

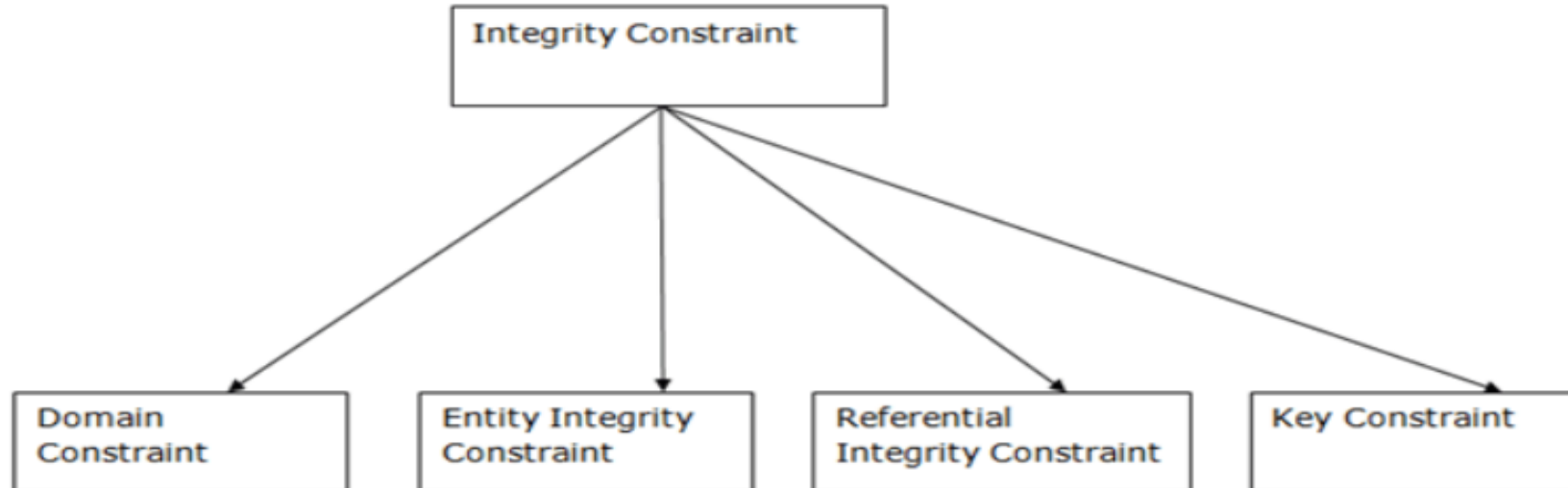
Q.1 What is integrity constraint? Write the various constraint available, in brief.

## Integrity Constraints

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- Integrity constraints are a set of rules. It is used to maintain the quality of information.
- Integrity constraints ensure that the data insertion, updating, and other processes have to be performed in such a way that data integrity is not affected.
- Thus, integrity constraint is used to guard against accidental damage to the database.

## Types of Integrity Constraint



# 1. Domain constraints

- Domain constraints can be defined as the definition of a valid set of values for an attribute.
- The data type of domain includes string, character, integer, time, date, currency, etc. The value of the attribute must be available in the corresponding domain.

## Example:

ID	NAME	SEMENSTER	AGE
1000	Tom	1 <sup>st</sup>	17
1001	Johnson	2 <sup>nd</sup>	24
1002	Leonardo	5 <sup>th</sup>	21
1003	Kate	3 <sup>rd</sup>	19
1004	Morgan	8 <sup>th</sup>	A

Not allowed. Because AGE is an integer attribute

# 2. Entity integrity constraints

- The entity integrity constraint states that primary key value can't be null.
- This is because the primary key value is used to identify individual rows in relation and if the primary key has a null value, then we can't identify those rows.
- A table can contain a null value other than the primary key field.

Example:

## EMPLOYEE

EMP_ID	EMP_NAME	SALARY
123	Jack	30000
142	Harry	60000
164	John	20000
	Jackson	27000

Not allowed as primary key can't contain a NULL value

## 3. Referential Integrity Constraints

- A referential integrity constraint is specified between two tables.
- In the Referential integrity constraints, if a foreign key in Table 1 refers to the Primary Key of Table 2, then every value of the Foreign Key in Table 1 must be null or be available in Table 2.

