

{ Pattern matching }

string Matching Algorithm

we were given text (string) of length 'n'

T | a | b | a | b | - - - |

have to match a pattern

P | a | b |

Length can be of 'm' size

* so pattern p is a subset of T

* characters of T & P are derived from finite alphabet Σ (sigma)

$\Sigma = \{0, 1\}$

$\Sigma = \{a, b, \dots, z\}$

shift

example से समझते हैं।

T | a | b | c | a | b | a | a | b | c | - -

match the pattern 'p'

P | a | b | a | a |

concept of shift is we start matching string from 0

$s=0$

a	b	c	a	b	a	a	b	c
a	b	a	a					

- not match

not match then $s = s+1$

$s = 1$ Now

which means we not consider the 1st element from text (string)

$s=1$ no consider

a	b	c	a	b	a	a	b	c
a	b	a	a					

no match

$s = s+1$

$s = 1+1 = 2$

$s=2$

a	b	c	a	b	a	a	b	c
a	a	a	a					

no match

$s = s+1$

$s = 3$

a	b	c	a	b	a	a	b	c
a	b	a	a					

pattern matched at $s=3$

boundaries of s

$a \leq s \leq n-m$

Naive String matching Algorithm

* simplest method for pattern matching

$$T[s+1 \dots s+m] = P[1 \dots m]$$

$$T[s+j] = P[j] \quad [1 \leq j \leq m]$$

Example

Algorithm {

- $n = T.length$
- $m = P.length$
- for $s = 0$ to $n - m$
- if $P[1..m] = T[s+1..s+m]$
- print("found");

Eg. 1

T = | a | c | a | a | b | c |

P = | a | a | b |

$s = 0$

a c a a b c

| f no match $s++$

a a b

$s = 1$

a | c a a b c

f $s++$

a a c

$s = 2$

a | c | a a b c

a a b found/printed

KNUTH - MORRIS - PRATT Algorithm

* It works on proper prefix and proper suffix

* In this kind of backtrace it starts

proper suffix - start from rhs.

proper prefix - L.H.S. to start

ex. a b c d \rightarrow ps
 ↓
 P.P.
 { a
 ab
 abc }

 { d
 cd
 bcd }

* Let any Text length = m

pattern length is = n

complexity $\therefore O(m+n)$

* If the beginning part of pattern is appearing anywhere in pattern or not that is to be observed.

(4)

Brice
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Find π table / Longest Proper Prefix
 → to avoid useless shift we use it
 only pattern is considered to generate π table.

	1	2	3	4	
P_1	a	b	a	b	sl - write index
	0	0	1	2	
	1	2	3	4	5
P_2	a	b	c	d	a
	0	0	0	0	1

P_2 a a a a b a a c d s2 - repeat P_1 at location P_2
 0 1 2 3 0 1 2 0 0

example to solve KMP Algo

T	a	b	a	b	c	a	b	c	a	b	a	b	a	b	d
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
P	a	b	a	b	c	a	b	d							
	0	0	1	2	0										

starting point

sl
 $i = 1$
 $j = 0$ if ($T[i] == P[j+1]$)
 $i++$;
 $j++$;

i → j

a b a b c a b c a b a b a b d

i → index

a b a b d

move j as well as i

i

a b a b c a b c a b a b a b d

i

a b a b d

here $s(i) = b$
 $P(i+1) = b$ match
 move i to j

(i)

a b a b c a b c a b a b a b d

a b a b d

(j)

here $s(i) = a$
 $P(j+1) = a$ match i & j + 1

(i)

a b a b c a b c a b a b a b d

a b a b d

(j)

$s(i) = b$
 $P(j+1) = b$ match i & j + 1

i

a b a b c a b c a b a b a b d

a b a b d

j

$s(i) = c$
 $P(j+1) = b$ not match

Now move j to its π index which is 2

2

②

a b a b c a b c a b a b a b d
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

③

a b a b d
1 2 3 4 5

$i = c$
 $j+1 = a$ not match

a b a b repeating
so maybe we have to start from next

i

a b a b c a b c a b a b a b d

a b a b d

④ m o f

$s(i) = c$
 $p(j+1) = a$
no match
increase i

⑤

a b a b c a b c a b a b a b d

a b a b d

$s(i) = a$
 $p(j+1) = a$ match
 $i++; j++;$

i

a b a b c a b c a b a b a b d

a b a b d

$s(i) = b$
 $p(j+1) = b$ match