



# SPIKING NEURAL NETWORKS

ICT in Intelligent Networks

Blagoj Hristov 157/2016

- Artificial Neural Networks - the first step towards true artificial intelligence
- An attempt to replicate the human brain through computational algorithms
- Evolution of the neural network architecture
- Generations of neural networks



- First Generation - the Perceptron algorithm (1958) - able to perform binary classification of data
- Second Generation - Multi-layer neural network architecture, multiple different types of neurons, deep learning - able to perform significantly more complex tasks
- Third generation - the future of artificial intelligence, but what does it entail?

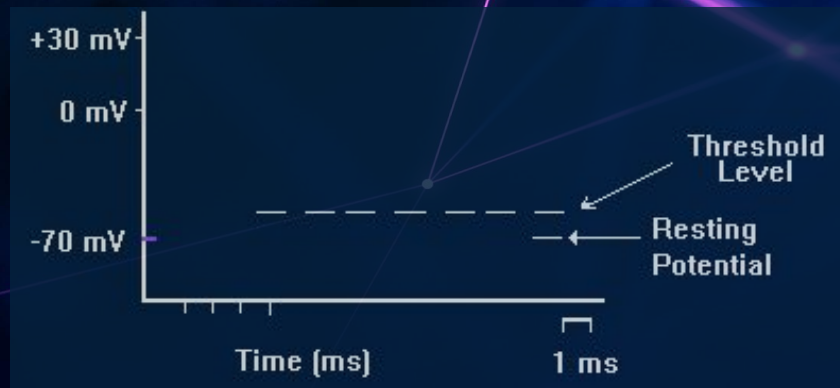
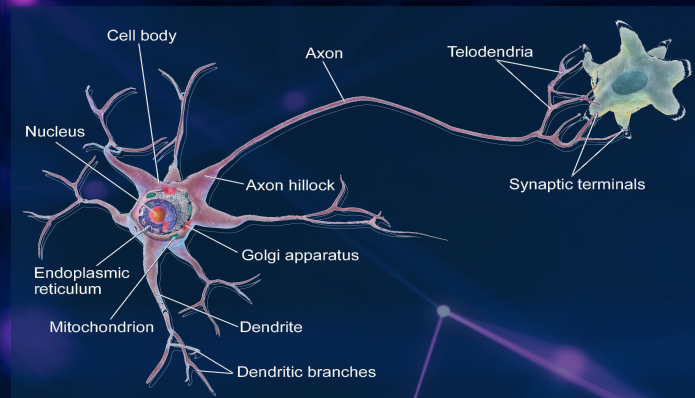


# SPIKING NEURAL NETWORKS

# SPIKING NEURAL NETWORKS – THE FUTURE OF AI?



- Biological neurons - how do they work?!
- Voltage spikes
- Receptive field
- Neural communication
- Refractory period

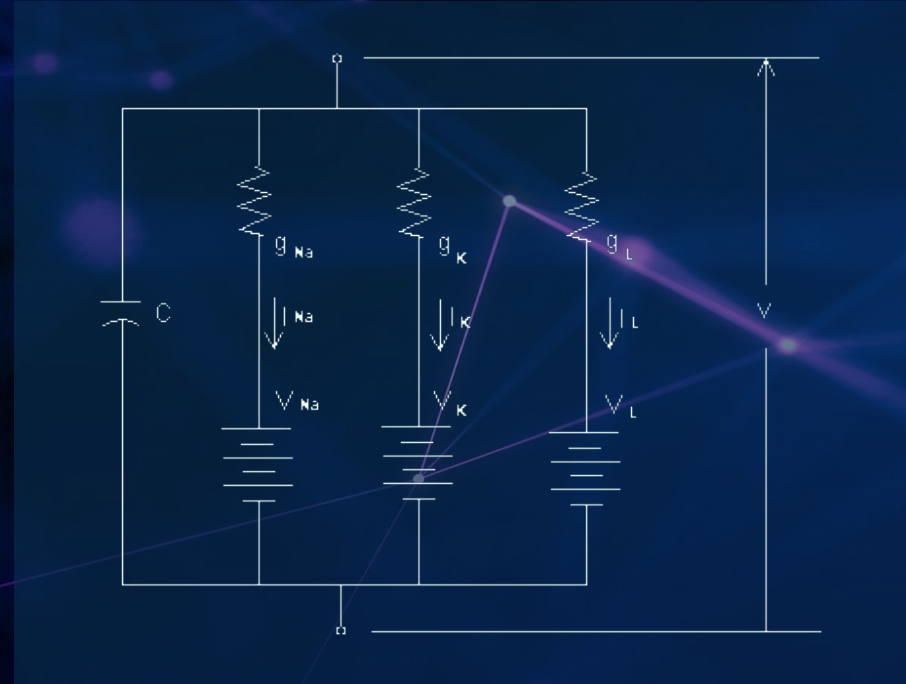




# COMPUTATIONAL MODELS OF NEURONS



- Hodgkin and Huxley model (1952)
- Simplification of neurons as an electrical circuit
- Based on the most common ions used in generation of action potentials
- Implement leaky current to simulate refractory period



