Assignment 3

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Question 1

Pick a real-world directed network dataset (with number of nodes > 100) from here. [2 points] Represent the network in terms of its 'adjacency matrix' as well as 'edge list'.
[28 points] Briefly describe the dataset chosen and report the following:
1. Number of Nodes
2. Number of Edges
3. Avg In-degree
4. Avg. Out-Degree
5. Node with Max In-degree
6. Node with Max out-degree
7. The density of the network

The dataset chosen for this assignment comes under the Internet peer-to-peer networks category and is called "p2p-Gnutella08". It is of directed type with 6,301 Nodes and 20,777 edges. It is the Gnutella peer to peer network from August 8, 2002.

1. The number of nodes is 6,301
2. The number of edges is 20,777
3. The average in-degree has been obtained according to the following code. The average has come out to be 3.3398167497186946 .

```
[5]  gl_list=[]
     for i in range(n):
         count=0
         for j in range(n):
             if(adj_matrix[j][i]==1):
                 count+=1
         if count!=0:
             gl_list.append(count)

     outdegree=0
     for k in gl_list:
         outdegree+=k
     print("Total Indegree:",outdegree)
     print("Avg of Indegree:",outdegree/len(gl_list))
```

```
Total Indegree: 20777
Avg of Indegree: 3.3398167497186946
```

4. The average out-degree has been obtained according to the following code. The average has come out to be 8.428803245436105 .

```
[4]  gl_list1=[]
     for i in range(n):
         count=0
         for j in range(n):
             if(adj_matrix[i][j]==1):
                 count+=1
         if count!=0:
             gl_list1.append(count)
     indegree=0
     for k in gl_list1:
         indegree+=k
     print("Total Outdegree:",indegree)
     print("Avg of Outdegree:",indegree/len(gl_list1))

     Total Outdegree: 20777
     Avg of Outdegree: 8.428803245436105
```

5. The node with the max in-degree has been found to be node 258. The value of the max in degree is 91.

```
[7]  temp=max(gl_list)
     print("value of max in degree:",temp)
     count=0
     for i in gl_list:
         if(i==temp):
             print("Node with maximum in degree:",count)
             break
         count+=1

     value of max in degree: 91
     Node with maximum in degree: 258
```

6. The node with the max out-degree has been found to be node 2314. The value of the max out degree is 48.

```
[6]  temp=max(gl_list1)
     print("value of max out degree:",temp)
     count=0
     for i in gl_list1:
         if(i==temp):
             print("Node with maximum out degree:",count)
             break
         count+=1
```

```
value of max out degree: 48
Node with maximum out degree: 2314
```

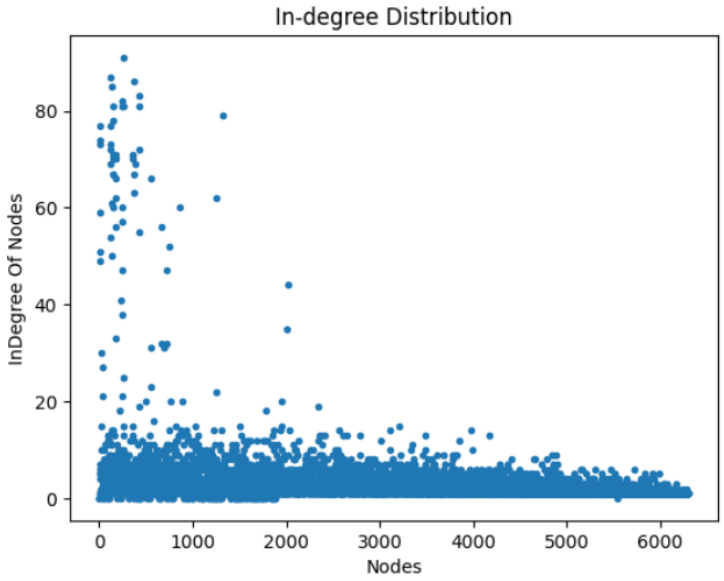
7. The density of the network can be computed by obtaining the ratio of the number of edges to the maximum number of edges that are possible in a directed graph. It must have the same number of nodes.

