

# 反馈与讨论

2014/12/3

## 8.3

- Fig. 8.5 shows two bipartite graphs  $G_1$  and  $G_2$ , each with sets  $U = \{v, w, x, y, z\}$  and  $W = \{a, b, c, d, e\}$ . In each case can  $U$  be matched to  $W$ ?

## 8.5

- Prove that every tree has at most one perfect matching.

## 8.14

- Prove that a graph  $G$  without isolated vertices has a perfect matching if and only if  $\alpha_1(G) = \beta_1(G)$ .

## 8.16

- Prove that if  $G$  is a graph of order  $n$  and maximum degree  $\Delta$ , then  $\alpha(G) \geq n/(\Delta + 1)$ .

## 8.18

- Give an example of a 5-regular graph that contains no 1-factor.

## 8.21

- Use Tutte's characterization of graphs with 1-factors (Theorem 8.10) to show that  $K_{3,5}$  does not have a 1-factor.

## 8.24

- Show that every 3-regular bridgeless graph contains a 2-factor.