

$O(n)$

q → queries

$l_i$   $r_i$

$$\text{sum}(l, r) = \text{sum}(0, r) - \text{sum}(0, l-1)$$

$O(1)$

prefix sum

2

0

2

4

$$\rightarrow a_0 + a_1 + a_2 + a_3 + a_4$$

1

3

$$\rightarrow a_1 + a_2 + a_3$$

2

5

$$\rightarrow a_2 + a_3 + a_4 + a_5$$

1

4

$$\rightarrow a_1 + a_2 + a_3 + a_4$$

$$\sum q(i) \times ans(i)$$

1 1 3 3 4 4

$O(q \times n)$

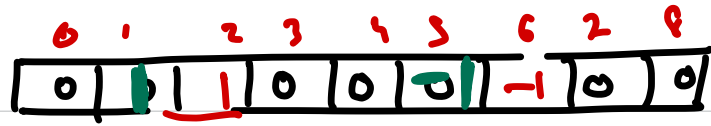


1 2 3

0	1	2	3	4	5
1	2	1	0	-1	2

1	3	4	4	3	1
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Q



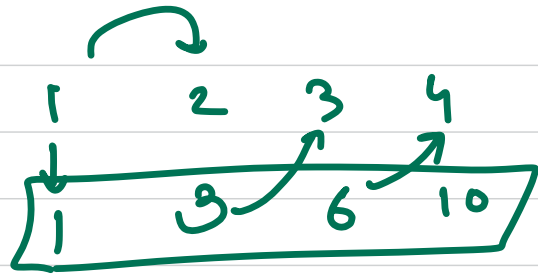
prefix sum → cumulative sum

q → query  
l: r

$a[l] += 1$   
 $a[r+1] -= 1$

$O(1)$   
 $O(n)$   
 $O(q+n)$

2 5  
 1 4



→ cumulative sum

Some indexes are occurring more frequently in  
our Sun

→ how about finding the index which is  
offered by most queries

5 3

5 2 4 1 3



1 2 3 4 5  
1 1 1 3 3

1 5 ~~✓~~ → 0 4

2 3 → 1 2

3 3 → 1 2

0	1	2	3	4
1	1	0	1	0

1 2 0 -2 0

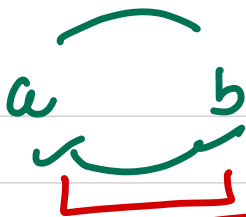
1 3 3 1 1

1 5 4 2 3

1x1 + 3x5 + 3x4 + 1x2 + 1x3

Sum

→



31

30

a, b, c

ab > ba

9

30

ab > ba

✓ ab

c

a b  
9 30  
-

c b  
30

$$ab > ba$$

$$bc > cb$$

$$ac > \underline{\underline{ca}}$$

b c a  
5 6 9  
9

$$\begin{array}{cc} ab & ba \\ 95 & 59 \\ > \end{array}$$
$$\begin{array}{cc} bc & cb \\ 56 & 65 \end{array}$$

$$\begin{array}{cc} ac & ca \\ 96 & 69 \end{array}$$

$\rightarrow a, b, c \rightarrow \underline{\underline{\text{non-negative}}}$

a, b, c

$ab > ba$  and  $bc > cb$  then

$a = 9$   $b = \underline{\underline{30}}$   
 $ab = \underline{\underline{930}}$   $9 \times 10^2 + 30$

$ac > ca$

$\rightarrow ab > bc$

$|x| \rightarrow \text{no. of digits}$

$\rightarrow a \times 10^{|b|} + b > b \times 10^{|a|} + a$

①

$bc > cb$

$b \times 10^{|c|} + c > c \times 10^{|b|} + b$

②

$$ab > bc$$

$$a \times 10^{|b|} + b > b \times 10^{|a|} + \underline{a}$$

$$bc > cb$$

$$b \times 10^{|c|} + c > c \times 10^{|b|} + b$$

$$\rightarrow a(10^{|b|} - 1) > b(10^{|a|} - 1)$$

$$b(10^{|c|} - 1) > c(10^{|b|} - 1)$$

$$\cancel{a} \cancel{b} (10^{|c|} - 1) \cancel{(10^{|b|} - 1)} > \cancel{b} \cancel{c} (10^{|a|} - 1) \cancel{(10^{|b|} - 1)}$$

$$a(10^{|c|} - 1) > c(10^{|a|} - 1)$$



$$a \times 10^{|c|} - a > c \times 10^{|a|} - c$$

$$a \times 10^{|c|} + c > c \times 10^{|a|} + a$$

$$\boxed{ac > ca} //$$

$$a \quad b \quad c$$

$$ab > ba, \quad bc > cb$$

$$\boxed{ac > ca}$$

ab

ba

$a = 30 \quad b = 37$

ba > ab

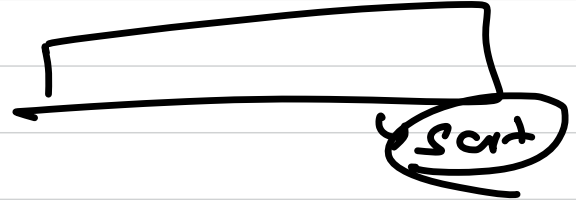
$a = 9 \quad b = 37$

ab > ba



cmp(a, b)

ab < ba



$[3, 30, 34]$

$3, 30, 34$

$3, 34, 30$

$[34, 3, 30]$

$[34, 3, 30]$

$(330)$

$303$   
 $[34, 3, 30]$   
 $4 \quad 3 \quad 0$

$ab > ba$

$bc > cb$

$ac > ca$

$3430 > 3034$

34, 3, 30  
 1, b, c

$ab > ba$   
 $bc > cb$

$ac > ca$

$ac > ca$   
 $(a)bc > cb(a)$

3430 > 3034  
3430 > 3034

11  
3, 30, 37

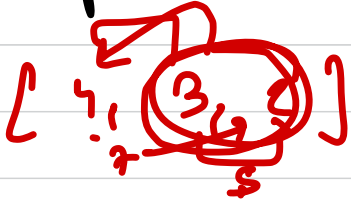
3 37 30

34 3 20  
✓✓



master sub

Q.2 You're given  $n$  ropes of diff length. We need to merge these ropes into one rope. Cost of merging 2 ropes is equal to Sum of their lengths. Merge all the ropes with min cost.



①  $5 + 9 \rightarrow 14$

②  $2 + 9 \rightarrow 16$

$\sum a_i \times f_i$

$(3+2) + (3+2+1) \Rightarrow 14$

$(4+3) + (4+3+2) \Rightarrow 16$

[

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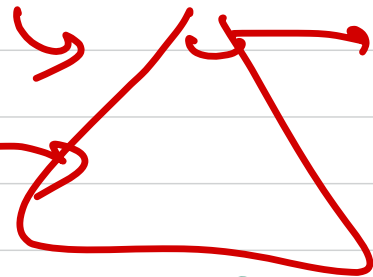
$\log n$

min heap

min element

$x$   
 $y$   $\rightarrow$   $2p-1$

$x+y$   $\rightarrow$  2



4, 3, 2

Ans for 2