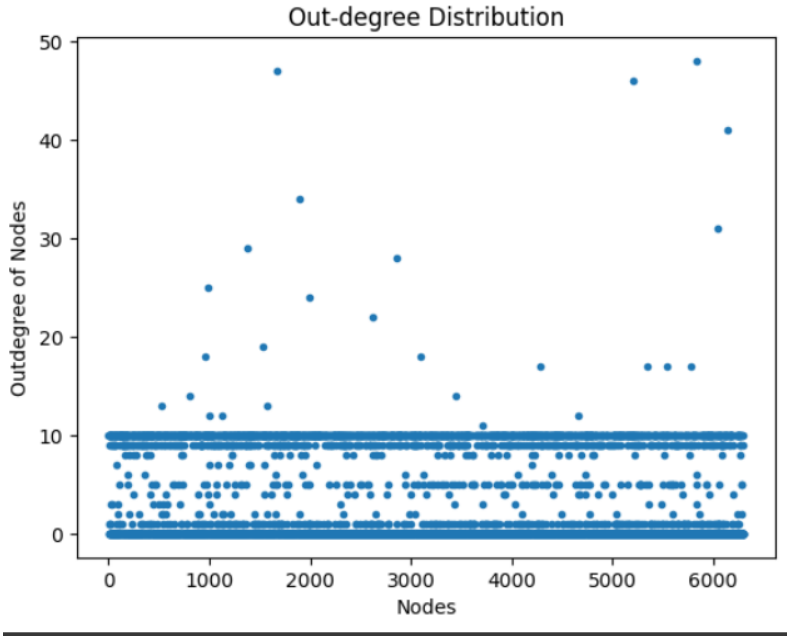
```
[8]  print("Density of Graph:",indegree/((n*(n-1))/2))
```

```
Density of Graph: 0.0010467978123905755
```

The following tasks have been performed:

1. **Plot degree distribution of the network (in case of a directed graph, plot in-degree and out-degree separately).**


In-degree Distribution
InDegree Of Nodes
Nodes
0
20
40
60
80
0
1000
2000
3000
4000
5000
6000


Out-degree Distribution
Outdegree of Nodes
Nodes
0
10
20
30
40
50
0
1000
2000
3000
4000
5000
6000

2. **Calculate the local clustering coefficient of each node and plot the clustering-coefficient distribution (lcc vs frequency of lcc) of the network.**

```
plt.plot(range(len(coefficient)),coefficient,'.')
plt.title("Clustering-coefficient distribution")
plt.xlabel("Nodes")
plt.ylabel("Clustering-coefficient")
plt.show()
```

Question 2

Question 2 - [35 points] PageRank, Hubs and Authority

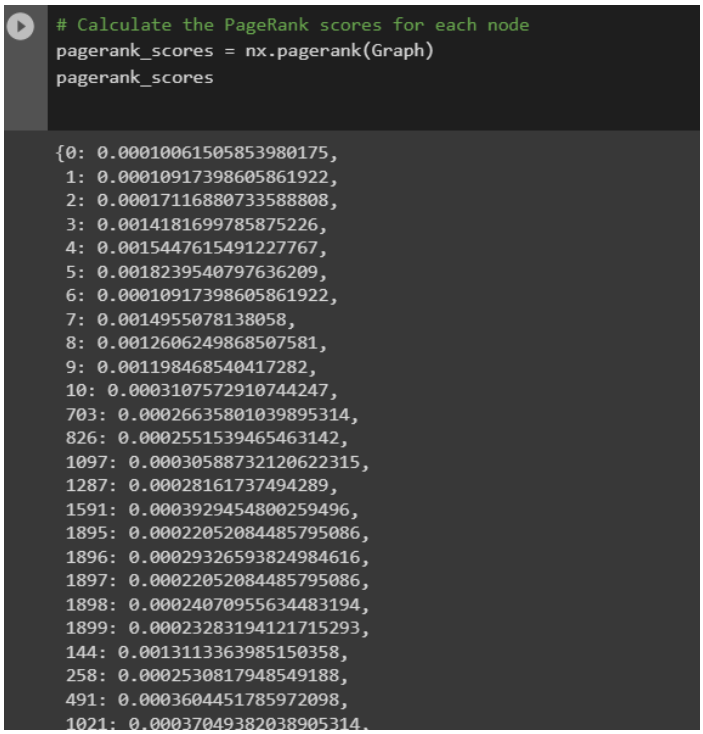
For the dataset chosen in the above question, calculate the following:

