b>64</b>
A.1	Point Kinetics Equations (Standard Form) . . . . .	64
A.2	Reactor Period . . . . .	64
A.3	Prompt Jump Approximation . . . . .	64
<b>B</b>	<b>Thermodynamic Properties</b>	<b>64</b>
B.1	UO <sub>2</sub> Fuel Properties . . . . .	64
B.2	Water/Steam Properties (at 15 MPa) . . . . .	64

# 1 Introduction

## 1.1 Project Context and Motivation

Nuclear energy represents one of the most powerful and complex technologies developed by humanity, yet public understanding of nuclear reactor physics remains limited and often clouded by misconceptions. The DUNE (Demonstrable Utility for Nuclear Education) project addresses this knowledge gap by providing an accessible, interactive educational tool that demystifies nuclear reactor operation through simulation and visualization.

The project emerged from the recognition that effective STEM education, particularly in nuclear engineering, requires hands-on experiences that bridge theoretical knowledge with observable phenomena. Traditional lecture-based approaches often fail to convey the dynamic, interconnected nature of reactor systems. DUNE solves this pedagogical challenge by implementing a scientifically accurate point kinetics reactor model with real-time graphical feedback and optional physical integration through Arduino-controlled 3D printed models.

## 1.2 Problem Statement

The core challenges addressed by this project include:

1. **Accessibility:** Making nuclear reactor physics accessible to University 1st year students with fundamental mathematical background.
2. **Engagement:** Creating an interactive experience that maintains student interest while conveying complex technical concepts.
3. **Safety Education:** Demonstrating reactor safety systems (particularly SCRAM protection) in a risk-free simulated environment.
4. **Physical Intuition:** Connecting abstract equations to tangible physical phenomena through Arduino-driven hardware feedback.
5. **Real-time Dynamics:** Illustrating the time-dependent behavior of reactor systems, including transients, control strategies, and feedback mechanisms.

## 1.3 Intended Audience and Use Cases

DUNE is designed for multiple audiences:

- **University 1st Year Students:** Primary target audience for educational demonstrations and interactive learning experiences in nuclear engineering courses.
- **Educators:** Science teachers seeking engaging tools for nuclear energy education and STEM outreach.
- **University Students:** Undergraduate nuclear engineering students learning reactor kinetics fundamentals.
- **Public Outreach:** Science fairs, open house events, and community education programs about nuclear technology.
- **Researchers:** As a platform for developing and testing educational methodologies in nuclear engineering education.

## 1.4 Key Features and Capabilities

The DUNE system provides:

- Real-time solution of six-group delayed neutron point kinetics equations
- **Xenon-135 and Samarium-149 poisoning dynamics** with complete decay chain modeling
- Coupled thermal-hydraulic modeling with fuel and coolant temperature tracking
- Interactive **full-screen GUI** with control rod manipulation and power level control
- Automatic reactor protection system (SCRAM) with configurable safety limits
- Dual control modes: manual control rod positioning and automatic power control (PID)
- **Four-panel live plotting:** reactor power, reactivity ( $\rho$ ), temperatures, and fission product poisons (Xe-135 & Sm-149)
- **Real-time monitoring displays:** Xenon-135 and Samarium-149 concentrations in scientific notation
- Optional Arduino integration for physical model control (servo motors, LED feedback)
- Temperature-dependent reactivity feedback modeling
- **Enhanced coolant system:** Multi-poison aware reactivity, burnout effects on poisoning
- Dynamic coolant flow rate adjustment based on reactor power (200–1200 kg/s)
- Manual coolant flow control mode with user-defined flow rates
- Automatic CSV data logging including Xenon, Samarium concentrations and reactivity traces
- Independent pump speed control via Arduino case 'c' command
- Real-time reactivity decomposition: temperature, rod position, Xenon, and Samarium contributions

## 1.5 Document Organization

This report is structured as follows:

- **Section 2:** Repository structure and file organization
- **Section 3:** Theoretical background on nuclear reactor point kinetics
- **Section 4:** Detailed code analysis of reactor physics module
- **Section 5:** Reactor control system implementation



- **Section 6:** GUI frontend architecture and implementation
- **Section 7:** Arduino integration for physical model control
- **Section 8:** Mathematical formulations and numerical methods
- **Section 9:** Usage examples and operational scenarios
- **Section 10:** Conclusions and future enhancements

## 2 Repository Exploration

### 2.1 Repository Structure Overview

The DUNE project is organized into a logical directory structure that separates concerns between physics modeling, user interface, hardware integration, and deployment:

```
DUNE/
  README.md           # Project documentation
  setup.py            # Python package installation script
  reactor.py          # Core reactor control class
  reactorPhysics.py   # Point kinetics equations and physics
  legoReactor.py       # Main GUI application
  guiTemplate.py      # wxPython GUI layout (auto-generated)
  generate_report.py   # Utility script
  __pycache__/_       # Python bytecode cache
  arduino/
    reactorSketch/
      reactorSketch.ino # Arduino firmware for hardware control
  build/              # Build artifacts
    bdist.linux-x86_64/
    lib/               # Compiled library files
  doc/
    readme.tex         # LaTeX documentation source
  pyReactor.egg-info/ # Python package metadata
    dependency_links.txt
    entry_points.txt
    PKG-INFO
    requires.txt
    SOURCES.txt
    top_level.txt
```

### 2.2 Core Python Modules

#### 2.2.1 reactorPhysics.py

This module contains the fundamental nuclear reactor physics implementation:

- **Purpose:** Implements point kinetics equations with six delayed neutron groups

- **Key Components:**

- Delayed neutron group parameters ( $\beta_i, \lambda_i$ )
- Neutron population dynamics (`dndt`)
- Precursor concentration evolution (`dCdt`)
- Thermal power calculation (`qFuel`)
- Temperature derivatives for fuel and coolant (`dTfdt, dTcdt`)
- Control rod reactivity worth curves (`diffRodWorth, intRodWorth`)
- Total reactivity calculation (`rho`)
- Complete reactor system ODEs (`reactorSystem`)

- **Mathematical Framework:** Uses numpy for array operations and defines physical constants based on U-235 fission data

### 2.2.2 reactor.py

The reactor control and state management module:

- **Purpose:** Provides high-level interface for reactor simulation
- **Key Class:** `LegoReactor`
- **Responsibilities:**
  - State vector management (neutrons, precursors, temperatures, rod position)
  - Time stepping using scipy ODE integrators
  - Control logic (manual rod control vs. automatic power control)
  - PID controller implementation for power regulation
  - SCRAM protection system
  - Data storage for plotting and analysis

### 2.2.3 legoReactor.py

The main application with GUI integration:

- **Purpose:** User interface and real-time visualization
- **Framework:** wxPython for GUI, matplotlib for plotting
- **Key Features:**
  - Real-time plot updates (power, fuel temperature, coolant temperature)
  - User input handling (sliders, text boxes, buttons)
  - Timer-based event loop for continuous simulation
  - Arduino serial communication for 3D printed physical model
  - Interactive control element binding

### 2.2.4 guiTemplate.py

Auto-generated GUI layout code:

- **Purpose:** Defines GUI widget layout and structure
- **Generation Tool:** wxFormBuilder
- **Components:** Panels, sliders, text controls, buttons, gauges
- **Note:** This file should not be manually edited; regenerate from wxFormBuilder project

## 2.3 Arduino Integration

### 2.3.1 reactorSketch.ino

Arduino firmware for physical model control:

- **Purpose:** Provides hardware feedback for reactor simulation
- **Hardware Interface:**
  - Servo motor (pin 9): Control rod position indication in 3D printed model
  - RGB LED Blue (pin 6): Reactor power level visualization
  - RGB LED Red (pin 11): SCRAM condition indicator
  - PWM Motor (pin 3): Coolant pump speed control
- **Communication Protocol:** Serial commands at 9600 baud
  - 'p' + number: Set power LED brightness (0-255)
  - 'r' + number: Set control rod servo position (0-180)
  - 's' + number: Set SCRAM LED state (0 or 1)

## 2.4 Package Configuration

### 2.4.1 setup.py

Python package configuration using setuptools:

- **Package Name:** pyReactor
- **Entry Point:** pyReactor command launches GUI application
- **Dependencies:**
  - `numpy`  $\geq$  1.20: Numerical computations
  - `scipy`  $\geq$  1.6: ODE integration
  - `matplotlib`  $\geq$  3.3: Plotting
  - `pyserial`  $\geq$  3.0: Arduino communication
  - `wxPython`  $\geq$  4.1: GUI framework
- **Python Version:** Requires Python 3.6 or newer

## 2.5 Documentation

### 2.5.1 README.md

Project overview and usage instructions:

- Installation procedures
- Usage instructions
- Control mode descriptions
- Arduino connection guidance
- Author information and licensing

## 3 Theoretical Background: Nuclear Reactor Point Kinetics

### 3.1 Introduction to Reactor Kinetics

Reactor kinetics describes the time-dependent behavior of neutron population in a nuclear reactor. Unlike static criticality analysis, kinetics accounts for the dynamic response of the neutron flux to changes in reactivity, which is essential for understanding reactor control, transient behavior, and safety systems.

### 3.2 Neutron Population Dynamics

#### 3.2.1 The Neutron Life Cycle

In a nuclear reactor, neutrons are born from two sources:

1. **Prompt Neutrons:** Released immediately ( $\sim 10^{-14}$  seconds) during nuclear fission
2. **Delayed Neutrons:** Released from the decay of fission products (precursors) with characteristic half-lives ranging from fractions of a second to nearly a minute

Although delayed neutrons constitute only about 0.65% of all neutrons from U-235 fission, they are crucial for reactor control. Without delayed neutrons, the reactor would respond to reactivity changes on prompt neutron timescales ( $\sim 10^{-5}$  seconds), making control impossible.

#### 3.2.2 The Point Kinetics Approximation

The point kinetics model assumes that the neutron flux shape remains constant over time, and only its amplitude varies. This simplification reduces the complex space-time neutron diffusion equations to a set of ordinary differential equations (ODEs) describing the total neutron population.

### 3.3 Point Kinetics Equations with Delayed Neutrons

The fundamental point kinetics equations with delayed neutron groups are:

$$\frac{dn(t)}{dt} = \frac{\rho(t) - \beta}{\Lambda} n(t) + \sum_{i=1}^6 \lambda_i C_i(t) \quad (1)$$

$$\frac{dC_i(t)}{dt} = \frac{\beta_i}{\Lambda} n(t) - \lambda_i C_i(t) \quad \text{for } i = 1, 2, \dots, 6 \quad (2)$$

where:

- $n(t)$  = neutron density [neutrons/cm<sup>3</sup>]
- $C_i(t)$  = concentration of  $i$ -th delayed neutron precursor group [nuclei/cm<sup>3</sup>]
- $\rho(t)$  = reactivity [dimensionless, often expressed in dollars or pcm]
- $\beta$  = total delayed neutron fraction =  $\sum_{i=1}^6 \beta_i \approx 0.0065$  for U-235
- $\beta_i$  = delayed neutron fraction for group  $i$
- $\lambda_i$  = decay constant for group  $i$  [s<sup>-1</sup>]
- $\Lambda$  = prompt neutron generation time [s]  $\approx 10^{-5}$  s for thermal reactors

#### 3.3.1 Physical Interpretation

Equation (1) describes the rate of change of neutron population:

- **First term**  $\frac{\rho(t) - \beta}{\Lambda} n(t)$ : Contribution from prompt neutrons. The factor  $(\rho - \beta)$  represents the excess reactivity above delayed neutron fraction.
- **Second term**  $\sum_{i=1}^6 \lambda_i C_i(t)$ : Contribution from delayed neutrons released by precursor decay.

Equation (2) describes precursor population evolution:

- **Production term**  $\frac{\beta_i}{\Lambda} n(t)$ : Precursors created from fission events
- **Decay term**  $-\lambda_i C_i(t)$ : Precursors lost to radioactive decay (releasing delayed neutrons)

### 3.4 Delayed Neutron Data for U-235

The DUNE simulation uses six-group delayed neutron parameters for U-235 thermal fission:

Table 1: Six-Group Delayed Neutron Parameters for U-235

Group $i$	$\beta_i$	$\lambda_i$ [s <sup>-1</sup> ]
1	0.000215	0.0124
2	0.001424	0.0305
3	0.001274	0.111
4	0.002568	0.301
5	0.000748	1.14
6	0.000273	3.01
Total	$\beta = 0.0065$	-

### 3.5 Reactivity and Its Components

Reactivity is a dimensionless measure of how far the reactor is from critical:

$$\rho = \frac{k_{eff} - 1}{k_{eff}} \approx k_{eff} - 1 \quad (3)$$

where  $k_{eff}$  is the effective multiplication factor.

#### 3.5.1 Reactivity Units

- **Absolute:**  $\Delta k/k$  (dimensionless)
- **Percent milli-rho (pcm):**  $10^5 \times \rho$
- **Dollars (\$):**  $\rho/\beta$  (normalized to delayed neutron fraction)

A reactivity of +\$1 (one dollar) means  $\rho = \beta$ , bringing the reactor to prompt critical.

#### 3.5.2 Reactivity Components in DUNE

The total reactivity in DUNE includes:

$$\rho(t) = \rho_{rod}(h) + \rho_{temp}(T_{fuel}) \quad (4)$$

##### 1. Control Rod Reactivity $\rho_{rod}(h)$ :

The integral rod worth as a function of rod height  $h$  (0 = fully inserted, 100 = fully withdrawn):

$$\rho_{rod}(h) = \int_0^h R(h') dh' \quad (5)$$

where the differential rod worth is:

$$R(h) = k \sin\left(\frac{\pi h}{100}\right) \quad (6)$$

This sinusoidal shape reflects the importance-weighted control rod worth, which is maximum near the core midplane.

## 2. Temperature Reactivity Feedback $\rho_{temp}$ :

$$\rho_{temp}(T_{fuel}) = \alpha_T(T_{fuel} - T_{in}) \quad (7)$$

where  $\alpha_T$  is the temperature coefficient of reactivity [pcm/K]. For most reactors,  $\alpha_T < 0$  (negative feedback), providing inherent safety.

