

## Measure of the Branching Ratio of the process

$$\eta_c \rightarrow K_S^0 K \pi$$

via the decay  $\psi(3686) \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$

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## The purpose of our work

Measure the branching ratio of the process  $\eta_c \rightarrow K_S K \pi$ , reducing the error measured before.

The process we study

$$\begin{aligned} \psi(3686) &\rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K_S^0 K \pi \\ \pi^0 &\rightarrow \gamma \gamma, K_S^0 \rightarrow \pi^+ \pi^- \end{aligned}$$

## Method to do it

- Fit  $\eta_c$  signal with invariant mass of  $K_S^0$ ,  $K$  and  $\pi$  (Corresponding to  $N_{Obs1}$  and  $\epsilon_1$ );
- Fit  $\eta_c$  signal with the recoil mass of  $\gamma$  and  $\pi^0$  (Corresponding to  $N_{Obs2}$  and  $\epsilon_2$ );
- The branching fraction will be acquired as the ratio of the two  $\eta_c$  signal as

$$Br(\eta_c \rightarrow K_S^0 K \pi) = \frac{N_{Obs1}}{N_{Obs2}} \cdot \frac{\epsilon_2}{\epsilon_1} \cdot \frac{1}{Br(K_S^0 \rightarrow \pi^+ \pi^-)}$$

# Data Set

- inclusive MC: 106M
- signal MC: 200K for each of the inclusive process and exclusive process
- BOSS version: 664p01

# the Exclusive Process

# Charged and Neutral Track Selection Criteria

## Charged Tracks Selection Criteria

- $|\cos \theta| < 0.93$
- $|R_z| < 10\text{cm}, R_{xy} < 1\text{cm}$  (for the charged tracks NOT from  $K_S^0$ )  
 $2 \leq N_{\text{good}} \leq 4$
- No vertex cut for the charged tracks from  $K_S^0$   
 $N_{\text{goodL}} \geq 4$

## Neutral Tracks Selection Criteria

- $E_\gamma > 25\text{MeV}, |\cos \theta| < 0.8$  ( barrel region )
- $E_\gamma > 50\text{MeV}, 0.86 < |\cos \theta| < 0.92$  ( end-cap region )
- $0 \leq t \leq 14$  ( in unit of 50 ns)
- $N_\gamma \leq 3$

## $\pi^0$ List, $\gamma\pi^0$ List and Reconstruction of $K_S^0$

### $\pi^0$ List and $\gamma\pi^0$ List

- $\pi^0$  list
- $0.08 < M_{\gamma\gamma} < 0.2$  (With 1-C)
  - $N_{\pi^0} \geq 1$

- $\gamma\pi^0$  list
- $2.8 < M_{\gamma\pi^0}^{recoil} < 3.2$
  - $3.3 < M_{\pi^0}^{recoil} < 3.7$

### Reconstruction of $K_S^0$

- A primary vertex fit and a secondary vertex fit are performed
- $|M_{\pi\pi} - m_{K_S^0}| < 20 \text{ MeV}/c^2$

## Other Selection Criteria

### Other Selection Criteria

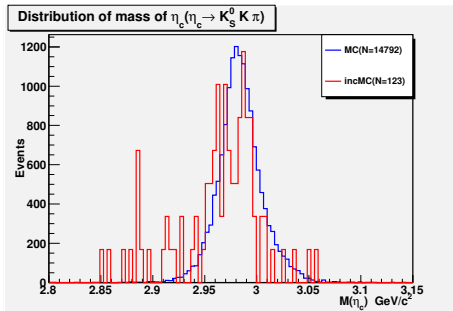
- Vertex Fit
- 4-C Kinematic Fit
- Minimum combined  $\chi^2 = \chi_{4C}^2 + \chi_{1C}^2 + \chi_{pid}^2 + \chi_{vertex}^2$  cut



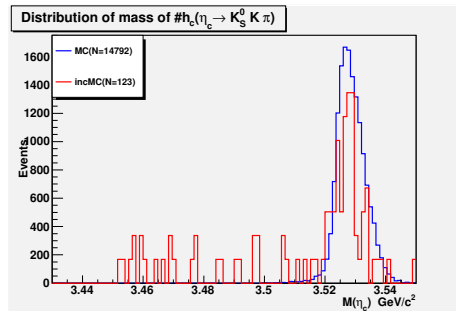
# Optimized Selection

Using ROOT scripts, we got the Optimized Selection as below:

