



Language  
Technologies  
Institute

Carnegie  
Mellon  
University

# Multimodal Machine Learning

Lecture 7.2: Reasoning 3  
Inference + Knowledge

Paul Liang

*\* Co-lecturer: Louis-Philippe Morency.  
Original course co-developed with Tadas Baltrusaitis.  
Spring 2021 edition taught by Yonatan Bisk*

# Midterm Project Report Instructions

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- **Goal:** Evaluate state-of-the-art models on your dataset and identify key issues through a detailed error analysis
  - It will inform the design of your new research ideas
- **Report format:** 2 column (ICML template)
  - The report should follow a similar structure to a research paper
  - Teams of 3: 8 pages, Teams of 4: 8.5 pages, Teams of 5: 10 pages. Teams of 6: 10.5 pages
- **Number of SOTA models**
  - Teams of 3 or 4 should have at least two baseline models
  - Teams of 5 or 6 should have at least three baseline models
- **Error analysis**
  - This is one of the most important part of this report. You need to understand where previous models can be improved.

# Examples of Possible Error Analysis Approaches

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- Dataset-based:
  - Split correct/incorrect by label
  - Manually inspect the samples that are incorrectly predicted
    - What are the commonalities?
    - What are differences with the correct ones?
  - Sub-dataset analysis: length of question, rare words, cluttered images, high frequency in signals?

# Examples of Possible Error Analysis Approaches

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- Perturbation-based:
  - Make targeted changes to specific parts of the image.
  - Change one word/paraphrase/add redundant tokens.
  - See whether the model remains robust

# Examples of Possible Error Analysis Approaches

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- Model-based:
  - Visualize feature attributions: LIME, 1<sup>st</sup>/2<sup>nd</sup> order gradients
  - Ablation studies to understand what model components are important
- Theory-based:
  - Write out the math! From optimization and learning perspective, does the model do what's expected?
  - Some useful tools: consider linear case/other simplest case and derive solution, do empirical sanity checks first.

[Liang et al., MultiViz: An Analysis Benchmark for Visualizing and Understanding Multimodal Models. arXiv 2022]

# Examples of Possible Error Analysis Approaches

Published as a conference paper at ICLR 2018

## ON THE CONVERGENCE OF ADAM AND BEYOND

Sashank J. Reddi, Satyen Kale & Sanjiv Kumar

Google New York

New York, NY 10011, USA

{sashank, satyenkale, sanjivk}@google.com

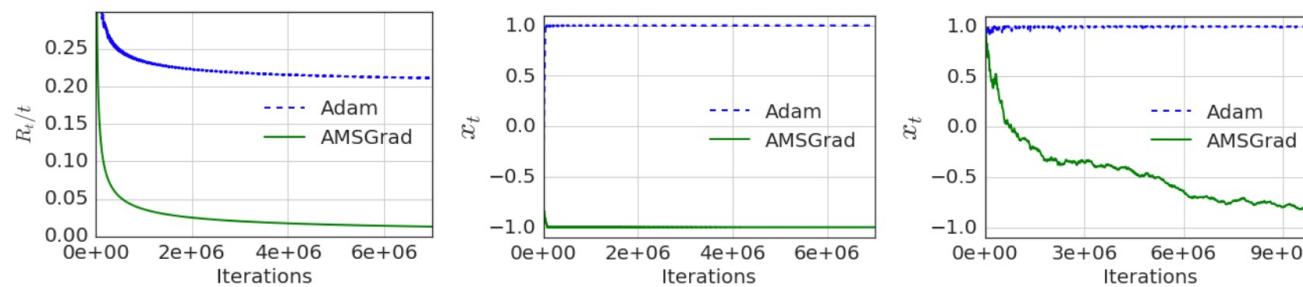
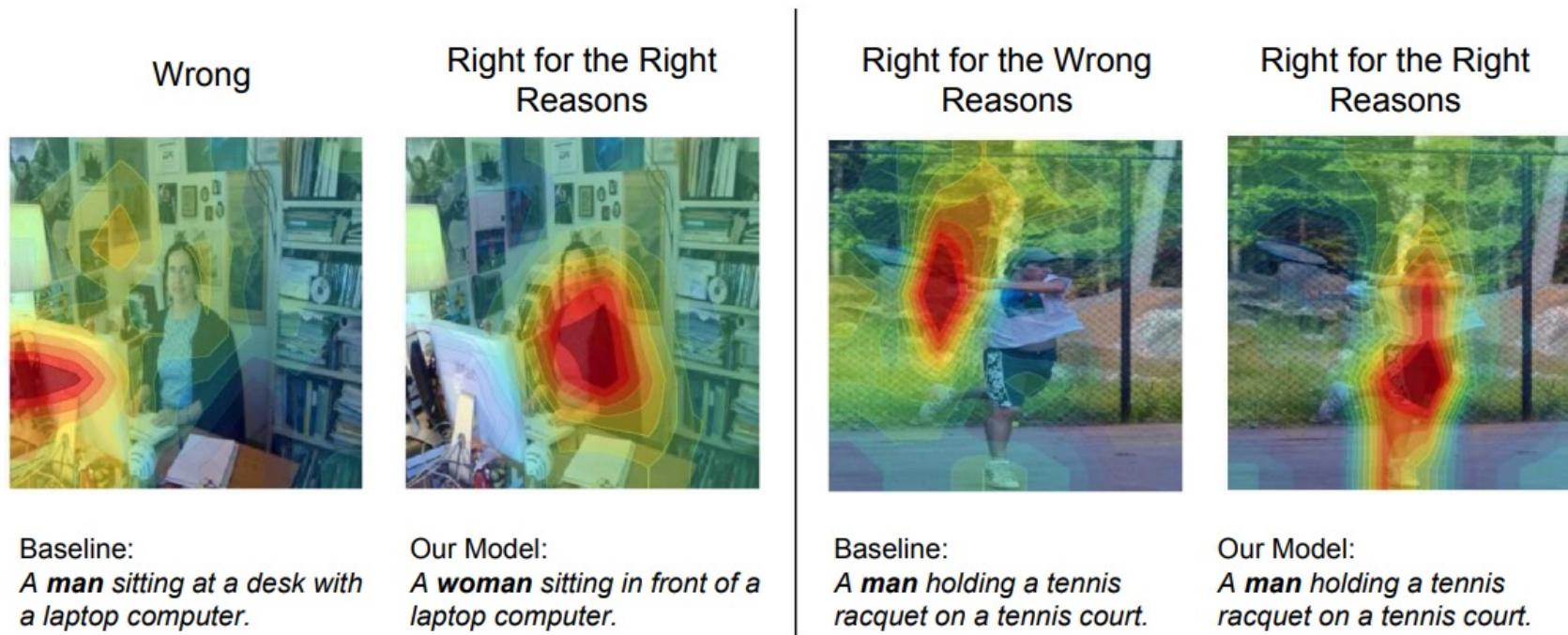


Figure 1: Performance comparison of ADAM and AMSGRAD on synthetic example on a simple one dimensional convex problem inspired by our examples of non-convergence. The first two plots (left and center) are for the online setting and the the last one (right) is for the stochastic setting.

[Reddi et al., On the Convergence of Adam and Beyond. ICLR 2018]

# Examples of Possible Error Analysis Approaches

**Finding:** Image captioning models capture spurious correlations between gender and generated actions



You'll see more in today's reasoning lecture and in quantification lectures

[Hendricks et al., Women also Snowboard: Overcoming Bias in Captioning Models. ECCV 2018]

# Midterm Project Report Instructions

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Main report sections:

- Abstract
- Introduction
- Related work
- Problem statement
- Multimodal baseline models
- Experimental methodology
- Results and discussion
- New research ideas



The structure is  
similar to a  
research paper  
submission 😊

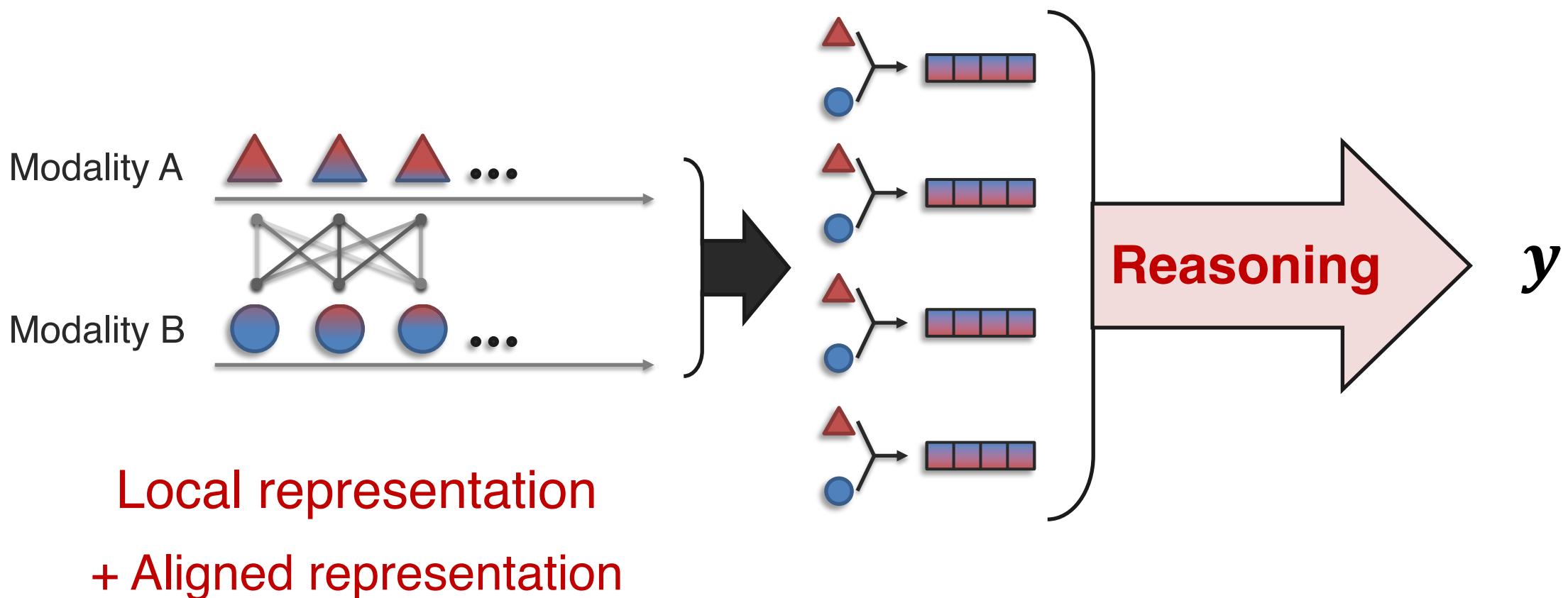
## Upcoming Deadlines

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- Monday October 31<sup>st</sup> 8pm: Midterm report deadline
- Tuesday and Thursday (11/1 and 11/3): midterm presentations
  - All students are expected to attend both presentation sessions in person
  - Each team will present either Tuesday or Thursday
  - The focus of these presentations is about your research ideas
  - Feedback will be given by all students, instructors and TAs

# Reasoning

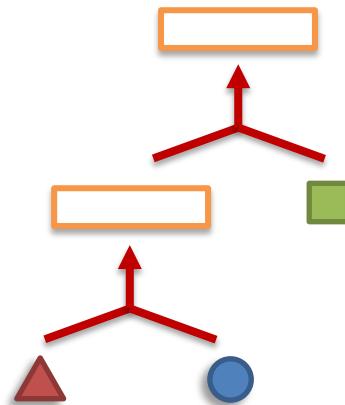
**Definition:** Combining knowledge, usually through multiple inferential steps, exploiting multimodal alignment and problem structure.



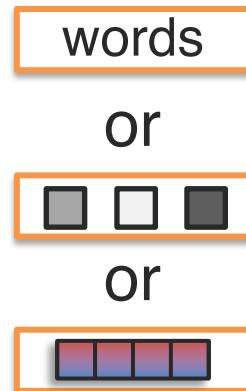
# Reasoning

**Definition:** Combining knowledge, usually through multiple inferential steps, exploiting multimodal alignment and problem structure.

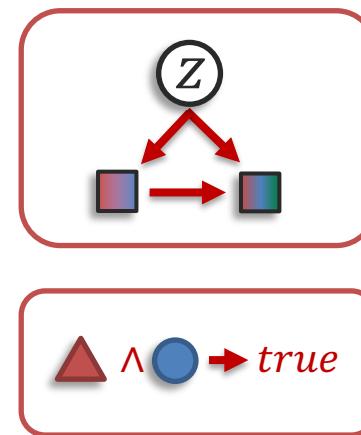
A Structure modeling



B Intermediate concepts



C Inference paradigm



D External knowledge



# Summary

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**Definition:** Combining knowledge, usually through multiple inferential steps, exploiting multimodal alignment and problem structure.