Example:

## EMPLOYEE

EMP_ID	EMP_NAME	SALARY
123	Jack	30000
142	Harry	60000
164	John	20000
	Jackson	27000

Not allowed as primary key can't contain a NULL value

## 3. Referential Integrity Constraints

- A referential integrity constraint is specified between two tables.
- In the Referential integrity constraints, if a foreign key in Table 1 refers to the Primary Key of Table 2, then every value of the Foreign Key in Table 1 must be null or be available in Table 2.

$\Pi_{\text{Name, Department}}(\sigma_{\text{salary} > 25000}(\text{EMPLOYEE}))$

Q.2 Why we use key in DBMS and define. Various key available in DBMS system.

- A Key is an attribute or a set of attributes in a relation that identifies a tuple (record) in a relation.
- The keys are defined in a table to access or sequence the stored data quickly and smoothly.
- They are also used to create relationship between different tables.

#### Types of Keys in Database

1. Primary Key
2. Candidate Key
3. Alternate Key
4. Super Key
5. Composite Key
6. Foreign Key
7. Unique Key

# Primary Key

- Which is *Unique & Can't be have NULL Value*
- Is the column you choose to maintain uniqueness in a table at row level.
- Here in *Employee* table we can choose either *EmployeeID* or *SSN* column for a PK.
- EmployeeID is preferable choice because SSN is a secure (PII) value.
- Primary key is the minimal super keys. In the ER diagram primary key is represented by underlining the primary key attribute.
- Ideally a primary key is composed of only a single attribute.
- But it is possible to have a primary key composed of more than one attribute

Employee
<u>EmployeeID</u>
EmployeeName
SSN
DeptID
DOB



## To define a field as primary key, following conditions had to be met :

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- No two rows can have the same primary key value.
- Every row must have a primary key value.
- The primary key field cannot be null.
- Value in a primary key column can never be modified or updated, if any foreign key refers to that primary key



# Candidate Key

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- Are individual columns in a table that qualifies for uniqueness of each row/tuple.
- Here in *Employee* table *EmployeeID* & *SSN* are eligible for a *Primary Key* and thus are *Candidate keys*.
- Candidate Keys are super keys for which no proper subset is a super key. *In other words candidate keys are minimal super keys.*

Employee
<u>EmployeeID</u>
EmployeeName
<u>SSN</u>
DeptID
DOB

# *Alternate Key*

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- Candidate column other than the Primary column, like if *EmployeeID* is set for a PK then *SSN* would be the Alternate key.

Employee
EmployeeID
EmployeeName
<u>SSN</u>
DeptID
DOB



# *Super Key*

- If you add any other Column / Attribute to a Primary Key then it become a Super Key, like *EmployeeID* + *EmployeeName* is a Super Key.
- Super key stands for superset of a key.
- *A Super Key is a set of one or more attributes that are taken collectively and can identify all other attributes uniquely.*

Employee
<u>EmployeeID</u>
<u>EmployeeName</u>
SSN
DeptID
DOB

# Composite Key

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- If a table do have a single column that qualifies for a Candidate key, then you have to select 2 or more columns to make a row unique.
- Like if there is no EmployeeID or SSN columns, then you can make *EmployeeName* + *DateOfBirth* (DOB) as *Composite Primary Key*. But still there can be a narrow chance of duplicate rows.

Employee

EmployeeID

EmployeeName

SSN

DeptID

DOB



# *Foreign Key*

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- Here in below tables *DeptID* of *Department* table is Primary Key where as *DeptID* of *Employee* is an *Foreign key*.
- It means it has referred to another table. This concept is also know as *Referential Integrity*.

Employee
EmployeeID
EmployeeName
SSN
<u>DeptID</u>
DOB

Department
<u>DeptID</u>
DeptName

# *Unique Key*

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- *Unique key* is same as primary with the difference being the existence of null.
- Unique key field allows one value as NULL value.

Employee

EmployeeID

EmployeeName

SSN

EmailID

DOB



### Q.3 Define Relational algebra with their various operation.

- Relational algebra is the basic set of operations for the relational model
- These operations enable a user to specify **basic retrieval requests** (or **queries**)
- The result of an operation is a *new relation*, which may have been formed from one or more *input* relations
  - This property makes the algebra “closed” (all objects in relational algebra are relations)
- The **algebra operations** thus produce new relations
  - These can be further manipulated using operations of the same algebra
- A sequence of relational algebra operations forms a **relational algebra expression**
  - The result of a relational algebra expression is also a relation that represents the result of a database query (or retrieval request)