- $0 < \chi_{4C}^2 < 25$ ;
- $0.125 < m_{\pi^0} < 0.138$  (after 4-C);
- $0.45 < E(\gamma_{E1}) < 0.53$  (after 4-C);
- $|m_{recoil}(\pi^0\pi^0) - M_{J/\psi}| < 0.033$ ;
- $|m_{recoil}(\gamma) - M_{\chi_{c0}}| < 0$ ;
- $|m_{recoil}(\gamma) - M_{\chi_{c1}}| < 0.004$ ;
- $|m_{recoil}(\gamma) - M_{\chi_{c2}}| < 0.002$ ;
- $|m_{recoil}(\pi^+\pi^-) - M_{J/\psi}| < 0.004$ . and exclusive process



Mass distribution of  $\eta_c$



Mass distribution of  $h_c$

# Topology analysis

No.	decay chain	final states	iTopo	nEvt	nTot
0	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^0 \pi^- K^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	2	38	38
1	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^- \pi^+ K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	6	35	73
2	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^0 \rho^- K^+, \bar{K}^0 \rightarrow K_S, \rho^- \rightarrow \pi^- \pi^0, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	24	6	79
3	$\psi' \rightarrow K^- \bar{K}^* \gamma \pi^+, \bar{K}^* \rightarrow \bar{K}^0 \pi^0, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	1	5	84
4	$\psi' \rightarrow \pi^- \gamma K^* K^+, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	5	4	88
5	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^- \rho^+ K^0, \rho^+ \rightarrow \pi^0 \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	14	3	91
6	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^* K^*, \bar{K}^* \rightarrow K^- \pi^+, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	11	2	93
7	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow \pi^0 K^0 K^*, K^0 \rightarrow K_S, K^* \rightarrow \pi^- K^+, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	12	2	95
8	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^- \rho^+ K^0, \rho^+ \rightarrow \pi^0 \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	13	2	97
9	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^* K^+, K^* \rightarrow \bar{K}^0 \pi^-, K^+ \rightarrow \pi^0 K^+, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	0	2	99
10	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^* K^+, K^* \rightarrow K^- \pi^0, K^+ \rightarrow \pi^+ K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	16	2	101
11	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow \bar{K}^0 \rho^- K^+, \bar{K}^0 \rightarrow K_S, \rho^- \rightarrow \pi^- \pi^0, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	3	2	103
12	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^- \pi^+ K^*, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	26	2	105
13	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^0 \pi^- K^+, \bar{K}^0 \rightarrow K_S, K^+ \rightarrow \pi^0 K^+, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	8	1	106
14	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^* \pi^0 K^0, \bar{K}^* \rightarrow K^- \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	9	1	107
15	$\psi' \rightarrow \gamma \eta_c, \eta_c \rightarrow K^- \pi^+ K^*, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	15	1	108
16	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow \bar{K}^* \pi^- K^+, \bar{K}^* \rightarrow \bar{K}^0 \pi^0, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	10	1	109
17	$\psi' \rightarrow K^- K_1^+, K_1^+ \rightarrow \rho^+ K^0, \rho^+ \rightarrow \pi^0 \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	17	1	110
18	$\psi' \rightarrow \bar{K}^* \pi^0 K_2^0, \bar{K}^* \rightarrow \bar{K}^0 \pi^0, K_2^0 \rightarrow \pi^- K^+, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	18	1	111
19	$\psi' \rightarrow K^- K_1^+, K_1^+ \rightarrow \rho^+ K^0, \rho^+ \rightarrow \gamma \text{FSR} \pi^+ \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \text{FSR} \pi^+ \pi^+ \pi^- K^-$	19	1	112
20	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \pi^- K^* K^+, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	20	1	113
21	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^* K^+, K^* \rightarrow K^- \pi^0, K^+ \rightarrow \pi^+ K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	21	1	114
22	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^0 \pi^0 K^*, \bar{K}^0 \rightarrow K_S, K^* \rightarrow \pi^- K^+, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	22	1	115
23	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^- \pi^0 K^+, K^+ \rightarrow \pi^+ K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	23	1	116
24	$\psi' \rightarrow \bar{K}^* \gamma K^*, \bar{K}^* \rightarrow K^- \pi^+, K^* \rightarrow \pi^0 K^0, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	4	1	117
25	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^- \bar{K}^0 \pi^0 \pi^+, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	25	1	118
26	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow \bar{K}^* \pi^0 K^0, \bar{K}^* \rightarrow K^- \pi^+, K^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^- K^-$	7	1	119
27	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^* \pi^0 K^+, K^* \rightarrow \bar{K}^0 \pi^-, \bar{K}^0 \rightarrow K_S, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	27	1	120
28	$\psi' \rightarrow \pi^- \pi^+ K_S K_S, K_S \rightarrow \pi^- \pi^+, K_S \rightarrow \pi^0 \pi^0,$	$\psi' \rightarrow \gamma \gamma \gamma \pi^+ \pi^+ \pi^- \pi^-$	28	1	121
29	$\psi' \rightarrow K_1^- K^+, K_1^- \rightarrow \bar{K}^0 \rho^-, \bar{K}^0 \rightarrow K_S, \rho^- \rightarrow \pi^- \pi^0, K_S \rightarrow \pi^- \pi^+,$	$\psi' \rightarrow \gamma \gamma K^+ \pi^+ \pi^- \pi^-$	29	1	122

