Initialize: $chain := genesis, F = \emptyset$

Upon receiving a valid fruit, \bullet let $F := F \cup \{fruit\}$

 \bullet let chain := chain'

Upon receiving a valid
$$chain'$$
, if $|chain'| > |chain|$:

Every time step, upon receiving input m from the environment:

• let h_{-1} be the reference of chain[-1];

• If $[h]_{-\kappa} < D_{p_f}$ (i.e., we "mined a fuit")

• let h' be the reference of chain[pos] where $pos = max(1, |chain| - \kappa)$;

• let F' be all fruits $f \in F$ that are recent w.r.t. chain;

• Pick random $\eta \in \{0,1\}^{\kappa}$ and let $h := \mathsf{H}(h_{-1};h';\eta;\mathsf{d}(F');\mathsf{m})$ - let $fruit := (h_{-1}; h'; \eta; \mathsf{d}(F'); \mathsf{m}, h), F := F \cup \{fruit\}, \text{ and broadcast } fruit$

• If $[h]_{:\kappa} < D_p$ (i.e., we "mined a block")

- let $chain := chain || ((h_{-1}; h'; \eta, d(F'); \mathbf{m}, h), F),$ and broadcast chain