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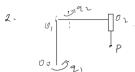
1. To prove: RS(a) Rt = S(Ra)

Consider s(la). R.a we will use the identity S(a). P = axp to separate Rand a ha S(Ra)

S(Ra). (Ra) z (Ra) x (Ra) = R. (axa) = R. S(a). a = R. S(a). I?.a = RISLA, RT R.a

S(Ra), $(Ra) = (R, S(a)R^T)(Ra)$

$$\Rightarrow$$
 $S(Ra) = (R.S(a).R^{T})$



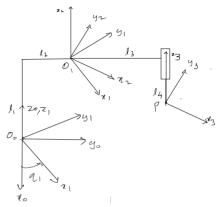
Or RRP SCARt schematte

P nitrally, M sinks are in the y-2 plane

$$R_{0}^{\prime} = \begin{bmatrix} R_{2}q_{1} \\ R_{2}q_{1} \end{bmatrix} = \begin{bmatrix} q_{1} & -sq_{1} & 0 \\ sq_{1} & (q_{1}) & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad d_{0}^{\prime} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$R_{1}^{2} = \begin{bmatrix} R_{2}q_{2} \end{bmatrix} = \begin{bmatrix} Q_{12} & -Q_{2} & 0 \\ Q_{1} & Q_{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
 $A_{1}^{2} = \begin{bmatrix} P_{11} & P_{12} & P_{13} \\ P_{11} & P_{12} & P_{13} \\ P_{13} & P_{13} & P_{13} \end{bmatrix}$

$$k_{1}^{3} = I^{3}$$
 $k_{1}^{3} = \begin{bmatrix} 0 \\ k_{3} \\ -k_{4} \end{bmatrix}$



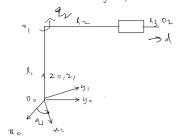
Ly is the fixed mitial length before extensional the prismoutiz joint

$$H_{0}^{1} = \begin{bmatrix} c_{11} & -c_{21} & 0 & 0 \\ c_{21} & c_{21} & c_{22} & c_{23} \\ c_{22} & c_{23} & c_{23} \\ c_{21} & c_{22} & c_{23} \\ c_{21} & c_{22} & c_{23} \\ c_{22} & c_{23} & c_{23} \\ c_{21} & c_{22} & c_{23} \\ c_{21} & c_{22} & c_{23} \\ c_{22} & c_{23} & c_{23} \\ c_{21} & c_{22} & c_{23} \\ c_{22} & c_{23} & c_{23} \\ c_{23} c_{23} &$$

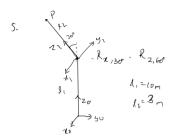
$$R_{01} = R_{201} \qquad d_{01} = 0 \qquad \qquad H_{01} = \begin{bmatrix} R_{201} & d_{01} \\ 0 & 1 \end{bmatrix}$$

$$R_{12} = R_{11}, R_{12}, R_{201} \qquad d_{12} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \qquad H_{12} = \begin{bmatrix} R_{201}, R_{201} & d_{01} \\ 0 & 1 \end{bmatrix}$$

mitially all links are in the y-z plane



$$\begin{aligned} &\mathcal{K}_{01} = & \mathcal{K}_{2} \mathbf{\hat{I}}_{1} & \mathcal{O}_{01} = \mathbf{0} \\ &\mathcal{R}_{11} = & \mathcal{R}_{11} \mathbf{\hat{I}}_{11} \mathbf{\hat{I}}_{12} + \mathcal{R}_{12} \mathbf{\hat{I}}_{12} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{1} \end{bmatrix} \\ &\mathcal{R}_{13} = \mathbf{I}^{2} \\ &\mathcal{R}_{3} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix} \end{aligned} \qquad \begin{aligned} &\mathcal{H}_{12} = \begin{bmatrix} \mathcal{R}_{13} \mathbf{1}_{12} & \mathcal{R}_{12} \\ \mathbf{0} \\ \mathbf{1} \end{bmatrix} \\ &\mathcal{R}_{23} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix} \end{aligned} \qquad \begin{aligned} &\mathcal{H}_{12} = \begin{bmatrix} \mathcal{R}_{13} \mathbf{1}_{12} & \mathcal{R}_{12} \\ \mathbf{0} \end{bmatrix} \\ &\mathcal{R}_{23} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{bmatrix} \end{aligned}$$



At final orientation, obstacle is 3m directly above the drone i.e w.r.t dione, posttion of 0 to take is 0,0,3. The means that the final rotation R2160 does not affect relative position of obstade.

(. Types of Gearboxes used for Motors in robotic applications:

Planetary Gearbox

Central sun gear rotates three to four planet gears that encircle it.

Pros- High torque produced in a small area, precise and durable.

Cons- Complex design and construction, high power dissipation.

oidal Drive
Also called speed reducers, they reduce the speed of rotation of the input shaft. The ratio of reduction can be high with low play or backlash.
Pros- Low backlash and hence lost energy, low noise, high impact resistance.
Cons- Manufacturing is complex and requires high precision.

Position of obstacle in base frame is $\left(0^{\frac{1}{4}} - \frac{3}{3} \frac{1}{3} + \left(10 + \frac{3}{13}\right) \hat{h}\right)$ in

In drone applications, BLDC motors are used due to low friction and hence higher efficiency. For a drone the motors rotate propellers that push air downwards and provide lift, thus moving the drone upwards. The torque required to do this is generally sufficiently provided by a BLDC motor. So a gearbox is not usually required. Also, gearboxes are usually heavy and add more to the payload of the drone. The high RPMs of the propeller can result in faster wear and tear for a gearbox. These factors make a gearbox undesirable in general drone applications.

Reference
[1]
P. L. García, S. Crispel, E. Saerens, T. Verstraten, and D. Lefeber, "Compact Gearboxes for Modern Robotics: A Review," Frontiers in Robotics and AI, vol. 7, Aug. 2020, doi: 10.1009/journal.1009/journal.1009



$$\mathcal{J}_{1} = \begin{bmatrix} z_{0} \times (0_{0}^{3} - 0_{0}^{0}) \end{bmatrix} \qquad \qquad \mathcal{J}_{1} = \begin{bmatrix} z_{1} \times (0_{0}^{3} - 0_{0}^{1}) \\ z_{0} \end{bmatrix} \qquad \qquad \mathcal{J}_{3} \begin{bmatrix} z_{3} \\ 0 \end{bmatrix}$$

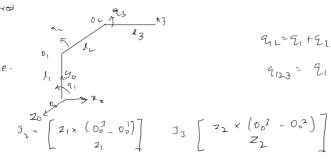
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J =-	-13912 - 1291 -138912 - 12891
	-135912 -12521
	0
	0
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Manipulator Jacobian for RRP SCARA

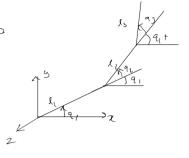
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Schematiz of the required RRR configuration:

> All links are coplana and are on the XY plane.







$$Z_0 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \qquad Z_1 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \qquad Z_2 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$O_{6} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \qquad O_{1} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \qquad O_{2} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \qquad O_{3} = \begin{bmatrix} 1$$

from 2R manipulator

$$J = \begin{bmatrix} -(l_1 s_1 + l_2 s_{11} + l_3 s_{11}) & -(l_2 s_{11} + l_3 s_{11}) & -l_3 s_{11} \\ l_1 c_1 + l_2 c_1 + l_3 c_{12} & l_2 c_1 + l_3 c_{12} \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

Which is the required menipulato Jacostan