Assignment 5

Hruday Beeravelli

Find Python Codes from below link

and Latex codes from below link

1 Examples 2

1.1 Question 11

Prove(by shewing that the area of the triangle formed by them is zero) that the following sets of three points are in a straight line $(-\frac{1}{2}, 3), (-5, 6)$ and (-8, 8)

1.2 Solution

$$\frac{1}{2} \left| (\mathbf{A} - \mathbf{B}) \left(\mathbf{A} - \mathbf{C} \right) \right|$$
Let $\mathbf{A} = \begin{pmatrix} -\frac{1}{2} \\ 3 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} -5 \\ 6 \end{pmatrix}$, $\mathbf{C} = \begin{pmatrix} -8 \\ 8 \end{pmatrix}$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} -\frac{1}{2} \\ 3 \end{pmatrix} - \begin{pmatrix} -5 \\ 6 \end{pmatrix} \tag{1.2.2}$$

$$= \begin{pmatrix} \frac{9}{2} \\ -3 \end{pmatrix} \tag{1.2.3}$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} -\frac{1}{2} \\ 3 \end{pmatrix} - \begin{pmatrix} -8 \\ 8 \end{pmatrix}$$
 (1.2.4)
= $\begin{pmatrix} \frac{15}{2} \\ -5 \end{pmatrix}$ (1.2.5)

Area of the triangle

$$= \frac{1}{2} \begin{vmatrix} \frac{9}{2} & \frac{15}{2} \\ -3 & -5 \end{vmatrix} \tag{1.2.6}$$

$$= \frac{1}{2} \left[\left(\frac{9}{2} \times -5 \right) - \left(\frac{15}{2} \times -3 \right) \right] \tag{1.2.7}$$

$$=\frac{1}{2}\left(-\frac{45}{2}+\frac{45}{2}\right) \tag{1.2.8}$$

$$= \frac{1}{2}(0)$$
= 0 (1.2.9)

Since the area is 0, the given points form a straight line.

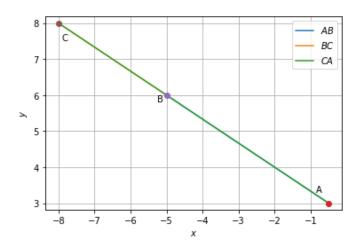


Fig. 0