

Assignment 6

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Q.1)

1. arr = [1, 3, 7, 9, 12, 10, 8, 16, 18, 22, 27]
Create a buildHeap method that returns a minheap.

heapify(arr, n, i):
// Write your own code

buildHeap(arr, n):
//Write your own code
heapify(arr, n, i)

Ans)

* javascript implementation

Code:

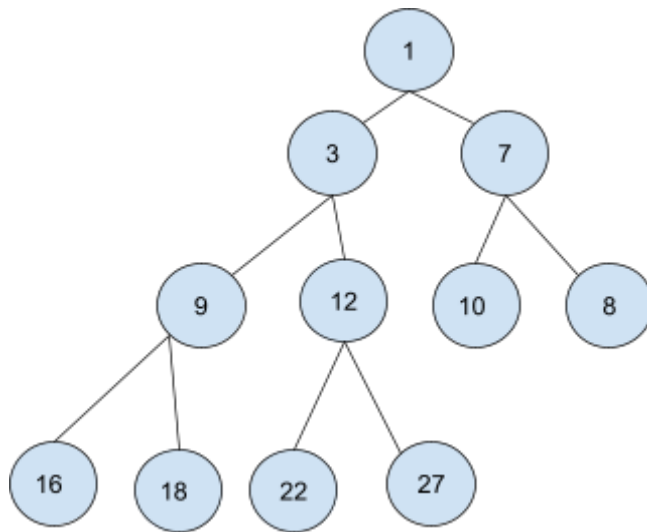
```
function swap(nthIndex,parentIndex,heap){
    let temp = heap[parentIndex];
    heap[parentIndex] = heap[nthIndex];
    heap[nthIndex] = temp;
    return heap;
}

function buildHeap(heap,arr,num){
    heap = arr;
    let n = num;
    let height = Math.floor((arr.length-1)/2)
    if(n<0){
        return heap
    }
    for (let i = 0; i < height; i++) {
        let parent = (Math.round(n/2))-1
        if(parent < 0){
            break;
        }
        if(heap[n] < heap[parent]){
            swap(n,parent,heap)
        }
        n = parent;
    }
    return buildHeap(heap,arr,--num);
}

function minHeap(arr){
    let heap=[];
    return buildHeap(heap,arr,arr.length-1);
}

const arr = [1, 3, 7, 9, 12, 10, 8, 16, 18, 22, 27]
const result = minHeap(arr);
console.log(result);
```

Output :



Comparison flowChart:

* The output generated by printing nodes and indexes dynamically

childIndex: 10 value => 27 , parentIndex: 4 value => 12
childIndex: 4 value => 12 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 9 value => 22 , parentIndex: 4 value => 12
childIndex: 4 value => 12 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 8 value => 18 , parentIndex: 3 value => 9
childIndex: 3 value => 9 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 7 value => 16 , parentIndex: 3 value => 9
childIndex: 3 value => 9 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 6 value => 8 , parentIndex: 2 value => 7
childIndex: 2 value => 7 , parentIndex: 0 value => 1

childIndex: 5 value => 10 , parentIndex: 2 value => 7
childIndex: 2 value => 7 , parentIndex: 0 value => 1

childIndex: 4 value => 12 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 3 value => 9 , parentIndex: 1 value => 3
childIndex: 1 value => 3 , parentIndex: 0 value => 1

childIndex: 2 value => 7 , parentIndex: 0 value => 1

childIndex: 1 value => 3 , parentIndex: 0 value => 1

Analysis :

Total No of Nodes = 11;

*Reference

Level =0;

Height = 1;

To find the height of the tree

$$N = 2^h - 1$$

$$N + 1 = 2^h$$

Taking log on both sides

$$\log(N + 1) = \log(2^h)$$

$$h * \log_2 2 = \log(N + 1)$$

$$h = \log(N + 1)$$

Taking the upper bound of the h

$$h = \log(11 + 1)$$

$$h = 4$$

Explanation:

Time Complexity = No of Comparisons + No of swaps

From the given input we can see that the input array is already sorted.
Hence,

No of swaps = 0; Best case;

Therefore, swaps can be neglected

Comparing the Comparison flowchart, we see that the number of comparisons has been reduced by 2 (Parent node).

Hence,

No of comparison = $n \cdot \log(n)$

n is the index of nodes starting at the leaf node. For each node n , the comparison goes until the root node with $\log(n)$ complexity

Total Time Complexity = $(n \cdot \log(n)) + O(1)$;
= $O(n \log(n))$

Auxiliary Space = $O(n)$, New array is created for heap