# SOLVING THE CIRCUIT



- Using Ohm's Law we get the equations at ( 1 ):
- By using the current - voltage relations we reach the expressions given at ( 2 ):
- The parameters  $g_{K\_bar}$  and  $g_{Na\_bar}$  are constant, while  $n$ ,  $m$  and  $h$  vary according to the following differential equations:

$$I_{Na} = g_{Na} (E - E_{Na})$$

$$I_K = g_K (E - E_K)$$

$$I_L = g_L (E - E_L)$$

( 1 )

$$I_{Na} = g_{Na} (V - V_{Na}) = g_{Na} (E_{Na} - E_R)$$

$$I_K = g_K (V - V_K) = g_K (E_K - E_R)$$

$$I_L = g_L (V - V_L) = g_L (E_L - E_R)$$

$$V = E - E_R$$

( 2 )

$$g_k = g_{K\_bar} n^4 \quad g_{Na} = m^3 h g_{Na\_bar}$$

# SOLVING THE CIRCUIT



$$\frac{dn}{dt} = \alpha_n(1 - n) - \beta_n n$$

$$\frac{dm}{dt} = \alpha_m(1 - m) - \beta_m m$$

$$\frac{dh}{dt} = \alpha_h(1 - h) - \beta_h h$$

- The Hodgkin - Huxley model is a great achievement for 20th century biophysics
- Not suitable for large scale simulation of spiking neural network
- It can be modified/improved in two ways

# IMPROVING THE MODEL FOR AI



- Create a more detailed model:
  - more types of ion channels
  - incorporate factors that influence conductance
  - take the shape of the neuron into account

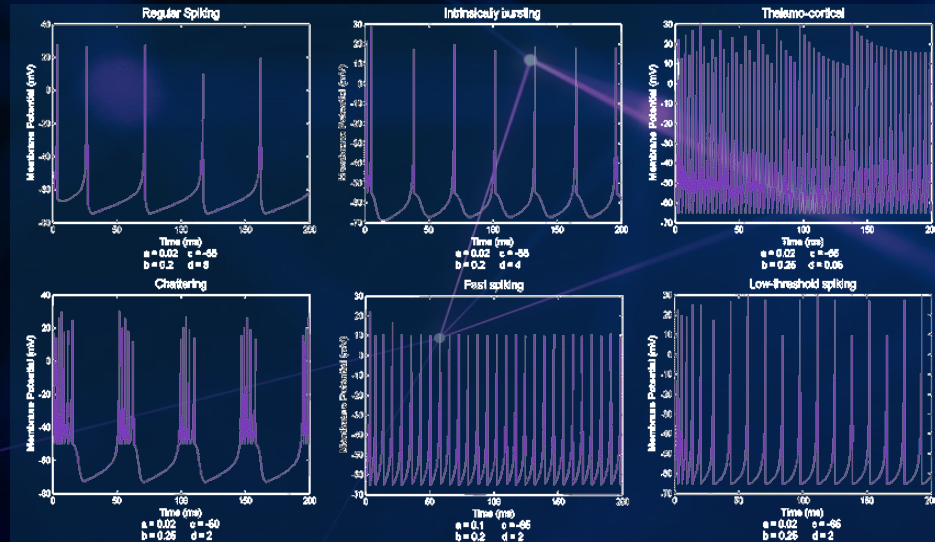
- Pros:
  - higher detail allows for more realistic behaviour
  - closest model to a real biological neuron
- Cons:
  - much more computationally expensive
  - impractical for data science due to extremely slow simulations



# IMPROVING THE MODEL FOR AI



- Alternative method: use spiking patterns!
- Just one spike doesn't carry enough data
- 1D vector of membrane voltage values in accordance to time carries much more information
- Different types of spiking patterns



