

week 9 課程作業

$$(1) H_0 = p_1 - p_2 \leq 0$$

$$H_1 = p_1 - p_2 > 0$$

$$(2) \alpha = 0.05$$

$$n_1 = 200, x = 108$$

$$n_2 = 150, y = 78$$

$$\hat{p}_1 = 0.54, \hat{p}_2 = 0.52$$

$$\bar{p} = \frac{x+y}{n_1+n_2} = \frac{108+78}{200+150}$$

$$= 0.531$$

→ 接受 H_0

Week 10 課堂作業

$$(1) H_0 = \frac{\sigma_1^2}{\sigma_2^2} = 1$$

$$H_1 = \frac{\sigma_1}{\sigma_2} \neq 0$$

$$(2) \alpha = 0.1$$

$$(3) C = \begin{cases} F < F_{0.95}(9, 7) \\ F > F_{0.05}(9, 7) \end{cases}$$

$$\begin{cases} F < \frac{1}{3.29} = 0.304 \\ F > 3.68 \end{cases}$$

$$(4) F = \frac{0.653^2}{0.627^2} = \frac{0.426409}{0.393129} \approx 1.08$$

Week 11 課堂作業

7-4

$$\begin{aligned} H_0 &= \mu = 30 \\ H_1 &= \mu \neq 30 \\ \alpha &= 0.05 \end{aligned}$$

棄原域 C

$$= \{ |Z| > z_{0.025} \}$$

$$= \{ |Z| > 1.96 \}$$

$$Z = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{30.563 - 30}{\frac{2.354}{\sqrt{64}}} = 1.913$$

$$\begin{aligned} p\text{值} &= 2P(Z > 1.913) \\ &\approx 2P(Z > 1.91) \\ &= 2 \times 0.0281 \\ &= 0.0562 > \alpha \end{aligned}$$

→ 接受 H_0

7-5

$$H_0 = \mu \leq 55$$

$$\bar{x} = 59.3125$$

$$H_1 = \mu > 55$$

$$\alpha = 0.05$$

$$① T = \frac{\bar{X} - \mu_0}{\frac{s}{\sqrt{n}}}$$

$$= \frac{59.3125 - 55}{\frac{13.189}{\sqrt{16}}} = 1.308$$

棄原域 C

$$= \{ T > t_{0.05}(16-1) \} \rightarrow \text{接受 } H_0$$

$$= \{ T > 1.753 \}$$

Week 12

$$\bar{Y}_A = 34.75$$

$$\bar{Y}_B = 41$$

$$\bar{Y}_C = 34.33$$

A	B	C
$Y_{11} = 40$	$Y_{21} = 38$	$Y_{31} = 32$
$Y_{12} = 42$	$Y_{22} = 41$	$Y_{32} = 34$
$Y_{13} = 29$	$Y_{23} = 45$	$Y_{33} = 28$
$Y_{14} = 30$	$Y_{24} = 37$	$Y_{34} = 42$
	$Y_{25} = 44$	$Y_{35} = 34$
		$Y_{36} = 36$

→ B課程有較好效果

平均數較大，這表示效果較小。

A107270053 $\frac{\sum x_i^2}{n}$ $\frac{\sum x_i}{n}$

$$E(\hat{\theta}_1) = E\left(\frac{\sum (x_i - \bar{x})^2}{n}\right)$$

$$= \frac{1}{n} \sum (\sum x_i^2 - n\bar{x}^2)$$

$$= \frac{1}{n} (n\sigma^2 + n\mu^2 - \sigma^2 - n\mu^2) = \frac{n-1}{n} \sigma^2 \rightarrow \text{偏誤估計量}$$

$$E(\hat{\theta}_2) = E\left(\frac{\sum (x_i - \bar{x})^2}{n-1}\right) = \frac{1}{n-1} E(\sum x_i^2 - n\bar{x}^2)$$

$$= \frac{1}{n-1} (n\sigma^2 + n\mu^2 - \sigma^2 - n\mu^2) = \sigma^2$$

\rightarrow 不偏估計量

dis