- Relational Algebra consists of several groups of operations
  - **Unary Relational Operations**
    - SELECT (symbol:  $\sigma$  (sigma))
    - PROJECT (symbol:  $\pi$  (pi))
    - RENAME (symbol:  $\rho$  (rho))
  - **Relational Algebra Operations From Set Theory**
    - UNION ( $\cup$ ), INTERSECTION ( $\cap$ ), DIFFERENCE (or MINUS,  $-$ )
    - CARTESIAN PRODUCT ( $\times$ )
  - **Binary Relational Operations**
    - JOIN (several variations of JOIN exist)
    - DIVISION
  - **Additional Relational Operations**
    - OUTER JOINS, OUTER UNION
    - AGGREGATE FUNCTIONS (These compute summary of information: for example, SUM, COUNT, AVG, MIN, MAX)

- The SELECT operation (denoted by  $\sigma$  (sigma)) is used to select a *subset* of the tuples from a relation based on a **selection condition**.
  - The selection condition acts as a **filter**
  - Keeps only those tuples that satisfy the qualifying condition
  - Tuples satisfying the condition are *selected* whereas the other tuples are discarded (*filtered out*)

- Examples:

- Select the EMPLOYEE tuples whose department number is 4:

$$\sigma_{DNO = 4} (EMPLOYEE)$$

- Select the employee tuples whose salary is greater than \$30,000:

$$\sigma_{SALARY > 30,000} (EMPLOYEE)$$

- In general, the *select* operation is denoted by  $\sigma_{\langle \text{selection condition} \rangle} (R)$  where
  - the symbol  $\sigma$  (sigma) is used to denote the *select* operator
  - the selection condition is a Boolean (conditional) expression specified on the attributes of relation R
  - tuples that make the condition **true** are selected
    - appear in the result of the operation

tuples that make the condition **false** are filtered out  
discarded from the result of the operation

- PROJECT Operation is denoted by  $\pi$  (pi)
- This operation keeps certain *columns* (attributes) from a relation and discards the other columns.
  - **PROJECT creates a vertical partitioning**
    - The list of specified columns (attributes) is kept in each tuple
    - The other attributes in each tuple are discarded
- Example: To list each employee's first and last name and salary, the following is used:

$\pi_{\text{LNAME, FNAME, SALARY}}(\text{EMPLOYEE})$

- The general form of the *project* operation is:

$$\pi_{\langle \text{attribute list} \rangle}(R)$$

- $\pi$  (pi) is the symbol used to represent the *project* operation
- $\langle \text{attribute list} \rangle$  is the desired list of attributes from relation R.
- The project operation *removes any duplicate tuples*
  - This is because the result of the *project* operation must be a *set of tuples*
    - Mathematical sets *do not allow* duplicate elements.

## ■ PROJECT Operation Properties

- The number of tuples in the result of projection  $\pi_{\langle \text{list} \rangle}(R)$  is always less or equal to the number of tuples in R
  - If the list of attributes includes a *key* of R, then the number of tuples in the result of PROJECT is *equal* to the number of tuples in R
- PROJECT is *not* commutative
  - $\pi_{\langle \text{list1} \rangle}(\pi_{\langle \text{list2} \rangle}(R)) = \pi_{\langle \text{list1} \rangle}(R)$  as long as  $\langle \text{list2} \rangle$  contains the attributes in  $\langle \text{list1} \rangle$

- The RENAME operator is denoted by  $\rho$  (rho)
- In some cases, we may want to *rename* the attributes of a relation or the relation name or both
  - Useful when a query requires multiple operations
  - Necessary in some cases (see JOIN operation later)
- The general RENAME operation  $\rho$  can be expressed by any of the following forms:
  - $\rho_{S(B_1, B_2, \dots, B_n)}(R)$  changes both:
    - the relation name to  $S$ , *and*
    - the column (attribute) names to  $B_1, B_1, \dots, B_n$
  - $\rho_S(R)$  changes:
    - the *relation name* only to  $S$
  - $\rho_{(B_1, B_2, \dots, B_n)}(R)$  changes:
    - the *column (attribute) names* only to  $B_1, B_1, \dots, B_n$