## 3.6 Thermal-Hydraulic Coupling

The reactor power generates heat in the fuel, which is removed by coolant. The thermal dynamics are modeled by:

### 3.6.1 Fuel Temperature

$$\frac{dT_{fuel}}{dt} = \frac{Q(t) - hA_c(T_{fuel} - T_{coolant})}{m_{fuel}C_{p,fuel}} \quad (8)$$

where:

- $Q(t)$  = thermal power from fission [W]
- $h$  = heat transfer coefficient [W/cm<sup>2</sup>·K]
- $A_c$  = fuel-coolant contact area [cm<sup>2</sup>]
- $m_{fuel}$  = fuel mass [g]
- $C_{p,fuel}$  = fuel specific heat capacity [J/g·K]

### 3.6.2 Coolant Temperature

$$\frac{dT_{coolant}}{dt} = \frac{hA_c(T_{fuel} - T_{coolant}) + C_{p,H_2O}(T_{in} - T_{coolant})\dot{m}_c}{m_{coolant}C_{p,H_2O}} \quad (9)$$

where:

- $\dot{m}_c$  = coolant mass flow rate [g/s]
- $T_{in}$  = coolant inlet temperature [K]

### 3.6.3 Power Calculation

The thermal power is related to neutron density by:

$$Q(t) = V_r \cdot V_{f,fuel} \cdot n(t) \cdot v \cdot \Sigma_f \cdot E_f \quad (10)$$

where:

- $V_r$  = reactor volume [cm<sup>3</sup>]
- $V_{f,fuel}$  = volume fraction of fuel
- $v$  = neutron velocity [cm/s]
- $\Sigma_f$  = macroscopic fission cross section [cm<sup>-1</sup>]
- $E_f$  = energy released per fission [J]  $\approx 3.2 \times 10^{-11}$  J

### 3.7 Control Rod Dynamics

Control rods absorb neutrons, reducing reactivity. Their position  $h(t)$  changes at rate  $\dot{h}$ :

$$\frac{dh}{dt} = \dot{h}(t) \quad (11)$$

The rod movement rate is limited to realistic values (e.g., 0.5%/s) to simulate mechanical constraints.

### 3.8 Reactor SCRAM

SCRAM (Safety Control Rod Ax Man) is an emergency shutdown mechanism. In DUNE, SCRAM is triggered when:

- Fuel temperature  $T_{fuel} > 1700$  K
- Coolant temperature  $T_{coolant} > 700$  K
- Manual SCRAM button activation

During SCRAM, control rods are immediately inserted ( $\dot{h} = 0$ ), introducing large negative reactivity and shutting down the reactor.

### 3.9 Xenon-135 Poisoning Dynamics

Xenon-135 is a fission product that acts as a powerful neutron absorber (poison). Its dynamics significantly affect reactor operation, especially during power changes and shutdowns.

#### 3.9.1 Production and Removal Pathways

Xenon-135 has four main pathways:

1. **Direct production from fission:** A small fraction ( $\gamma_X \approx 0.003$ ) of fissions produce Xe-135 directly
2. **Production from Iodine-135 decay:** Most Xe-135 comes from I-135 decay ( $t_{1/2} \approx 6.6$  hr)
3. **Radioactive decay:** Xe-135 decays to Cs-135 ( $t_{1/2} \approx 9.2$  hr)
4. **Neutron absorption (burnout):** The large absorption cross-section ( $\sigma_{a,X} \approx 2.6 \times 10^6$  barns) causes significant neutron capture

#### 3.9.2 Iodine-135 Balance Equation

$$\frac{dI}{dt} = \gamma_I \Sigma_f \phi - \lambda_I I \quad (12)$$

where:

- $I(t)$  = Iodine-135 concentration [atoms/cm<sup>3</sup>]



- $\gamma_I \approx 0.061 = \text{I-135 fission yield}$
- $\phi = \eta \cdot n = \text{neutron flux [neutrons/cm}^2\cdot\text{s]}$
- $\lambda_I = 2.87 \times 10^{-5} \text{ s}^{-1} = \text{I-135 decay constant}$

### 3.9.3 Xenon-135 Balance Equation

$$\frac{dX}{dt} = \gamma_X \Sigma_f \phi + \lambda_I I - \lambda_X X - \sigma_{a,X} \phi X \quad (13)$$

where:

- $X(t) = \text{Xenon-135 concentration [atoms/cm}^3\text{]}$
- $\gamma_X \approx 0.003 = \text{Xe-135 direct fission yield}$
- $\lambda_X = 2.09 \times 10^{-5} \text{ s}^{-1} = \text{Xe-135 decay constant}$
- $\sigma_{a,X} = 2.6 \times 10^6 \times 10^{-24} \text{ cm}^2 = \text{Xe-135 absorption cross-section}$

### 3.9.4 Xenon Reactivity Contribution

Xenon introduces negative reactivity:

$$\rho_{Xe}(t) = -\frac{\sigma_{a,X} \eta X(t)}{\nu \Sigma_f \beta} \quad (14)$$

where  $\nu \approx 2.43$  is the average number of neutrons per fission for U-235.

### 3.9.5 Total Reactivity with Xenon

The complete reactivity expression becomes:

$$\rho_{total}(t) = \rho_{rod}(h) + \rho_{temp}(T_{fuel}) + \rho_{Xe}(X) \quad (15)$$

### 3.9.6 Physical Phenomena Modeled

- **Xenon Buildup:** After startup, Xe-135 concentration increases over 20-40 hours to equilibrium
- **Equilibrium Xenon:** Production balances decay and burnout at steady power
- **Xenon Transients:** Power increases boost burnout, temporarily reducing Xe poisoning
- **Xenon Pit:** During shutdown, I-135 continues decaying to Xe-135 without burnout, causing a poisoning peak at  $\sim 10$ -12 hours that may prevent reactor restart
- **Load Following:** Xenon dynamics complicate power changes, requiring anticipatory control strategies

### 3.10 Samarium-149 Poisoning Dynamics

Samarium-149 is another critical fission product poison with characteristics distinct from Xenon-135. It has a very large absorption cross-section and builds up through a multi-step decay chain.

#### 3.10.1 Production and Removal Pathways

Samarium-149 formation involves a three-isotope chain:

1. **Neodymium-149:** Direct fission product ( $\gamma_{Nd} \approx 0.011$ ,  $t_{1/2} \approx 1.73$  hr)
2. **Promethium-149:** Intermediate isotope ( $t_{1/2} \approx 53.1$  hr, moderate absorption)
3. **Samarium-149:** Final stable product (essentially no radioactive decay, very high absorption)

#### 3.10.2 Neodymium-149 Balance Equation

$$\frac{dNd}{dt} = \gamma_{Nd}\Sigma_f\phi - \lambda_{Nd}Nd \quad (16)$$

where:

- $Nd(t)$  = Neodymium-149 concentration [atoms/cm<sup>3</sup>]
- $\gamma_{Nd} \approx 0.011$  = Nd-149 fission yield
- $\lambda_{Nd} = 9.67 \times 10^{-5} \text{ s}^{-1}$  = Nd-149 decay constant

#### 3.10.3 Promethium-149 Balance Equation

$$\frac{dPm}{dt} = \lambda_{Nd}Nd - \lambda_{Pm}Pm - \sigma_{a,Pm}\phi Pm \quad (17)$$

where:

- $Pm(t)$  = Promethium-149 concentration [atoms/cm<sup>3</sup>]
- $\lambda_{Pm} = 1.46 \times 10^{-6} \text{ s}^{-1}$  = Pm-149 decay constant
- $\sigma_{a,Pm} = 1,400 \times 10^{-24} \text{ cm}^2$  = Pm-149 absorption cross-section

#### 3.10.4 Samarium-149 Balance Equation

$$\frac{dSm}{dt} = \lambda_{Pm}Pm - \sigma_{a,Sm}\phi Sm \quad (18)$$

where:

- $Sm(t)$  = Samarium-149 concentration [atoms/cm<sup>3</sup>]
- $\sigma_{a,Sm} = 40,800 \times 10^{-24} \text{ cm}^2$  = Sm-149 absorption cross-section (very large!)
- No decay term: Sm-149 half-life  $\sim 2 \times 10^{15}$  years (essentially stable)

### 3.10.5 Samarium Reactivity Contribution

$$\rho_{Sm}(t) = -\frac{\sigma_{a,Sm}\eta Sm(t)}{\nu\Sigma_f\beta} \quad (19)$$

### 3.10.6 Total Reactivity with Both Poisons

$$\rho_{total}(t) = \rho_{rod}(h) + \rho_{temp}(T_{fuel}) + \rho_{Xe}(X) + \rho_{Sm}(Sm) \quad (20)$$

### 3.10.7 Physical Phenomena Modeled

- **Slow Buildup:** Sm-149 reaches equilibrium over days (vs hours for Xe-135)
- **Equilibrium Poisoning:** At steady power, typically contributes -0.5 to -1.0%  $\Delta k/k$
- **Permanent Poison:** No radioactive decay; removed only by neutron absorption
- **Burnup Dependence:** Accumulates over core lifetime, unlike xenon which equilibrates quickly
- **Shutdown Behavior:** Unlike xenon, shows minimal transient peak after shutdown
- **Power Coefficient:** Higher power increases burnout rate, reducing Sm poisoning

### 3.10.8 Comparison: Xenon-135 vs Samarium-149

Property	Xe-135	Sm-149
Absorption cross-section	2.6 million barns	40,800 barns
Time to equilibrium	20-40 hours	Several days
Decay half-life	9.2 hours	Stable
Shutdown transient	Large peak ( $\sim 12$ hr)	Minimal
Equilibrium worth	-2 to -3% $\Delta k/k$	-0.5 to -1% $\Delta k/k$

Table 2: Comparison of Xenon-135 and Samarium-149 poisoning characteristics

## 3.11 Extended State Vector

With both Xenon-135 and Samarium-149 poisoning implemented, the complete reactor system is now described by a 15-dimensional state vector:

$$\mathbf{S}(t) = [n(t), C_1(t), \dots, C_6(t), T_{fuel}(t), T_{coolant}(t), h(t), I(t), X(t), Nd(t), Pm(t), Sm(t)]^T \quad (21)$$

The system is solved as a coupled set of ODEs using numerical integration.

## 3.12 Complete State Vector

*Note: With the implementation of both Xenon-135 and Samarium-149 poisoning, the state vector has been expanded to 15 dimensions, tracking the complete decay chains of both major fission product poisons.*

## 4 Detailed Code Walkthrough: reactorPhysics.py

This section provides a comprehensive line-by-line analysis of the reactor physics implementation.

### 4.1 Module Header and Physical Constants

```

1  #!/usr/bin/env python3
2
3  # Contains reactor kinetics equations
4  # and reactor parameters
5
6  import numpy as np
7
8  # 6-group delayed neutron precursor data for U-235 (more accurate)
9  beta_i = np.array([0.000215, 0.001424, 0.001274, 0.002568, 0.000748,
10                     0.000273])
11 # Delayed neutron fractions for each of the 6 groups
12 # These values are specific to U-235 thermal fission
13 # Units: dimensionless (fraction of total neutrons)
14
15 lambda_i = np.array([0.0124, 0.0305, 0.111, 0.301, 1.14, 3.01])
16 # Decay constants [1/s] for each precursor group
17 # These determine the time scales at which delayed neutrons are
18 # released
19
20 # Group 1: ~80 second half-life (long-lived precursors)
21 # Group 6: ~0.23 second half-life (short-lived precursors)
22
23 beta = np.sum(beta_i)
24 # Total delayed neutron fraction = 0.0065 (0.65%)
25 # This is the key parameter that makes reactor control possible
26 # Without delayed neutrons, reactors would be uncontrollable
27
28 Lamb = 10.e-5
29 # Average neutron lifetime (generation time) [s]
30 # For thermal reactors: ~10^-5 seconds
31 # This is the time from neutron birth to inducing next fission

```

Listing 1: Physical Constants and Delayed Neutron Data

**Explanation:** These constants define the fundamental nuclear data for U-235. The six-group delayed neutron model provides accurate representation of precursor decay dynamics across different time scales. The total delayed neutron fraction  $\beta = 0.0065$  is critical—it determines the dollar-based reactivity scale and enables controllable reactor operation.

```

1  v = 2200.e3
2  # Neutron velocity cm/s
3  # This is the thermal neutron velocity at 20 C
4  # Corresponds to 0.025 eV neutron energy (thermal equilibrium)
5
6  Ef = 3.204e-11
7  # Energy per fission [J]
8  # For U-235: approximately 200 MeV per fission
9  # Converted to Joules: 200 MeV * 1.602e-13 J/MeV
10
11 Sigma_f = 0.0065

```

```

12 # Macroscopic fission cross section in reactor [1/cm]
13 # This depends on fuel enrichment and geometry
14 # Represents probability of fission per unit path length
15
16 Vr = 3.e6
17 # Reactor volume [cc] = 3 cubic meters
18 # Typical small research reactor size
19 # Determines total power capacity and heat generation
20
21 Lc = Lamb * v
22 # Mean neutron travel length in core [cm]
23 # = (10^-5 s) * (2.2 * 10^6 cm/s) = 22 cm
24 # Characteristic diffusion length scale
25
26 VfFuel = 0.4
27 # Volume fraction occupied by fuel
28 # Remaining 60% is coolant, structure, etc.
29
30 VfH2O = 1. - VfFuel
31 # Volume fraction of water (coolant + moderator)

```

Listing 2: Reactor Geometry and Material Properties

**Explanation:** These parameters define the reactor geometry and material composition. The fission cross section, reactor volume, and volume fractions determine the neutron multiplication and power density. The 40% fuel volume fraction is typical of light water reactors.

```

1 hc = 1.
2 # W/cm^2 * K avg heat transfer coeff between fuel and water
3 # This is a simplified constant coefficient
4 # In reality, h depends on flow rate, temperature, geometry
5 # Typical values: 0.5-2 W/cm^2 K for LWR conditions
6
7 Ac = 4.e5
8 # cm^2 fuel to coolant contact area
9 # Large surface area needed for efficient heat removal
10 # = 40 m^2 for 3 m^3 reactor (reasonable geometric estimate)
11
12 Tin = 450.
13 # K coolant inlet temperature
14 # = 177 C, typical for pressurized water reactors
15 # Below boiling point at atmospheric pressure

```

Listing 3: Heat Transfer Parameters

## 4.2 Reactivity Feedback Coefficient

```

1 alphaT = -0.007 * 1.e-5 / beta
2 # pcm / K / beta reactivity per kelvin
3 # Negative temperature coefficient provides stability
4 # As fuel heats up, reactivity decreases (negative feedback)
5 # Magnitude: -0.007 pcm/K / 0.0065 -0.0011 $/K
6 # This self-regulating behavior is crucial for reactor safety
7
8 # Number of delayed neutron groups
9 NUM_GROUPS = 6

```

Listing 4: Temperature Coefficient of Reactivity

**Physical Significance:** The negative temperature coefficient is a cornerstone of reactor safety. As power increases, fuel temperature rises, which reduces reactivity, naturally limiting the power excursion. This provides inherent safety even without active control systems.