(A) Structure modeling

(B) Intermediate concepts

(C) Inference paradigm

(D) External knowledge

Last Thursday

Temporal  
Hierarchical

Continuous

Tuesday

Interactive

Today

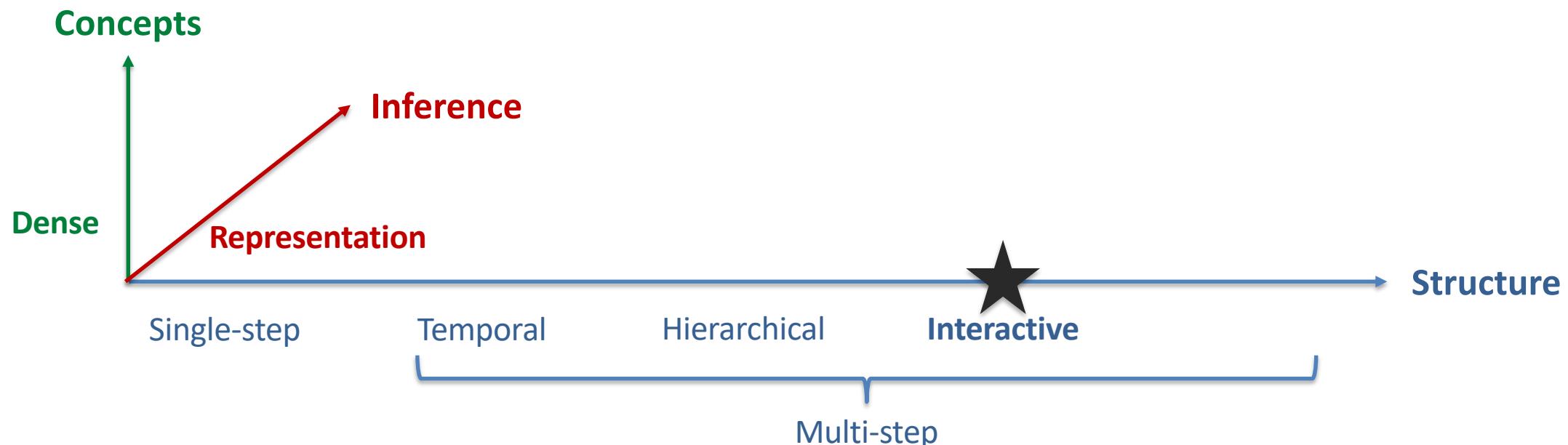
Discovery

Discrete

Causal  
Logical

Knowledge  
Commonsense

## Sub-Challenge 3a: Structure Modeling

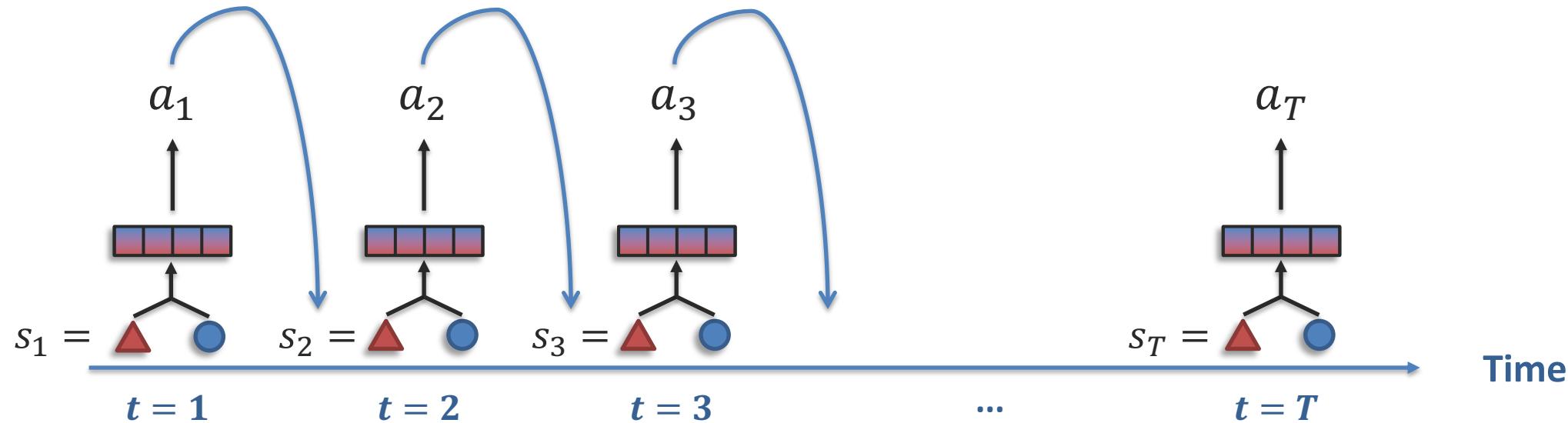


# Interactive Structure

**Structure defined through interactive environment**

Main difference from temporal - actions taken at previous time steps affect future states

Integrates multimodality into the reinforcement learning framework

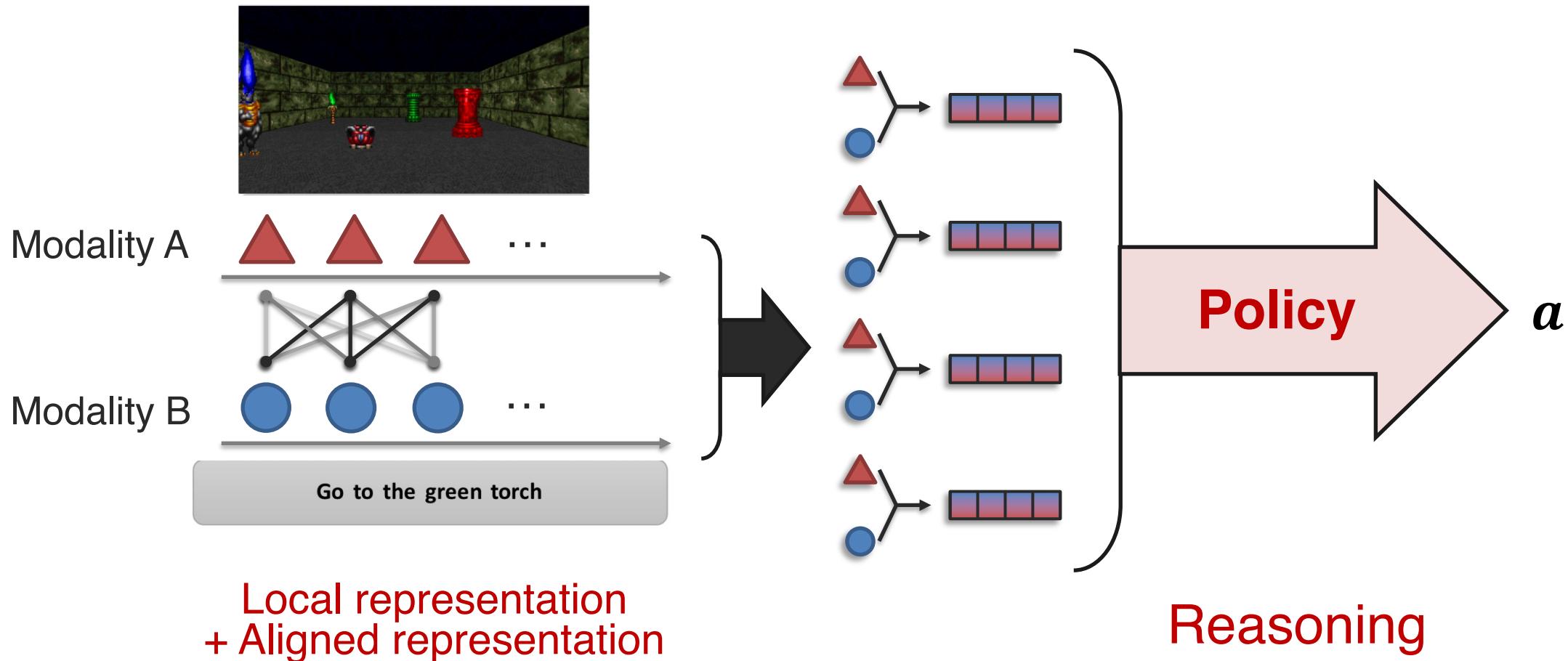


[Luketina et al., A Survey of Reinforcement Learning Informed by Natural Language. IJCAI 2019]

# Interactive Structure

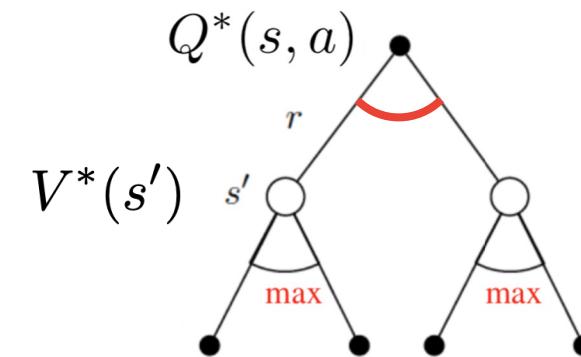
## Structure defined through interactive environment

Main difference from temporal - actions taken at previous time steps affect future states



# Summary: Exact Methods

Fully known MDP states transitions rewards	Bellman optimality equations	$Q^*(s, a)$	Q-value iteration
		$V^*(s)$	Value iteration



$$Q^*(s, a) = \mathbb{E}_{s'} [r(s, a, s') + \gamma V^*(s')]$$

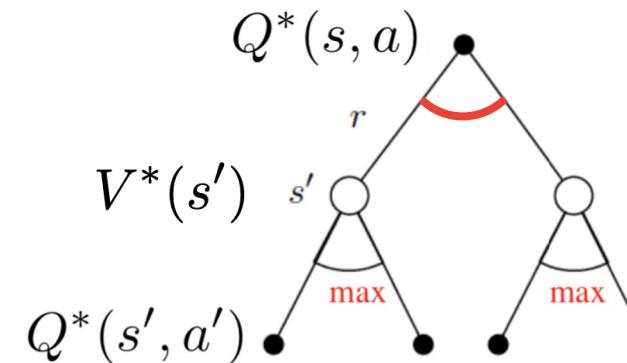
# Summary: Exact Methods

Fully known MDP  
states  
transitions  
rewards

Bellman optimality equations

$$\begin{aligned} Q^*(s, a) \\ V^*(s) \end{aligned}$$

Q-value iteration  
Value iteration



$$\begin{aligned} Q^*(s, a) &= \mathbb{E}_{s'} [r(s, a, s') + \gamma V^*(s')] \\ &= \mathbb{E}_{s'} \left[ r(s, a, s') + \gamma \max_{a'} Q^*(s', a') \right] \end{aligned}$$

# Summary: Exact Methods

Fully known MDP  
states  
transitions  
rewards

Bellman optimality equations

$$\begin{aligned} Q^*(s, a) & \quad \text{Q-value iteration} \\ V^*(s) & \quad \text{Value iteration} \end{aligned}$$

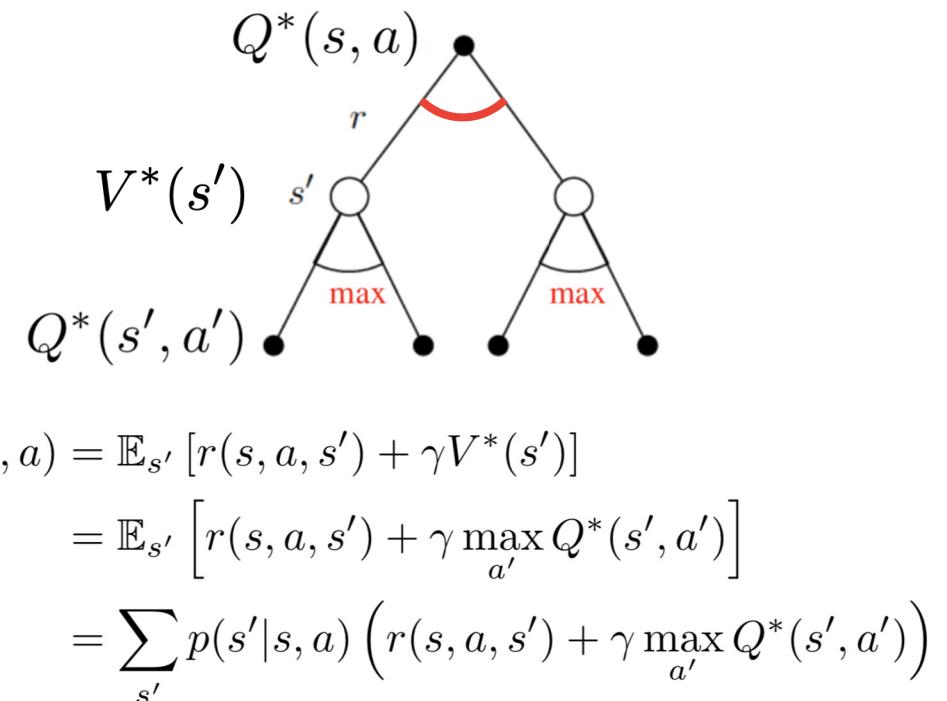
$Q^*(s, a)$  = expected utility starting in  $s$ , taking action  $a$ , and (thereafter) acting optimally

Bellman Equation:

$$Q^*(s, a) = \sum_{s'} P(s'|s, a)(R(s, a, s') + \gamma \max_{a'} Q^*(s', a'))$$

Q-Value Iteration:

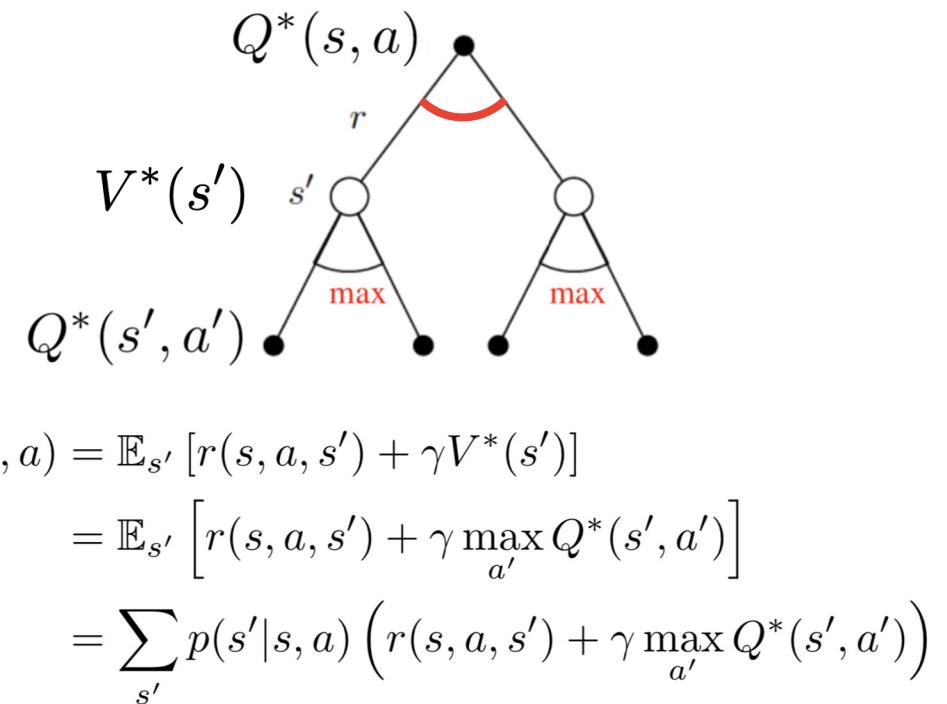
$$Q_{k+1}^*(s, a) \leftarrow \sum_{s'} P(s'|s, a)(R(s, a, s') + \gamma \max_{a'} Q_k^*(s', a'))$$



# Summary: Exact Methods

Fully known MDP states transitions rewards	Bellman optimality equations	$Q^*(s, a)$	Q-value iteration
		$V^*(s)$	Value iteration
	Bellman expectation equations	$Q^\pi(s, a)$	Q-policy iteration
		$V^\pi(s)$	Policy iteration

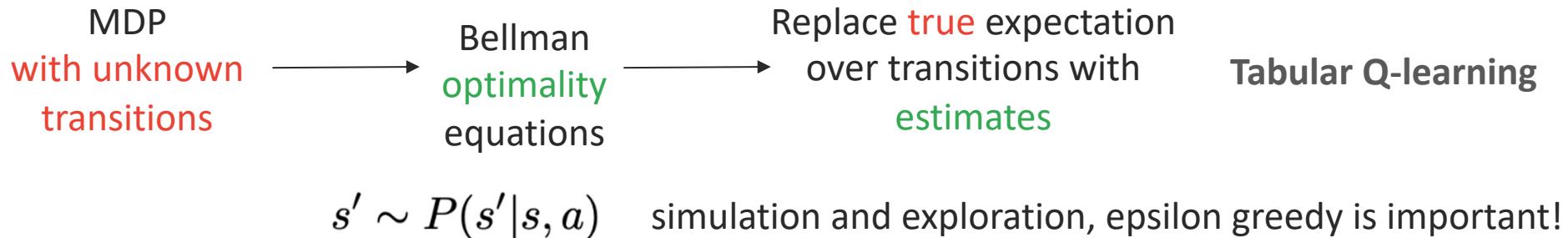
Repeat until policy converges. Guaranteed to converge to optimal policy.