- For convenience, we also use a *shorthand* for renaming attributes in an intermediate relation:
  - If we write:
    - $\text{RESULT} \leftarrow \pi_{\text{FNAME, LNAME, SALARY}}(\text{DEP5\_EMPS})$
    - RESULT will have the *same attribute names* as DEP5\_EMPS (same attributes as EMPLOYEE)
  - If we write:
    - $\text{RESULT (F, M, L, S, B, A, SX, SAL, SU, DNO)} \leftarrow \pi_{\text{FNAME, LNAME, SALARY}}(\text{DEP5\_EMPS})$
    - The 10 attributes of DEP5\_EMPS are *renamed* to F, M, L, S, B, A, SX, SAL, SU, DNO, respectively

- UNION Operation
  - Binary operation, denoted by  $\cup$
  - The result of  $R \cup S$ , is a relation that includes all tuples that are either in R or in S or in both R and S
  - Duplicate tuples are eliminated
  - The two operand relations R and S must be “type compatible” (or UNION compatible)
    - R and S must have same number of attributes
    - Each pair of corresponding attributes must be type compatible (have same or compatible domains)

- Example:

- To retrieve the social security numbers of all employees who either *work in department 5* (RESULT1 below) or *directly supervise an employee who works in department 5* (RESULT2 below)
- We can use the UNION operation as follows:

$$\begin{aligned} \text{DEP5\_EMPS} &\leftarrow \sigma_{\text{DNO}=5} (\text{EMPLOYEE}) \\ \text{RESULT1} &\leftarrow \pi_{\text{SSN}} (\text{DEP5\_EMPS}) \\ \text{RESULT2}(\text{SSN}) &\leftarrow \pi_{\text{SUPERSSN}} (\text{DEP5\_EMPS}) \\ \text{RESULT} &\leftarrow \text{RESULT1} \cup \text{RESULT2} \end{aligned}$$

- The union operation produces the tuples that are in either RESULT1 or RESULT2 or both

- INTERSECTION is denoted by  $\cap$
- The result of the operation  $R \cap S$ , is a relation that includes all tuples that are in both R and S
  - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be “type compatible”
- SET DIFFERENCE (also called MINUS or EXCEPT) is denoted by  $-$
- The result of  $R - S$ , is a relation that includes all tuples that are in R but not in S
  - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be “type compatible”

- Notice that both union and intersection are *commutative* operations; that is
  - $R \cup S = S \cup R$ , and  $R \cap S = S \cap R$
- Both union and intersection can be treated as n-ary operations applicable to any number of relations as both are *associative* operations; that is
  - $R \cup (S \cup T) = (R \cup S) \cup T$
  - $(R \cap S) \cap T = R \cap (S \cap T)$
- The minus operation is not commutative; that is, in general
  - $R - S \neq S - R$
- CARTESIAN (or CROSS) PRODUCT Operation
  - This operation is used to combine tuples from two relations in a combinatorial fashion.
  - Denoted by  $R(A_1, A_2, \dots, A_n) \times S(B_1, B_2, \dots, B_m)$
  - Result is a relation Q with degree  $n + m$  attributes:
    - $Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_m)$ , in that order.
  - The resulting relation state has one tuple for each combination of tuples—one from R and one from S.
  - Hence, if R has  $n_R$  tuples (denoted as  $|R| = n_R$ ), and S has  $n_S$  tuples, then  $R \times S$  will have  $n_R * n_S$  tuples.
  - The two operands do NOT have to be "type compatible"

Q.4 Write the Relational algebraic expression for the following questions :-

(Employee table given in Question)

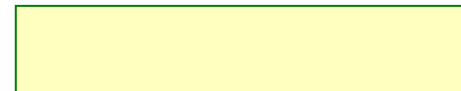
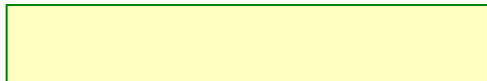
- Display the employee name, department who has salary greater than 25000.
- Retrieves the social security numbers. Of all employees who either work in department no. 5 or directly supervise an employee who works in department no. 5
- Retrieve the names of female employees and their dependents.

