

NUMBER SYSTEMS

WRITING A VALUE

How many different ways can you represent the number '7'

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






















































7, VII, IIIIII, IIII, 7 apples etc

EARLY HUMANS



How did they communicate numbers?

IMPROVED SYSTEMS...

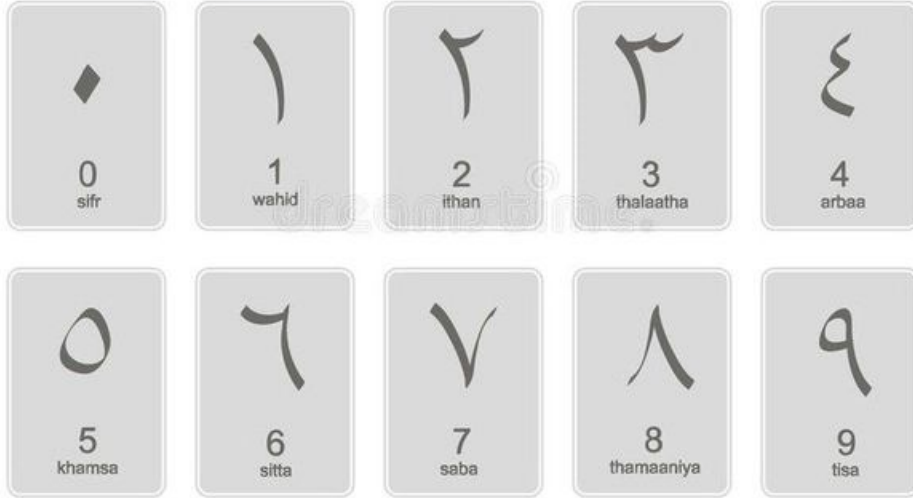
| | | | | | |
|--|--|--|---|--|--|
| 1  | 11  | 21  | 31  | 41  | 51  |
| 2  | 12  | 22  | 32  | 42  | 52  |
| 3  | 13  | 23  | 33  | 43  | 53  |
| 4  | 14  | 24  | 34  | 44  | 54  |
| 5  | 15  | 25  | 35  | 45  | 55  |
| 6  | 16  | 26  | 36  | 46  | 56  |
| 7  | 17  | 27  | 37  | 47  | 57  |
| 8  | 18  | 28  | 38  | 48  | 58  |
| 9  | 19  | 29  | 39  | 49  | 59  |
| 10  | 20  | 30  | 40  | 50  | |

FURTHER IMPROVEMENTS...

| | | | | | |
|----|------|----|-------|------|---|
| 1 | I | 11 | XI | 50 | L |
| 2 | II | 12 | XII | 100 | C |
| 3 | III | 13 | XIII | 500 | D |
| 4 | IV | 14 | XIV | 1000 | M |
| 5 | V | 15 | XV | | |
| 6 | VI | 16 | XVI | | |
| 7 | VII | 17 | XVII | | |
| 8 | VIII | 18 | XVIII | | |
| 9 | IX | 19 | XIX | | |
| 10 | X | 20 | XX | | |

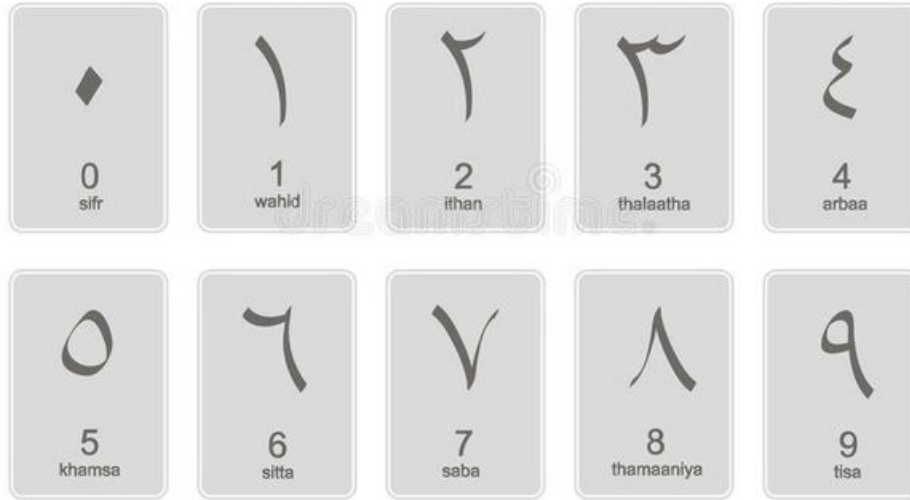
What patterns do you observe in the roman numbering system?

TODAY...



The decimal number system - How many symbols? Why this quantity?

TODAY...



After the last symbol, the numbers will repeat for the first time. Hence we put a '1' before them.

10

The number '10' means 0 is repeating for the first time.