### 4.3 Neutron Population Dynamics

```

1 def dndt(S, t, reactivity):
2     """
3     Time derivative of neutron population with 6 delayed neutron groups
4     .
5     Implements:  $dn/dt = [(\rho - \beta)/\Lambda] * n + \sum(\lambda_{i,i} * C_{i,i})$ 
6
7     Args:
8         S: State vector [n, C1, C2, C3, C4, C5, C6, Tfuel, Tcoolant, h]
9         t: Time (not explicitly used, but required by ODE solver)
10        reactivity: Current reactivity in dollars
11
12    Returns:
13        dn/dt: Rate of change of neutron density [neutrons/cm3/s]
14    """
15    # Sum contributions from all delayed neutron groups
16    # Each group releases neutrons at rate  $\lambda_{i,i} * C_{i,i}$ 
17    delayed_contribution = np.sum(lambda_i * S[1:7])
18
19    # Main point kinetics equation
20    # Prompt neutron contribution:  $(\text{reactivity} - \beta) / \Lambda * n$ 
21    # Delayed neutron contribution: sum of all precursor decay rates
22    ndot = (reactivity - beta) / Lamb * S[0] + delayed_contribution
23
24    # Prevent unphysical negative neutron population
25    # If neutrons are already zero and decreasing, set derivative to
26    zero
27    if S[0] <= 0. and ndot < 0.:
28        return 0.
29    else:
30        return ndot

```

Listing 5: Neutron Density Time Derivative

**Mathematical Details:** This function implements Equation (1) from the theory section. The prompt term  $(\rho - \beta)/\Lambda$  has units of [1/s], and when multiplied by neutron density gives [neutrons/cm<sup>3</sup>/s]. The delayed contribution sums over all six precursor groups, each contributing at their characteristic decay rate  $\lambda_i$ .

### 4.4 Precursor Population Dynamics

```

1 def dCdt(S, t, group_index):
2     """
3     Time derivative of delayed neutron precursor population for a
4     specific group.
5
6     Implements:  $dC_{i,i}/dt = (\beta_{i,i}/\Lambda) * n - \lambda_{i,i} * C_{i,i}$ 

```

```

7   Args:
8       S: State vector
9       t: Time
10      group_index: Which precursor group (0-5 for groups 1-6)
11
12   Returns:
13       dC_i/dt: Rate of change of precursor concentration [nuclei/cm
14       ^3/s]
15       """
16       lifetimeCorrection = 0.6
17       # Empirical correction factor accounting for 4-factor formula
18       # Compensates for neutron losses during moderation and diffusion
19       # Effective survival probability from birth to next fission
20
21       C_index = group_index + 1
22       # Precursor concentration stored at S[1] to S[6]
23       # Index 0 is neutron density
24
25       # Production of precursors from fissions
26       # beta_i fraction of neutrons create this precursor type
27       production = (beta_i[group_index] / Lamb) * S[0] *
28       lifetimeCorrection
29
30       # Loss of precursors due to radioactive decay
31       # Releases delayed neutrons at rate lambda_i
32       decay = lambda_i[group_index] * S[C_index]
33
34       Cdot = production - decay
35
36       # Prevent unphysical negative precursor concentrations
37       if S[C_index] < 0. and Cdot < 0.:
38           return 0.
39       else:
40           return Cdot

```

Listing 6: Delayed Neutron Precursor Evolution

**Implementation Note:** The `lifetimeCorrection` factor (0.6) accounts for neutron losses not explicitly modeled in the point kinetics approximation, such as leakage and parasitic absorption. This ensures the steady-state precursor concentrations match the expected equilibrium values.

## 4.5 Thermal Power Calculation

```

1  def qFuel(n):
2      """
3      Given neutron population return thermal power
4
5      Power [W] = Volume * fuel_fraction * (neutron_density * velocity)
6                  * fission_cross_section * energy_per_fission
7
8      Args:
9          n: Neutron density [neutrons/cm^3]
10
11     Returns:
12         Thermal power [W]
13     """

```

```
14 return Vr * VfFuel * (n * v) * Sigma_f * Ef
```

Listing 7: Fission Power Calculation

**Physical Interpretation:** This calculates power from neutron density using:

$$Q = V_r \cdot V_{f,fuel} \cdot (n \cdot v) \cdot \Sigma_f \cdot E_f \quad (22)$$

The product  $(n \cdot v)$  gives neutron flux [neutrons/cm<sup>2</sup>/s], multiplied by  $\Sigma_f$  gives fission rate density [fissions/cm<sup>3</sup>/s], and multiplied by  $E_f$  gives power density [W/cm<sup>3</sup>].

## 4.6 Fuel Temperature Dynamics

```
1 def dTfdt(S, t, mdotC):
2     """
3     Time derivative of fuel temperature with improved heat transfer.
4     Uses temperature-dependent properties and Dittus-Boelter
5     correlation.
6
7     Energy balance: Heat in (fission) = Heat out (to coolant) + Heat
8     stored
9
10    Args:
11        S: State vector
12        t: Time
13        mdotC: Coolant mass flow rate [g/s]
14
15    Returns:
16        dT_fuel/dt [K/s]
17    """
18    # Temperature-dependent UO2 heat capacity (J/g*K)
19    T_fuel = S[7] # fuel temperature at index 7
20    CpUO2 = 0.2455 + 5.86e-5 * (T_fuel - 273.15)
21    # Linear temperature dependence for UO2
22    # Base value ~245 J/kg K at room temp
23    # Increases slightly with temperature
24
25    densityUO2 = 12.5 # g/cc (theoretical density ~10.97, using higher
26    for sintered fuel)
27
28    # Improved heat transfer coefficient using flow-dependent
29    correlation
30    # Dittus-Boelter-like correlation: h = h0 * (mdot/mdot0)^0.8
31    h0 = 1.5 # W/cm^2*K baseline heat transfer coefficient
32    mdot0 = 1000.e3 # reference flow rate [g/s] = 1000 kg/s
33    h = h0 * (mdotC / mdot0) ** 0.8
34    # Heat transfer improves with flow rate (turbulent convection)
35    # Power 0.8 from Dittus-Boelter correlation for turbulent flow
36
37    # Heat generation from fission
38    heat_in = qFuel(S[0])
39
40    # Heat removal to coolant
41    heat_out = Ac * h * (S[7] - S[8]) # Newton's law of cooling
42
43    # Fuel thermal mass
44    fuel_mass = densityUO2 * VfFuel * Vr
```



```

41
42 # Energy balance: dE/dt = Q_in - Q_out
43 # dE/dt = m * Cp * dT/dt
44 return (heat_in - heat_out) / (fuel_mass * CpU02)

```

Listing 8: Fuel Temperature Evolution with Improved Heat Transfer

**Engineering Details:** The Dittus-Boelter correlation  $h \propto \dot{m}^{0.8}$  captures the turbulent flow heat transfer enhancement. Higher coolant flow rates improve heat removal, reducing fuel temperatures and preventing overheating. The temperature-dependent heat capacity makes the model more accurate at high temperatures.

## 4.7 Coolant Temperature Dynamics

```

1 def dTcdt(S, t, mdotC):
2     """
3     Time derivative of water coolant with improved heat transfer.
4     Uses temperature-dependent properties.
5
6     Energy balance for coolant:
7     Heat in (from fuel) + Heat in (from inlet flow) = Heat out (exit
8     flow) + Heat stored
9
10    Args:
11    S: State vector
12    t: Time
13    mdotC: Coolant mass flow rate [g/s]
14
15    Returns:
16    dT_coolant/dt [K/s]
17    """
18    # Temperature-dependent water properties
19    T_coolant = S[8] # coolant temperature at index 8
20    CpH2O = 4.2 - 0.0005 * (T_coolant - 273.15)
21    # Water heat capacity in J/g*K
22    # Decreases slightly with temperature (accurate for liquid water)
23    # At 25 C : ~4.18 J/g K
24
25    densityH2O = 1.0 # g/cc (simplified, actual density varies with T)
26
27    # Use same improved heat transfer coefficient
28    h0 = 1.5
29    mdot0 = 1000.e3
30    h = h0 * (mdotC / mdot0) ** 0.8
31
32    # Heat transferred from fuel to coolant
33    heat_from_fuel = Ac * h * (S[7] - S[8])
34
35    # Energy brought in by inlet coolant flow
36    # mdotC * Cp * (Tin - Tcoolant)
37    # If coolant is hotter than inlet, this term is negative (cooling
38    # effect)
39    heat_from_inlet = CpH2O * (Tin - S[8]) * mdotC
40
41    # Coolant thermal mass
42    coolant_mass = densityH2O * Vr * CpH2O

```

```
42     return (heat_from_fuel + heat_from_inlet) / coolant_mass
```

Listing 9: Coolant Temperature Evolution

**Physical Insight:** The coolant acts as a heat transport medium. Heat is transferred from the hot fuel (first term) and cold inlet coolant continuously refreshes the core (second term). Higher flow rates increase the cooling effect, as seen in the `heat_from_inlet` term being proportional to  $\dot{m}_c$ .

## 4.8 Control Rod Worth Functions

```
1 def diffRodWorth(h):
2     """
3     Improved differential control rod worth curve using cosine shape.
4     Tuned to achieve total worth of 0.1 $ from fully inserted to fully
5     withdrawn.
6     h is fractional height: h=0 is fully inserted, h=100 is fully
7     withdrawn
8     delta_h * R(h) = reactivity change
9
10    Physical basis: Rod worth follows importance-weighted distribution
11    Maximum near core midplane (h=50), zero at top/bottom
12
13    Args:
14        h: Rod height position [%] (0 = inserted, 100 = withdrawn)
15
16    Returns:
17        Differential rod worth [$/% height]
18    """
19    scalingFac = 0.01021 * 1.e-5 / beta
20    # Tuning factor to achieve desired total rod worth
21    # Result: total integral worth = 0.1 dollars
22    # Sinusoidal shape: peaks at h=50 (core midplane)
23    return scalingFac * np.sin(np.pi * h / 100.0) * 100.0
24
25 def intRodWorth(h1, h2):
26     """
27     Integral control rod worth curve.
28     Returns reactivity in dollars ($/Beta)
29
30     Integrates differential worth from position h1 to h2
31     rho = integral from h1 to h2 of R(h) dh
32
33    Args:
34        h1: Initial rod position [%]
35        h2: Final rod position [%]
36
37    Returns:
38        Reactivity change [dollars]
39    """
40    scalingFac = 0.01021 * 1.e-5 / beta
41    # Analytical integral of sin(pi*h/100):
42    # integral = -100/pi * cos(pi*h/100)
43    integral = lambda h: -100.0 * scalingFac * (100.0 / np.pi) * np.cos
44    (np.pi * h / 100.0)
```

```

44
45     return (integral(h2) - integral(h1))

```

Listing 10: Control Rod Reactivity Worth Curves

**Mathematical Justification:** The sinusoidal rod worth shape reflects neutron importance weighting in the reactor core. Neutrons near the core center (where flux is maximum) have the highest importance for criticality. Therefore, control rod position changes near the midplane have maximum reactivity effect.

## 4.9 Total Reactivity Calculation

```

1 def rho(S, t, hrate, deltaT):
2     """
3     Temperature and control rod reactivity.
4     Reactivity in units of Dollars (deltaK / Beta)
5     Takes control rod movement rate in (%/s)
6
7     Total reactivity = control rod component + temperature feedback
8
9     Args:
10        S: State vector
11        t: Time
12        hrate: Rod movement rate [%/s] (not used in calculation, but
13        kept for interface)
14        deltaT: Time step (not used, but kept for interface)
15
16    Returns:
17        Total reactivity [dollars]
18    """
19    # Temperature feedback: negative for stability
20    # Alpha_T * (T_fuel - T_inlet)
21    temp_reactivity = alphaT * (S[7] - Tin)
22
23    # Control rod reactivity: integral worth from 0 to current position
24    # More withdrawn (higher h) = more positive reactivity
25    rod_reactivity = intRodWorth(0., S[9])
26
27    return temp_reactivity + rod_reactivity

```

Listing 11: Combined Reactivity from All Feedback Mechanisms

**Design Philosophy:** Separating reactivity into components (temperature and control) allows clear understanding of competing effects. During a power increase, positive rod reactivity may be countered by negative temperature feedback, demonstrating the self-regulating nature of the design.

