



# HOW TO DYNAMIC PROGRAMMING

---

Benjamin Chu

3/13/2020

## Step 1: Compute optimal haplotype set for every window, distinguishing strands

	Window 1	Window 2	Window 3	Window 4
Candidate Haplotypes	$h_1, h_2, h_3$	$h_1, h_2, h_6$	$h_1, h_3$	$h_4, h_5, h_8$
$(S_{w,h_i}, S_{w,h_j})$	$h_4, h_5, h_6$	$h_5, h_7, h_8$	$h_1, h_5$	$h_4, h_6, h_8$

## Step 2: For each window, compute all possible pairs

Window 1	Window 2	Window 3	Window 4
$h_1, h_2, h_3$	$h_1, h_2, h_6$	$h_1, h_3$	$h_4, h_5, h_8$
$h_4, h_5, h_6$	$h_5, h_7, h_8$	$h_1, h_5$	$h_4, h_6, h_8$



Possible  
pairs:

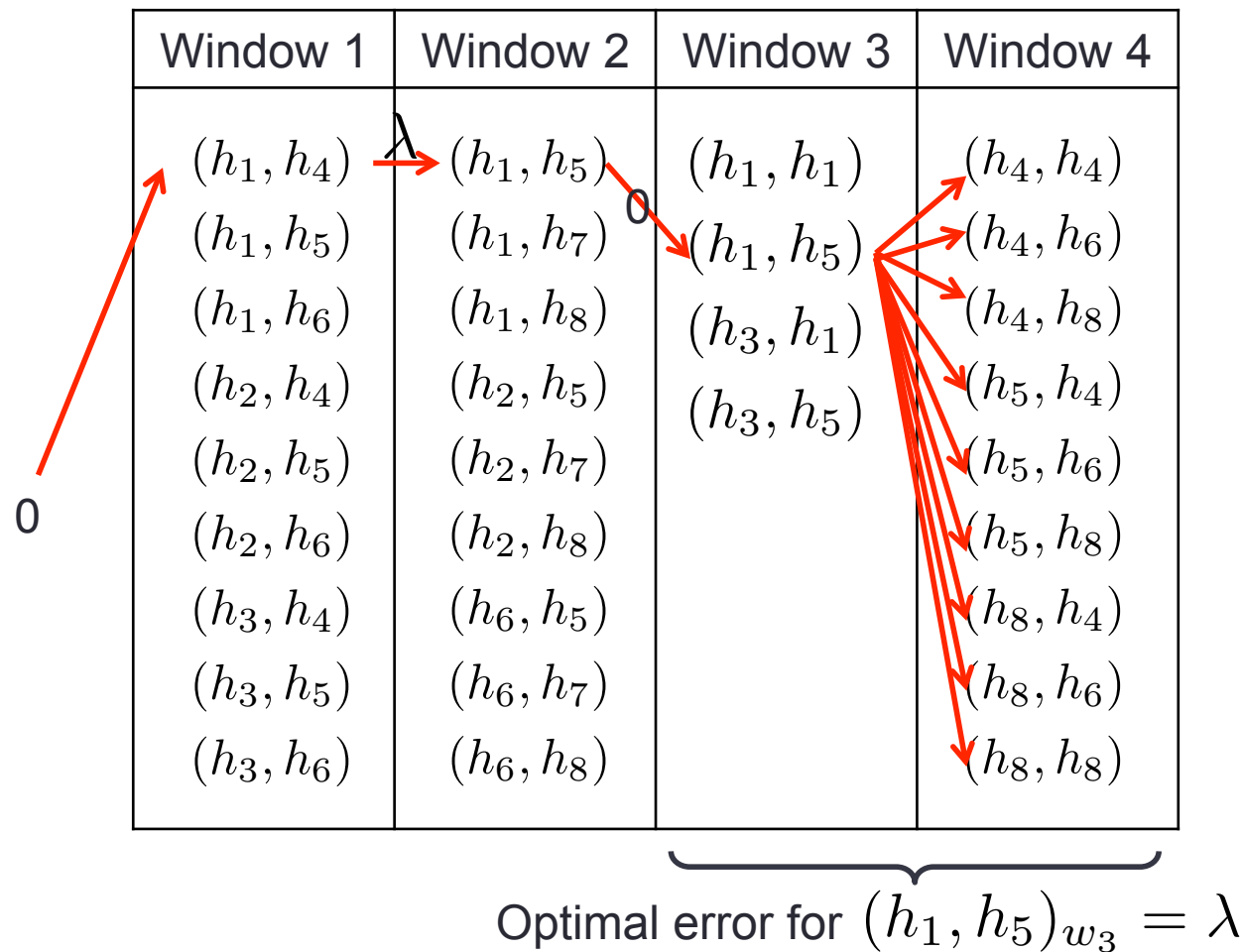
Window 1	Window 2	Window 3	Window 4
$(h_1, h_4)$	$(h_1, h_5)$	$(h_1, h_1)$	$(h_4, h_4)$
$(h_1, h_5)$	$(h_1, h_7)$	$(h_1, h_5)$	$(h_4, h_6)$
$(h_1, h_6)$	$(h_1, h_8)$	$(h_3, h_1)$	$(h_4, h_8)$
$(h_2, h_4)$	$(h_2, h_5)$	$(h_3, h_5)$	$(h_5, h_4)$
$(h_2, h_5)$	$(h_2, h_7)$		$(h_5, h_6)$
$(h_2, h_6)$	$(h_2, h_8)$		$(h_5, h_8)$
$(h_3, h_4)$	$(h_6, h_5)$		$(h_8, h_4)$
$(h_3, h_5)$	$(h_6, h_7)$		$(h_8, h_6)$
$(h_3, h_6)$	$(h_6, h_8)$		$(h_8, h_8)$

## Step 3: Exhaustive search

Window 1	Window 2	Window 3	Window 4
$(h_1, h_4)$	$\xrightarrow{\lambda} (h_1, h_5)$	$\xrightarrow{\lambda} (h_1, h_1)$	$\xrightarrow{2\lambda} (h_4, h_4) \xrightarrow{\quad} 4\lambda$
$(h_1, h_5)$	$(h_1, h_7)$	$(h_1, h_5)$	$(h_4, h_6)$
$(h_1, h_6)$	$(h_1, h_8)$	$(h_3, h_1)$	$(h_4, h_8)$
$(h_2, h_4)$	$(h_2, h_5)$	$(h_3, h_5)$	$(h_5, h_4)$
$(h_2, h_5)$	$(h_2, h_7)$		$(h_5, h_6)$
$(h_2, h_6)$	$(h_2, h_8)$		$(h_5, h_8)$
$(h_3, h_4)$	$(h_6, h_5)$		$(h_8, h_4)$
$(h_3, h_5)$	$(h_6, h_7)$		$(h_8, h_6)$
$(h_3, h_6)$	$(h_6, h_8)$		$(h_8, h_8)$

Search all possible combinations will minimize haplotype switches.

## Step 4: Memoization to avoid exponential search space



**Store this result, so future searches do not have to recompute this sub-tree. Thus search space is *linear***