Single expression versus sequence of relational operations (Example)

- To retrieve the first name, last name, and salary of all employees who work in department number 5, we must apply a select and a project operation
- We can write a *single relational algebra expression* as follows:
  - $\pi_{\text{FNAME, LNAME, SALARY}}(\sigma_{\text{DNO}=5}(\text{EMPLOYEE}))$
- OR We can explicitly show the *sequence of operations*, giving a name to each intermediate relation:

- $\text{DEP5\_EMPS} \leftarrow \sigma_{\text{DNO}=5}(\text{EMPLOYEE})$

- $\text{RESULT} \leftarrow \pi_{\text{FNAME, LNAME, SALARY}}(\text{DEP5\_EMPS})$



# Relational Algebra Operations from Set Theory: UNION

- Example:
  - To retrieve the social security numbers of all employees who either *work in department 5* (RESULT1 below) or *directly supervise an employee who works in department 5* (RESULT2 below)
  - We can use the UNION operation as follows:

$$\text{DEP5\_EMPS} \leftarrow \sigma_{\text{DNO}=5} (\text{EMPLOYEE})$$
$$\text{RESULT1} \leftarrow \pi_{\text{SSN}}(\text{DEP5\_EMPS})$$
$$\text{RESULT2}(\text{SSN}) \leftarrow \pi_{\text{SUPERSSN}}(\text{DEP5\_EMPS})$$
$$\text{RESULT} \leftarrow \text{RESULT1} \cup \text{RESULT2}$$

- The union operation produces the tuples that are in either RESULT1 or RESULT2 or both



# Example of the result of a UNION operation

- UNION Example

**Figure 6.3**

Result of the  
UNION operation  
 $\text{RESULT} \leftarrow \text{RESULT1} \cup \text{RESULT2}$ .

**RESULT1**

Ssn
123456789
333445555
666884444
453453453

**RESULT2**

Ssn
333445555
888665555

**RESULT**

Ssn
123456789
333445555
666884444
453453453
888665555

## Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT (cont.)

- To keep only combinations where the DEPENDENT is related to the EMPLOYEE, we add a SELECT operation as follows
- Example (meaningful):
  - $\text{FEMALE\_EMPS} \leftarrow \sigma_{\text{SEX}='F'}(\text{EMPLOYEE})$
  - $\text{EMP\_NAMES} \leftarrow \pi_{\text{FNAME, LNAME, SSN}}(\text{FEMALE\_EMPS})$
  - $\text{EMP\_DEPENDENTS} \leftarrow \text{EMP\_NAMES} \times \text{DEPENDENT}$
  - $\text{ACTUAL\_DEPS} \leftarrow \sigma_{\text{SSN}=\text{ESSN}}(\text{EMP\_DEPENDENTS})$
  - $\text{RESULT} \leftarrow \pi_{\text{FNAME, LNAME, DEPENDENT\_NAME}}(\text{ACTUAL\_DEPS})$
- RESULT will now contain the name of female employees and their dependents

Q.5 what are the various aggregate functions used/available in DBMS?  
Explain with an example.

Sum, average, maximum, minimum, count with example

## Additional Relational Operations: Aggregate Functions and Grouping

- A type of request that cannot be expressed in the basic relational algebra is to specify mathematical **aggregate functions** on collections of values from the database.
- Examples of such functions include retrieving the average or total salary of all employees or the total number of employee tuples.
  - These functions are used in simple statistical queries that summarize information from the database tuples.
- Common functions applied to collections of numeric values include
  - SUM, AVERAGE, MAXIMUM, and MINIMUM.
- The COUNT function is used for counting tuples or values.

# Aggregate Function Operation

- Use of the Aggregate Functional operation  $\mathcal{F}$ 
  - $\mathcal{F}_{\text{MAX Salary}}(\text{EMPLOYEE})$  retrieves the maximum salary value from the EMPLOYEE relation
  - $\mathcal{F}_{\text{MIN Salary}}(\text{EMPLOYEE})$  retrieves the minimum Salary value from the EMPLOYEE relation
  - $\mathcal{F}_{\text{SUM Salary}}(\text{EMPLOYEE})$  retrieves the sum of the Salary from the EMPLOYEE relation
  - $\mathcal{F}_{\text{COUNT SSN, AVERAGE Salary}}(\text{EMPLOYEE})$  computes the count (number) of employees and their average salary
    - Note: count just counts the number of rows, without removing duplicates

Q.6 why we use join operation in DBMS. Write the various join operations with an example.

## Binary Relational Operations: JOIN

- JOIN Operation (denoted by  $\bowtie$ )
  - The sequence of CARTESIAN PRODECT followed by SELECT is used quite commonly to identify and select related tuples from two relations
  - A special operation, called JOIN combines this sequence into a single operation
  - This operation is very important for any relational database with more than a single relation, because it allows us *combine related tuples* from various relations
  - The general form of a join operation on two relations  $R(A_1, A_2, \dots, A_n)$  and  $S(B_1, B_2, \dots, B_m)$  is:

$$R \bowtie_{\langle \text{join condition} \rangle} S$$

- where R and S can be any relations that result from general *relational algebra expressions*.