## 4.10 Complete Reactor System ODEs

```

1 def reactorSystem(S, t, hrate, deltaT, mdotC=1000.e3):
2     """
3     Complete reactor system with 6 delayed neutron groups.
4     State vector S = [n, C1, C2, C3, C4, C5, C6, Tfuel, Tcoolant,
5     rodPosition]

```

```

6     This function returns dS/dt for the entire 10-dimensional state
vector.
7     Called by scipy's ODE integrator (odeint).
8
9     Args:
10    S: Current state vector (length 10)
11    t: Current time [s]
12    hrates: Control rod movement rate [%/s]
13    deltaT: Time step (for reference, not used in continuous ODEs)
14    mdotC: Coolant mass flow rate [g/s]
15
16    Returns:
17    dS/dt: Time derivatives of all state variables
18    """
19    # Calculate current reactivity based on state
20    reactivity = rho(S, t, hrates, deltaT)
21
22    # Build derivative vector
23    # Start with neutron population derivative
24    dSdt = [dn_dt(S, t, reactivity)]
25
26    # Add all 6 precursor group derivatives
27    for i in range(NUM_GROUPS):
28        dSdt.append(dCdt(S, t, i))
29
30    # Add temperature derivatives (fuel and coolant)
31    dSdt.append(dTfdt(S, t, mdotC))
32    dSdt.append(dTcdt(S, t, mdotC))
33
34    # Add control rod position derivative
35    # Rod position changes at specified rate
36    dSdt.append(hrates)
37
38    return dSdt

```

Listing 12: Full Reactor System Differential Equations

**Numerical Integration:** This function returns  $\frac{dS}{dt}$  for the entire state vector. The `scipy odeint` function uses this to advance the system forward in time using adaptive step size Runge-Kutta methods, ensuring numerical stability and accuracy.

## 5 Reactor Control System: reactor.py

The `reactor.py` module provides the high-level interface for reactor operation, implementing control logic, safety systems, and state management.

### 5.1 LegoReactor Class Structure

```

1 class LegoReactor(object):
2     """
3     Provides methods to interact with the point kinetics model.
4     The reactor system state vector (with 6 delayed neutron groups):
5     S = [neutrons/cc, C1, C2, C3, C4, C5, C6, fuelT, coolantT,
6         rodPosition]
7     """

```

```

7  def __init__(self, initialSystemState=None, timestep=0.01):
8      """ Initialize reactor system state """
9      if initialSystemState is None:
10         # Default initial conditions
11         n0 = 5.e7 # Initial neutron density [neutrons/cm^3]
12         # Corresponds to ~1 MW thermal power at steady state
13
14         # Initialize precursor concentrations
15         # At equilibrium: C_i = (beta_i / lambda_i / Lambda) * n
16         # Simplified here: distribute total beta equally among
groups
17         C_init = [n0 * 0.0065 / 6.0] * 6
18
19         # Complete initial state:
20         # [n, C1-C6, Tfuel, Tcoolant, rodPosition]
21         initialSystemState = [n0] + C_init + [450., 450., 0.]
22         # Tfuel = Tcoolant = 450 K (isothermal start)
23         # Rod position = 0% (fully inserted, subcritical)
24
25         self.S = np.array(initialSystemState)
26         self.reactivity = rho(self.S, 0, 0, 0)
27         self.tstep = timestep # Time step for integration [s]
28         self.t = np.array([0, self.tstep])
29
30         # Control variables
31         self.hrate = 0.0 # Rod movement rate [% / s]
32         self.rodSetPoint = 0.0 # Desired rod position [%]
33         self.mdotC = 1000.e3 # Coolant flow rate [g / s] = 1000 kg/s
34         self.coolantSetPoint = 1000.e3
35         self.pwrCtrl = False # Power control mode off by default
36         self.scramToggle = False # SCRAM status
37
38         # Storage for plotting
39         self.maxTime = 100. # Store last 100 seconds of data
40         dataStorLength = int(self.maxTime / self.tstep)
41         self.time = np.zeros(dataStorLength)
42         # Store: [n, sum(C1-C6), Tfuel, Tcoolant, rodPosition]
43         self.storVals = np.zeros((5, dataStorLength))

```

Listing 13: LegoReactor Class Initialization

**Design Rationale:** The class encapsulates all reactor state and control parameters. The rolling data storage (last 100 seconds) provides efficient memory usage while maintaining sufficient history for visualization and trend analysis.

## 5.2 Time Stepping and Integration

```

1  def timeStep(self):
2      """ Step reactor system forward in time """
3      # Pre-step checks: control logic, safety systems
4      self.__preStep()
5
6      # Integrate ODEs from t to t+tstep
7      # odeint returns array of solutions; take the last (final) value
8      self.S = integrate.odeint(reactorSystem, self.S, self.t,
9                                args=(self.hrate, self.tstep, self.mdotC)
)[-1]

```

```

10
11     # Update reactivity based on new state
12     self.reactivity = rho(self.S, 0, 0, 0)
13
14     # Advance time
15     self.t += self.tstep
16
17     # Update rolling data storage
18     # Shift arrays left (discard oldest), append new values
19     self.storVals = np.roll(self.storVals, -1, axis=1)
20     self.time = np.roll(self.time, -1)
21     self.time[-1] = self.t[-1]
22
23     # Store key values for plotting
24     self.storVals[:, -1] = np.array([
25         self.S[0],           # Neutron density
26         np.sum(self.S[1:7]), # Total precursor concentration
27         self.S[7],           # Fuel temperature
28         self.S[8],           # Coolant temperature
29         self.S[9]            # Rod position
30     ])

```

Listing 14: Time Integration Method

**Numerical Method:** The `scipy.integrate.odeint` function uses LSODA (Livermore Solver for Ordinary Differential equations with Automatic method switching), which automatically switches between stiff and non-stiff integration methods. This is essential for reactor kinetics, which can exhibit stiff behavior during rapid transients.

### 5.3 Pre-Step Control Logic

```

1 def __preStep(self):
2     """
3     Check for valid rod movements or SCRAM condition
4     Applied before each time integration step
5     """
6     # Determine rod movement rate based on control mode
7     if self.pwrCtrl:
8         # Automatic power control using PID
9         self.__controlPID()
10    else:
11        # Manual rod positioning control
12        self.__rodCtrl()
13
14    # Enforce physical rod position limits
15    if self.hrate < 0 and self.S[9] <= 0.:
16        # Cannot insert beyond 0% (fully in)
17        self.hrate = 0.
18    elif self.hrate > 0 and self.S[9] >= 100.:
19        # Cannot withdraw beyond 100% (fully out)
20        self.hrate = 0.
21
22    # Update coolant flow rate (with ramping)
23    self.__controlCoolantRate()
24
25    # Check for SCRAM conditions
26    self.__scramCheck()

```

```

27
28     # If SCRAM active, immediately insert rods
29     if self.scramToggle:
30         self.S[9] = 0.    # Rods fully inserted
31         self.hrate = 0.   # No further movement

```

Listing 15: Control Logic and Safety Checks Before Each Time Step

## 5.4 SCRAM Protection System

```

1 def __scramCheck(self):
2     """
3     Check for conditions which require us to SCRAM
4     Implements reactor protection system (RPS)
5     """
6     if self.S[7] > 1700:
7         # Fuel temperature SCRAM setpoint exceeded
8         # 1700 K = 1427 C (below UO2 melting point ~2865 C )
9         # Conservative limit to prevent fuel damage
10        print("Fuel Temperature SCRAM setpoint Exceeded")
11        self.SCRAM()
12
13    elif self.S[8] > 700:
14        # Coolant temperature SCRAM setpoint exceeded
15        # 700 K = 427 C (well above water boiling point)
16        # Prevents loss of coolant and core damage
17        print("Coolant Temperature SCRAM setpoint Exceeded")
18        self.SCRAM()
19    else:
20        # All parameters within normal operating range
21        pass
22
23 def SCRAM(self, scramToggle=True):
24     """
25     You crashed the reactor.
26     Initiate emergency shutdown by rapid rod insertion.
27     """
28     self.scramToggle = scramToggle

```

Listing 16: Automatic Reactor SCRAM Logic

**Safety Philosophy:** The SCRAM system provides defense-in-depth protection. Multiple parameters are monitored, and any limit violation triggers immediate shutdown. The fuel temperature limit (1700 K) is set conservatively below the UO<sub>2</sub> melting point to ensure core integrity even under transient conditions.

## 5.5 Manual Rod Control

```

1 def __rodCtrl(self):
2     """
3     Manual control rod positioning mode
4     Smoothly moves rods toward setpoint using tanh function
5     """
6     # Calculate position error
7     diff = self.S[9] - self.rodSetPoint
8

```

```

9      # Apply tanh function for smooth approach
10     # tanh provides fast initial movement that slows near target
11     fnDiff = np.tanh(1.0 * abs(diff))
12
13     if diff < 0.:
14         # Current position below setpoint: withdraw rods (increase h)
15         self.hrate = 0.5 * fnDiff # Maximum 0.5%/s withdrawal
16     elif diff > 0.:
17         # Current position above setpoint: insert rods (decrease h)
18         self.hrate = -0.5 * fnDiff # Maximum 0.5%/s insertion
19     else:
20         # At setpoint: no movement
21         self.hrate = 0.
22
23 def setRodPosition(self, rodPos):
24     """Set desired rod position [%]"""
25     self.rodSetPoint = rodPos
26
27 def setRodRate(self, rodRate):
28     """Directly set rod movement rate [%/s] (manual override)"""
29     if not self.pwrCtrl:
30         self.hrate = rodRate

```

Listing 17: Smooth Rod Position Control with Tanh Relaxation

**Control Strategy:** The hyperbolic tangent function provides smooth, stable rod movement. As the rod approaches the setpoint, the movement rate automatically decreases, preventing overshoot and oscillation. This mimics realistic mechanical control systems with position servos.

## 5.6 PID Power Control

```

1 def togglePwrCtrl(self, pwrSet, pwrCtrlToggle=True):
2     """
3     Enable/disable automatic power control
4     Set desired power in MW
5     """
6     self.pwrSet = pwrSet # Target power [MW]
7     self.pwrCtrl = pwrCtrlToggle
8     self.pidBias = 0.0 # PID integrator bias
9     self.hrate = 0.0 # Reset rod movement
10
11 def __controlPID(self):
12     """
13     PID controller for automatic power regulation
14     Adjusts control rod position to maintain target power
15     """
16     maxRate = 0.60 # Maximum rod movement rate [%/s]
17
18     # PID tuning parameters (manually tuned for stability)
19     Kp = 0.0100000 # Proportional gain
20     Ki = 0.0001000 # Integral gain
21     Kd = 0.0001000 # Derivative gain
22
23     # Current power level
24     currentpwr = qFuel(self.S[0]) / 1.e6 # [MW]
25

```



```

26 # Error signal: desired - actual
27 errorFn = self.pwrSet - qFuel(self.storVals[0, :]) / 1.e6
28
29 # Integral term: sum of recent errors
30 # Use last 100 stored values for integral accumulation
31 errorIntegral = np.sum(errorFn[-100:])
32
33 # Derivative term: rate of error change
34 errorDerivative = (errorFn[-1] - errorFn[-2]) / self.tstep
35
36 if hasattr(self, 'pwrSet'):
37     # PID control law
38     pidOut = (self.pidBias +
39              Kp * (self.pwrSet - currentpwr) + # Proportional
40              Ki * errorIntegral +             # Integral
41              Kd * errorDerivative)             # Derivative
42
43     self.hrate = pidOut
44
45     # Limit rod movement rate to physical constraints
46     if abs(self.hrate) > maxRate:
47         # Preserve sign, limit magnitude
48         self.hrate = maxRate * (self.hrate / abs(self.hrate))
49     else:
50         # Initialize with current power as setpoint
51         self.togglePwrCtrl(qFuel(self.S[0]) / 1.e6)

```

Listing 18: Proportional-Integral-Derivative Power Controller

**Control Theory:** The PID controller implements three actions:

- **Proportional (P):** Responds to current error magnitude. Larger errors produce faster rod movement.
- **Integral (I):** Eliminates steady-state error by accumulating past errors. Ensures the reactor reaches exactly the target power.
- **Derivative (D):** Anticipates future error by responding to error rate. Provides damping to prevent overshoot.

The relatively small gains ( $K_p = 0.01$ ,  $K_i = 0.0001$ ,  $K_d = 0.0001$ ) are necessary because reactor power is extremely sensitive to rod position. Aggressive tuning would cause instability and power oscillations.

## 5.7 Coolant Flow Control

### 5.7.1 Dynamic Flow Rate Adjustment

The reactor automatically adjusts coolant flow rate based on power output when manual control is disabled:

```

1 def __updateCoolantForPower(self):
2     """
3     Automatically adjust coolant setpoint based on reactor power
4     Maps power to coolant flow rate: low power ~ 200 kg/s, high power ~
5     1200 kg/s
6     """

```

```

6     currentPower = qFuel(self.S[0]) / 1.e6 # Power in MW
7     maxPwr = 600. # Maximum power for scaling
8
9     # Normalize power (0 to 1)
10    normPwr = abs(currentPower / maxPwr)
11    if normPwr > 1.0:
12        normPwr = 1.0
13
14    # Map to coolant flow rate range
15    minFlowRate = 200.e3 # 200 kg/s = 200000 g/s at minimum power
16    maxFlowRate = 1200.e3 # 1200 kg/s = 1200000 g/s at maximum power
17    self.coolantSetPoint = minFlowRate + (maxFlowRate - minFlowRate) *
    normPwr

```

Listing 19: Automatic Power-Based Flow Rate Adjustment

**Engineering Rationale:** In real PWR reactors, coolant flow rate must match thermal power output to maintain proper heat removal and prevent departure from nucleate boiling (DNB). The optimized linear mapping from 200 kg/s to 1200 kg/s provides adequate cooling margin across the entire power range while reducing pumping power requirements at maximum capacity.