# INTEGRATE-AND-FIRE MODEL



- One of the first computational models of a biological neuron (1907)
- Simple differential equation that uses the equation for capacitor current to simulate a voltage spike ( 1 )
- Can be improved by incorporating a refractory period  $t_{ref}$  making the model more realistic ( 2 )
- Not biologically accurate due to no time-dependent memory

$$I(t) = C_m \frac{dV_m(t)}{dt} \quad (1)$$

$$f(I) = \frac{I}{C_m V_{th} + t_{ref} I} \quad (2)$$

# LEAKY INTEGRATE-AND-FIRE



- Improvement of the basic integrate-and-fire model
- Modification of the equation by adding a 'leak' term to the membrane potential to solve the memory problem ( 1 )
- The firing frequency no longer increases linearly as the input current increases ( 2 )

$$I(t) - \frac{V_m(t)}{R_m} = C_m \frac{dV_m(t)}{dt} \quad (1)$$

$$f(I) = \begin{cases} 0, & I \leq I_{th} \\ [t_{ref} - R_m C_m \log(1 - \frac{V_{th}}{IR_m})]^{-1}, & I > I_{th} \end{cases} \quad (2)$$

# IZHIKEVICH NEURONS



- Simple implementation of spiking neurons by Eugene M. Izhikevich
- Combines the Hodgkin - Huxley biologically plausible dynamics with integrate-and-fire computationally efficient neurons
- Using bifurcation methodologies, we can reduce the equations of the Hodgkin - Huxley model:

$$C_m \frac{dv}{dt} = k (v - v_r) (v - v_t) - u + I$$

$$\frac{du}{dt} = a [b (v - v_r) - u]$$

→ Using auxiliary after-spike resetting:

if  $v \geq 30\text{mV}$ , then reset:

$$v = c$$

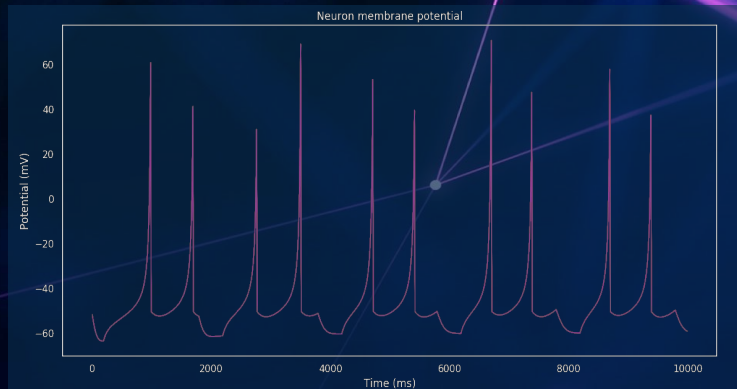
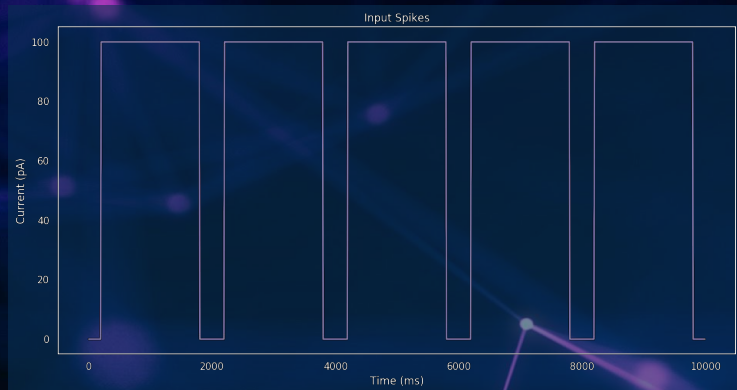
$$u = u + d$$



# IZHIKEVICH NEURONS



- The parameter  $a$  describes the time-scale of the recovery variable  $u$ . Smaller values  $\rightarrow$  slower recovery
- The parameter  $b$  describes the sensitivity of the recovery variable  $u$
- The parameter  $c$  describes the after-spike reset value of the membrane voltage  $v$
- The parameter  $d$  describes the after-spike reset of the recovery variable  $u$
- The parameter  $C_m$  describes the membrane capacitance
- The parameter  $v_r$  is the resting membrane potential while  $v_t$  is the instantaneous threshold potential
- The parameter  $k$  is a constant defined as  $1/R$  where  $R$  is the membrane resistance



$a = 0.03$  [kHz]  
 $b = -2$  [S]  
 $c = -50$  [mV]  
 $d = 100$  [pA]  
 $C_m = 100$  [pF]  
 $k = 0.7$  [S]  
 $v_r = -60$  [mV]  
 $v_t = -40$  [mV]