## Limitations:

Iterate over and storage for all states and actions: requires small, discrete state and action space  
Update equations require fully observable MDP and known transitions

# Summary: Tabular Q-learning



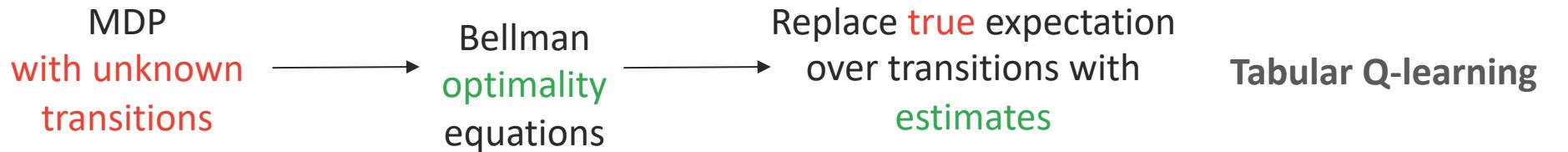
Poor estimates of  $Q(s,a)$  at the start:

Bad initial estimates in the first few cases can drive policy into sub-optimal region, and never explore further.

$$\pi(s) = \begin{cases} \max_a \hat{Q}(s, a) & \text{with probability } 1 - \epsilon \\ \text{random action} & \text{otherwise} \end{cases}$$

Gradually decrease epsilon as policy is learned.

# Summary: Tabular Q-learning



$s' \sim P(s'|s, a)$  simulation and exploration, epsilon greedy is important!

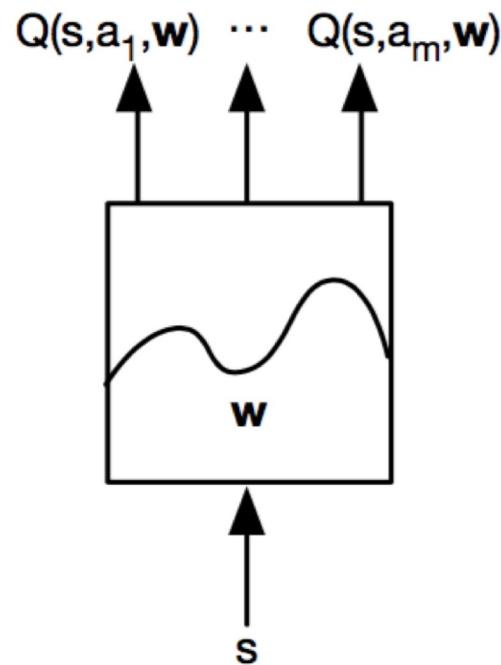
$$Q^*(s, a) = \underbrace{\mathbb{E}_{s'} \left[ r(s, a, s') + \gamma \max_{a'} Q^*(s', a') \right]}_{\text{target}}$$

**old estimate**   **target**

$$Q_{k+1}(s, a) \leftarrow Q_k(s, a) + \alpha \left( r(s, a, s') + \gamma \max_{a'} Q_k(s', a') - Q_k(s, a) \right)$$

Tabular: keep a  $|S| \times |A|$  table of  $Q(s, a)$   
Still requires small and discrete state and action space  
How can we generalize to unseen states?

# Summary: Deep Q-learning



$$Q^*(s, a) = \underbrace{\mathbb{E}_{s'} \left[ r(s, a, s') + \gamma \max_{a'} Q^*(s', a') \right]}_{\text{old estimate}} \quad \underbrace{\text{target}}$$

$$\mathcal{L}_i(w_i) = \mathbb{E}_{s, a, r, s' \sim \mathcal{D}_i} \left[ \underbrace{\left( r + \gamma \max_{a'} Q(s', a'; w_i^-) - Q(s, a; w_i) \right)^2}_{\text{Q-learning target}} \right] \quad \underbrace{\text{Q-network}}$$

Stochastic gradient descent + Experience replay + Fixed Q-targets

Works for high-dimensional state and action spaces  
Generalizes to unseen states

# Can we Directly Learn the Policy?

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- Often  $\pi$  can be simpler than Q or V
  - E.g., robotic grasp
- V: doesn't prescribe actions
  - Would need dynamics model (+ compute 1 Bellman back-up)
- Q: need to be able to efficiently solve  $\arg \max_a Q^*(s, a)$ 
  - Challenge for continuous / high-dimensional action spaces

$Q(s, a)$  and  $V(s)$  very high-dimensional  
But policy could be just 'open/close hand'

$$\pi^*(a|s) = \begin{cases} 1 - \epsilon, & \text{if } a = \arg \max_a \mathbb{E}_{s'} [r(s, a, s') + \gamma V^*(s')] \\ \epsilon, & \text{else} \end{cases} \quad \pi^*(a|s) = \begin{cases} 1 - \epsilon, & \text{if } a = \arg \max_a Q^*(s, a) \\ \epsilon, & \text{else} \end{cases}$$

[Slides from Fragkiadaki, 10-703 CMU]

# Summary: Policy Gradients

$$\pi(a | s)$$

1. Initialize a policy network at random

2. **Repeat Forever:**

3. Collect a bunch of rollouts with the policy

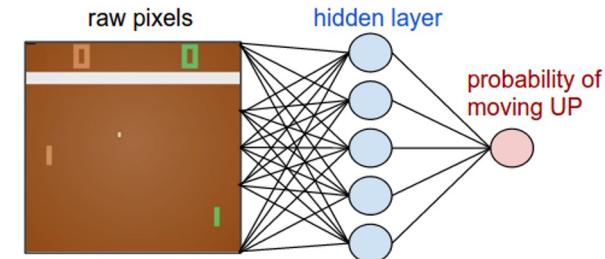
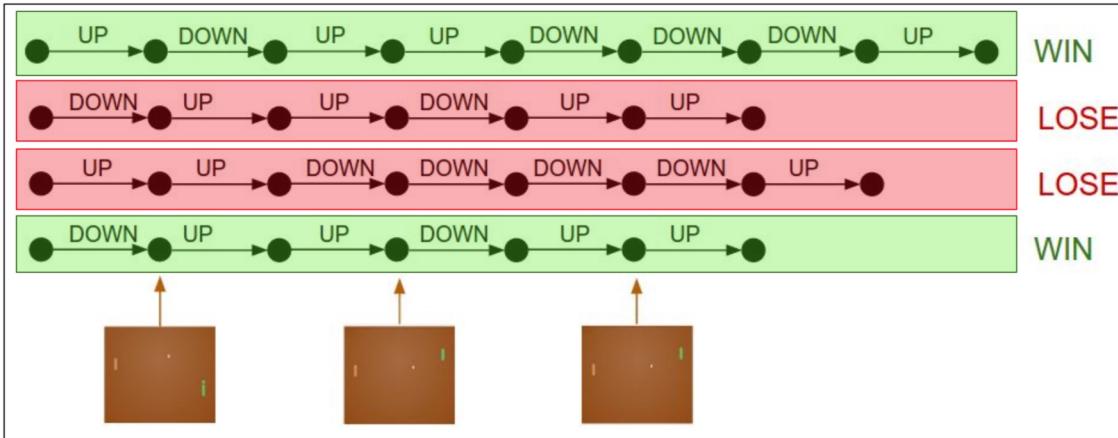
4. Increase the probability of actions that worked well

Pretend every action we took here  
was the correct label.

$$\text{maximize: } \log p(y_i | x_i)$$

Pretend every action we took  
here was the wrong label.

$$\text{maximize: } (-1) * \log p(y_i | x_i)$$



**epsilon greedy!**

$$\sum_i A_i * \log p(y_i | x_i)$$

Does not require transition probabilities  
Does not estimate Q(), V()  
Predicts policy directly

[Slides from Karpathy]

# Summary: Policy Gradients

Gradient estimator:

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

Interpretation:

- If **r(trajectory)** is high, push up the probabilities of the actions seen
- If **r(trajectory)** is low, push down the probabilities of the actions seen

## REINFORCE, A Monte-Carlo Policy-Gradient Method (episodic)

Input: a differentiable policy parameterization  $\pi(a|s, \theta)$ ,  $\forall a \in \mathcal{A}, s \in \mathcal{S}, \theta \in \mathbb{R}^n$

Initialize policy weights  $\theta$

Repeat forever:

Generate an episode  $S_0, A_0, R_1, \dots, S_{T-1}, A_{T-1}, R_T$  following  $\pi(\cdot | \cdot, \theta)$

For each step of the episode  $t = 0, \dots, T - 1$ :

$G_t \leftarrow$  return from step  $t$

epsilon greedy

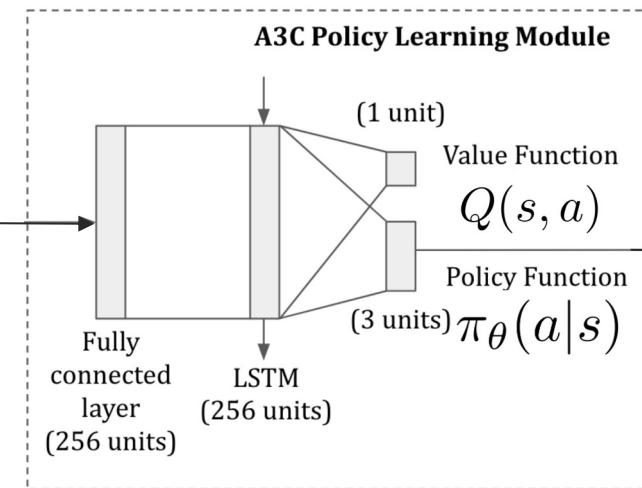
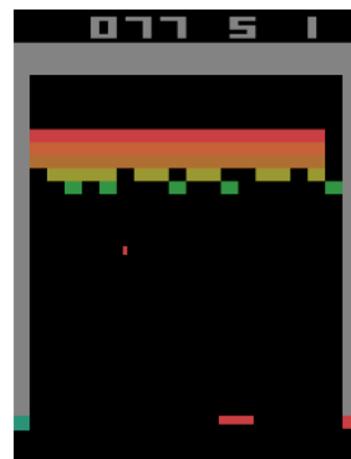
$\theta \leftarrow \theta + \alpha \gamma^t G_t \nabla_{\theta} \log \pi(A_t | S_t, \theta)$

# Summary: Actor-Critic Methods

**Problem:** The raw reward of a trajectory isn't necessarily meaningful. E.g. if all rewards are positive, you keep pushing up probabilities of all actions.

**What is important then?** Whether a reward is higher or lower than what you expect to get.

**Yes,** using Q-learning! We can combine Policy Gradients and Q-learning by training both an **actor** (the policy) and a **critic** (the Q function)



Critic: evaluates how good the action is      Fixed targets

$$\mathcal{L}_i(w_i) = \mathbb{E}_{s,a,r,s' \sim \mathcal{D}_i} \left[ \underbrace{\left( r + \gamma \max_{a'} Q(s', a'; w_i^-) - Q(s, a; w_i) \right)^2}_{\text{Q-learning target}} \right]$$

Q-network

Actor: decides what actions to take

$$\nabla_\theta J(\theta) \approx \sum_{t \geq 0} (Q^{\pi_\theta}(s_t, a_t) - V^{\pi_\theta}(s_t)) \nabla_\theta \log \pi_\theta(a_t | s_t)$$

Variance reduction with a baseline

[Minh et al., Asynchronous Methods for Deep Reinforcement Learning. ICML 2016]

# Summary: RL Methods

Epsilon greedy + exploration

Experience replay

Decorrelate samples

Fixed targets

- › Value Based

- Learned Value Function

- Implicit policy (e.g.  $\epsilon$ -greedy)

- › Policy Based

- No Value Function

- Learned Policy

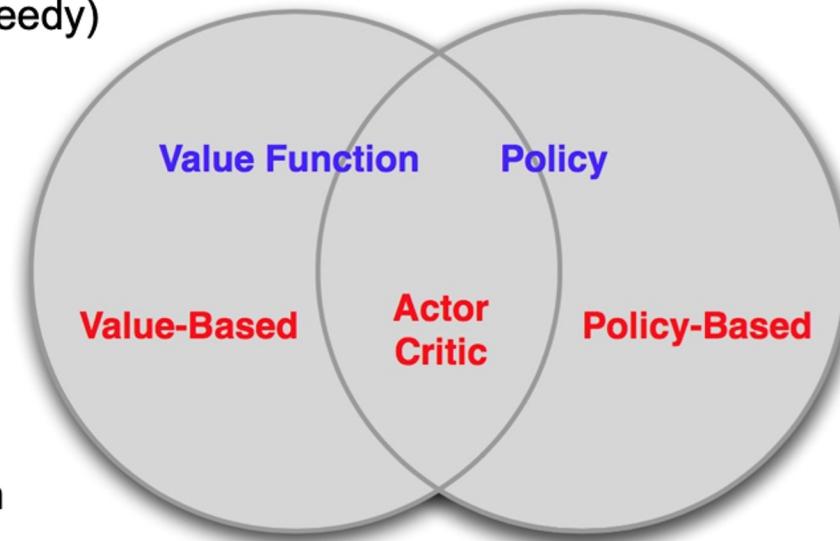
Variance reduction with a baseline

- › Actor-Critic

- Learned Value Function

- Learned Policy

Actor (policy)  
Critic (Q-values)

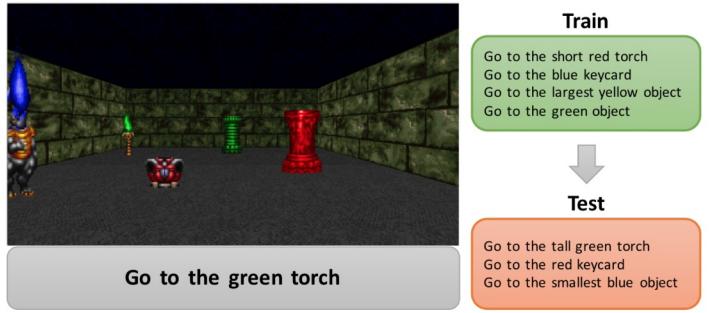


[Slides from Fragkiadaki, 10-703 CMU]

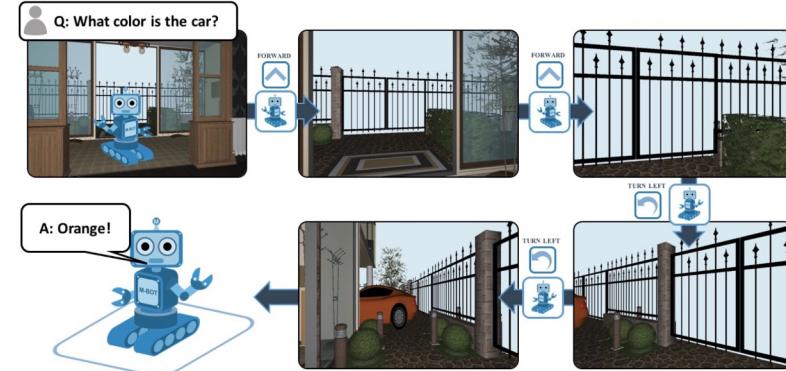


# Summary: Interactive Reasoning

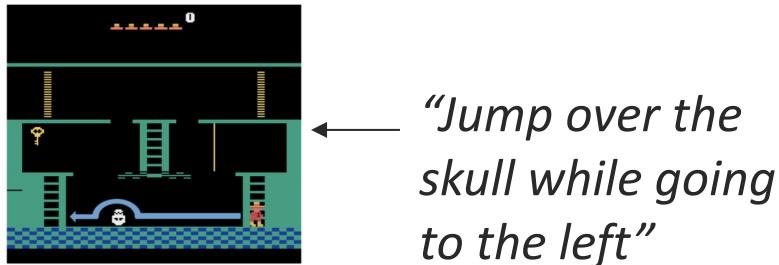
## Instruction following



## Embodied learning



## Reward shaping



## Domain knowledge



The natural resources available where a population settles affects its ability to produce food and goods. Build your city on a plains or grassland square with a river running through it if possible.