## Binary Relational Operations: JOIN (cont.)

- Example: Suppose that we want to retrieve the name of the manager of each department.
  - To get the manager's name, we need to combine each DEPARTMENT tuple with the EMPLOYEE tuple whose SSN value matches the MGRSSN value in the department tuple.
  - We do this by using the join operation.
- $DEPT\_MGR \leftarrow DEPARTMENT \underset{MGRSSN=SSN}{\Join} EMPLOYEE$
- MGRSSN=SSN is the join condition
  - Combines each department record with the employee who manages the department
  - The join condition can also be specified as DEPARTMENT.MGRSSN=EMPLOYEE.SSN



# Example of applying the JOIN operation

**DEPT\_MGR**

Dname	Dnumber	Mgr_ssn	...	Fname	Minit	Lname	Ssn	...
Research	5	333445555	...	Franklin	T	Wong	333445555	...
Administration	4	987654321	...	Jennifer	S	Wallace	987654321	...
Headquarters	1	888665555	...	James	E	Borg	888665555	...

**Figure 6.6**

Result of the JOIN operation

# Some properties of JOIN

- Consider the following JOIN operation:
  - $R(A_1, A_2, \dots, A_n) \quad \mid \quad S(B_1, B_2, \dots, B_m)$   
 $R.A_i = S.B_j$
  - Result is a relation Q with degree  $n + m$  attributes:
    - $Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_m)$ , in that order.
  - The resulting relation state has one tuple for each combination of tuples— $r$  from  $R$  and  $s$  from  $S$ , but *only if they satisfy the join condition*  $r[A_i] = s[B_j]$
  - Hence, if  $R$  has  $n_R$  tuples, and  $S$  has  $n_S$  tuples, then the join result will generally have *less than*  $n_R * n_S$  tuples.
  - Only related tuples (based on the join condition) will appear in the result

# Some properties of JOIN

- The general case of JOIN operation is called a Theta-join:  $R \bowtie_{\theta} S$
- The join condition is called *theta*
- *Theta* can be any general boolean expression on the attributes of R and S; for example:
  - $R.A_i < S.B_j \text{ AND } (R.A_k = S.B_l \text{ OR } R.A_p < S.B_q)$
- Most join conditions involve one or more equality conditions “AND”ed together; for example:
  - $R.A_i = S.B_j \text{ AND } R.A_k = S.B_l \text{ AND } R.A_p = S.B_q$

## Binary Relational Operations: EQUIJOIN

- EQUIJOIN Operation
- The most common use of join involves join conditions with *equality comparisons* only
- Such a join, where the only comparison operator used is =, is called an EQUIJOIN.
  - In the result of an EQUIJOIN we always have one or more pairs of attributes (whose names need not be identical) that have identical values in every tuple.
  - The JOIN seen in the previous example was an EQUIJOIN.

# Binary Relational Operations:

## NATURAL JOIN Operation

- NATURAL JOIN Operation
  - Another variation of JOIN called NATURAL JOIN — denoted by  $*$  — was created to get rid of the second (superfluous) attribute in an EQUIJOIN condition.
    - because one of each pair of attributes with identical values is superfluous
  - The standard definition of natural join requires that the two join attributes, or each pair of corresponding join attributes, *have the same name* in both relations
  - If this is not the case, a renaming operation is applied first.

# Binary Relational Operations NATURAL JOIN (contd.)

- Example: To apply a natural join on the DNUMBER attributes of DEPARTMENT and DEPT\_LOCATIONS, it is sufficient to write:
  - $DEPT\_LOCS \leftarrow DEPARTMENT * DEPT\_LOCATIONS$
- Only attribute with the same name is DNUMBER
- An implicit join condition is created based on this attribute:  
 $DEPARTMENT.DNUMBER = DEPT\_LOCATIONS.DNUMBER$
- Another example:  $Q \leftarrow R(A,B,C,D) * S(C,D,E)$ 
  - The implicit join condition includes *each pair* of attributes with the same name, “AND”ed together:
    - $R.C = S.C \text{ AND } R.D = S.D$
  - Result keeps only one attribute of each such pair:
    - $Q(A,B,C,D,E)$

# Example of NATURAL JOIN operation

(a)

**PROJ\_DEPT**

Pname	<u>Pnumber</u>	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01

(b)

**DEPT\_LOCS**

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston

**Figure 6.7**

Results of two NATURAL JOIN operations.