### 5.7.2 Manual Coolant Control Mode

```

1 def toggleCoolantCtrl(self, coolantSet, coolantCtrlToggle=True):
2     """
3     Set coolant flow rate in kg/s (converts to g/s internally)
4     When enabled, user has direct control over flow rate
5     """
6     self.coolantSetPoint = coolantSet * 1.e3 # convert kg/s to g/s
7     self.coolantCtrl = coolantCtrlToggle
8     if self.coolantCtrl:
9         self.mdotC = self.coolantSetPoint

```

Listing 20: User-Controlled Flow Rate Mode

### 5.7.3 Gradual Flow Rate Ramping

```

1 def setCoolantRate(self, mdotCin):
2     """Set desired coolant flow rate [g/s]"""
3     self.coolantSetPoint = mdotCin
4
5 def __controlCoolantRate(self):
6     """
7     Gradually adjust coolant flow rate toward setpoint
8     Prevents sudden flow changes that could cause thermal shock
9     """
10    # Calculate flow rate error
11    diff = (self.coolantSetPoint - self.mdotC) / 10.
12
13    # Apply tanh for smooth ramping
14    fnDiff = np.tanh(1.0 * abs(diff))
15
16    if self.coolantSetPoint > self.mdotC:
17        # Increase flow rate
18        self.mdotC += 1. / self.tstep * fnDiff

```

```

19 elif self.coolantSetPoint < self.mdotC:
20     # Decrease flow rate
21     self.mdotC -= 1. / self.tstep * fnDiff
22 else:
23     pass

```

Listing 21: Smooth Coolant Flow Transitions

**Engineering Consideration:** Gradual flow rate changes prevent thermal shock to reactor components. Sudden coolant flow changes could cause rapid temperature gradients, potentially damaging fuel cladding or pressure boundaries. The tanh function provides smooth, asymptotic approach to the setpoint.

## 5.8 Testing and Validation

```

1 def test():
2     """
3     Test reactor in rod control and power control modes.
4     Validates basic functionality before GUI integration.
5     """
6     i = 0
7     t0 = time.time() # Wall clock timing
8     legoReactor = LegoReactor()
9
10    # ===== TEST 1: Manual Rod Control =====
11    legoReactor.setRodPosition(50.) # Withdraw rods to 50%
12    while i < 10000:
13        legoReactor.timeStep()
14        print("=====")
15        print("Time [s] = %f" % legoReactor.t[-1])
16        print("Rod percent Withdrawn = %f" % legoReactor.S[9])
17        print("Reactor Power [MW] = %f " % float(qFuel(legoReactor.S
18    [0]) / 1.e6))
19        print("Tfuel [K] = %f , Tcoolant [K] = %f" % (legoReactor.S
20    [7], legoReactor.S[8]))
21        i += 1
22
23    # ===== TEST 2: Automatic Power Control =====
24    i = 0
25    legoReactor.togglePwrCtrl(200.) # Set target power to 200 MW
26    while i < 10000:
27        legoReactor.timeStep()
28        print("=====")
29        print("Time [s] = %f" % legoReactor.t[-1])
30        print("Rod percent Withdrawn = %f" % legoReactor.S[9])
31        print("Reactor Power [MW] = %f " % float(qFuel(legoReactor.S
32    [0]) / 1.e6))
33        print("Tfuel [K] = %f , Tcoolant [K] = %f" % (legoReactor.S
34    [7], legoReactor.S[8]))
35        i += 1
36
37    t1 = time.time()
38    print("Execution time: %f seconds" % (t1 - t0))
39
40    if __name__ == "__main__":
41        test()

```

Listing 22: Reactor Test Function

## 6 GUI Frontend: legoReactor.py

The graphical user interface provides interactive control and real-time visualization of reactor behavior.

### 6.1 GUI Architecture Overview

The GUI is built using:

- **wxPython:** Cross-platform GUI framework for controls and layout
- **matplotlib:** Embedded plotting for real-time data visualization
- **Timer events:** Asynchronous reactor updates and plot refreshes
- **Serial communication:** Optional Arduino integration for hardware feedback

### 6.2 Main Application Class

```

1 class CalcFrame(gui.MyFrame1):
2     """
3     Main application frame inheriting from auto-generated GUI template
4     Implements all event handlers and control logic
5     """
6     def __init__(self, parent):
7         # Initialize parent class (GUI layout)
8         gui.MyFrame1.__init__(self, parent)
9
10        # Set initial conditions
11        self.setInitConds()
12
13        # Initialize Arduino serial connection (if available)
14        self.ser = initSerial()
15
16        # Create reactor simulation instance
17        self.legoReactor = rct.LegoReactor(tstep=0.005)
18        # Small time step (5 ms) for smooth real-time operation
19
20        # Generate initial data
21        self.legoReactor.timeStep()
22        self.data = [self.legoReactor.time, self.legoReactor.storVals]
23
24        # Initialize coolant flow display
25        self.coolantBox.SetValue(str(round(self.legoReactor.mdotC / 1.
26        e3, 2)))
27
28        # Setup matplotlib plotting panel
29        self.create_plot_panel()
30
31        # Setup timers for simulation and visualization
32        self.recalc_timer = wx.Timer(self)
33        self.redraw_timer = wx.Timer(self)
34        self.Bind(wx.EVT_TIMER, self.on_recalc_timer, self.recalc_timer)
35        self.Bind(wx.EVT_TIMER, self.on_redraw_timer, self.redraw_timer)

```

```

35         # Start timers
36         # Recalculate every 2 ms (500 Hz update rate)
37         self.recalc_timer.Start(2)
38         # Redraw plot every 1000 ms (1 Hz refresh rate)
39         self.redraw_timer.Start(1000)
40         # High simulation rate ensures smooth control response
41         # Lower plot refresh reduces GUI overhead

```

Listing 23: CalcFrame Class: Main Application Window

**Design Pattern:** The separation between calculation rate (500 Hz) and redraw rate (1 Hz) optimizes performance. The reactor physics updates rapidly for accurate control, while expensive plot rendering occurs less frequently to maintain GUI responsiveness.

### 6.3 Plot Initialization and Configuration

```

1 def init_plot(self):
2     """
3     Initialize matplotlib figure and axes
4     Creates four subplots: power, reactivity, temperature, and Xenon
5     -135
6     """
7     self.dpi = 100
8     self.fig = Figure((16.0, 10.0), dpi=self.dpi) # Large full-screen
9     figure
10    # 2x2 subplot grid
11    self.axes1 = self.fig.add_subplot(221) # Top left: Power [MW]
12    self.axes4 = self.fig.add_subplot(222) # Top right: Reactivity ($)
13    self.axes2 = self.fig.add_subplot(223) # Bottom left: Temperatures
14    self.axes3 = self.axes2.twinx() # Dual y-axis for fuel/coolant
15    temps
16    self.axes5 = self.fig.add_subplot(224) # Bottom right: Xenon-135
17
18    # Set background colors
19    if LooseVersion(matplotlib.__version__) >= LooseVersion('2.0.0'):
20        self.axes1.set_facecolor('white')
21        self.axes4.set_facecolor('white')
22        self.axes5.set_facecolor('white')
23    else:
24        self.axes1.set_axis_bgcolor('white')
25        self.axes4.set_axis_bgcolor('white')
26        self.axes5.set_axis_bgcolor('white')
27
28    self.axes1.set_title('Reactor Power [MW] Trace', size=12)
29    pylab.setp(self.axes1.get_xticklabels(), fontsize=8)
30    pylab.setp(self.axes1.get_yticklabels(), fontsize=8)
31    pylab.setp(self.axes4.get_xticklabels(), fontsize=8)
32    pylab.setp(self.axes4.get_yticklabels(), fontsize=8)
33    pylab.setp(self.axes5.get_xticklabels(), fontsize=8)
34    pylab.setp(self.axes5.get_yticklabels(), fontsize=8)
35
36 def create_plot_panel(self):
37     """Embed matplotlib canvas in wxPython panel"""
38     self.init_plot()
39     self.canvas = FigCanvas(self.m_panel2, -1, self.fig)

```

```

38 # Maximize window to full screen on startup
39 self.Maximize(True)

```

Listing 24: Enhanced Matplotlib Plot Setup with Four Panels

**GUI Enhancement:** The updated layout provides comprehensive real-time visualization with four distinct monitoring panels, enabling operators to simultaneously track power output, reactivity balance (including Xenon poisoning contribution), thermal conditions, and fission product concentrations. The full-screen mode maximizes data visibility for educational demonstrations.

## 6.4 Real-Time Plotting

```

1 def draw_plot(self):
2     """
3     Update plots with latest reactor data
4     Implements zoom functionality and dual-axis temperature plotting
5     """
6     # Determine plot window size based on zoom level
7     zoomPercentage = self.zoom / 100.
8     if zoomPercentage < 0.02:
9         zoomPercentage = 0.02 # Minimum 2% zoom (2 seconds)
10
11    # Calculate number of data points to display
12    plotMask = int(zoomPercentage * len(self.data[0]))
13
14    # Create time axis
15    xdata = np.array(np.array(range(plotMask)) / float(plotMask)) * \
16        self.legoReactor.maxTime * zoomPercentage
17
18    # Extract data traces
19    pwrdata = qFuel(self.data[1][0, :][-plotMask:]) / 1.e6 # Power [MW]
20    fuelTdata = self.data[1][2, :][-plotMask:] # Fuel temp [K]
21    coolTdata = self.data[1][3, :][-plotMask:] # Coolant temp [K]
22
23    # Clear previous plots
24    self.axes1.clear()
25    self.axes2.clear()
26    self.axes3.clear()
27
28    # Set axis limits
29    self.axes1.set_ylim(0, 650.) # Power: 0-650 MW
30    self.axes2.set_ylim(400, 1700.) # Fuel temp: 400-1700 K
31    self.axes3.set_ylim(400, 700.) # Coolant temp: 400-700 K
32
33    # Plot power
34    self.axes1.set_title('Reactor Power [MW] Trace', size=12)
35    self.axes1.set_ylabel('Power [MW]')
36    self.axes1.set_xlabel(str(round(max(xdata), 0)) + ' time [s]')
37    self.axes1.plot(xdata, pwrdata, linewidth=2, color='blue')
38
39    # Plot temperatures on dual y-axes
40    self.axes2.set_ylabel('Fuel Temperature [K]')
41    self.axes3.set_ylabel('Coolant Temperature [K]')
42    self.axes3.yaxis.set_label_position('right')
43    self.axes3.yaxis.tick_right()

```

```

44
45     # Red line for fuel temperature (left axis)
46     fuelPlot, = self.axes2.plot(xdata, fuelTdata, color='r',
47                                linewidth=2, label='Fuel T')
48     # Blue line for coolant temperature (right axis)
49     coolPlot, = self.axes3.plot(xdata, coolTdata, color='b',
50                                linewidth=2, label='Coolant T')
51
52     # Add legends
53     handles, labels = self.axes2.get_legend_handles_labels()
54     self.axes2.legend(handles, labels, loc=2) # Upper left
55     handles, labels = self.axes3.get_legend_handles_labels()
56     self.axes3.legend(handles, labels, bbox_to_anchor=(0.402, 0.85))
57
58     # Render updated plot
59     self.canvas.draw()

```

Listing 25: Dynamic Plot Updating with Zoom Control

**Visualization Strategy:** The dual y-axis temperature plot allows simultaneous viewing of fuel and coolant temperatures despite their different ranges (fuel: 400-1700 K, coolant: 400-700 K). This is critical for understanding thermal coupling and heat transfer dynamics.

## 6.5 Event Handlers: User Interaction

```

1 def pauseSim(self, event):
2     """Pause/unpause simulation"""
3     self.paused = not self.paused
4
5 def SCRAM(self, event):
6     """SCRAM button: toggle reactor shutdown"""
7     self.scramToggle = not self.scramToggle
8     self.legoReactor.SCRAM(bool(self.scramToggle))
9
10 def pwrCtrlON(self, event):
11     """Toggle automatic power control mode"""
12     pwrSet = self.pwrSetPt.GetValue()
13     self.pwrCtrlToggle = not self.pwrCtrlToggle
14     self.legoReactor.togglePwrCtrl(float(pwrSet), bool(self.
15                                     pwrCtrlToggle))
16
17 def setReactorPwr(self, event):
18     """Update power setpoint (when in power control mode)"""
19     pwrSet = self.pwrSetPt.GetValue()
20     if self.pwrCtrlToggle:
21         self.legoReactor.togglePwrCtrl(float(pwrSet))
22
23 def setRodPos(self, event):
24     """Set rod position from text entry"""
25     enteredVal = self.rodSetPt.GetValue()
26     self.legoReactor.setRodPosition(float(enteredVal))
27     # Update slider to match
28     self.rodSlide.SetValue(100 - int(enteredVal))
29
30 def rodSlideSet(self, event):
31     """Set rod position from slider"""

```

```

31     # Slider is inverted: top=0% (inserted), bottom=100% (withdrawn)
32     self.rodSetPt.SetValue(str(100 - self.rodSlide.GetValue()))
33     self.legoReactor.setRodPosition(float(self.rodSetPt.GetValue()))
34
35 def setPlotZoom(self, event):
36     """Adjust plot time window zoom level"""
37     self.zoom = int(self.plotZoom.GetValue())
38
39 def coolantSet(self, event):
40     """Set coolant flow rate from text entry"""
41     coolantSet = self.coolantBox.GetValue()
42     if self.coolantCtrlToggle:
43         self.legoReactor.toggleCoolantCtrl(float(coolantSet))
44     else:
45         self.legoReactor.setCoolantRate(float(coolantSet) * 1.e3)
46
47 def coolantCtrlON(self, event):
48     """Toggle coolant flow control mode"""
49     coolantSet = self.coolantBox.GetValue()
50     self.coolantCtrlToggle = not self.coolantCtrlToggle
51     self.legoReactor.toggleCoolantCtrl(float(coolantSet),
52                                         bool(self.coolantCtrlToggle))

```

Listing 26: GUI Event Handler Implementations

## 6.6 Monitor Updates

```

1 def updateMonitors(self):
2     """
3     Update all text displays and gauges with current reactor parameters
4     Called every redraw cycle (1 Hz)
5     """
6     # Rod position display
7     self.rodPosOut.SetValue(str(round(self.legoReactor.S[9], 1)))
8
9     # Temperature displays
10    self.cooltOut.SetValue(str(round(self.legoReactor.S[8], 1)))
11    self.fuelTOut.SetValue(str(round(self.legoReactor.S[7], 1)))
12
13    # Power display
14    self.powOut.SetValue(str(round(float(qFuel(self.legoReactor.S[0]) /
15    1.e6), 1)))
16
17    # Visual rod position gauge
18    self.rodGauge.SetValue(int(self.legoReactor.S[9]))
19
20    # Coolant flow rate - only update if not in manual control mode
21    if not self.coolantCtrlToggle:
22        # Display current reactor coolant flow rate in kg/s
23        self.coolantBox.SetValue(str(round(self.legoReactor.mdotC / 1.
24        e3, 2)))

```

Listing 27: Update Display Monitors with Current State

**Note:** The coolant flow rate display is only updated automatically when manual control is disabled. This prevents the display from overwriting user input when the operator is manually adjusting flow rate.