Figure 1: An excerpt from the user manual of the game Civilization II.

# Interactive Reasoning Challenges

Open challenges

## Learning from open-ended manuals



**ALIEN**  
20th Century Fox  
Games of the Century  
(picture of the ALIEN movie poster)  
"In space no one can hear you scream"  
Game Instructions  
Fox Video Games

**ALIEN**

TO SET UP: Set up your video computer system and left joystick controller as instructed in your manufacturer's manual. Move the Color/B-W lever to the correct setting. Turn the power OFF and insert the Alien game cartridge.

(Screen shot of the ALIEN maze setup: Alien, Alien Egg, Human, Pulsar and Play Level-demo mode only)

TO BEGIN: Turn the power ON. Use the Game Select lever and Difficulty Switches to choose a play level. Press the Game Reset lever and get ready to run for your life.

THE OBJECTIVE: Your job is to run through the hallways of your space ship and crush all the Alien Eggs which have been placed there. You must also avoid or destroy the adult Aliens and snatch up as many prizes as possible.

THE CONTROLS: Tilt the joystick forward, backward, left and right to maneuver through the hallways. To smash Eggs, simply run over them. You may travel off one side of the maze and back into the other using the "Hyperwarp Passage." Each Human is equipped with a Flame Thrower that is activated by the joystick button (see below).

SCREEN DISPLAY: The Play Level and Humans allowed per Play Level are displayed in the bottom left corner of the screen when Alien is not in play. During the game, the current score and Humans remaining are shown there.

LEVELS OF PLAY/DIFFICULTY SWITCHES/BONUS ROUNDS: Each game of Alien lasts until you run out of Humans. If you can clear all of the Eggs out of a playing screen, you get the chance to earn extra points in a "Bonus Round" and then are returned to a new and more difficult playing screen. All points and Humans remaining are carried over to the new screens.

Bonus Rounds: The object of the Bonus Round is to travel STRAIGHT UP to the top of the screen and grab the prize shown there. You have only eight seconds to do so. You do not lose a human if you fail, but you earn the point value of the prize if you succeed.

Left Difficulty Switch A: Aliens travel in random order about the screen.  
Left Difficulty Switch B: Aliens travel in fixed patterns about the screen.  
Right Difficult Switch C: Capturing a Pulsar has standard effect on the Aliens.  
Right Difficult Switch D: Capturing a Pulsar has no effect on the Aliens.

(Screen shot of ALIEN maze: Flame Thrower, Prize, Hyperwarp Passages, Humans Remaining and Current Score)

LEVEL 1 - NORMAL GAME PLAY: You begin with three Humans and receive a bonus Human after successfully clearing the second screen. Prizes appear in chart order.

LEVEL 2 - ADVANCED GAME PLAY: You begin with two Humans and receive no bonus Humans. Prizes appear in chart order.

LEVEL 3 - FOR EXPERTS ONLY: You begin with three Humans and receive no bonus Human after clearing the first screen. All Prizes in Level 3 are Saturns.

LEVEL 4 - EASY PRACTICE GAME: You begin with six Humans and receive 1 bonus Human after clearing the first screen. All Prizes in Level 4 are also Saturns.

OBJECTS/SCORING: Each time an Alien catches you, one Human is lost. You score points for smashing Eggs and frying Aliens with the aid of your Flame Thrower or Pulsar. In addition, you can gain points for picking up Prizes. Be sure to record your high scores on the back of this booklet!

(Screen shot of the bonus round with the human at the bottom of the screen, the prize at the top of the screen and the horizontal moving Aliens in the centre portion -- similar to the road portion of Frogger.)

FLAME THROWER - 1 PER HUMAN: A spurt of flam from this contraption cause Aliens to turn away from you or become immobilized for a short period of time. Use the Throwers carefully. Each has only four seconds of flame and the Thrower will not operate in the extreme left or right areas of the screen. You can also use the Flame Thrower to run over a Pulsar without picking it up, allowing you to save the Pulsar to use at a later time.

PULSARS - 3 PER MAZE: Capturing a Pulsar causes the Aliens to weaken and turn blue. Then, for a short period of time, you can destroy them by running over and touching them. The instant the Aliens return to their original color, however, they once again become deadly.

PRIZES - 2 PER MAZE: Prizes appear in all levels of play and in the Bonus Rounds.

### POINT CHART:

OBJECT	POINTS	PRIZES	POINTS	OBJECT	
Eggs	10			Rocket	500
Pulsar	100	Saturn	1,000		
1st Alien	500	Star Ship	2,000		
2nd Alien	1,000	1st Surprise	2,000-3,000		
3rd Alien	2,000	2nd Surprise	3,000		
Completed Screen	1	3rd Surprise	5,000		

### HINTS FROM DALLAS NORTH...

A good playing strategy is to crush all of the Eggs in one area at a time, keeping within easy reach of a Pulsar. The best way to destroy Aliens is to sit near a Pulsar until the Aliens are almost upon you. Then grab that Pulsar and go get 'em!

Use the Hyperwarp Passage to ditch Aliens. Many times they won't follow you in.

If you're having trouble with the Bonus Rounds, try going between the Alien pairs rather than around them.

SUPER SMASHERS (a place to enter your high scores)  
Name \_\_\_\_\_ Level \_\_\_\_\_ Score \_\_\_\_\_

# Interactive Reasoning Challenges

Open challenges

## Learning from text-based games

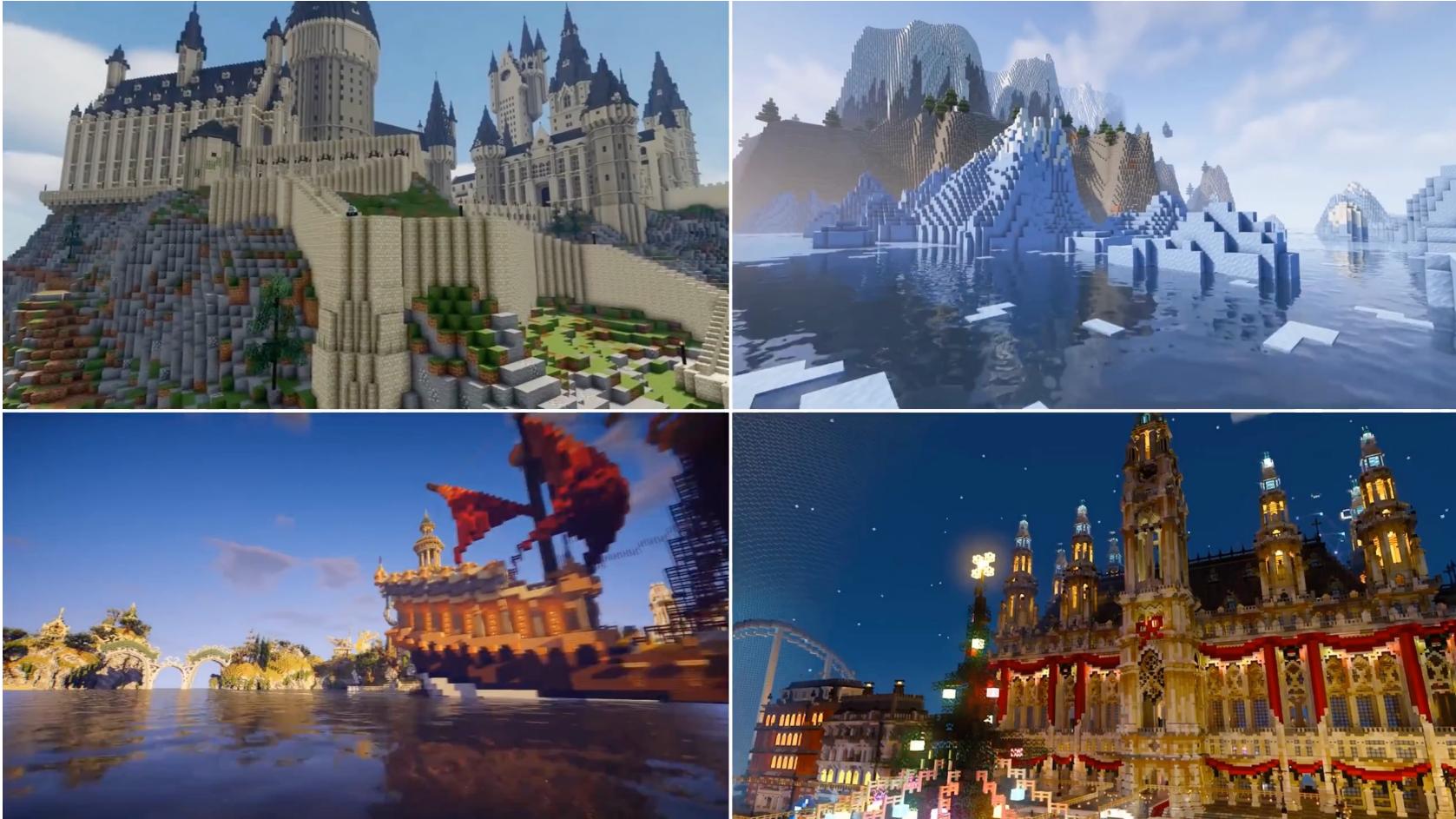


[Zhong et al., SILG: The Multi-environment Symbolic Interactive Language Grounding Benchmark. NeurIPS 2021]

# Interactive Reasoning Challenges

Open challenges

Learning from lots of offline data



[Fan et al., MineDojo: Building Open-Ended Embodied Agents with Internet-Scale Knowledge. arXiv 2022]

# Interactive Reasoning Challenges

Open challenges

Hard to specify reward, but only final goal



[Habitat Rearrangement Challenge 2022]

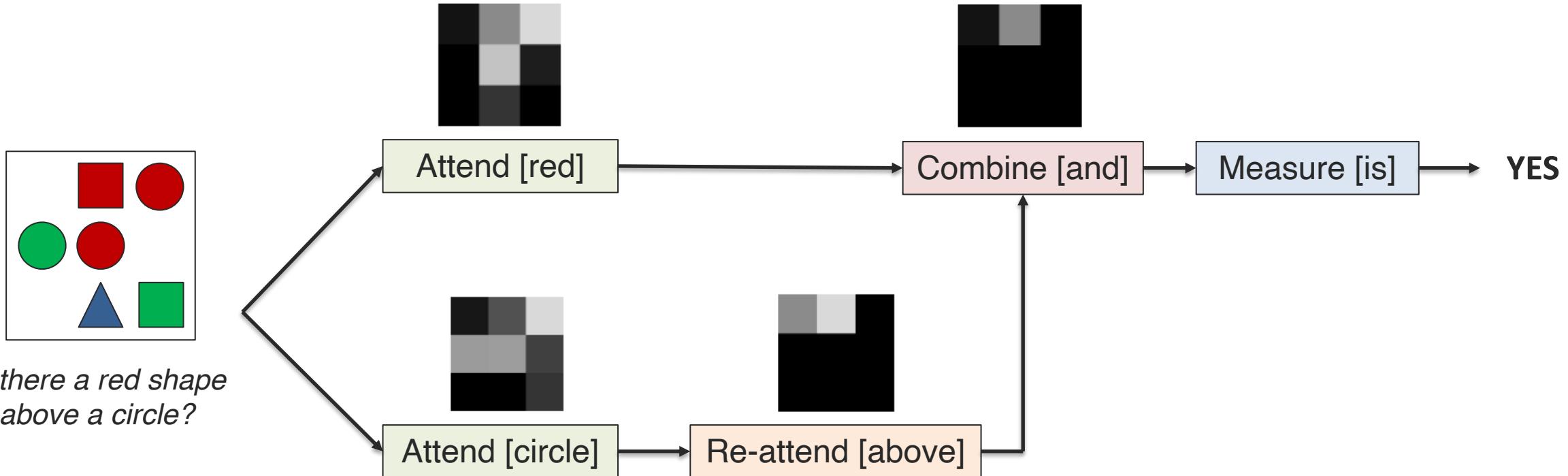
## Sub-Challenge 3a: Structure Modeling



# Structure Discovery

## End-to-end neural module networks

Recall structure - leverage syntactic structure of language based on parsing

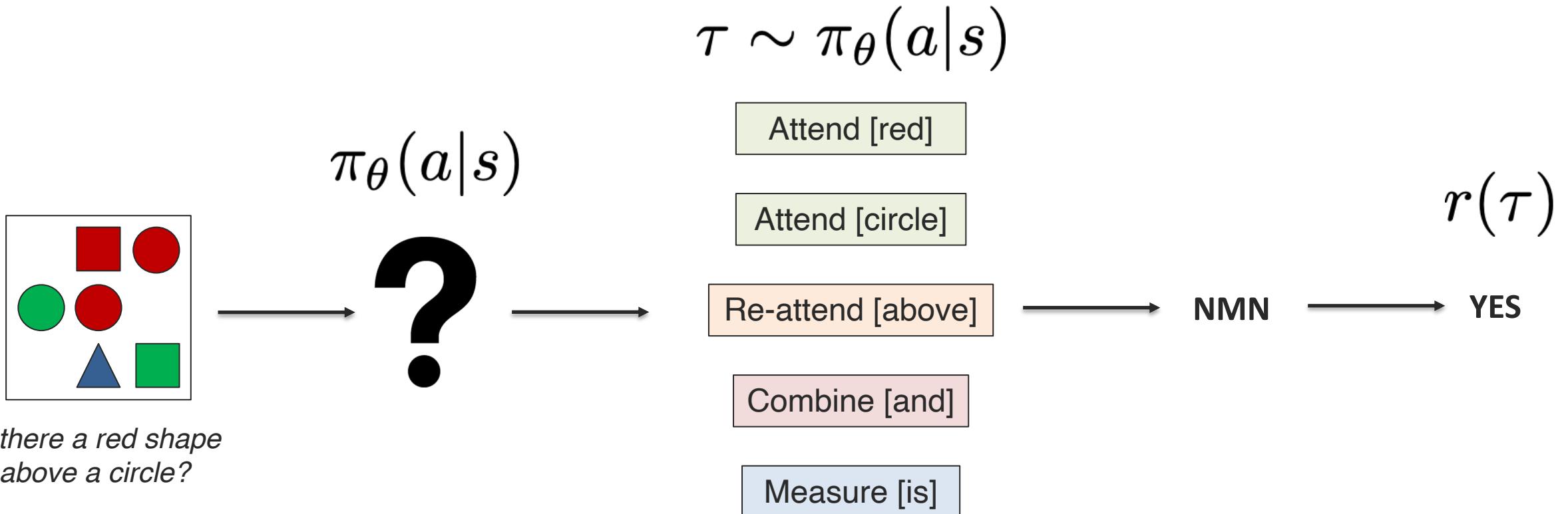


[Andreas et al., Neural Module Networks. CVPR 2016]

# Structure Discovery

## End-to-end neural module networks

Can we learn the structure end-to-end?