Table 1:

# Preliminary Event Selection

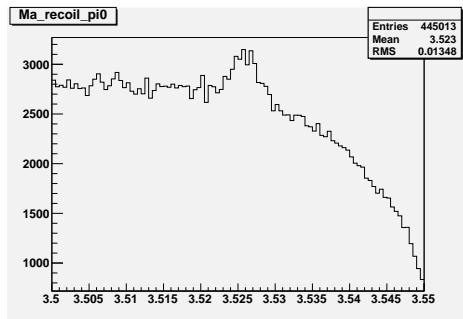
## Selection of $\gamma_{E1}$ and $\pi^0$ candidates

- $E_\gamma > 25\text{MeV}, |\cos\theta| < 0.8$  ( barrel region )
- $E_\gamma > 50\text{MeV}, 0.86 < |\cos\theta| < 0.92$  ( end-cap region )
- $465\text{MeV} < E(\gamma_{E1}) < 535\text{MeV}$
- $120 < M_{\gamma\gamma} < 145\text{MeV}/c^2$  ( With 1C )
- photons used in  $\gamma_{E1}$  candidates cannot form  $\pi^0$  with another good photon
- We keep the  $\pi^0$  candidates with the minimum 1-C fit  $\chi^2$  even if the daughter photons can be used in more than one  $\pi^0$  candidates
- We keep the events with only one  $\pi^0$  in the  $3.517 - 3.535\text{GeV}/c^2$  recoil-mass region.

# Optimized Event Selection

Using ROOT scripts, we got the Optimized Selection as below:

- $E(\text{deposition}) < 0.6 \text{ GeV};$
- $|m_{\text{recoil}}(\pi^0\pi^0) - M_{J/\psi}| < 0.02;$
- $|m_{\text{recoil}}(\gamma) - M_{\chi_{c0}}| < 0.004;$
- $|m_{\text{recoil}}(\gamma) - M_{\chi_{c1}}| < 0.004;$
- $|m_{\text{recoil}}(\gamma) - M_{\chi_{c2}}| < 0.003;$
- $|m_{\text{recoil}}(\pi^+\pi^-) - M_{J/\psi}| < 0.01.$