(a) PROJ\_DEPT  $\leftarrow$  PROJECT \* DEPT.

(b) DEPT\_LOCS  $\leftarrow$  DEPARTMENT \* DEPT\_LOCATIONS.

Q.7 write about Relational calculus expression for the following questions.

- Relational calculus is considered to be a **nonprocedural** language.
- This differs from relational algebra, where we must write a *sequence of operations* to specify a retrieval request; hence relational algebra can be considered as a **procedural** way of stating a query.
- The tuple relational calculus is based on specifying a number of tuple variables.
- Each tuple variable usually ranges over a particular database relation, meaning that the variable may take as its value any individual tuple from that relation.
- A simple tuple relational calculus query is of the form

$$\{t \mid \text{COND}(t)\}$$

- where  $t$  is a tuple variable and  $\text{COND}(t)$  is a conditional expression involving  $t$ .
- The result of such a query is the set of all tuples  $t$  that satisfy  $\text{COND}(t)$ .



# The Existential and Universal Quantifiers

- Two special symbols called quantifiers can appear in formulas; these are the universal quantifier ( $\forall$ ) and the existential quantifier ( $\exists$ ).
- Informally, a tuple variable  $t$  is bound if it is quantified, meaning that it appears in an  $(\forall t)$  or  $(\exists t)$  clause; otherwise, it is free.
- If  $F$  is a formula, then so are  $(\exists t)(F)$  and  $(\forall t)(F)$ , where  $t$  is a tuple variable.
  - The formula  $(\exists t)(F)$  is true if the formula  $F$  evaluates to true for some (at least one) tuple assigned to free occurrences of  $t$  in  $F$ ; otherwise  $(\exists t)(F)$  is false.
  - The formula  $(\forall t)(F)$  is true if the formula  $F$  evaluates to true for every tuple (in the universe) assigned to free occurrences of  $t$  in  $F$ ; otherwise  $(\forall t)(F)$  is false.
- $\forall$  is called the universal or “for all” quantifier because every tuple in “the universe of” tuples must make  $F$  true to make the quantified formula true.
- $\exists$  is called the existential or “there exists” quantifier because any tuple that exists in “the universe of” tuples may make  $F$  true to make the quantified formula true.

# Languages Based on Tuple Relational Calculus

- The language **SQL** is based on tuple calculus. It uses the basic block structure to express the queries in tuple calculus:
  - **SELECT** <list of attributes>
  - **FROM** <list of relations>
  - **WHERE** <conditions>
- **SELECT** clause mentions the attributes being projected, the **FROM** clause mentions the relations needed in the query, and the **WHERE** clause mentions the selection as well as the join conditions.
  - **SQL syntax is expanded further to accommodate other operations. (See Chapter 8).**
- Another language which is based on tuple calculus is **QUEL** which actually uses the range variables as in tuple calculus. Its syntax includes:
  - **RANGE OF** <variable name> **IS** <relation name>
- Then it uses
  - **RETRIEVE** <list of attributes from range variables>
  - **WHERE** <conditions>
- This language was proposed in the relational DBMS INGRES.

- Another variation of relational calculus called the domain relational calculus, or simply, domain calculus is equivalent to tuple calculus and to relational algebra.
- The language called QBE (Query-By-Example) that is related to domain calculus was developed almost concurrently to SQL at IBM Research, Yorktown Heights, New York.
  - Domain calculus was thought of as a way to explain what QBE does.
- Domain calculus differs from tuple calculus in the type of variables used in formulas:
  - Rather than having variables range over tuples, the variables range over single values from domains of attributes.
- To form a relation of degree  $n$  for a query result, we must have  $n$  of these domain variables— one for each attribute.
- An expression of the domain calculus is of the form
 
$$\{ x_1, x_2, \dots, x_n \mid \text{COND}(x_1, x_2, \dots, x_n, x_{n+1}, x_{n+2}, \dots, x_{n+m}) \}$$
  - where  $x_1, x_2, \dots, x_n, x_{n+1}, x_{n+2}, \dots, x_{n+m}$  are domain variables that range over domains (of attributes)
  - and COND is a condition or formula of the domain relational calculus.

- Retrieve the birthdate and address of the employee whose name is 'John B. Smith'.