[Hu et al., Learning to Reason: End-to-End Module Networks for Visual Question Answering. ICCV 2017]

# Stochastic Optimization

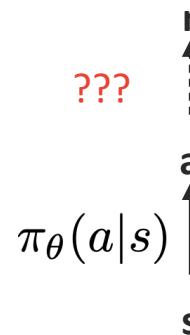
$$\max_{\theta} \mathbb{E}_{q_{\theta}(\mathbf{z})}[f(\mathbf{z})]$$

RL

$$\max_{\theta} J(\theta) \quad \text{Reward}$$

$$\max_{\theta} \mathbb{E}_{\tau \sim p(\tau; \theta)}[r(\tau)]$$

In RL (at least for discrete actions):  
- T is a sequence of discrete actions  
-  $p(T; \theta)$  is not reparameterizable  
-  $r(T)$  is a black box function  
i.e. the environment



REINFORCE is a general-purpose solution!

# Revisiting REINFORCE

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$$\max_{\theta} \mathbb{E}_{q_{\theta}(\mathbf{z})}[f(\mathbf{z})] \quad (\text{we will revisit this equation for generative models})$$

We want to take gradients wrt  $\theta$  of the term:

$$\nabla_{\theta} \mathbb{E}_{q_{\theta}(\mathbf{z})}[f(\mathbf{z})] = \mathbb{E}_{q_{\theta}(\mathbf{z})}[f(\mathbf{z}) \nabla_{\theta} \log q_{\theta}(\mathbf{z})]$$

We can now compute a Monte Carlo estimate:

Sample  $\mathbf{z}^1, \mathbf{z}^2, \dots, \mathbf{z}^K$  from  $q_{\theta}(\mathbf{z})$  and estimate

$$\nabla_{\theta} \mathbb{E}_{q_{\theta}(\mathbf{z})}[f(\mathbf{z})] \approx \frac{1}{K} \sum_k [f(\mathbf{z}^k) \nabla_{\theta} \log q_{\theta}(\mathbf{z}^k)]$$

What we derived: sample trajectories and compute:

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

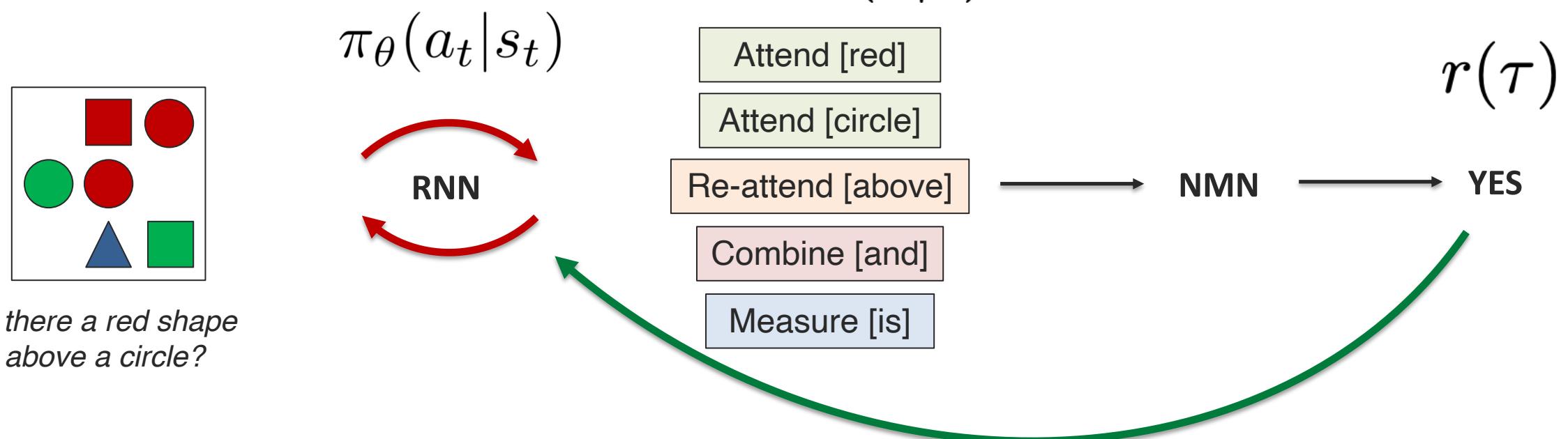
- $\mathbf{z}$  can be discrete or continuous!
- $q(\mathbf{z})$  can be a discrete and continuous distribution!
- $q(\mathbf{z})$  must allow for easy sampling and be differentiable wrt  $\theta$
- $f(\mathbf{z})$  can be a black box!

# Structure Discovery

## End-to-end neural module networks

Can we learn the structure end-to-end?

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$



*Is there a red shape  
above a circle?*

$$\pi_{\theta}(a_t | s_t)$$



$$\tau \sim \pi_{\theta}(a | s)$$

- Attend [red]
- Attend [circle]
- Re-attend [above]
- Combine [and]
- Measure [is]



NMN

$$r(\tau)$$

YES

[Hu et al., Learning to Reason: End-to-End Module Networks for Visual Question Answering. ICCV 2017]

# Structure Discovery

Structure fully learned from optimization and data

1. Define basic representation building blocks



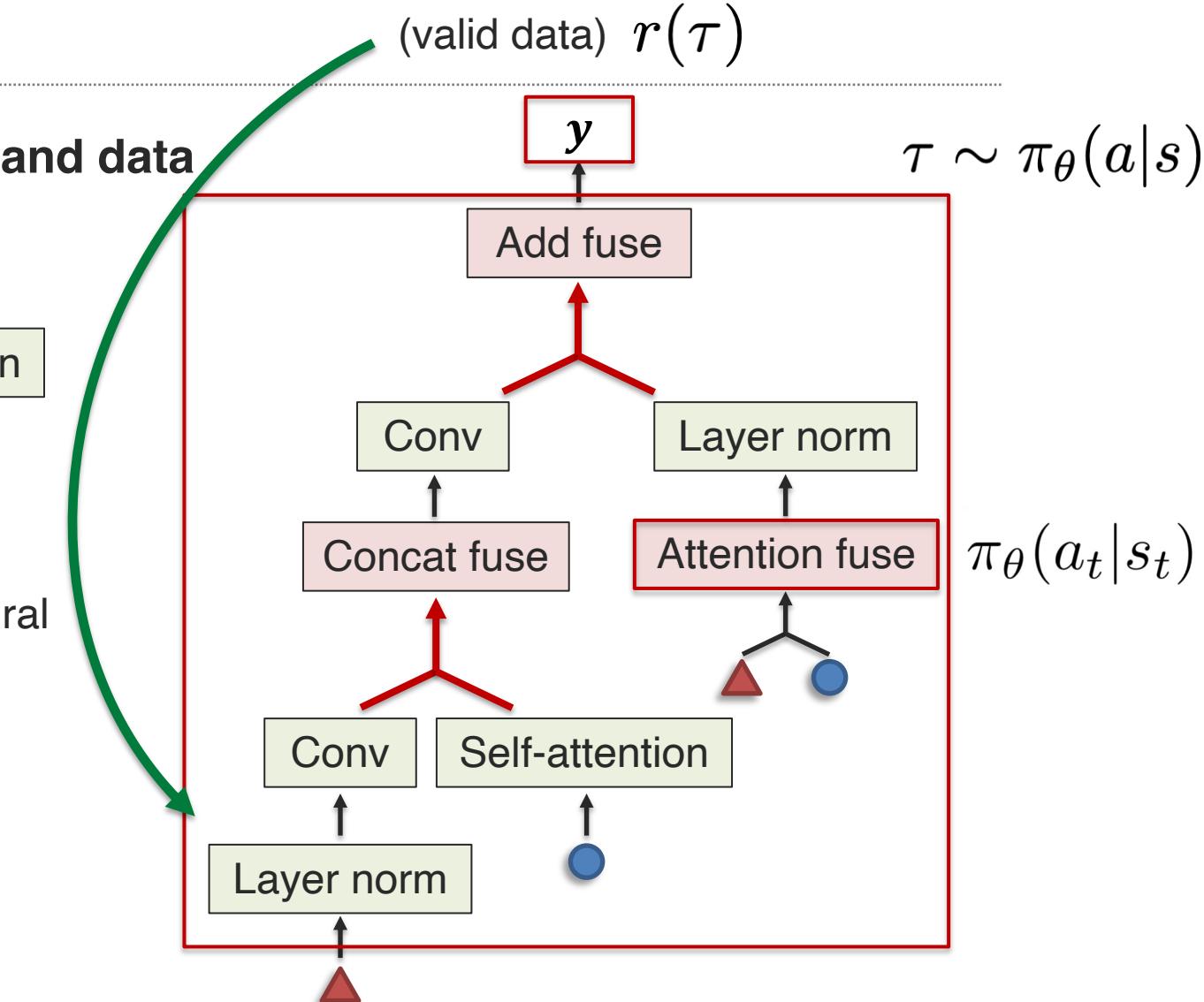
2. Define basic fusion building blocks



3. Automatically search for composition using neural architecture search

$$\nabla_{\theta} J(\theta) \approx \sum_{t \geq 0} r(\tau) \nabla_{\theta} \log \pi_{\theta}(a_t | s_t)$$

Nice, but slow!



[Xu et al., MUFASA: Multimodal Fusion Architecture Search for Electronic Health Records. AAAI 2021]

# Continuous Structure Discovery

Biggest problem: discrete optimization is slow.

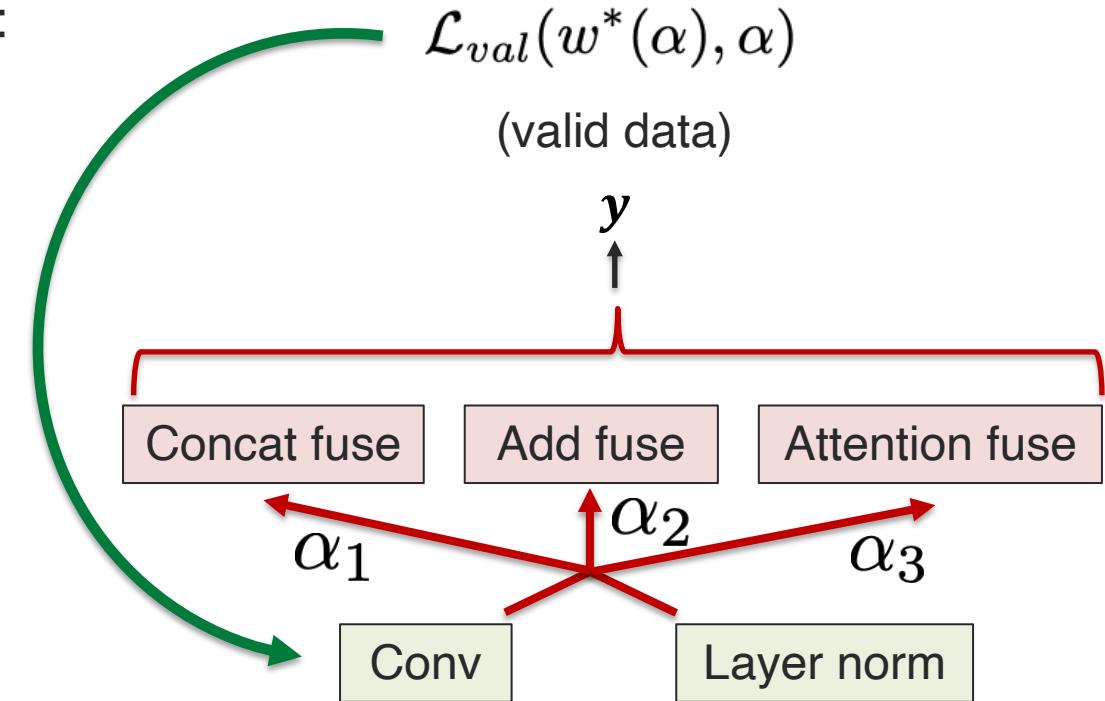
Differentiable optimization for structure learning:

1. Approximate selection with softmax:

$$o'(x) = \sum_i \frac{\exp(\alpha_i)}{\sum_i \exp(\alpha_i)} o_i(x)$$

2. Solve bi-level optimization problem

$$\begin{aligned} \min_{\alpha} \quad & \mathcal{L}_{val}(w^*(\alpha), \alpha) \\ \text{s.t.} \quad & w^*(\alpha) = \operatorname{argmin}_w \mathcal{L}_{train}(w, \alpha) \end{aligned}$$



[Liu et al., DARTS: Differentiable Architecture Search. ICLR 2019]

# Continuous Structure Discovery

Biggest problem: discrete optimization is slow.

Differentiable optimization for structure learning:

1. Approximate selection with softmax:

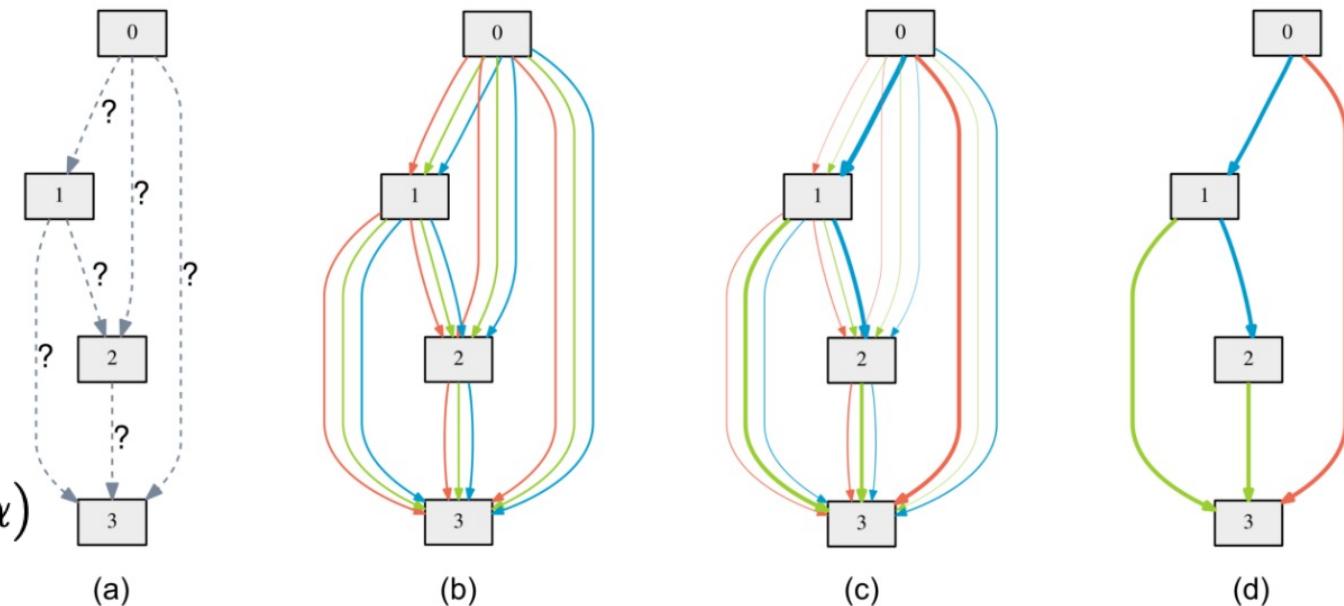
$$o'(x) = \sum_i \frac{\exp(\alpha_i)}{\sum_i \exp(\alpha_i)} o_i(x)$$