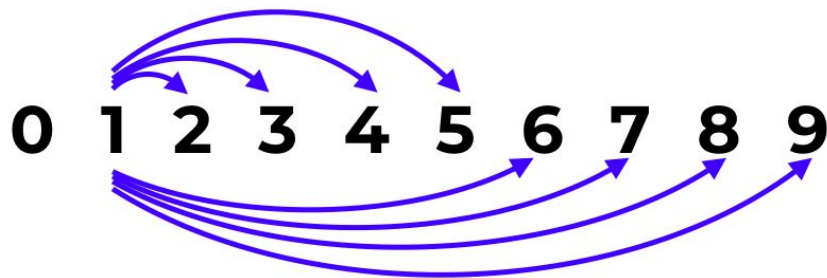
20

The number '20' means 0 is repeating for the second time.

A GENERAL PATTERN.

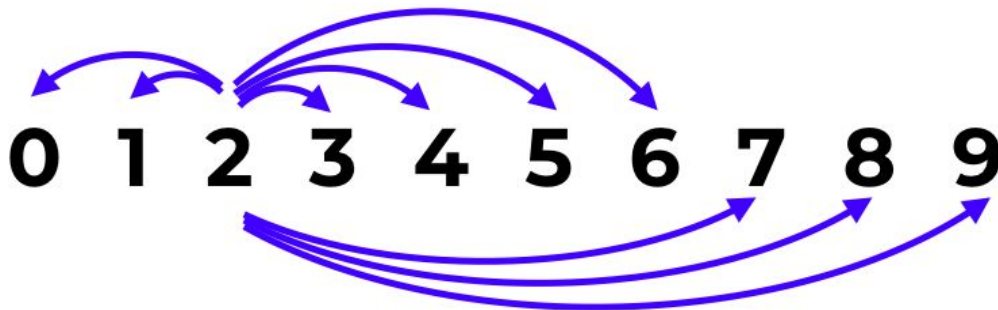
So after the basic 9 symbols, how do we make the next numbers?

10
├──┘
0 1 2 3 4 5 6 7 8 9



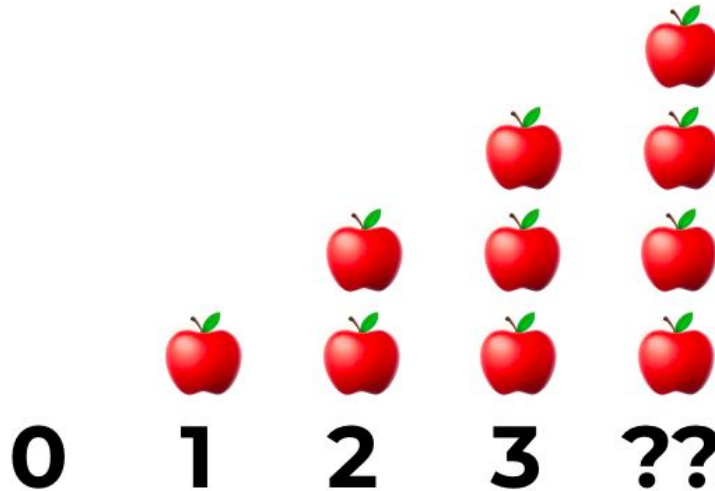
A GENERAL PATTERN.

So on and so forth...



QUESTION

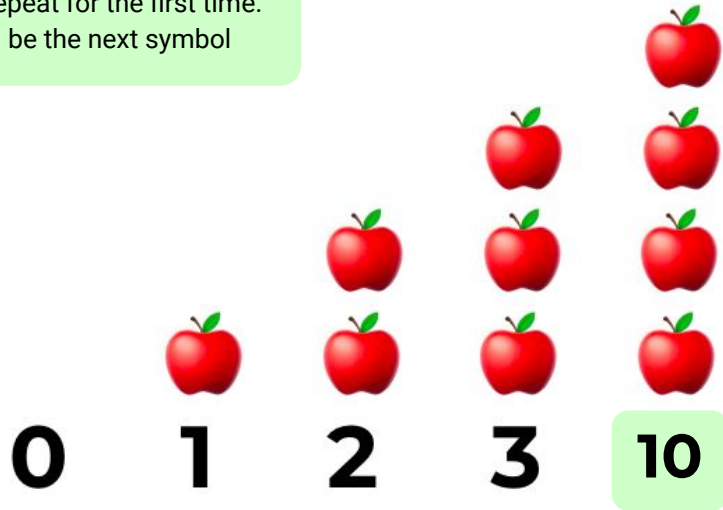
A number system has only four symbols - 0, 1, 2, & 3. What will be the next number in the sequence?