1. [15 points] PageRank score for each node

2. [15 points] Authority and Hub score for each node

[5 points] Compare the results obtained from both the algorithms in parts 1 and 2 based on the node scores.

1. PageRank is an algorithm that assigns a numerical weight to each element of a set of links or web pages and measures its importance within the set. In the dataset we have used, there are 6301 nodes and 20777 edges. The pagerank score was calculated for all the nodes. The below screenshot displays a screenshot of a part of the nodes that were printed by the system.



```
# Calculate the PageRank scores for each node
pagerank_scores = nx.pagerank(Graph)
pagerank_scores
```

```
{0: 0.00010061505853980175,
 1: 0.00010917398605861922,
 2: 0.00017116880733588808,
 3: 0.0014181699785875226,
 4: 0.0015447615491227767,
 5: 0.0018239540797636209,
 6: 0.00010917398605861922,
 7: 0.0014955078138058,
 8: 0.0012606249868507581,
 9: 0.001198468540417282,
 10: 0.0003107572910744247,
 703: 0.00026635801039895314,
 826: 0.0002551539465463142,
 1097: 0.00030588732120622315,
 1287: 0.00028161737494289,
 1591: 0.0003929454800259496,
 1895: 0.00022052084485795086,
 1896: 0.00029326593824984616,
 1897: 0.00022052084485795086,
 1898: 0.00024070955634483194,
 1899: 0.00023283194121715293,
 144: 0.0013113363985150358,
 258: 0.0002530817948549188,
 491: 0.0003604451785972098,
 1021: 0.0003704938203890531
```

https://docs.google.com/document/d/1RyqAlQWEOKXTRyQAqLC-0K3XgXIGkNDzSXsXKM6sgfs/edit?usp=sharing