2. Solve bi-level optimization problem

$$\min_{\alpha} \mathcal{L}_{val}(w^*(\alpha), \alpha)$$

$$\text{s.t. } w^*(\alpha) = \operatorname{argmin}_w \mathcal{L}_{train}(w, \alpha)$$

3. Convert softmax to argmax



Faster but still non-trivial

[Liu et al., DARTS: Differentiable Architecture Search. ICLR 2019]

# Continuous Structure Discovery

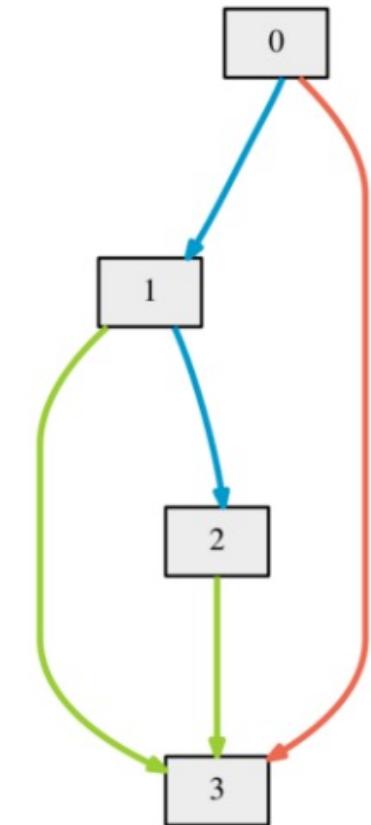
In general, optimization over directed acyclic graphs (DAGs):

Graph  $\mathbf{G}$ , Data  $\mathbf{X}$ , Adjacency matrix  $\mathbf{W}$ :

$$\begin{array}{ll} \min_{\mathbf{W}} \ell(\mathbf{W}; \mathbf{X}) & \iff \\ \text{s.t. } \mathbf{G}(\mathbf{W}) \in \text{DAG} & \min_{\mathbf{W}} \ell(\mathbf{W}; \mathbf{X}) \\ & \text{s.t. } \mathbf{h}(\mathbf{W}) = 0 \end{array}$$

(combinatorial 😱)

(smooth 😎)



(d)

[Zheng et al., DAGs with NO TEARS: Continuous Optimization for Structure Learning. NeurIPS 2018]

# Continuous Structure Discovery

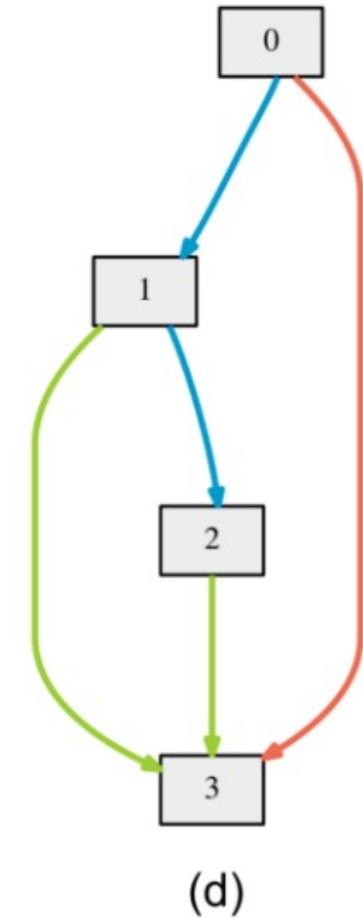
$$\begin{aligned} \min_W \ell(W; X) \\ \text{s.t. } G(W) \in \text{DAG} \end{aligned}$$

?

$$\begin{aligned} \min_W \ell(W; X) \\ \text{s.t. } h(W) = 0 \end{aligned}$$

In [our paper](#), we showed that such a function  $h$  exists,

$$h(W) = \text{tr}(e^{W \circ W}) - d,$$



[Zheng et al., DAGs with NO TEARS: Continuous Optimization for Structure Learning. NeurIPS 2018]

# Continuous Structure Discovery

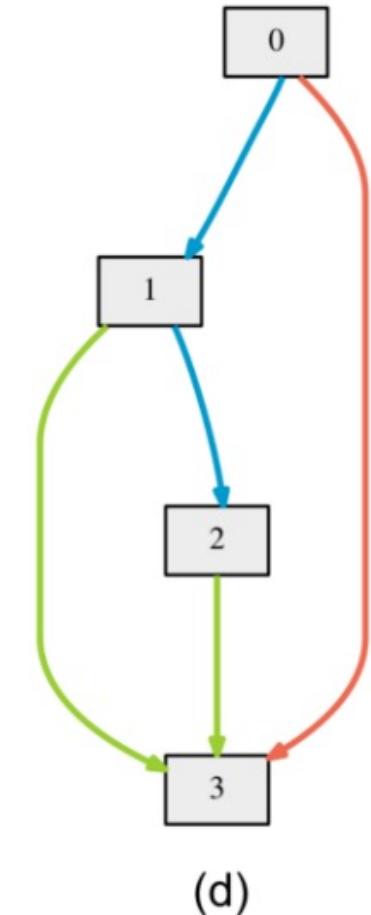
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In [our paper](#), we showed that such a function  $h$  exists,

$$h(W) = \text{tr}(e^{W \circ W}) - d,$$

and that it has a simple gradient:

$$\nabla h(W) = (e^{W \circ W})^T \circ 2W.$$



[Zheng et al., DAGs with NO TEARS: Continuous Optimization for Structure Learning. NeurIPS 2018]

# Continuous Structure Discovery

$$\begin{array}{ll} \min_W \ell(W; X) & \iff \\ \text{s.t. } G(W) \in \text{DAG} & \min_W \ell(W; X) \\ & \text{s.t. } h(W) = 0 \end{array}$$

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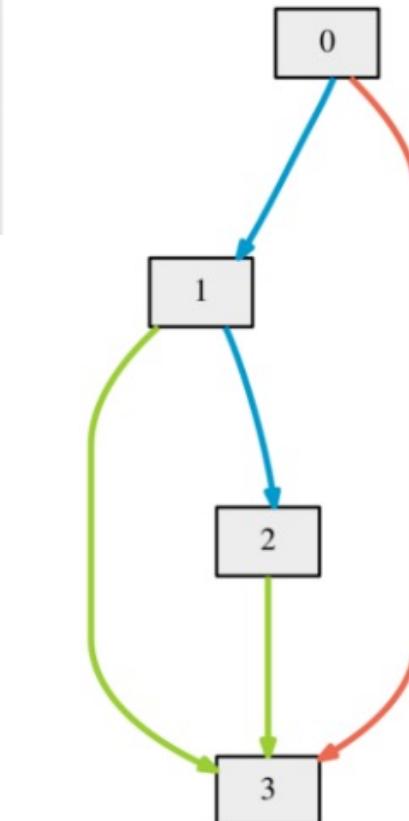
and that it has a simple gradient:

$$\nabla h(W) = (e^{W \circ W})^T \circ 2W.$$

Here the  $\circ$  is the element-wise product,  $d$  is the size of the graph,  $\text{tr}$  is the trace of a matrix, and the matrix exponential is defined as the infinite power series

$$e^A = I + A + \frac{1}{2!}A^2 + \frac{1}{3!}A^3 + \dots \quad (\text{d})$$

[Zheng et al., DAGs with NO TEARS: Continuous Optimization for Structure Learning. NeurIPS 2018]



# Continuous Structure Discovery

$$\begin{aligned} \min_W \ell(W; X) \\ \text{s.t. } G(W) \in \text{DAG} \end{aligned}$$

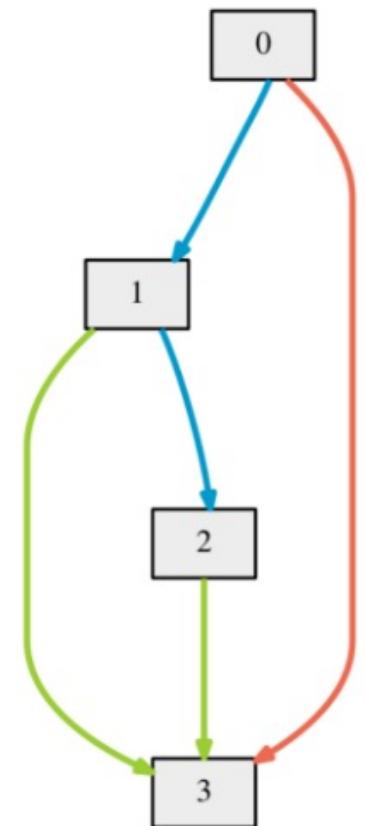
$\Leftrightarrow ?$

$$\begin{aligned} \min_W \ell(W; X) \\ \text{s.t. } h(W) = 0 \end{aligned}$$

$$h(W) = \text{tr}(e^{W \circ W}) - d,$$

$$e^A = I + A + \frac{1}{2!} A^2 + \frac{1}{3!} A^3 + \dots$$

- $K$ -th power of adjacency matrix  $W$  counts the number of  $k$ -step paths from one node to another.
- If the diagonal of the matrix power is all zeros, there are no  $k$ -step cycles.
- Acyclic = check all  $k = 1, 2, \dots, \text{size of graph}$ .

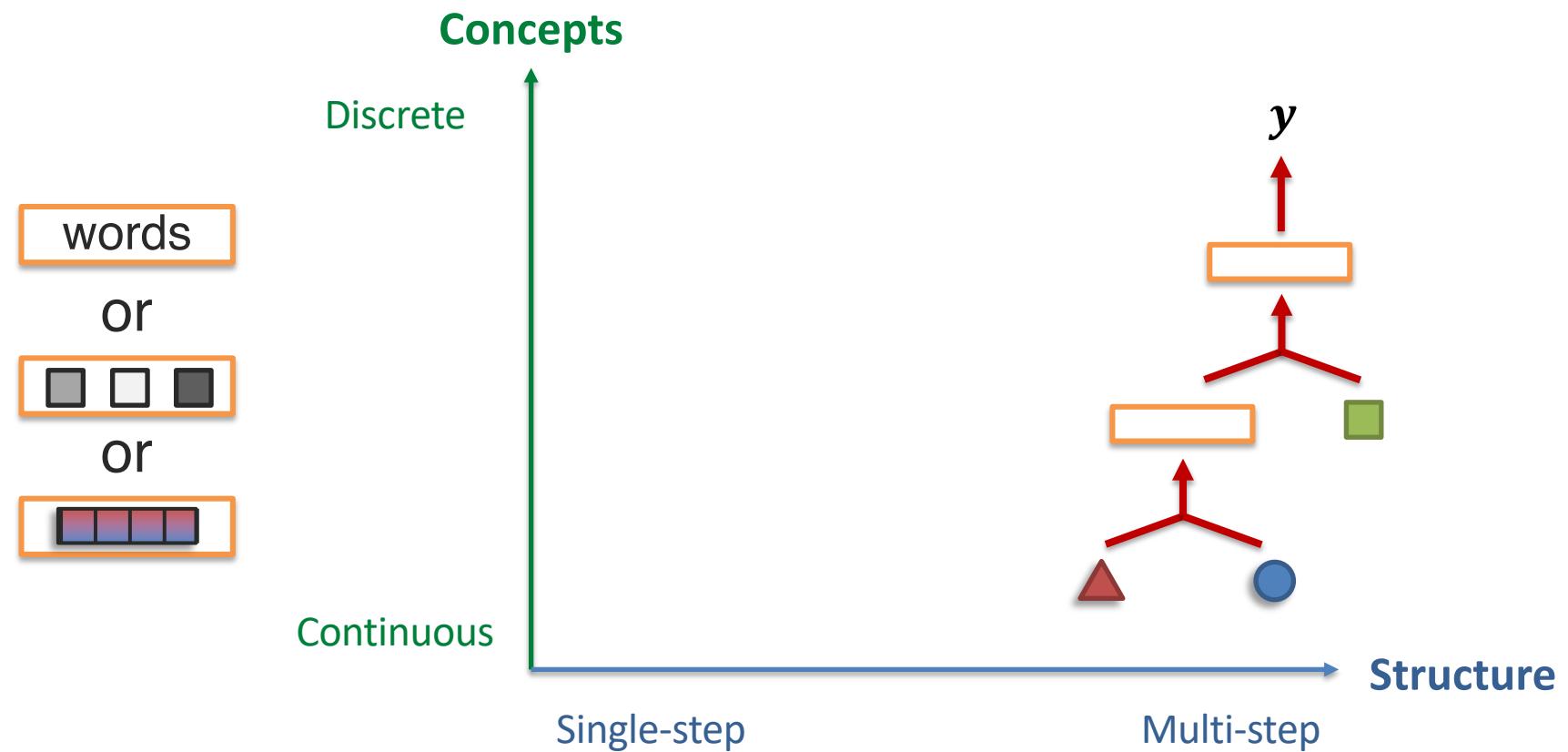


Can now do continuous optimization to solve for  $W$ , but **nonconvex**

[Zheng et al., DAGs with NO TEARS: Continuous Optimization for Structure Learning. NeurIPS 2018]

## Sub-Challenge 3b: Intermediate Concepts

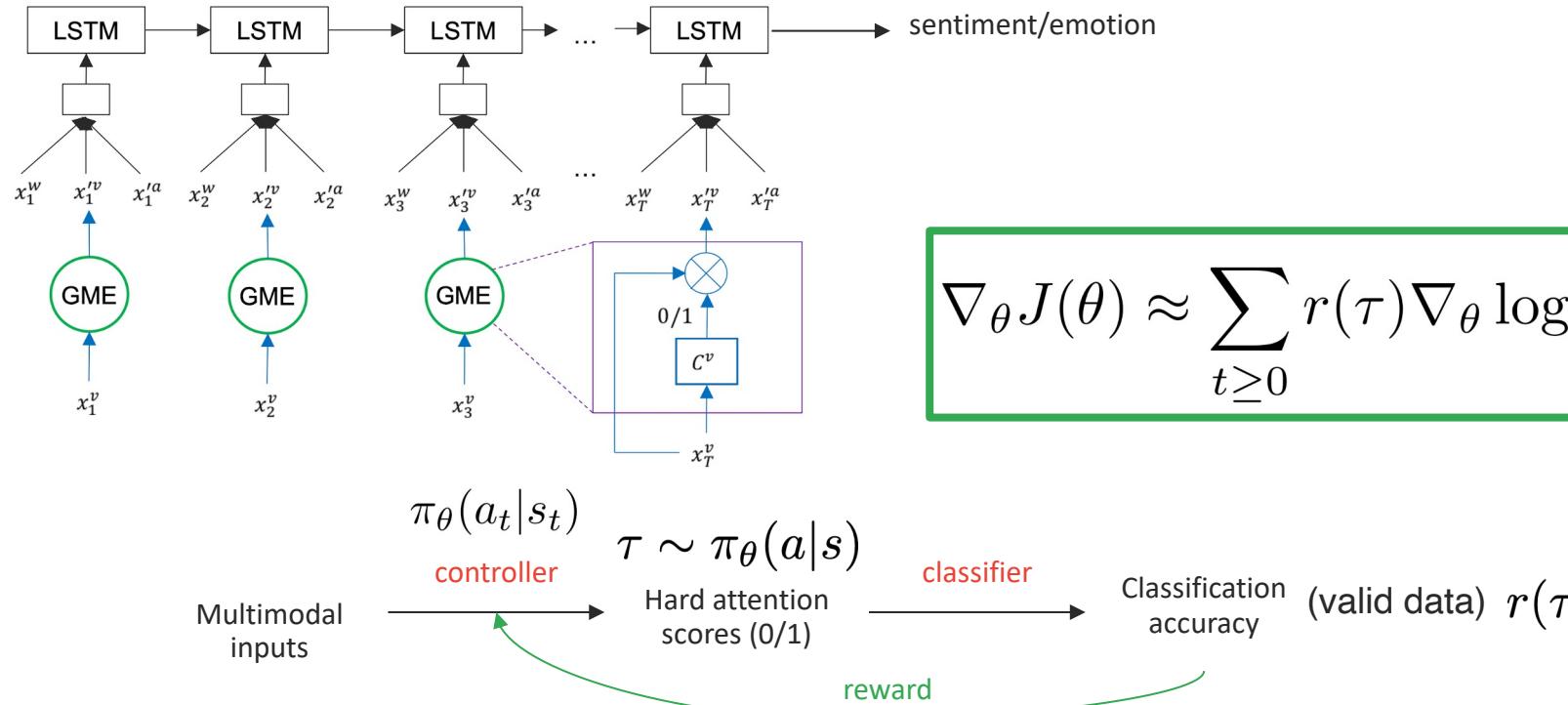
**Definition:** The parameterization of individual multimodal concepts in the reasoning process.