Mass distribution of  $h_c$

# Topology analysis

No.	decay chain	final states	iTopo	nEvt	nTot
0	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \pi^- \pi^- \pi^0 \pi^+ \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^0 \pi^0 \pi^- \pi^-$	54	153	153
1	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^- K_L \pi^+$	$\psi' \rightarrow \gamma \pi^+ K_L \pi^0 K^-$	391	84	237
2	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^- \pi^- \pi^0 \pi^+ K^+$	$\psi' \rightarrow \gamma K^+ \pi^+ \pi^0 \pi^0 \pi^- K^-$	218	80	317
3	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \pi^- K_L K^+$	$\psi' \rightarrow \gamma K^+ K_L \pi^0 \pi^-$	309	77	394
4	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow K^- \pi^- \pi^0 \pi^+ K^+$	$\psi' \rightarrow K^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^- K^-$	210	73	467
5	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \pi^- \pi^- \pi^0 \pi^0 \pi^+ \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^- \pi^-$	69	63	530
6	$\psi' \rightarrow \bar{p} \pi^0 \pi^+ n$	$\psi' \rightarrow n \pi^+ \pi^0 \bar{p}$	172	61	591
7	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \pi^- \pi^- \pi^+ \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^- \pi^-$	617	58	649
8	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \bar{p} \pi^+ n$	$\psi' \rightarrow \gamma n \pi^+ \pi^0 \bar{p}$	519	57	706
9	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \pi^- \pi^- \pi^- \pi^0 \pi^+ \pi^+ \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^- \pi^- \pi^-$	185	53	759
10	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow e^- e^+$	$\psi' \rightarrow \pi^0 \pi^0 e^+ e^-$	196	52	811
11	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow b_1^- \pi^0 \pi^0 \pi^+, b_1^- \rightarrow \pi^- \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^0 \pi^- \pi^-$	124	51	862
12	$\psi' \rightarrow \gamma \chi_{c0}, \chi_{c0} \rightarrow b_1^- \pi^0 \pi^+, b_1^- \rightarrow \pi^- \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^0 \pi^- \pi^-$	718	51	913
13	$\psi' \rightarrow \eta J/\psi, \eta \rightarrow \pi^0 \pi^0 \pi^0, J/\psi \rightarrow \pi^- \pi^- \pi^0 \pi^+ \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^- \pi^-$	645	49	962
14	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \pi^- \eta b_1^+, \eta \rightarrow \gamma \gamma, b_1^+ \rightarrow \pi^+ \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^-$	173	49	1011
15	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \pi^- \gamma \pi^0 \pi^0 \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^0 \pi^0 \pi^0 \pi^0 \pi^-$	215	48	1059
16	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \pi^- \pi^- \pi^- \pi^+ \pi^+ \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^+ \pi^0 \pi^- \pi^-$	98	47	1106
17	$\psi' \rightarrow \gamma \chi_{c0}, \chi_{c0} \rightarrow \pi^- \pi^+ b_1^0, b_1^0 \rightarrow \pi^0 \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^0 \pi^- \pi^-$	342	44	1150
18	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow b_1^- \pi^+ \eta, b_1^- \rightarrow \pi^- \omega, \eta \rightarrow \gamma \gamma, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \gamma \gamma \pi^+ \pi^+ \pi^0 \pi^0 \pi^0 \pi^-$	582	43	1193
19	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^- \pi^+ K_S, K_S \rightarrow \pi^- \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^- K^-$	475	43	1236
20	$\psi' \rightarrow \pi^- \pi^0 \pi^0 b_1^+, b_1^+ \rightarrow \pi^+ \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \pi^+ \pi^+ \pi^+ \pi^0 \pi^0 \pi^- \pi^-$	205	42	1278
21	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \bar{n} \pi^+ \Delta^-, \Delta^- \rightarrow \pi^- n$	$\psi' \rightarrow n \pi^+ \pi^0 \pi^0 \pi^- \bar{n}$	756	41	1319
22	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^{*-} \pi^+ K^*, K^{*-} \rightarrow \pi^- K_L, K^* \rightarrow \pi^- K^+$	$\psi' \rightarrow \gamma K^+ \pi^+ K_L \pi^0 \pi^- \pi^-$	200	39	1358
23	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \pi^- K_S K^+, K_S \rightarrow \pi^- \pi^+$	$\psi' \rightarrow \gamma K^+ \pi^+ \pi^0 \pi^- \pi^-$	123	38	1396
24	$\psi' \rightarrow \bar{n} K^* \Lambda, K^* \rightarrow \pi^- K^+, \Lambda \rightarrow \pi^0 n$	$\psi' \rightarrow n K^+ \pi^0 \pi^- \bar{n}$	104	37	1433
25	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^* \pi^- K^{*+}, \bar{K}^* \rightarrow K^- \pi^+, K^{*+} \rightarrow K_L \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ K_L \pi^0 \pi^- K^-$	134	35	1468
26	$\psi' \rightarrow \pi^0 \pi^0 J/\psi, J/\psi \rightarrow \bar{n} \pi^- \pi^+ n$	$\psi' \rightarrow n \pi^+ \pi^0 \pi^0 \pi^- \bar{n}$	369	35	1503
27	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \pi^- \pi^+ b_1^0, b_1^0 \rightarrow \pi^0 \omega, \omega \rightarrow \pi^- \pi^0 \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^0 \pi^- \pi^-$	151	35	1538
28	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow \rho^0 \rho^0, \rho^0 \rightarrow \pi^- \pi^+, \rho^0 \rightarrow \pi^- \pi^+$	$\psi' \rightarrow \gamma \pi^+ \pi^+ \pi^0 \pi^- \pi^-$	250	35	1573
29	$\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c \rightarrow K^* \pi^- K^+, \bar{K}^* \rightarrow K^- \pi^+$	$\psi' \rightarrow \gamma K^+ \pi^+ \pi^0 \pi^- K^-$	79	35	1608

Table 1:

- Fit the  $\gamma \pi^0$  recoil mass
- Do IO check for inclusive process
- Run data to get the branching ratio.



# References

- PRD **86**, 092009 (2012).
- PRL **104**, 132002 (2010).