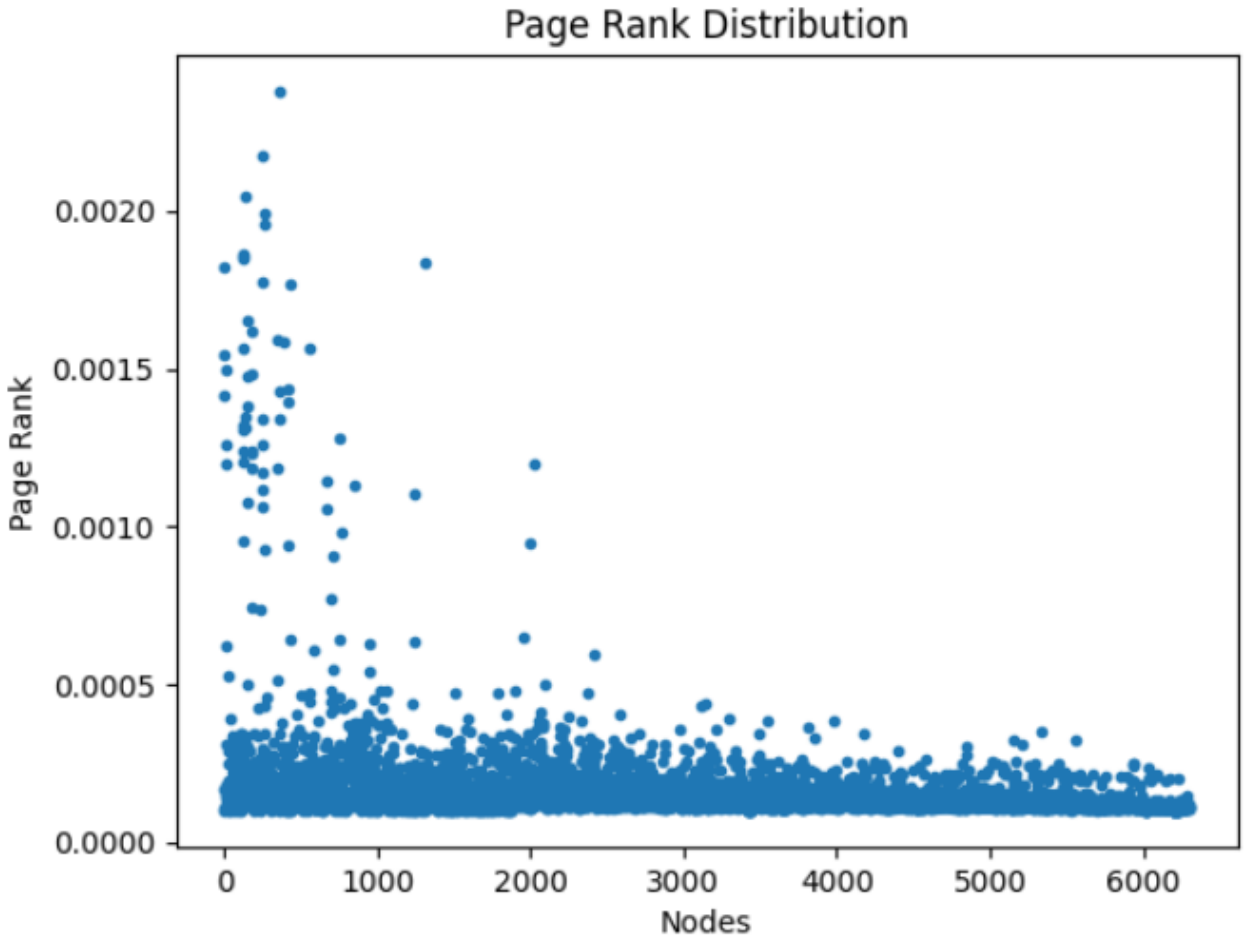
The nx.pagerank() function used in the above, computes the PageRank scores of the nodes in the graph given as input. The graph in this case is a directed graph. The function returns a dictionary mapping each node in the graph to its corresponding PageRank score.
The values always lie between 0 and 1. A higher value closer to 1 shows that it holds more importance in its set.

Matplotlib has been used to plot the PageRank distribution. The code is as given below:

```python
import matplotlib.pyplot as plt

#Plot the Page Rank
nodes = list(pagerank_scores.keys())
pg_rank = list(pagerank_scores.values())
plt.plot(nodes, pg_rank, '.')
plt.xlabel("Nodes")
plt.ylabel("Page Rank")
plt.title("Page Rank Distribution")
plt.show()
```

The plot for the same is given below:



2. Authority and Hub scores need to be calculated for each of the nodes. These are calculated by HITS, which ranks web pages based on their importance. The authority score of a web page is said to be a measure of its importance or relevance as a destination page. It may or may not be linked through other pages. A high authority score indicates that the same would be linked by several other pages. The Hub score denotes the importance of a page that links to other pages. A high score indicates that it would link to several other pages.

```
# Calculate the Authority and Hub scores for each node
hub_scores,authority_scores  = nx.hits(Graph)

print(nx.hits(Graph)[0])
print(nx.hits(Graph)[1])
```

```
{0: 0.0014846327801683308, 1: -0.0, 2: -0.0, 3: 3.122849119296286e-06, 4:
{0: 0.0, 1: 0.0001520388797981095, 2: 0.0007538676999129756, 3: 0.0185882
```

```
authority_scores
```

```
{0: -0.0,
 1: 0.00015203887979810878,
 2: 0.0007538676999129743,
 3: 0.01858823919434389,
 4: 0.012476140139730972,
 5: 0.016476113958807347,
 6: 0.0001520388797981087,
 7: 0.011349393317842028,
 8: 0.015424677465390385,
 9: 0.010585035288038298,
 10: 0.001258101148198516,
 703: 1.867611572887343e-06,
 826: 3.5608785803279456e-05,
 1097: 1.4493926067247085e-05,
 1287: 2.1561791677959163e-06,
 1591: 6.097900820466594e-05,
 1895: 3.1980600739641573e-07,
 1896: 6.618174287205826e-05,
 1897: 3.1980600739677535e-07,
 1898: 6.857403512646581e-07,
 1899: 8.410444717558508e-07,
 144: 0.016239121558457734,
 258: 3.042176996332582...e-05
```