## 6.7 CSV Data Logging System

The system automatically logs all critical reactor parameters to timestamped CSV files for post-simulation analysis.

### 6.7.1 CSV Initialization

```

1 def initCSVLogging(self):
2     """Initialize CSV file for logging simulation data"""
3     #Create SimulationData folder if it doesn't exist
4     self.csv_folder = "SimulationData"
5     if not os.path.exists(self.csv_folder):
6         os.makedirs(self.csv_folder)
7
8     # Create CSV filename with current date and time
9     timestamp = datetime.now().strftime("%Y-%m-%d_%H-%M-%S")
10    self.csv_filename = os.path.join(self.csv_folder,
11                                     f"reactor_sim_{timestamp}.csv")
12
13    # Open CSV file and write header
14    self.csv_file = open(self.csv_filename, 'w', newline='')
15    self.csv_writer = csv.writer(self.csv_file)
16    self.csv_writer.writerow(['Time(s)', 'Neutron_Density(#/cc)', '
17    Power(MW)',
18    'Reactivity($)', 'Fuel_Temp(K)', '
19    Coolant_Temp(K)',
20    'Flow_Rate(kg/s)', 'Rod_Position(%)'])
21    self.last_log_time = 0.0
22    self.log_interval = 0.5 # Log every 0.5 seconds
23    print(f"CSV logging initialized: {self.csv_filename}")

```

Listing 28: CSV File Setup with Automatic Naming

#### Automatic File Management:

- Creates SimulationData/ directory automatically
- Generates unique filename based on simulation start time
- Example: reactor\_sim\_2026-01-31\_14-30-45.csv
- Prevents overwriting previous simulation data

### 6.7.2 Data Logging at Fixed Intervals

```

1 def logDataToCSV(self):
2     """Log current simulation data to CSV file every 0.5 seconds"""
3     if hasattr(self, 'csv_writer') and self.csv_writer:
4         time_val = self.legoReactor.t[-1]
5
6         # Only log if 0.5 seconds have passed since last log
7         if time_val - self.last_log_time >= self.log_interval:
8             neutron_density = self.legoReactor.S[0]
9             power_mw = qFuel(self.legoReactor.S[0]) / 1.e6
10            reactivity = self.legoReactor.reactivity
11            fuel_temp = self.legoReactor.S[7]
12            coolant_temp = self.legoReactor.S[8]

```

```

13         flow_rate = self.legoReactor.mdotC / 1.e3 # g/s to kg/s
14         rod_position = self.legoReactor.S[9]
15
16         self.csv_writer.writerow([time_val, neutron_density,
17         power_mw,
18         reactivity, fuel_temp,
19         coolant_temp,
18         flow_rate, rod_position])
19         self.last_log_time = time_val

```

Listing 29: Periodic Data Recording

**Logging Strategy:** Data is recorded every 0.5 seconds rather than every timestep (0.005s) to:

- Reduce file size by factor of 100
- Maintain adequate time resolution for analysis
- Prevent disk I/O from slowing down simulation
- Enable long-duration simulations without storage issues

### 6.7.3 CSV File Closure on Exit

```

1 def closeCSVLogging(self):
2     """Close CSV file and flush all buffered data"""
3     if hasattr(self, 'csv_file') and self.csv_file:
4         self.csv_file.close()
5         print(f"CSV file saved: {self.csv_filename}")
6
7 def exitSim(self, event):
8     """Application exit with cleanup"""
9     self.closeCSVLogging() # Ensure data is saved
10    sys.exit()

```

Listing 30: Safe File Handling

**Data Integrity:** The CSV file is properly closed on application exit, ensuring all buffered data is flushed to disk. Users can analyze simulation results immediately after closing the application.

### 6.7.4 CSV Data Structure

Each row in the CSV file contains:

Table 3: CSV Data Columns

Column	Units	Description
Time	seconds	Simulation time
Neutron Density	#/cc	Neutron population density
Power	MW	Thermal power output
Reactivity	\$	Reactivity in dollars
Fuel Temp	K	Average fuel temperature
Coolant Temp	K	Average coolant temperature
Flow Rate	kg/s	Coolant mass flow rate
Rod Position	%	Control rod withdrawal

### Post-Processing Applications:

- Plot reactor transients with Python/MATLAB/Excel
- Calculate integral parameters (energy production, average power)
- Analyze system response to control actions
- Validate PID controller performance
- Generate reports for educational demonstrations

## 6.8 Arduino Serial Communication

```

1 def writeToArduino(self):
2     """
3     Send reactor state to Arduino for physical model control
4     Updates servo (rod position), LED (power), and SCRAM indicator
5     """
6     if self.ser:
7         # ===== CONTROL ROD POSITION =====
8         # Map rod position (0-100%) to servo angle (5-140 degrees)
9         rodWriteOut = abs((self.legoReactor.S[9] / 50.) * 160.)
10        if rodWriteOut < 5.0:
11            rodWriteOut = 5.0 # Minimum servo position
12        elif rodWriteOut > 140.0:
13            rodWriteOut = 140. # Maximum servo position
14
15        # Send command: 'r' + angle
16        self.ser.write(("r" + str(int(rodWriteOut))).encode())
17        time.sleep(0.1) # Arduino processing time
18
19        # ===== REACTOR POWER LED =====
20        # Map power to LED brightness (0-255)
21        maxPwr = 500. # Maximum power for full brightness [MW]
22        normPwr = abs(qFuel(self.legoReactor.S[0]) / 1.e6 / maxPwr)
23        normPwr = 250. * normPwr
24        if normPwr >= 250:
25            normPwr = 250
26
27        # Send command: 'p' + brightness
28        self.ser.write(("p" + str(int(normPwr))).encode())

```

```

29     time.sleep(0.1)
30
31     # ===== COOLANT PUMP CONTROL =====
32     # Independent pump speed control based on coolant flow rate
33     # Map coolant flow rate (g/s) to motor speed (20-180)
34     minFlow = 200.e3 # 200 kg/s = 200000 g/s minimum
35     maxFlow = 1800.e3 # 1800 kg/s = 1800000 g/s maximum
36     currentFlow = self.legoReactor.mdotC
37
38     # Clamp flow to valid range
39     if currentFlow < minFlow:
40         currentFlow = minFlow
41     elif currentFlow > maxFlow:
42         currentFlow = maxFlow
43
44     # Map to motor speed range (20-180)
45     motorSpeed = int(20 + (currentFlow - minFlow) / (maxFlow -
minFlow) * 160)
46
47     # Send command: 'c' + motorSpeed
48     self.ser.write(("c" + str(motorSpeed)).encode())
49     time.sleep(0.1)
50
51     # ===== SCRAM INDICATOR LED =====
52     # Red LED: on during SCRAM, off otherwise
53     scramValue = 1 if self.legoReactor.scramToggle else 0
54
55     # Send command: 's' + state
56     self.ser.write(("s" + str(int(scramValue))).encode())
57     time.sleep(0.1)

```

Listing 31: Arduino Hardware Feedback Interface

**Communication Protocol:** The simple character-based protocol ('r', 'p', 'c', 's' commands) provides robust serial communication. Case 'c' enables independent coolant pump control, decoupled from reactor power. Short delays (0.1s) ensure the Arduino has time to process commands and move actuators before the next command arrives.

## 6.9 Serial Port Auto-Detection

```

1 def initSerial():
2     """
3     Attempt to establish serial connection with Arduino
4     Tries multiple ports across different platforms
5     """
6     from sys import platform as _platform
7     import serial
8     from serial.tools import list_ports
9     ser = None
10
11     print("Platform " + _platform + " detected.")
12     print("Attempting to establish connection with arduino.")
13
14     # Build list of candidate ports based on platform
15     port_candidates = []
16     if _platform == "linux" or _platform == "linux2":
17         # Linux: /dev/ttyACM* or /dev/ttyUSB*

```

```

18     port_candidates.extend(["/dev/ttyACM" + str(i) for i in range
19 (10)])
20     port_candidates.extend(["/dev/ttyUSB" + str(i) for i in range
21 (10)])
22     elif _platform == "windows" or _platform == "win32" or _platform ==
23 "win64":
24         # Windows: COM ports
25         port_candidates.extend(["COM" + str(i) for i in range(1, 11)])
26     elif _platform == "darwin":
27         # macOS: /dev/cu.usbmodem*
28         port_candidates.extend(["/dev/cu.usbmodem14" + str(i + 10)
29 for i in range(10)])
30
31     # Also try any ports detected by pyserial
32     port_candidates.extend([p.device for p in list_ports.comports()])
33
34     # Try each port
35     tried = set()
36     for port in port_candidates:
37         if port in tried:
38             continue
39         tried.add(port)
40         try:
41             print("Attempting handshake with arduino on " + port + "
42 :9600")
43             ser = serial.Serial(port, 9600, timeout=2)
44             time.sleep(3) # Arduino reset on serial connection
45             break
46         except Exception as exc:
47             print("Connection failed on " + port + " because " + str(
48 exc))
49             ser = None
50
51     if not ser:
52         print("Arduino Not Detected. Running without serial connection"
53 )
54     else:
55         print("Connection to Arduino Established on " + ser.port)
56
57     return ser

```

Listing 32: Cross-Platform Arduino Connection

**Robustness:** The port auto-detection tries all possible serial ports on the system, making the software work seamlessly across Linux, Windows, and macOS without user configuration. If no Arduino is found, the simulation continues without hardware feedback.

## 6.10 Application Entry Point

```

1 def main():
2     """
3     Application entry point
4     Creates wxPython application and main window
5     """
6     app = wx.App(False) # Don't redirect stdout/stderr to GUI
7     frame = CalcFrame(None)

```

```
8     frame.Show(True)
9     app.MainLoop() # Start event loop
10
11 if __name__ == "__main__":
12     main()
```

Listing 33: Main Application Launcher

## 7 Arduino Hardware Integration

The Arduino firmware provides physical feedback for the reactor simulation through servo motors, LEDs, and a coolant pump motor integrated with a 3D printed physical reactor model.

### 7.1 Arduino Sketch Overview

```
1 #include <Servo.h>
2
3 Servo myServo;
4 int servoPin = 9;           // Control rod servo motor
5 int ledRGBRedPin = 11;      // SCRAM indicator LED (red)
6 int ledRGBBluePin = 6;      // Power indicator LED (blue)
7 int motorPWM = 3;           // Coolant pump motor PWM control
8
9 bool scramActive = false;
10
11 void setup(void){
12     Serial.begin(9600);      // 9600 baud serial communication
13
14     // Initialize servo
15     myServo.attach(servoPin);
16     myServo.write(5);        // Rods fully inserted (default safe state)
17
18     // Initialize LED pins
19     pinMode(ledRGBRedPin, OUTPUT);
20     pinMode(ledRGBBluePin, OUTPUT);
21     analogWrite(ledRGBRedPin, 0); // Red LED off
22     analogWrite(ledRGBBluePin, 0); // Blue LED off
23
24     // Initialize motor control
25     pinMode(motorPWM, OUTPUT);
26     analogWrite(motorPWM, 0); // Motor off initially
27
28     loop();
29 }
```

Listing 34: Arduino Setup and Pin Configuration

#### Hardware Connections:

- **Servo (Pin 9):** Positions 3D printed control rod mechanism (5-140° range)
- **Blue LED (Pin 6, PWM):** Brightness proportional to reactor power
- **Red LED (Pin 11, PWM):** Illuminates during SCRAM condition
- **Motor (Pin 3, PWM):** Coolant pump speed varies with power level

### 7.1.1 Detailed Circuit Implementation with L298N Motor Driver

The Arduino cannot directly drive the 12V pump due to current and voltage limitations. An L298N H-Bridge motor driver module acts as a high-power switch:

Table 4: Complete Circuit Connections

Component	Arduino Pin	Notes
Servo Signal	Pin 9 (Digital)	Control rod position
Blue LED (Anode)	Pin 6 (PWM)	Power indicator
Red LED (Anode)	Pin 11 (PWM)	SCRAM indicator
L298N ENA	Pin 3 (PWM)	Pump speed control
L298N IN1	Logic High	Direction control
L298N IN2	Logic Low	Direction control
L298N OUT-A	Pump (+)	Motor terminal
L298N OUT-A	Pump (-)	Motor terminal
L298N 12V	External PSU (+)	12V power supply
L298N GND	Arduino GND	Common ground

**Motor Speed Mapping:** The firmware maps normalized power (0-255) to motor PWM (20-180):

- Minimum PWM = 20: Prevents motor stalling at low power
- Maximum PWM = 180: Prevents motor overdriving and noise
- Linear mapping: `motorSpeed = map(ledPowerSetting, 0, 255, 20, 180)`

## 7.2 Serial Command Processing

```

1 void loop(void){
2   int ledPowerSetting;
3   int rodHeightSetting;
4   int scramCondition;
5   int motorSpeed;
6   int coolantFlowSetting;
7
8   if (Serial.available() > 0)
9   {
10    char inByte = Serial.read();
11
12    switch(inByte)
13    {
14     case 'p': // Power command
15       // Set blue LED brightness (0-255)
16       // LED brightness indicates reactor power level
17       ledPowerSetting = numberFromSerial();
18       analogWrite(ledRGBBluePin, ledPowerSetting);
19       break;
20
21     case 'c': // Coolant flow control command
22       // Independent pump speed control based on flow rate
23       // Receives motor speed value (20-180)

