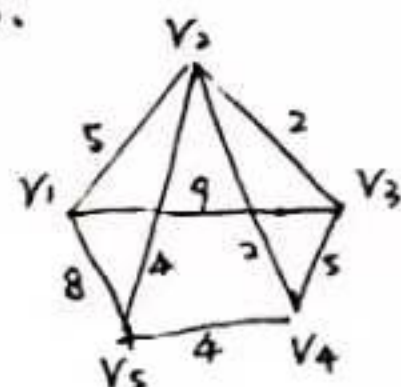


# 离散数学 (2) 第六次作业

16.



奇数度数点有  $V_1, V_3, V_4, V_5$

①  $V_1 - V_3, V_4 - V_5$

$$\begin{array}{l} \text{dist}(V_1, V_3) = 7 \\ \text{dist}(V_4, V_5) = 4 \end{array} \Rightarrow \text{cost } 1 = 11$$

②  $V_1 - V_4, V_3 - V_5$

$$\begin{array}{l} \text{dist}(V_1, V_4) = 7 \\ \text{dist}(V_3, V_5) = 6 \end{array} \Rightarrow \text{cost } 2 = 13$$

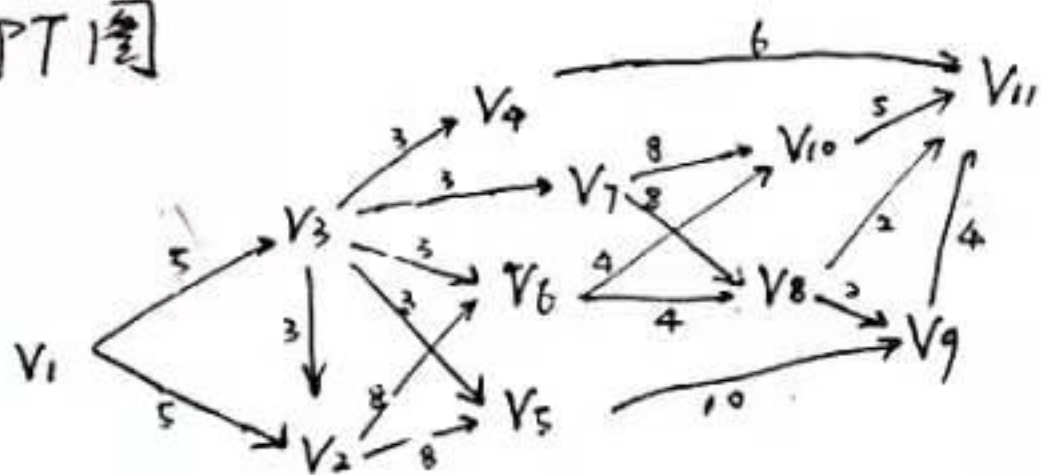
③  $V_1 - V_5, V_3 - V_4$

$$\begin{array}{l} \text{dist}(V_1, V_5) = 8 \\ \text{dist}(V_3, V_4) = 4 \end{array} \Rightarrow \text{cost } 3 = 12$$

则  $V_1 - V_3, V_4 - V_5$  配对代价最小.

总代价为  $\sum_{e \in E} w(e) + \text{cost } 1 = 39 + 11 = 50$

17. 建PT图



采用拓扑排序, 设  $\text{dist } V_i$  为  $V_i$  点前距  $V_1$  最大值

$V_1 \rightarrow$	$\text{dist } V_3 = 5 \rightarrow V_3 \text{ in queue}$	$\text{pre } V_3 = 1$
	$\text{dist } V_2 = 5$	$\text{pre } V_2 = 1$
$V_3 \rightarrow$	$\text{dist } V_2 = 8 \rightarrow V_2 \text{ in queue}$	$\text{pre } V_2 = 3$
	$\text{dist } V_5 = 8$	$\text{pre } V_5 = 8$
	$\text{dist } V_6 = 8$	$\text{pre } V_6 = 8$
	$\text{dist } V_7 = 8 \rightarrow V_7 \text{ in queue}$	$\text{pre } V_7 = 8$
	$\text{dist } V_4 = 8 \rightarrow V_4 \text{ in queue}$	$\text{pre } V_4 = 3$
$V_2 \rightarrow$	$\text{dist } V_6 = 16 \rightarrow V_6 \text{ in queue}$	$\text{pre } V_6 = 2$
	$\text{dist } V_5 = 16 \rightarrow V_5 \text{ in queue}$	$\text{pre } V_5 = 2$
$V_7 \rightarrow$	$\text{dist } V_{10} = 16$	$\text{pre } V_{10} = 7$
	$\text{dist } V_8 = 16$	$\text{pre } V_8 = 7$
$V_4 \rightarrow$	$\text{dist } V_{11} = 14$	$\text{pre } V_{11} = 4$
$V_6 \rightarrow$	$\text{dist } V_{10} = 20 \rightarrow V_{10} \text{ in queue}$	$\text{pre } V_{10} = 6$
	$\text{dist } V_8 = 20 \rightarrow V_8 \text{ in queue}$	$\text{pre } V_8 = 6$
$V_5 \rightarrow$	$\text{dist } V_9 = 26$	$\text{pre } V_9 = 5$
$V_{10} \rightarrow$	$\text{dist } V_{11} = 25$	$\text{pre } V_{11} = 10$
$V_8 \rightarrow$	$\text{dist } V_9 = 26 \rightarrow V_9 \text{ in queue}$	
	$\text{dist } V_{11} = 25$	
$V_9 \rightarrow$	$\text{dist } V_{11} = 30$	$\text{pre } V_{11} = 9$

即关键路径为  $V_1 \rightarrow V_3 \rightarrow V_2 \rightarrow V_5 \rightarrow V_9 \rightarrow V_{11}$  时间共 30