# TRAINING SPIKING NEURAL NETWORKS

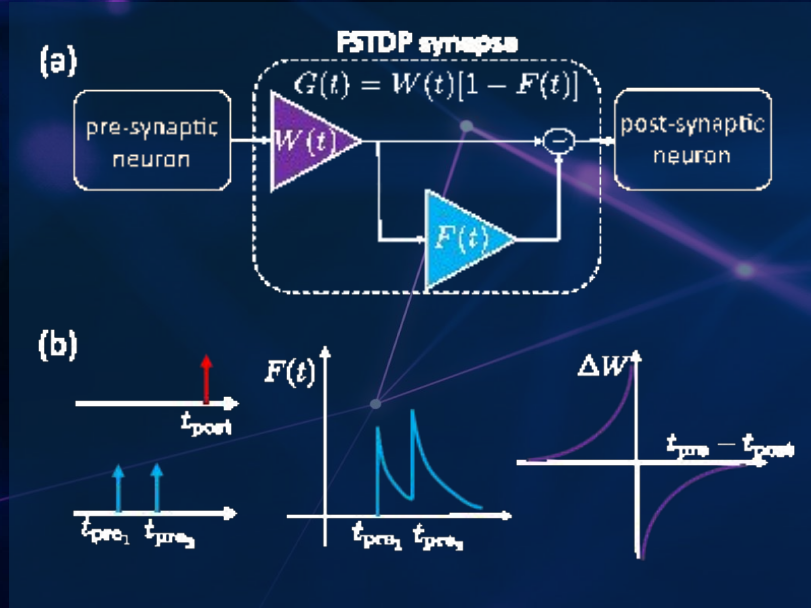


- Backpropagation - the training algorithm for second generation neural networks
- Can it be used in the third generation?
- Possible, but most likely not the way forward
- Biological training algorithms - how do our brains learn?
- Spike-timing-dependent plasticity (STDP)

# SPIKE-TIMING-DEPENDENT PLASTICITY



- Biological process that adjusts the strength of connections between neurons
- Adjustment of connections based on relative timing of a neuron's input and output action potentials (spikes)
- Inputs more likely to be the cause of the post-synaptic neuron's excitation are made even more likely to contribute in the future
- Can this process be used for Spiking Neural Networks?

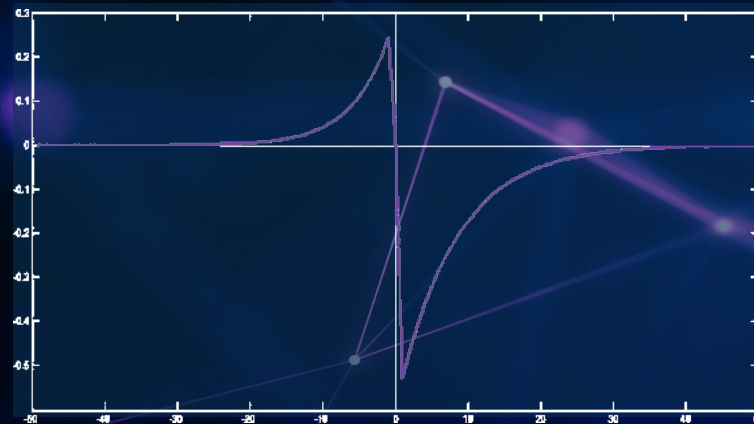


# SPIKE-TIMING-DEPENDENT PLASTICITY



- Yes, it can!
- However, a simplified interpretation is used
- An approximation of a classical asymmetric reinforcement curve present in biological neurons is used, taking time units as variables
- The equations for calculating the weight changes are as follows:

$$\text{STDP}(\Delta t) = \Delta w = \begin{cases} A^- \exp^*\left(\frac{\Delta t}{\tau^-}\right), & \text{if } \Delta t \leq -2 \\ 0, & \text{if } -2 < \Delta t < 2 \\ A^+ \exp^*\left(\frac{\Delta t}{\tau^+}\right), & \text{if } \Delta t \geq 2 \end{cases}$$




$$w_{\text{new}} = \begin{cases} w_{\text{old}} + \sigma \Delta w (w_{\text{max}} - w_{\text{old}}), & \text{if } \Delta w > 0 \\ w_{\text{old}} + \sigma \Delta w (w_{\text{old}} - w_{\text{min}}), & \text{if } \Delta w \leq 0 \end{cases}$$



# WHAT DOES THE FUTURE HOLD?



- The advancement of computational power will lead to the possibility of more detailed models of biological neurons
- Every year we are closer to a true-to-concept biologically accurate artificial neural network
- Spiking Neural Networks could be the way towards General Artificial Intelligence and possibly more



THANK YOU FOR YOUR  
ATTENTION!