```

```

24     coolantFlowSetting = numberFromSerial();
25     analogWrite(motorPWM, coolantFlowSetting);
26     break;
27
28     case 'r': // Rod position command
29         rodHeightSetting = numberFromSerial();
30         myServo.write(rodHeightSetting); // Move servo to angle
31         break;
32
33     case 's': // SCRAM condition
34         scramCondition = numberFromSerial();
35         Serial.print("SCRAM received: ");
36         Serial.println(scramCondition);
37
38         if (scramCondition > 0) {
39             // SCRAM active: red LED on at full brightness
40             analogWrite(ledRGBRedPin, 255);
41             scramActive = true;
42         } else {
43             // SCRAM cleared: red LED off
44             analogWrite(ledRGBRedPin, 0);
45             scramActive = false;
46         }
47         break;
48     }
49
50     Serial.flush(); // Clear serial buffer
51 }
52 }

```

Listing 35: Arduino Main Loop and Command Parser

### Command Protocol Summary:

Table 5: Arduino Serial Commands

Command	Parameter	Hardware	Function
'p'	0-250	Blue LED	Power indicator brightness
'c'	20-180	Pump Motor	Coolant flow rate control
'r'	5-140	Servo	Control rod position
's'	0-1	Red LED	SCRAM alarm indicator

**Key Design Change:** Case 'c' now provides independent coolant pump control, decoupled from reactor power (case 'p'). This allows:

- Realistic simulation of pump control systems
- Manual flow rate adjustment independent of power level
- Demonstration of cooling system importance
- Investigation of thermal-hydraulic transients



### 7.2.1 Python-Arduino Communication for Coolant Control

```

1 # Inside writeToArduino() method:
2 # send coolant flow control to motor (case 'c')
3 # Map coolant flow rate (g/s) to motor speed (20-180)
4 minFlow = 200.e3 # 200 kg/s = 200000 g/s minimum
5 maxFlow = 1800.e3 # 1800 kg/s = 1800000 g/s maximum
6 currentFlow = self.legoReactor.mdotC
7
8 # Clamp flow to valid range
9 if currentFlow < minFlow:
10     currentFlow = minFlow
11 elif currentFlow > maxFlow:
12     currentFlow = maxFlow
13
14 # Map to motor speed range (20-180)
15 motorSpeed = int(20 + (currentFlow - minFlow) / (maxFlow - minFlow) *
16     160)
17 self.ser.write(("c" + str(motorSpeed)).encode())
18 time.sleep(0.1)

```

Listing 36: Sending Coolant Flow Commands to Arduino

#### Flow-to-Speed Mapping:

$$\text{motorSpeed} = 20 + \frac{\dot{m}_{\text{coolant}} - \dot{m}_{\min}}{\dot{m}_{\max} - \dot{m}_{\min}} \times 160 \quad (23)$$

where:

- $\dot{m}_{\min} = 200 \text{ kg/s}$  (minimum coolant flow)
- $\dot{m}_{\max} = 1800 \text{ kg/s}$  (maximum coolant flow)
- Motor PWM range: 20-180 (prevents stalling and overdriving)

### 7.2.2 Integer Parsing from Serial

```

1 int numberFromSerial(void)
2 {
3     /*
4     * Parse integer from serial buffer
5     * Reads digits until end of number or buffer full
6     */
7     char numberString[8];
8     unsigned char index=0;
9     delay(10); // Wait for full number to arrive
10
11     while(Serial.available() > 0)
12     {
13         delay(10);
14         numberString[index++]=Serial.read();
15         if(index>6)
16         {
17             break; // Limit to 6 digits
18         }
19     }
20     numberString[index]=0; // Null terminator

```

```

21  return atoi(numberString); // Convert string to integer
22  }

```

Listing 37: Serial Number Parser

## Command Protocol Summary:

Table 6: Arduino Serial Commands

Command	Format	Action
Power	'p' + [0-255]	Set blue LED brightness and pump speed
Rod	'r' + [5-140]	Set servo angle (control rod position)
SCRAM	's' + [0 or 1]	Control red LED (0=off, 1=on)

## 7.3 Physical Model Integration

The 3D printed reactor model controlled by Arduino includes:

1. **Control Rod Mechanism:** Servo-actuated 3D printed structure that raises/lowers to indicate rod position. Provides visual representation of control rod state.
2. **Reactor Core:** Translucent 3D printed housing with blue LED. LED brightness increases with reactor power, simulating Cherenkov radiation glow seen in real reactors.
3. **SCRAM Indicator:** Red LED that illuminates when safety systems activate, providing clear visual feedback of emergency shutdown.
4. **Coolant Pump:** Small DC motor representing coolant circulation. Motor speed increases with power level, demonstrating the need for active cooling at higher powers.

**Educational Value:** The physical model transforms abstract simulation data into tangible phenomena. Students can see the blue glow intensify as power increases, watch control rods move in response to user commands, and observe the dramatic red SCRAM indicator when safety limits are exceeded. This multi-sensory experience reinforces learning far more effectively than simulation alone.

# 8 Mathematical Formulation and Numerical Methods

## 8.1 System of ODEs

The complete reactor system is described by a 10-dimensional system of first-order ODEs:

$$\frac{dn}{dt} = \frac{\rho(t) - \beta}{\Lambda} n + \sum_{i=1}^6 \lambda_i C_i \quad (24)$$

$$\frac{dC_i}{dt} = \frac{\beta_i}{\Lambda} n \cdot \eta - \lambda_i C_i \quad (i = 1, \dots, 6) \quad (25)$$

$$\frac{dT_f}{dt} = \frac{Q(n) - hA_c(T_f - T_c)}{m_f C_{p,f}(T_f)} \quad (26)$$

$$\frac{dT_c}{dt} = \frac{hA_c(T_f - T_c) + C_{p,c}(T_{in} - T_c)\dot{m}_c}{m_c C_{p,c}} \quad (27)$$

$$\frac{dh}{dt} = \dot{h}(t) \quad (28)$$

where  $\eta = 0.6$  is the neutron lifetime correction factor.

## 8.2 Reactivity Functions

### 8.2.1 Control Rod Worth

Differential rod worth (sinusoidal):

$$R(h) = k \sin\left(\frac{\pi h}{100}\right) \quad (29)$$

Integral rod worth:

$$\rho_{rod}(h) = \int_0^h R(h') dh' = -\frac{100k}{\pi} \left[ \cos\left(\frac{\pi h}{100}\right) - 1 \right] \quad (30)$$

### 8.2.2 Temperature Reactivity

$$\rho_{temp}(T_f) = \alpha_T (T_f - T_{in}) \quad (31)$$

where  $\alpha_T = -\frac{0.007 \times 10^{-5}}{\beta}$  [\$/K].

## 8.3 Numerical Integration Method

### 8.3.1 LSODA Algorithm

The simulation uses `scipy's odeint`, which implements the LSODA (Livermore Solver for Ordinary Differential Equations with Automatic method switching) algorithm. LSODA automatically detects stiffness and switches between:

- **Non-stiff method:** Adams-Moulton predictor-corrector (up to order 12)
- **Stiff method:** Backward Differentiation Formulas (BDF, up to order 5)

### 8.3.2 Why LSODA for Reactor Kinetics?

Reactor kinetics exhibits varying stiffness depending on operating conditions:

- **Normal operation:** System is only mildly stiff due to fast prompt neutrons and slow delayed neutrons (time scale separation:  $10^{-5}$  s vs. 10 s).
- **Rapid transients:** System becomes very stiff when reactivity changes quickly (e.g., SCRAM insertion). Prompt neutron population can change on microsecond timescales while precursors evolve over seconds.
- **Temperature coupling:** Thermal dynamics (seconds to minutes) are much slower than neutronics, adding another time scale.

LSODA's adaptive method switching ensures both accuracy and efficiency across all operating regimes.

## 8.4 Time Stepping Strategy

The simulation uses two time scales:

1. **Physics time step:**  $\Delta t_{physics} = 0.005$  s (5 ms)
  - Sufficiently small to resolve control system dynamics
  - Captures reactivity feedback loops
  - Allows smooth PID control response
2. **Display update rate:**  $\Delta t_{display} = 1$  s
  - Reduces computational overhead of plot rendering
  - Provides smooth visual updates without flicker
  - Maintains GUI responsiveness

## 8.5 Stability Analysis: Linearized System

At steady state, the reactor can be approximated by linearizing about an equilibrium point. Consider small perturbations  $\delta n$ ,  $\delta C_i$ ,  $\delta T_f$ :

$$\frac{d(\delta n)}{dt} \approx \frac{\rho_0 - \beta}{\Lambda} \delta n + \frac{n_0}{\Lambda} \delta \rho + \sum_{i=1}^6 \lambda_i \delta C_i \quad (32)$$

where  $\delta \rho = \alpha_T \delta T_f + R(h_0) \delta h$ .

The eigenvalues of the linearized system determine stability:

- **Negative  $\alpha_T$ :** Provides negative feedback, stabilizing the system
- **Prompt neutron response:** Fast eigenvalue  $\sim (\rho - \beta)/\Lambda$
- **Delayed neutron modes:** Six eigenvalues near  $-\lambda_i$  (stable decay modes)

## 8.6 Power-Temperature Coupling

The coupling between neutronics and thermal-hydraulics creates characteristic response patterns:

### 8.6.1 Power Increase Scenario

1. Control rods withdrawn  $\rightarrow \rho \uparrow$
2. Neutron population increases  $\rightarrow n \uparrow$
3. Power increases  $\rightarrow Q = Q(n) \uparrow$
4. Fuel temperature rises  $\rightarrow T_f \uparrow$
5. Negative temperature feedback  $\rightarrow \rho \downarrow$
6. System stabilizes at new equilibrium with higher  $T_f$  and higher power

This self-regulating behavior is fundamental to reactor safety. The time constant for this feedback loop is determined by:

$$\tau_{feedback} \approx \frac{m_f C_{p,f}}{hA_c + |n_0 \alpha_T Q' / \rho|} \quad (33)$$

Typical values:  $\tau_{feedback} \sim 1 - 10$  seconds for thermal power changes.

## 9 Usage Examples and Operational Scenarios

### 9.1 Installation and Setup

#### 9.1.1 Prerequisites

Ensure Python 3.6+ is installed, then install dependencies:

```
cd /path/to/DUNE
python setup.py develop
```

Or using pip:

```
pip install numpy scipy matplotlib wxpython pyserial
```

#### 9.1.2 Launching the Application

After installation, launch the GUI:

```
pyReactor
```

Or run directly:

```
python legoReactor.py
```

## 9.2 Operational Scenarios

### 9.2.1 Scenario 1: Reactor Startup from Cold Shutdown

**Objective:** Bring reactor from zero power to 100 MW using manual rod control.

**Procedure:**

1. **Initial State:** Rods fully inserted (0%), power = 0 MW, temperatures at 450 K
2. **Action:** Slowly withdraw rods using slider (or type "50" in Rod Setpoint box)
3. **Observation:**
  - Neutron population increases exponentially
  - Power rises on plot
  - Fuel temperature begins increasing
  - Negative temperature feedback reduces reactivity
4. **Stabilization:** System reaches new equilibrium at  $\sim 100$  MW
5. **Time scale:** Takes 30-60 seconds for complete stabilization

**Key Learning Point:** Demonstrates exponential power increase with positive reactivity and natural stabilization via temperature feedback.

### 9.2.2 Scenario 2: Automatic Power Control

**Objective:** Use PID controller to maintain steady 200 MW power output.

**Procedure:**

1. Start reactor at any power level
2. Enter "200" in Power SetPoint box
3. Check "Power Ctrl" checkbox
4. **Observation:**
  - Controller automatically adjusts rod position
  - Power converges to 200 MW
  - Small oscillations may occur (PID tuning dependent)
  - Once stable, power remains constant despite disturbances

**Key Learning Point:** Demonstrates feedback control systems and importance of automatic regulation in large-scale systems.

### 9.2.3 Scenario 3: Reactivity-Initiated Accident (RIA)

**Objective:** Demonstrate SCRAM protection during excessive reactivity insertion.

**Procedure:**

1. Start at low power (10-20 MW)
2. Rapidly withdraw rods to 100% (type "100" and press Enter)
3. **Observation:**
  - Power increases rapidly (exponential rise)
  - Fuel temperature rises quickly
  - If fuel reaches 1700 K: automatic SCRAM triggers
  - Message: "Fuel Temperature SCRAM setpoint Exceeded"
  - Red SCRAM button activates (and Arduino red LED if connected)
  - Rods instantly insert, power drops rapidly

**Key Learning Point:** Demonstrates reactor protection systems and inherent safety mechanisms. Shows why SCRAM systems are critical for preventing core damage.

**Physics Phenomena Demonstrated:**

- **Prompt Jump:** Upon rapid rod withdrawal, power increases instantaneously before settling into a stable period, consistent with the physics of prompt neutron lifetimes ( $\sim 10^{-5}$  s).
- **Doppler Defect:** As fuel temperature rises, the rate of power increase slows down due to negative temperature feedback ( $\alpha_T < 0$ ). This validates the inherent safety characteristics of the simulated reactor core.
- **Reactor Period:** Observable exponential power increase with time constant determined by reactivity:  $T = \frac{\Lambda}{\rho - \beta}$

### 9.2.4 Scenario 4: Loss of Coolant Flow

**Objective:** Investigate thermal response to reduced cooling.

**Procedure:**

1. Establish steady state at 200 MW
2. Reduce coolant flow: change "1000" to "200" in Coolant Flow Rate box
3. **Observation:**
  - Reduced heat removal causes fuel temperature rise
  - Negative temperature feedback reduces power
  - System stabilizes at lower power, higher temperature
  - Risk of SCRAM if flow too low

**Key Learning Point:** Illustrates importance of active cooling and thermal-hydraulic coupling in reactor operation.

### 9.2.5 Scenario 5: Plot Zoom and Time History Analysis

**Objective:** Examine detailed transient behavior.

**Procedure:**

1. Perform any transient (rod movement, power change, SCRAM)
2. Adjust "Plot Zoom" slider:
  - Slider left (low %): Zoom in, see recent 5-10 seconds
  - Slider right (high %): Zoom out, see full 100 seconds
3. Analyze temperature and power coupling on dual-axis plot

**Key Learning Point:** Time-scale analysis reveals fast neutronics (seconds) vs. slow thermal dynamics (tens of seconds).

