

Assignment 1

Name : Hrishikesh Rajan

Email : hrishikeshrajan3@gmail.com

LinkedIn : <https://www.linkedin.com/in/hrishikesh-rajan-96aa70165>

Question 2)

You are a product manager and currently leading a team to develop a new product. Unfortunately, the latest version of your product fails the quality check. Since each version is developed based on the previous version, all the versions after a bad version are also bad. Suppose you have a version and you want to find out the first bad one, which causes all the following ones to be bad. Also, talk about the time complexity of your code.

Test Cases:

Input: [0,0,0,1,1,1,1,1,1]

Output: 3

Explanation: 0 indicates a good version and 1 indicates a bad version. So, the index of the first 1 is at 3. Thus, the output is 3

*A Javascript implementation is provided

Answer :

```
function findBadVersion(arr, low, high, goodVersion, badVersion){

    if(low <= high){
        let mid = Math.floor(low + ((high - low)/2));

        if((goodVersion === arr[mid-1] && badVersion === arr[mid]) || arr[mid] === badVersion &&
arr.length === 1){
            return mid;
        }
        if(badVersion > arr[mid] ){
            return findBadVersion(arr, mid+1, high, goodVersion, badVersion);
        }
        if(badVersion <= arr[mid]){
            return findBadVersion(arr, low, mid-1, goodVersion, badVersion);
        }
    }
    return -1;
}

const arr = [0,0,0,1,1,1,1,1,1];
```

```
const result = findBadVersion(arr,0,arr.length-1,0,1)
console.log(result)
```

Output : 3

Time Complexity :

The recurrence relation is formed by

$$T(n) = T(n/2) + c, \quad c = \text{constant.} \quad (1)$$

The reason for $T(n/2)$ is that at a time our search space was limited to half of n , that is $n/2$, where n is the total length of the array.

Applying Master's Theorem

$$T(n) = aT(n/b) + f(n), \text{ where } f(n) = \Theta(n^k \log^p n) \quad (2)$$

From the above recurrence relation (1)

$$a=1$$

$$b=2$$

$$k=0$$

$$p=0$$

Substituting values

$$\log_a^b = \log_2^1 = 0$$

That means $\log_a^b = k$ and $P > -1$, This relation comes under case 2.

Then the equation becomes $\Theta(n^k \log^{p+1} n)$

$$= \Theta(n^0 \log^{0+1} n)$$

$$= \Theta(1 * \log^1 n)$$

$$= \Theta(\log n)$$

Time Complexity = $O(\log n)$

Space Complexity = $O(1)$