

③ The unicorn is magical if it is horned.

can we prove that a unicorn is mythical? magical? or horned?

$$① \quad U_{\text{myth}} \rightarrow \sim U_{\text{mort}}$$

$$\sim U_{\text{yth}} \rightarrow U_{\text{mar}} \wedge U_{\text{mamm}}$$

$$② \quad \sim U_{\text{mort}} \vee U_{\text{mamm}} \rightarrow U_{\text{horn}}$$

$$③ \quad U_{\text{horn}} \rightarrow U_{\text{mag}}$$

incomplete
5/8/10

Predicate logic . ∴

- ① $\sim(\sim F) = F$
- ② $\forall x F(x) \vee G \equiv \forall x (F(x) \vee G)$
- ③ $\exists x F(x) \vee G \equiv \exists x (F(x) \vee G)$
- ④ $\forall x F(x) \wedge G \equiv \forall x (F(x) \wedge G)$
- ⑤ $\exists x F(x) \wedge G \equiv \exists x (F(x) \wedge G)$
- ⑥ $\sim(\forall x) F(x) = \exists x \sim(F(x))$
- ⑦ $\sim(\exists x) F(x) = \forall x \sim(F(x))$
- ⑧ $\forall x F(x) \wedge \forall x G(x) = \forall x (F(x) \wedge G(x))$
- ⑨ ~~$\forall x F(x) \vee \forall$~~
- ⑩ $\exists x F(x) \vee \exists x G(x) = \exists x (F(x) \vee G(x))$

0. All dog have tail

$$\forall (x) :- \text{dog}(x) \rightarrow \text{tail}(x).$$

8. Some employees are sick today.

$$\exists (x) E :- \text{employee}(x) \rightarrow \text{sick}(\text{today}).$$

9. Every gardner likes the sun.

$$\forall (x) A :- \text{gardner}(x) \rightarrow \text{likes}(x, \text{sun}).$$

10. Not every gardner likes ^{the} sun.

$$\neg \forall (x) A :- \text{gardner}(x) \rightarrow \text{likes}(x, \text{sun}).$$

$$\sim (\forall x) :- \text{gardner}(x) \rightarrow \text{likes}(x, \text{sun}).$$

→ Ram is not tall
 $\sim \text{tall}(\text{ram})$.

* All purple mushrooms are poisonous
 $x. \forall (x) : \text{purple}(x) \rightarrow \text{poisonous}(\text{mushroom } x)$

$\forall (x) : (\text{mus}(x) \wedge \text{pur}(x)) \rightarrow \text{pois}(x)$

NO purple mushrooms are poisonous.

$\exists x : (\text{mus}(x) \wedge \text{pur}(x)) \rightarrow \sim \text{pois}(x)$