QUESTION

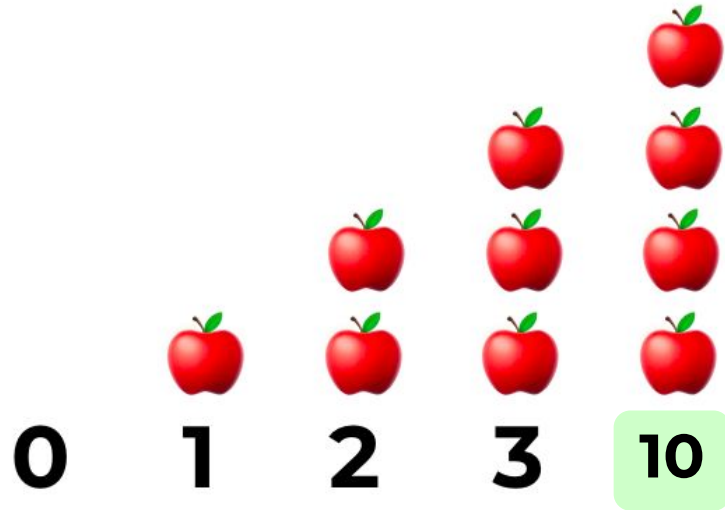
A number system has only four symbols - 0, 1, 2, & 3. What will be the next number in the sequence?

Symbol '0' will repeat for the first time.
Hence **10** will be the next symbol



QUESTION

Why isn't '4' the symbol you would put here?



QUESTION



In the same number system, what quantity of apples are shown here?

QUESTION



In the same number system, what quantity of apples are shown here?

11 apples are shown here.

GUIDED PRACTICE

**Given a number system that has 5 digits - A, B, C, D, E.
Expand this number system to the first 20 numbers**

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Given a number system that has 5 digits - A, B, C, D, E.
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How many stars are shown
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How many stars are shown
according to this system?

CA stars are shown here.

GUIDED PRACTICE

Given a number system that has 5 digits - A, B, C, D, E.
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BCA, BCB, _____, BCD, _____.

Fill in the missing numbers

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Given a number system that has 5 digits - A, B, C, D, E.
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BCA, BCB, _____, BCD, _____.

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BCC, BCE.

GUIDED PRACTICE

A new number system used in a machine understands only 3 digits - □, △, ○

Which digit represents decimal zero?

What will be the next digit in the series?

Apoorva has 2 apples. How will he use this number system to show the quantity of apples?

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INDEPENDENT PRACTICE

Design your own number system with any number of digits(try keeping it less than 12) and any types of symbols (arabic numbers, english letters, hindi letters, shapes).
Write at least the first fifteen numbers in this system.

CONVERTING TO DECIMAL

EXPAND THE FOLLOWING NUMBERS - 264, 2867

PLACE VALUE

EXPAND THE FOLLOWING NUMBERS - 264, 2867

$$364 = 3 \times 100 + 6 \times 10 + 4 \times 1$$

$$2867 = 2 \times 1000 + 8 \times 100 + 6 \times 10 + 7 \times 1$$

What did we do here? Do you notice a pattern?

BY THIS LOGIC

A system has 4 digits - A, B, C, D, then which of the following will be correct for a number BAC?

(Option 1) $BAC = B \times 10^2 + A \times 10^1 + C \times 10^0$

(Option 2) $BAC = B \times 4^2 + A \times 4^1 + C \times 4^0$

CONVERT A NUMBER TO DECIMAL

STEP 1 - Take the symbols
and assign a decimal number
to each character.

Example -

A \rightarrow 0

B \rightarrow 1

C \rightarrow 2

D \rightarrow 3

CONVERT A NUMBER TO DECIMAL

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STEP 2 - Now, write the expanded place value form of the symbols

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Example -

$$BAC = B \times 4^2 + A \times 4^1 + C \times 4^0$$

STEP 3 - Replace each digit with the corresponding number from step 1.

Example -

B becomes 1, A becomes 0, C becomes 2

$$BAC = 1 \times 4^2 + 0 \times 4^1 + 2 \times 4^0$$

CONVERT A NUMBER TO DECIMAL

STEP 1 - Take the symbols and assign a decimal number to each character.

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$$BAC = B \times 4^2 + A \times 4^1 + C \times 4^0$$

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Example -

B becomes 1, A becomes 0, C becomes 2

$$BAC = 1 \times 4^2 + 0 \times 4^1 + 2 \times 4^0$$

STEP 4 - Solve this equation, you'll get the conversion

Example -

BAC = 18 in decimal

PRACTICE

STEP 1 - Take the symbols and assign a decimal number to each character.

STEP 2 - Now, write the expanded place value form of the symbols

STEP 3 - Replace each digit with the corresponding number from step 1.

STEP 4 - Solve this equation, you'll get the conversion

A number system has 5 digits - M, N, O, P, Q. Convert the numbers NNO, QO, OQP into decimal.

TRUE OR FALSE

In a number system - X, Y, Z - the next number in the series would be XY

In a number system - X, Y, Z - the number '5' is represented by YZ

The number 623 indicates that the number '23' is repeating for the 6th time.

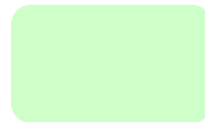
A symbol such as '10' can represent  or  based on the number system.

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