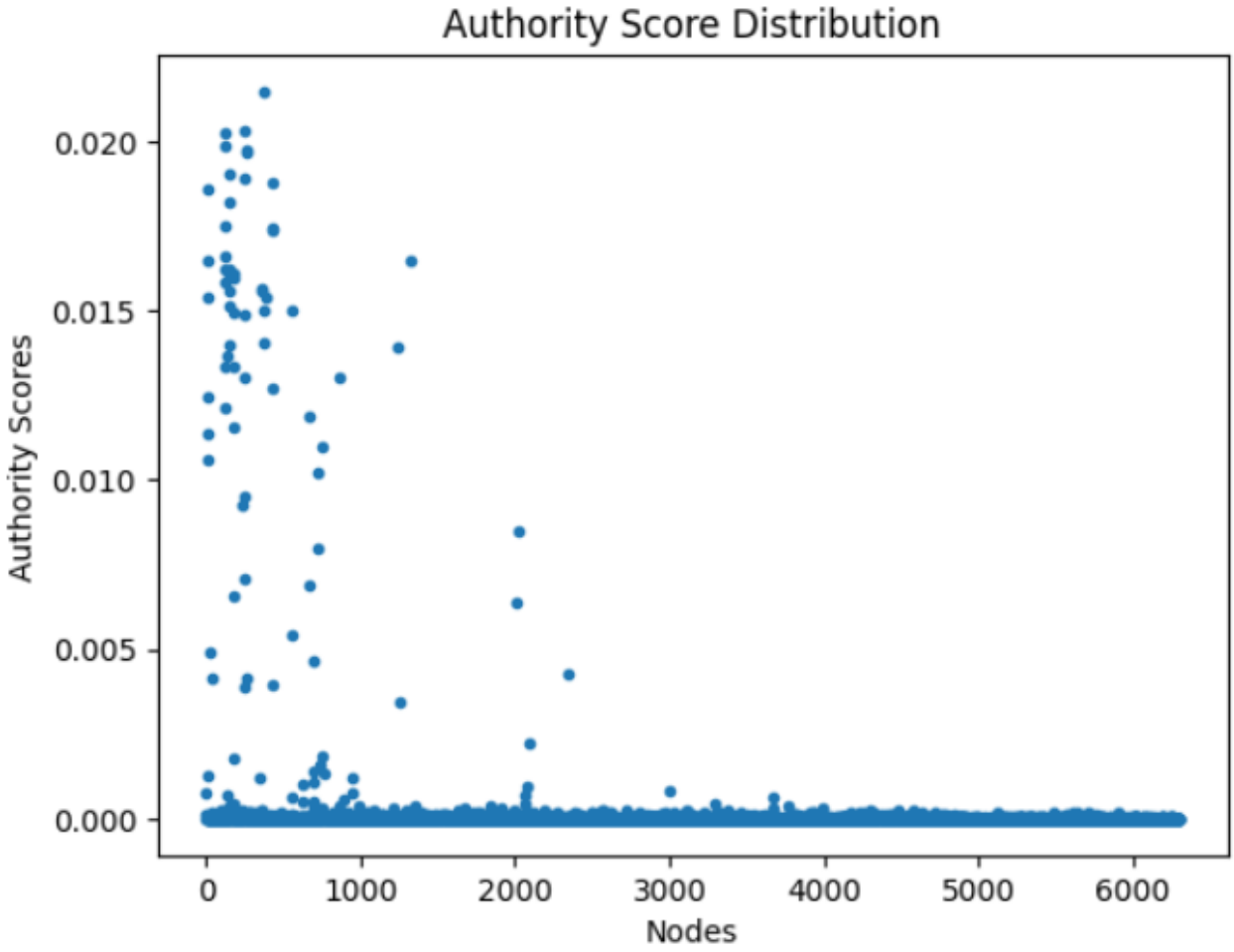
```
hub_scores
```

```
{0: 0.0014846327801683308,
 1: -0.0,
 2: -0.0,
 3: 3.1228491192961536e-06,
 4: 0.00028870360896923904,
 5: 0.0026073101209297626,
 6: -0.0,
 7: 0.0013825856712709028,
 8: 8.355942526740936e-06,
 9: 0.0023270408452820295,
 10: -0.0,
 703: 8.033917828095867e-07,
 826: -0.0,
 1097: -0.0,
 1287: 4.676780759882044e-06,
 1591: -0.0,
 1895: 3.1356163669013894e-08,
 1896: 1.5988563218134413e-05,
 1897: -0.0,
 1898: -0.0,
 1899: -0.0,
 144: 0.002392451944124439,
 258: -0.0,
 491: -0.0,
 1021: -0.0,
 1418: -0.0,
 1669: 4.198376218783717e-06,
 1900: -0.0,
 1901: -0.0,
 1902: -0.0,
```