- Query :

$\{uv \mid (\exists q) (\exists r) (\exists s) (\exists t) (\exists w) (\exists x) (\exists y) (\exists z)$

$(\text{EMPLOYEE}(qrstuvwxyz) \text{ and } q=\text{'John'} \text{ and } r=\text{'B'} \text{ and } s=\text{'Smith'})\}$

- Ten variables for the employee relation are needed, one to range over the domain of each attribute in order.
  - Of the ten variables  $q, r, s, \dots, z$ , only  $u$  and  $v$  are free.
- Specify the *requested attributes*, BDATE and ADDRESS, by the free domain variables  $u$  for BDATE and  $v$  for ADDRESS.
- Specify the condition for selecting a tuple following the bar (  $\mid$  )—
  - namely, that the sequence of values assigned to the variables  $qrstuvwxyz$  be a tuple of the employee relation and that the values for  $q$  (FNAME),  $r$  (MINIT), and  $s$  (LNAME) be 'John', 'B', and 'Smith', respectively.

Q.8 write the relational calculus expression for the following question.

- Retrieve the name and address of all employees who work for the research department.
- Find the names of employees who work in all the projects controlled by department number 5.
- Retrieve the birthdate and address of the employee whose name is 'John B.smith'.

### Example Query Using Existential Quantifier

- Retrieve the name and address of all employees who work for the 'Research' department. The query can be expressed as :

**{t.FNAME, t.LNAME, t.ADDRESS | EMPLOYEE(t) and ( $\exists$  d)  
(DEPARTMENT(d) and d.DNAME='Research' and d.DNUMBER=t.DNO) }**

- The only *free tuple variables* in a relational calculus expression should be those that appear to the left of the bar ( | ).
  - In above query, t is the only free variable; it is then *bound successively* to each tuple.
- If a tuple *satisfies the conditions* specified in the query, the attributes FNAME, LNAME, and ADDRESS are retrieved for each such tuple.
  - The conditions EMPLOYEE (t) and DEPARTMENT(d) specify the range relations for t and d.
  - The condition d.DNAME = 'Research' is a selection condition and corresponds to a SELECT operation in the relational algebra, whereas the condition d.DNUMBER = t.DNO is a JOIN condition.

# Example Query Using Universal Quantifier

- Find the names of employees who work on *all* the projects controlled by department number 5. The query can be:

**{e.LNAME, e.FNAME | EMPLOYEE(e) and ( (  $\forall x$  )(not(PROJECT(x)) or not(x.DNUM=5)  
OR ( (  $\exists w$  )(WORKS\_ON(w) and w.ESSN=e.SSN and x.PNUMBER=w.PNO))))}**

- Exclude from the universal quantification all tuples that we are not interested in by making the condition true *for all such tuples*.
  - The first tuples to exclude (by making them evaluate automatically to true) are those that are not in the relation R of interest.
- In query above, using the expression **not(PROJECT(x))** inside the universally quantified formula evaluates to true all tuples x that are not in the PROJECT relation.
  - Then we exclude the tuples we are not interested in from R itself. The expression not(x.DNUM=5) evaluates to true all tuples x that are in the project relation but are not controlled by department 5.
- Finally, we specify a condition that must hold on all the remaining tuples in R.

**( (  $\exists w$  )(WORKS\_ON(w) and w.ESSN=e.SSN and x.PNUMBER=w.PNO)**

# Example Query Using Domain Calculus

- Retrieve the birthdate and address of the employee whose name is 'John B. Smith'.

- Query :

$\{uv \mid (\exists q) (\exists r) (\exists s) (\exists t) (\exists w) (\exists x) (\exists y) (\exists z)$

**$(\text{EMPLOYEE}(qrstuvwxyz) \text{ and } q=\text{'John'} \text{ and } r=\text{'B'} \text{ and } s=\text{'Smith'})\}$**

- Ten variables for the employee relation are needed, one to range over the domain of each attribute in order.
  - Of the ten variables  $q, r, s, \dots, z$ , only  $u$  and  $v$  are free.
- Specify the *requested attributes*, BDATE and ADDRESS, by the free domain variables  $u$  for BDATE and  $v$  for ADDRESS.
- Specify the condition for selecting a tuple following the bar (  $\mid$  )—
  - namely, that the sequence of values assigned to the variables  $qrstuvwxyz$  be a tuple of the employee relation and that the values for  $q$  (FNAME),  $r$  (MINIT), and  $s$  (LNAME) be 'John', 'B', and 'Smith', respectively.