# Discrete Concepts via Hard Attention

Hard attention ‘gates’ (0/1) rather than soft attention (softmax between 0-1)

- Can be seen as discrete layers in between differentiable neural net layers



[Xu et al., Show, Attend and Tell: Neural Image Caption Generation with Visual Attention. ICML 2015]

[Chen et al., Multimodal Sentiment Analysis with Word-level Fusion and Reinforcement Learning. ICMI 2017]

# Discrete Concepts via Hard Attention

Hard attention ‘gates’ (0/1) rather than soft attention (softmax between 0-1)

- Can be seen as discrete layers in between differentiable neural net layers

Sentiment analysis,  
emotion recognition



Reject

Pass

Reject

Image captioning

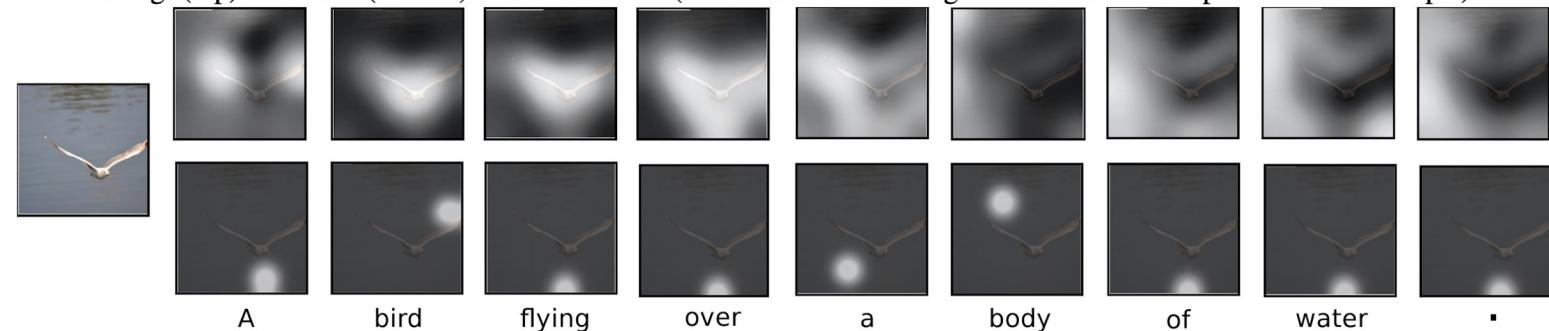


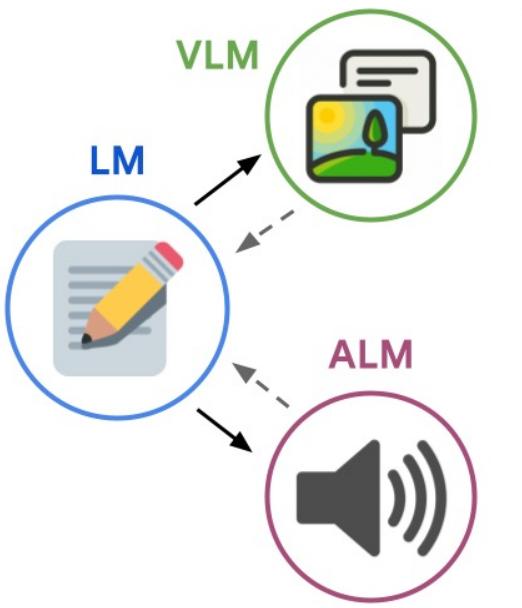
Figure 3. Visualization of the attention for each generated word. The rough visualizations obtained by upsampling the attention weights and smoothing. (top) “soft” and (bottom) “hard” attention (note that both models generated the same captions in this example).

[Xu et al., Show, Attend and Tell: Neural Image Caption Generation with Visual Attention. ICML 2015]

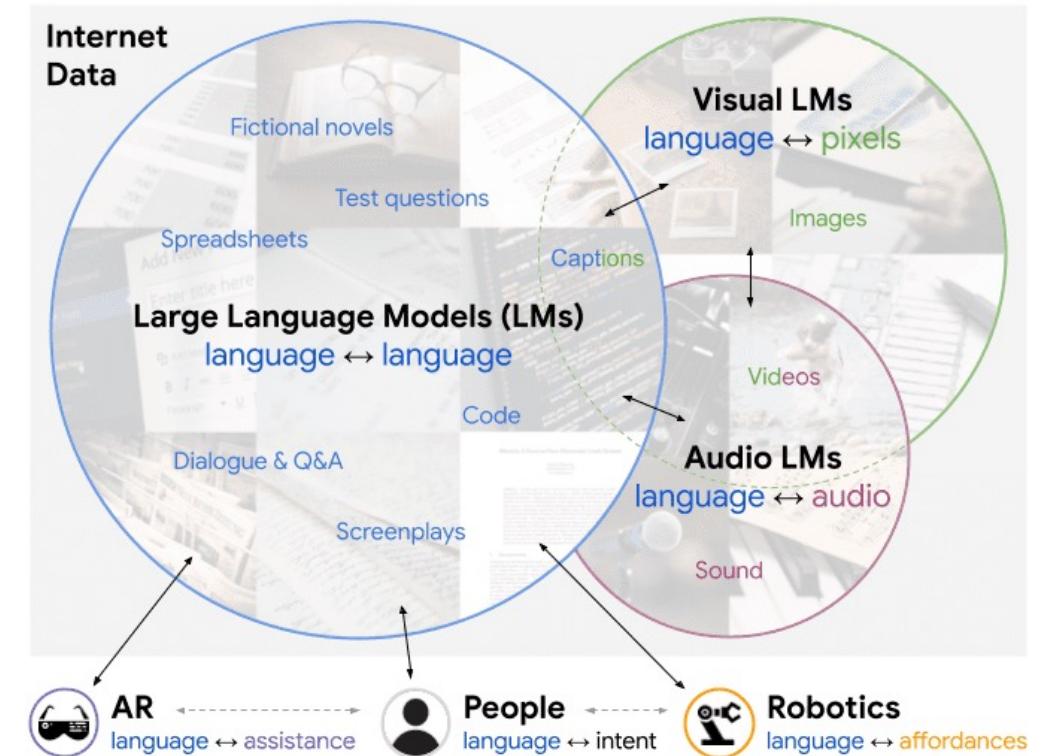
[Chen et al., Multimodal Sentiment Analysis with Word-level Fusion and Reinforcement Learning. ICMI 2017]

# Discrete Concepts via Language

- Large language/video/audio models interacting with each other
- Each language model has its own distinct *domain knowledge*
- Interaction is scripted and zero-shot



- language ↔ language
- language-represented visual or audio entities
- ←--- similarity → language
- language-represented visual entities → similarity
- language-represented audio entities → similarity



Guided multimodal discussion

Combining domain knowledge

[Zeng et al., Socratic Models: Composing Zero-Shot Multimodal Reasoning with Language. arXiv 2022]

# Discrete Concepts via Language

---

Image captioning

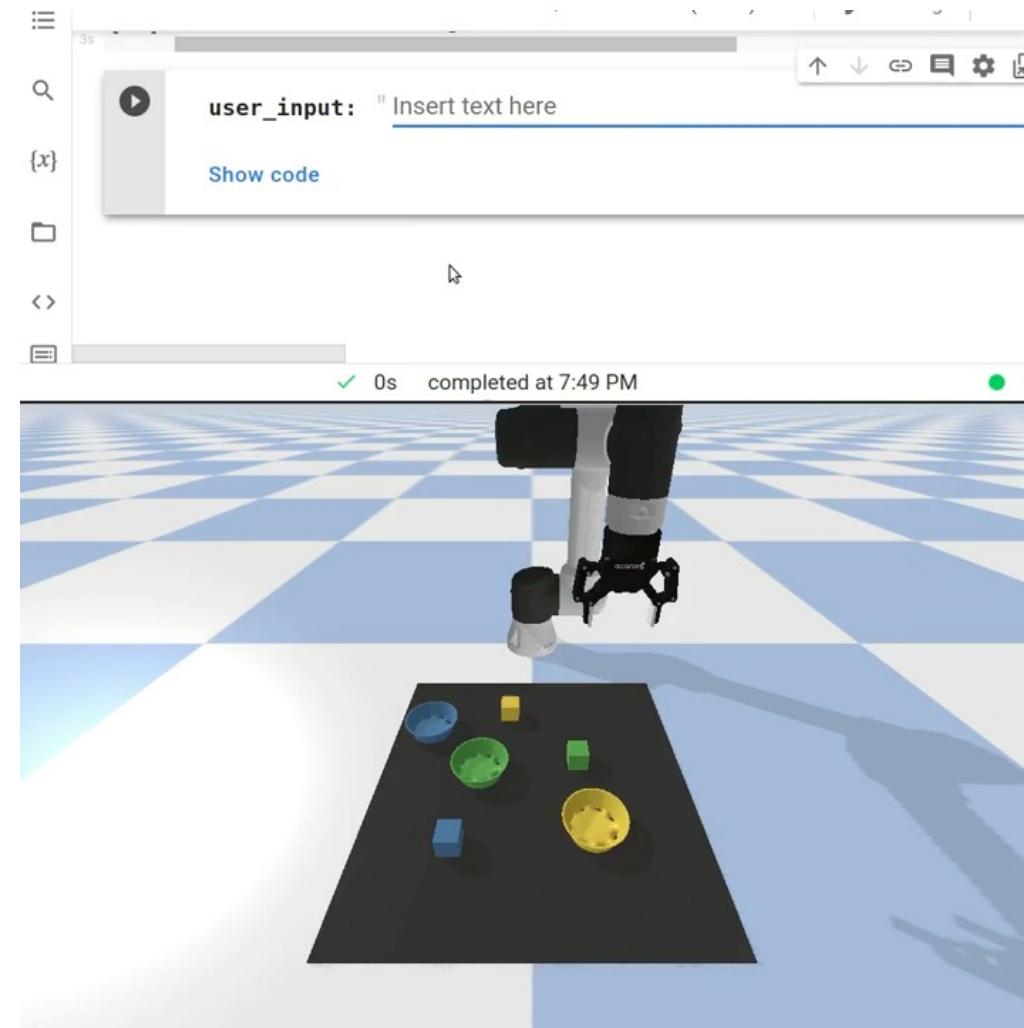


Zero-Shot  
Socratic  
Internet  
Image  
Captioning

[Zeng et al., Socratic Models: Composing Zero-Shot Multimodal Reasoning with Language. arXiv 2022]

# Discrete Concepts via Language

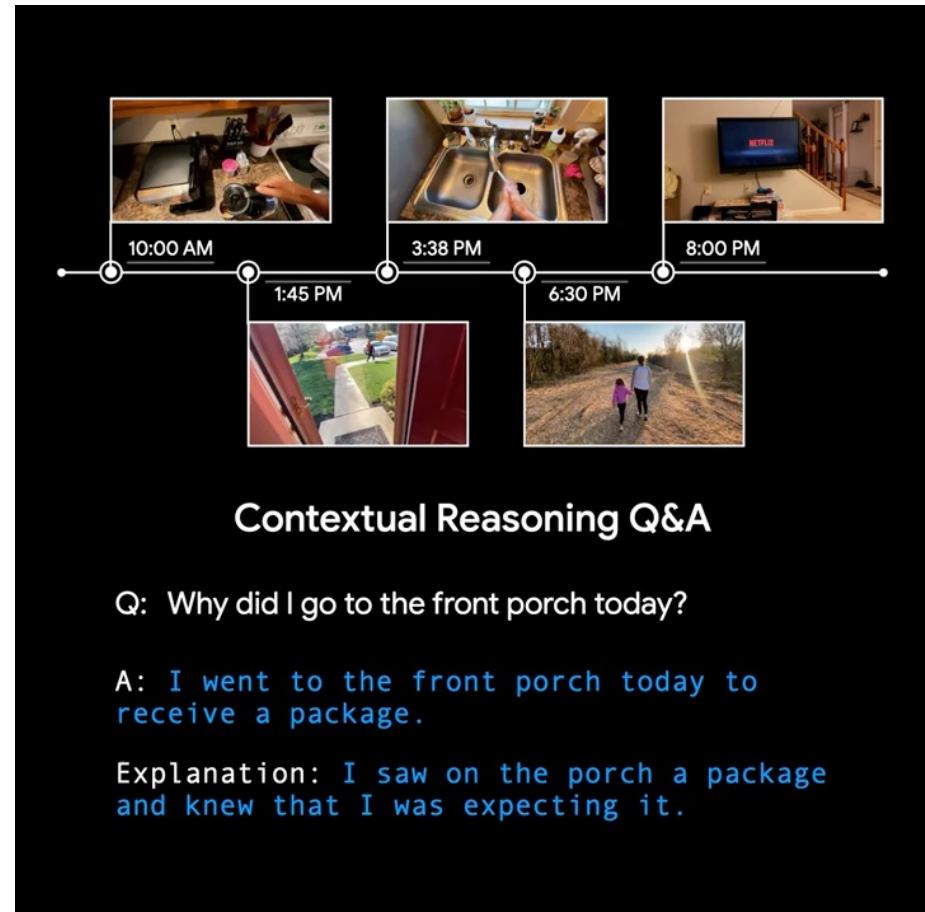
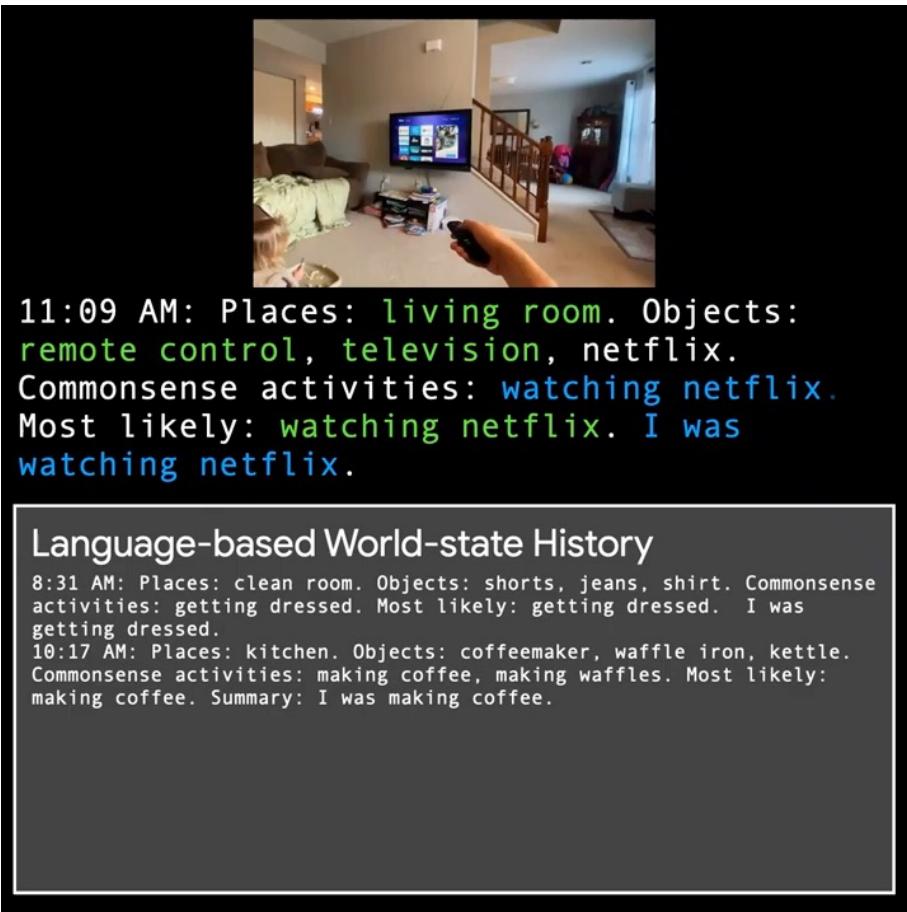
Robot perception and planning