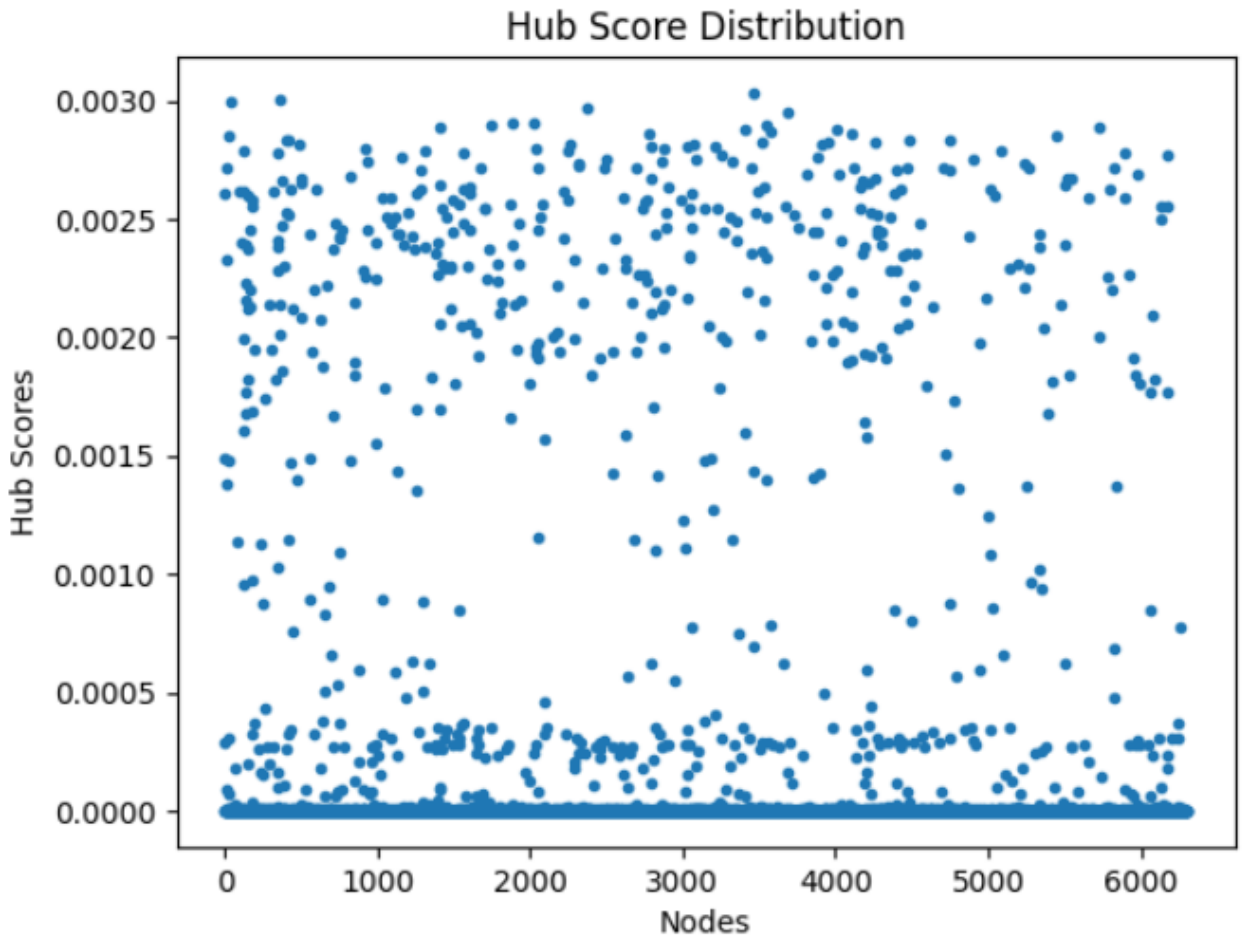
The distributions for the above scores have been plotted using matplotlib and are as follows with their respective codes:

```python
import matplotlib.pyplot as plt

#Plot the Authority Score
nodes = list(authority_scores.keys())
auth_score = list(authority_scores.values())
plt.plot(nodes,auth_score, '.')
plt.xlabel("Nodes")
plt.ylabel("Authority Scores")
plt.title("Authority Score Distribution")
plt.show()
```



```
#Plot the Hub Score
nodes = list(hub_scores.keys())
hub_score = list(hub_scores.values())
plt.plot(nodes,hub_score, '.')
plt.xlabel("Nodes")
plt.ylabel("Hub Scores")
plt.title("Hub Score Distribution")
plt.show()
```



```
[9]  # Create a table of node scores
     final_scores = []
     for x in Graph.nodes():
         final_scores.append((x, pagerank_scores[x], authority_scores[x], hub_scores[x]))
     final_scores.sort(key=lambda x: x[1], reverse=True)

     print("Node  PageRank  Authority Hub")
     for i in final_scores:
         print(f"{i[0]}\t{i[1]:.4f}\t{i[2]:.4f}\t{i[3]:.4f}")
