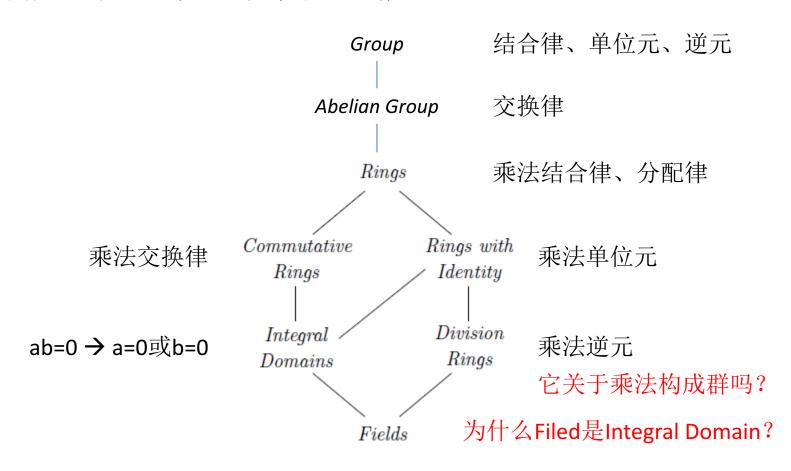
- 教材讨论
  - TJ第16章第1、2、5节

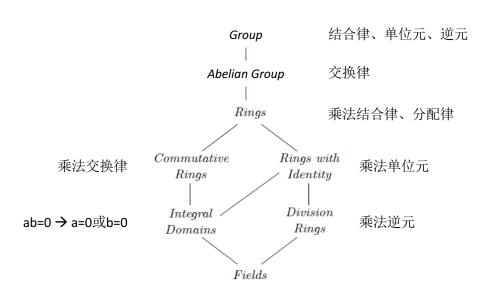
#### 问题1: 环和域

• 你能"增量式"地定义这些概念吗?



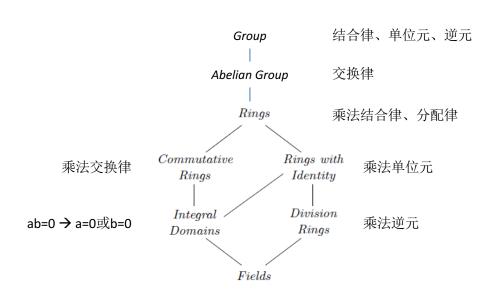
#### 问题2: 环和域的例子

- 自然数?
- 整数?
- 有理数?
- 实数?
- 复数?



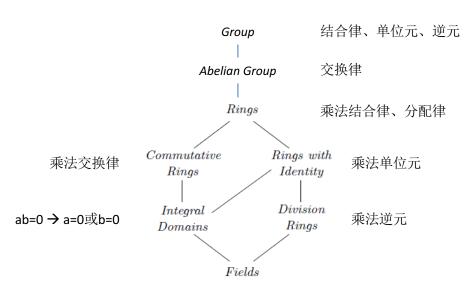
## 问题2: 环和域的例子

- 自然数?
  - 连Group都不是
- 整数?
  - Integral Domain
- 有理数?
  - Field
- 实数?
  - Field
- 复数?
  - Field

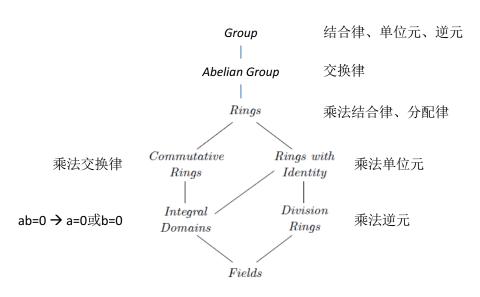


- Gaussian integer?
  - Integral Domain

$$\mathbb{Z}[i] = \{a + bi \mid a, b \in \mathbb{Z}\}, \text{ where } i^2 = -1.$$

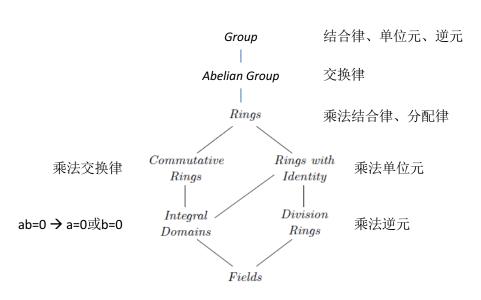


- $Z_n$ ?
  - Commutative Ring & Ring with Identity
- · 增加什么条件可以成为Field?
  - n是质数



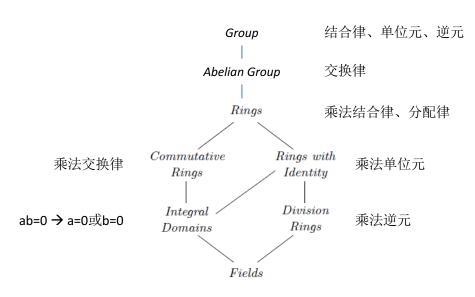
- 2x2实数矩阵?
  - Ring with Identity

$$\left\{ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \middle| a, b, c, d \in \mathbb{R} \right\}$$

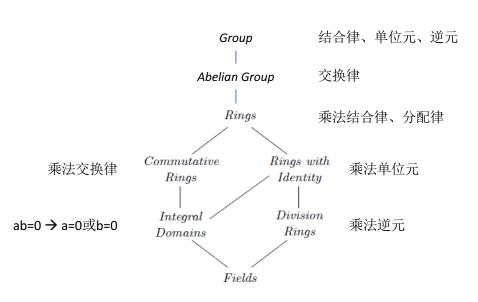


- 实数多项式?
  - Integral Domain

$$p = p_0 + p_1 X + p_2 X^2 + \dots + p_{m-1} X^{m-1} + p_m X^m,$$



- 怎样基于S的幂集构造一个Ring?
  - 加法: 对称差
  - 乘法: 交集
- 它是Commutative Ring吗?
- 它是Ring with Identity吗?
- 它是Integral Domain吗?
- 它是Division Ring吗?



#### 问题3: 子环

- 你能找出以下环的子环吗?
  - 整数
  - Gaussian integer
  - $-Z_n$
  - 2x2实数矩阵
  - 实数多项式
  - S的幂集

$$\mathbb{Z}[i] = \{a + bi \mid a, b \in \mathbb{Z}\}, \text{ where } i^2 = -1.$$

$$\left\{ \begin{pmatrix} a & b \\ c & d \end{pmatrix} \middle| a, b, c, d \in \mathbb{R} \right\}$$

$$p = p_0 + p_1 X + p_2 X^2 + \dots + p_{m-1} X^{m-1} + p_m X^m,$$

