

Ans

Challenge 1

We use openssl commands on our terminal to obtain key from priv.pem, input from cipher.bin and prints the output after decryption which is our flag.txt

Challenge 2

The name of the issuer can be seen by going to <https://www.cse.iitb.ac.in> and then going to the section connection security details in safari browser settings. After that tap on show certificate & you view a certificate on which the issuer's name appears

Challenge 3

n = order of generator
 h_1 & h_2 are the hash of the first 2 elements of the message list that we choose

$$S_{13} \cdot S_{14} = h_1 + x_2 \pmod{n} \quad S_{23} = h_2 + x_2 \pmod{n}$$

[x will be same]

Subtracting $(s_1 - s_2)k = h_1 - h_2 \pmod{n}$

$$k = \frac{h_1 - h_2}{s_1 - s_2} \cdot (s_1 - s_2)^{-1} \pmod{n}$$

$$s_1 k = h_1 - s_2 \pmod{n} \rightarrow s_2 = s_1 k - h_1 \pmod{n}$$

$$x = (s_1 k - h_1) \cdot s_2^{-1} \pmod{n}$$

Challenge 4

Variant 1:

If Eve has a signature (R_1, S) on any message m , it can:
 • Recompute γ locally by evaluating $H(m||P_2) \pmod{q}$

• Compute $h = H(R_1, P_2, m) \pmod{q}$ like the signer

$$\gamma = (S - \gamma) \cdot h^{-1} \pmod{q}$$

Steps:

• Obtain ~~private~~ public key P_2

• Request a single signature on a chosen message m

• Recompute $\gamma = H(m||P_2) \pmod{q}$

$$h = H(R_1, P_2, m) \pmod{q}$$

$$\text{Compute } \gamma = (S - \gamma) \cdot h^{-1} \pmod{q}$$

• Forge signature on challenge message using the recovered γ .

Variant 2:

We choose messages such that their first halves are identical.

For a 1 byte message m we have $\lfloor m/2 \rfloor = 0$ hence $m_{[0]}$ is the empty string. Therefore for any single byte message the hash inputs become identical, and thus the server computes the same s for each such signed message.

$$s_1 = s + h_1 \cdot x \pmod{g}$$

$$s_2 = s + h_2 \cdot x \pmod{g}$$

$$s_1 - s_2 = (h_1 - h_2) \cdot x \pmod{g}$$

$$x = (s_1 - s_2)(h_1 - h_2)^{-1} \pmod{g}$$

With x recovered we proceed like in variant 1 to compute correct s for the challenge message & forms a valid signature (R, s) that will pass verification.