```

```
775     0.0001  0.0000  0.0000
797     0.0001  -0.0000 0.0000
896     0.0001  -0.0000 0.0000
929     0.0001  -0.0000 0.0000
948     0.0001  0.0000  0.0001
961     0.0001  0.0000  0.0003
992     0.0001  -0.0000 0.0016
994     0.0001  -0.0000 0.0000
999     0.0001  0.0000  0.0000
1075    0.0001  -0.0000 0.0000
1098    0.0001  0.0000  0.0000
1108    0.0001  0.0000  0.0000
1117    0.0001  -0.0000 0.0006
1161    0.0001  0.0000  0.0028
1181    0.0001  -0.0000 0.0000
1200    0.0001  0.0000  0.0000
1218    0.0001  0.0000  0.0000
1222    0.0001  0.0000  0.0000
1237    0.0001  -0.0000 0.0000
1247    0.0001  -0.0000 0.0000
1260    0.0001  -0.0000 0.0000
1286    0.0001  -0.0000 0.0000
1294    0.0001  0.0000  0.0005
1307    0.0001  0.0000  0.0000
1398    0.0001  -0.0000 0.0000
1403    0.0001  0.0000  0.0000
```

Please note that due to the large amount of data in these sets, the whole cannot be effectively displayed. In order to cross-check the data it needs to be done manually by running the codes that have been submitted for the assignment.