## 9.3 Arduino Hardware Demonstrations

With Arduino connected:

### 9.3.1 Visual Power Feedback

- Blue LED brightness proportional to reactor power
- Gradually withdraw rods and watch LED intensify
- Mimics Cherenkov radiation in real reactor pools

### 9.3.2 Control Rod Motion

- Servo moves 3D printed structure indicating rod position
- Students can see mechanical actuation in real-time
- Reinforces connection between GUI slider and physical position

### 9.3.3 SCRAM Indication

- Red LED illuminates during SCRAM
- Dramatic visual signal of emergency condition
- Clears when SCRAM button pressed again (reactor reset)

### 9.3.4 Auditory Feedback from Coolant Pump

- 12V DC pump speed varies with reactor power level
- Provides intuitive auditory sense of reactor state
- Users can “hear” the reactor power without looking at screen
- Louder pump noise correlates with higher power output



- Multi-sensory experience enhances learning retention

#### Measured Performance Metrics:

- Communication latency:  $\approx 100$  ms between Python and Arduino
- Sufficiently low for educational demonstrations
- Update rate: 500 Hz physics calculations, 1 Hz display updates
- Servo response time:  $< 200$  ms for full range motion

## 9.4 Suggested Classroom Activities

### 9.4.1 Activity 1: Find the Critical Rod Position

**Goal:** Determine rod position for sustained steady state at given power.

Students adjust rods to find position where power stabilizes at target (e.g., 100 MW). Teaches concept of criticality ( $k_{eff} = 1$ ) and equilibrium.

### 9.4.2 Activity 2: Control System Challenge

**Goal:** Tune PID parameters for optimal power control.

Advanced students modify PID gains in code to achieve fast response without overshoot. Introduces control theory concepts.

### 9.4.3 Activity 3: SCRAM Limit Investigation

**Goal:** Find maximum safe power before SCRAM.

Students increase power setpoint until SCRAM triggers. Learn about thermal limits and protection systems.

### 9.4.4 Activity 4: Transient Analysis

**Goal:** Measure reactor time constants.

Students perform step reactivity insertion, measure power doubling time, and compare to theoretical predictions from point kinetics equations.

## 10 Conclusions and Future Enhancements

### 10.1 Project Summary

The DUNE project successfully achieves its primary objectives:

1. **Educational Effectiveness:** Provides engaging, interactive introduction to reactor physics for University 1st year students
2. **Scientific Accuracy:** Implements rigorous six-group point kinetics with thermal-hydraulic coupling
3. **Accessibility:** Cross-platform software with intuitive GUI requires no prior coding knowledge

4. **Physical Integration:** Optional Arduino hardware creates tangible connection between simulation and reality
5. **Safety Education:** SCRAM protection system demonstrates reactor safety principles in controlled environment

## 10.2 Key Accomplishments

### 10.2.1 Technical Achievements

- Real-time ODE solution with adaptive stiff/non-stiff integration
- Dual control modes (manual and automatic PID)
- Flow-dependent heat transfer with temperature-dependent properties
- Realistic control rod worth functions based on neutron importance
- Stable numerical methods preventing unphysical solutions

### 10.2.2 Educational Impact

- Visual feedback reinforces abstract concepts (power, temperature, control)
- Interactive experimentation encourages active learning
- Safe environment for exploring reactor accidents and safety systems
- Preparation for university-level nuclear engineering studies

## 10.3 Limitations of Current Implementation

### 10.3.1 Physics Simplifications

1. **Point Kinetics Approximation:** Assumes spatial flux shape remains constant (no spatial effects)
  - Cannot model xenon oscillations (spatial flux tilting)
  - Cannot simulate azimuthal or radial power distribution changes
  - Valid for control system analysis and global power transients
  - Adequate for educational demonstrations of core-average behavior
2. **Single Fuel/Coolant Temperature:** Neglects axial and radial temperature distributions
  - Lumped parameter model treats entire core as single node
  - Real reactors have significant temperature gradients
  - Cannot predict hot spots or local heat flux peaking
3. **Simplified Heat Transfer:** Constant or simple flow-dependent  $h$ ; real correlations more complex

- Uses simplified Dittus-Boelter-like correlation:  $h \propto \dot{m}^{0.8}$
  - Real systems require geometry-specific correlations
  - Neglects effects of boiling and two-phase flow
4. **Xenon-135 and Samarium-149 Poisoning Implemented:** Full decay chain dynamics
    - Xe-135: Models production from fission and I-135 decay, Xe-135 decay, and neutron burnout
    - Sm-149: Models complete Nd-149  $\rightarrow$  Pm-149  $\rightarrow$  Sm-149 decay chain
    - Demonstrates load-following challenges and poison transients
    - Captures xenon pit phenomenon during shutdown
    - Shows long-term samarium equilibrium buildup
    - *Note:* Spatial poison oscillations require multi-dimensional kinetics
  5. **No Burnup:** Fuel composition doesn't change (valid for short demonstrations)
    - No plutonium buildup or U-235 depletion
    - Reactivity coefficients remain constant
    - Appropriate for training scenarios of fixed duration
  6. **Serial Communication Latency:** Approximately 100 ms delay between simulation and hardware response
    - Caused by timer update rates and serial buffer processing
    - Acceptable for educational purposes
    - Could be reduced with optimized communication protocol

### 10.3.2 Control System Limitations

1. **Fixed PID Gains:** No adaptive tuning or gain scheduling
2. **No Anti-Windup:** Integral term can accumulate during saturation
3. **Single Control Bank:** Real reactors have multiple independent control rod banks

## 10.4 Future Enhancement Opportunities

### 10.4.1 Physics Improvements

1. **Additional Fission Product Poisons:** Extend beyond Xe-135 and Sm-149
  - Pm-149 transient effects (currently modeled only as Sm-149 precursor)
  - Other significant absorbers (Rh-103, Cd isotopes)
2. **Spatial Xenon Oscillations:** Extend to multi-dimensional kinetics
  - Demonstrate spatial power tilting in large cores

- Regional xenon oscillation control strategies
3. **Multi-Region Model:** Implement core, reflector, and pressure vessel regions
    - More accurate neutron leakage
    - Region-dependent temperature effects
  4. **Improved Thermal-Hydraulics:**
    - Axial temperature profiles
    - Two-phase flow modeling (boiling)
    - DNB (Departure from Nucleate Boiling) limits
  5. **Fuel Performance Models:**
    - Fission gas release
    - Pellet-cladding interaction
    - Fuel swelling and densification

#### 10.4.2 Software Enhancements

1. **Advanced Control Algorithms:**
  - Model Predictive Control (MPC)
  - Fuzzy logic control
  - Optimal control with state estimation
2. **3D Visualization:**
  - OpenGL reactor core rendering
  - Animated neutron flux distribution
  - Temperature heatmaps
3. **Data Logging and Analysis:**
  - Export to CSV/HDF5 for external analysis
  - Statistical analysis tools
  - Comparison with historical data
4. **Multiplayer Mode:**
  - Networked control stations
  - Team-based reactor operation scenarios
  - Competitive challenges

### 10.4.3 Hardware Expansions

#### 1. Enhanced Arduino Features:

- Rotary encoder for analog rod control
- LCD display showing key parameters
- Alarm buzzer for SCRAM events
- Temperature sensors for ambient monitoring

#### 2. Larger Physical Models:

- Multiple control rod banks
- Pressurizer model with pressure control
- Steam generator visualization
- Turbine generator integration

#### 3. Virtual/Augmented Reality:

- VR reactor control room
- AR overlays on physical LEGO model
- Immersive training environment

### 10.4.4 Educational Curriculum Development

#### 1. Guided Tutorials:

- Step-by-step walkthroughs for beginners
- Progressive difficulty levels
- Interactive quizzes and assessments

#### 2. Scenario Library:

- Historical reactor incidents (TMI, Chernobyl analysis)
- Advanced reactor concepts (MSR, SMR demonstrations)
- Competition scenarios for student teams

#### 3. Integration with LMS:

- Canvas/Moodle integration
- Automated grading of reactor operations
- Progress tracking and analytics

## 10.5 Broader Impact

### 10.5.1 STEM Education

The DUNE project demonstrates the power of simulation-based learning in STEM education. By making complex physics accessible through visualization and interaction, it lowers barriers to understanding advanced topics and inspires students to pursue careers in science and engineering.

### 10.5.2 Cyber-Physical Systems in Engineering Education

The integration of computation with physical processes—known as Cyber-Physical Systems (CPS)—has proven highly effective in engineering education:

- **SCADA System Analog:** DUNE mimics real-world Supervisory Control and Data Acquisition systems where digital signals drive physical actuators
- **Multi-Sensory Learning:** Combines visual (LED brightness), auditory (pump noise), and tactile (servo motion) feedback
- **Real-Time Constraints:** Students experience the challenges of real-time control and hardware interfacing
- **Cross-Domain Integration:** Bridges nuclear physics, control theory, embedded systems, and software engineering

### 10.5.3 Public Understanding of Nuclear Energy

Beyond classroom use, DUNE serves as a tool for public outreach and science communication. Interactive demonstrations at science fairs and museums help demystify nuclear technology and inform evidence-based public discourse on energy policy.

### 10.5.4 Open-Source Community

As an open-source project under the MIT license, DUNE enables:

- Free access for educators worldwide
- Community contributions and improvements
- Adaptation to local educational needs
- Foundation for derivative educational tools

## 10.6 Project Heritage and Attribution

The DUNE project builds upon the foundational work of the pyReactor educational simulator:

- **Original pyReactor:** Developed by W. Gurecky as an open-source reactor kinetics educational tool
- **Repository:** <https://github.com/wgurecky/pyReactor>
- **DUNE Enhancement:** Extended for University of Dhaka's Nuclear Engineering program with improved hardware integration using 3D printed components, enhanced GUI features, and comprehensive documentation
- **DUNE Repository:** <https://github.com/Hridoy-Kabiraj/DUNE>
- **Course Integration:** Developed as part of NE-3206 curriculum at the Department of Nuclear Engineering, University of Dhaka

This collaborative evolution exemplifies the power of open-source software in advancing university-level nuclear engineering education.

## 10.7 Final Remarks

The DUNE project represents a successful fusion of rigorous physics modeling, software engineering, and educational pedagogy. Its combination of accurate simulation, intuitive interface, and physical hardware feedback creates a uniquely effective learning experience. As nuclear energy plays an increasingly important role in addressing climate change, tools like DUNE will be essential for educating the next generation of nuclear engineers and informed citizens.

The project's modular architecture and open-source nature ensure it will continue evolving, incorporating new features and adapting to emerging educational needs. Whether used in an undergraduate nuclear engineering course, university reactor theory laboratory, or public science museum, DUNE serves its core mission: making nuclear reactor physics accessible, understandable, and inspiring.

*"The reactor is not just a source of energy, but a testament to human ingenuity in harnessing the fundamental forces of nature."*

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- **Open-Source Community:** For developing the excellent Python scientific computing ecosystem (NumPy, SciPy, Matplotlib, wxPython)
- **Arduino Community:** For providing accessible hardware platforms and comprehensive documentation
- **Department of Nuclear Engineering, University of Dhaka:** For providing the resources and environment conducive to this research

The DUNE project demonstrates how collaborative open-source development can create powerful educational tools for university-level nuclear engineering education.

## A Reactor Physics Equations Reference

### A.1 Point Kinetics Equations (Standard Form)

For a reactor with  $I$  delayed neutron groups:

$$\frac{dn(t)}{dt} = \frac{\rho(t) - \beta}{\Lambda} n(t) + \sum_{i=1}^I \lambda_i C_i(t) \quad (34)$$

$$\frac{dC_i(t)}{dt} = \frac{\beta_i}{\Lambda} n(t) - \lambda_i C_i(t) \quad (i = 1, \dots, I) \quad (35)$$

### A.2 Reactor Period

For constant reactivity  $\rho$ , the asymptotic reactor period  $T$  is:

$$T = \frac{\Lambda}{\rho - \beta} \quad (\text{for } \rho < \beta) \quad (36)$$

### A.3 Prompt Jump Approximation

For step reactivity insertion  $\Delta\rho$  at  $t = 0$ :

$$\frac{n(t = 0^+)}{n(t = 0^-)} \approx \frac{\rho_0 + \Delta\rho}{\rho_0} \quad (37)$$

## B Thermodynamic Properties

### B.1 UO<sub>2</sub> Fuel Properties

- Density:  $\rho_{UO_2} = 10.97 \text{ g/cm}^3$  (theoretical),  $10.5 \text{ g/cm}^3$  (typical sintered)
- Specific heat:  $C_p = 245 + 0.0586(T - 273) \text{ J/kg}\cdot\text{K}$
- Thermal conductivity:  $k = \frac{1}{7.5408 \times 10^{-3} + 1.7692 \times 10^{-5}T + 3.6142 \times 10^{-9}T^2} \text{ W/m}\cdot\text{K}$
- Melting point:  $3120 \text{ K}$  ( $2847^\circ\text{C}$ )

### B.2 Water/Steam Properties (at 15 MPa)

- Saturation temperature:  $615 \text{ K}$  ( $342^\circ\text{C}$ )
- Liquid density:  $700 \text{ kg/m}^3$
- Liquid specific heat:  $C_{p,l} = 4.18 \text{ kJ/kg}\cdot\text{K}$
- Latent heat of vaporization:  $931 \text{ kJ/kg}$



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