[Zeng et al., Socratic Models: Composing Zero-Shot Multimodal Reasoning with Language. arXiv 2022]

# Discrete Concepts via Language

## Video reasoning



[Zeng et al., Socratic Models: Composing Zero-Shot Multimodal Reasoning with Language. arXiv 2022]

## Sub-Challenge 3b: Intermediate Concepts



Many open directions

Prompt engineering – what is going on???

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### Pre-train, Prompt, and Predict: A Systematic Survey of Prompting Methods in Natural Language Processing

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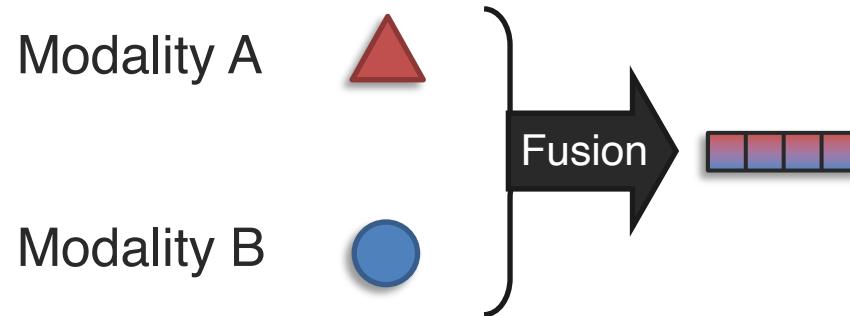
We'll see more of this in transference

[Liu et al., Pre-train, Prompt, and Predict: A Systematic Survey of Prompting Methods in Natural Language Processing. arXiv 2021]

## Sub-Challenge 3c: Inference Paradigm

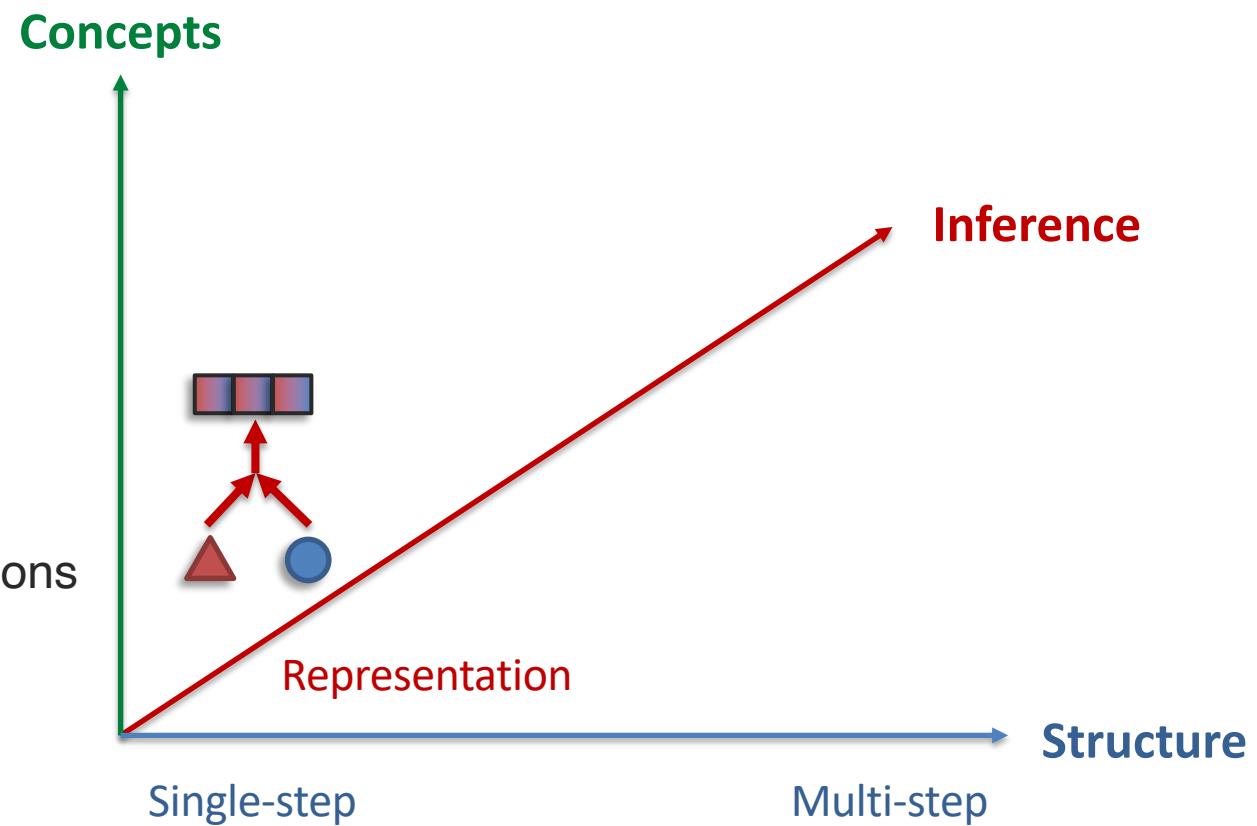
**Definition:** How increasingly abstract concepts are inferred from individual multimodal evidences.

Recall representation fusion:



**Potential issues:**

- Models may capture spurious correlations
- Not robust to targeted manipulations
- Lack of interpretability/control

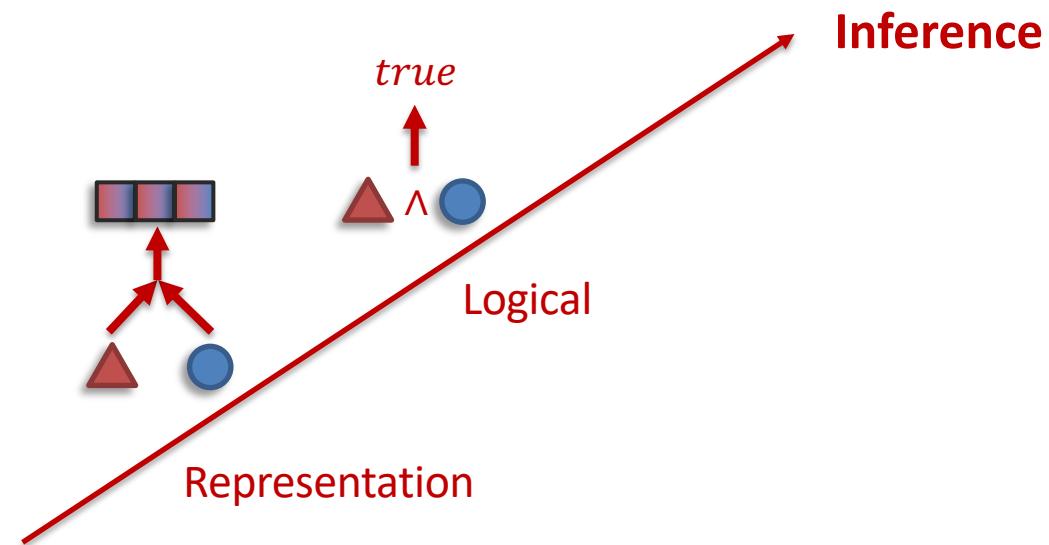


## Sub-Challenge 3c: Inference Paradigm

**Definition:** How increasingly abstract concepts are inferred from individual multimodal evidences.

**Towards explicit inference paradigms:**

1. Logical inference: given premises inferred from multimodal evidence, how can one derive **logical** conclusions?



# Logical Inference

Recall error analysis!

## Inference through logical operators in question



*Is there beer AND is there a  
WINE GLASS?*

*Is the man NOT wearing  
shoes AND is there beer?*

*Is there beer?*

*Is the man wearing shoes?*

Adversarial antonyms

**X**

Logical connectives

**X**

Basic premises

**✓**

Existing models struggle to capture logical connectives.  
How can we make them more logical?

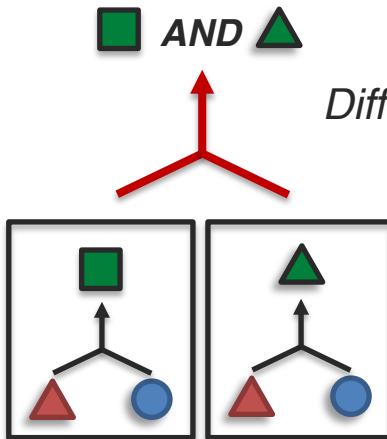
[Gokhale et al., VQA-LOL: Visual Question Answering Under the Lens of Logic. ECCV 2020]

# Logical Inference

Inference through logical operators in question



*Are they in a restaurant **AND** are they all boys?*



*Differentiable **AND** composition operator!*



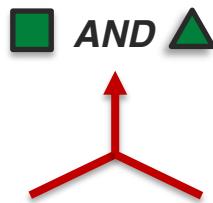
*Are they in a restaurant?*

*Are they all boys?*

*Also applies to other logic connectives:  
**AND, OR, NOT***

# Soft Logical Operators

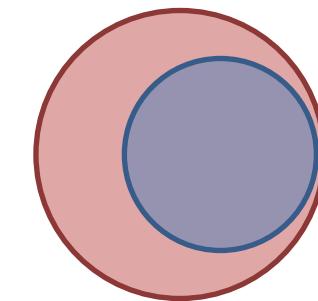
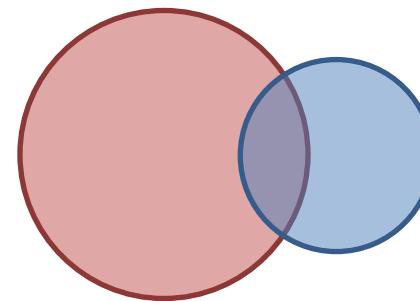
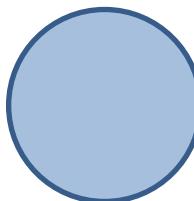
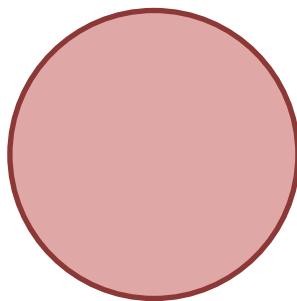
Inference through logical operators in question



*Differentiable AND composition operator!*

Fréchet inequalities:

$$\max(0, p(A_1) + p(A_2) - 1) \leq p(A_1 \wedge A_2) \leq \min(p(A_1), p(A_2)).$$



$$p(A_1 \wedge A_2) = p(A_1) + p(A_2) - p(A_1 \vee A_2)$$

$$p(A_1 \vee A_2) \leq 1$$

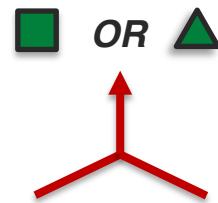
$$p(A_1 \wedge A_2) \geq p(A_1) + p(A_2) - 1$$

[Gokhale et al., VQA-LOL: Visual Question Answering Under the Lens of Logic. ECCV 2020]

# Soft Logical Operators

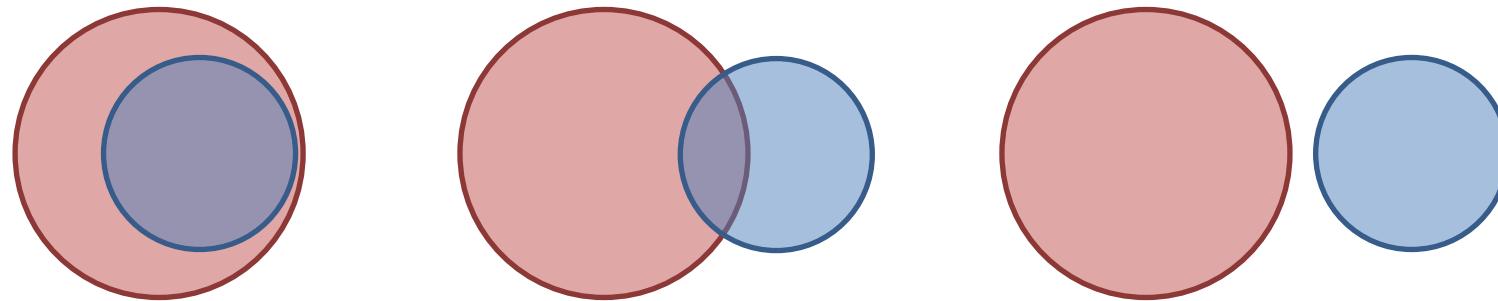
Inference through logical operators in question

Fréchet inequalities:



*Differentiable **OR** composition operator!*

$$\max(0, p(A_1) + p(A_2) - 1) \leq p(A_1 \wedge A_2) \leq \min(p(A_1), p(A_2)).$$



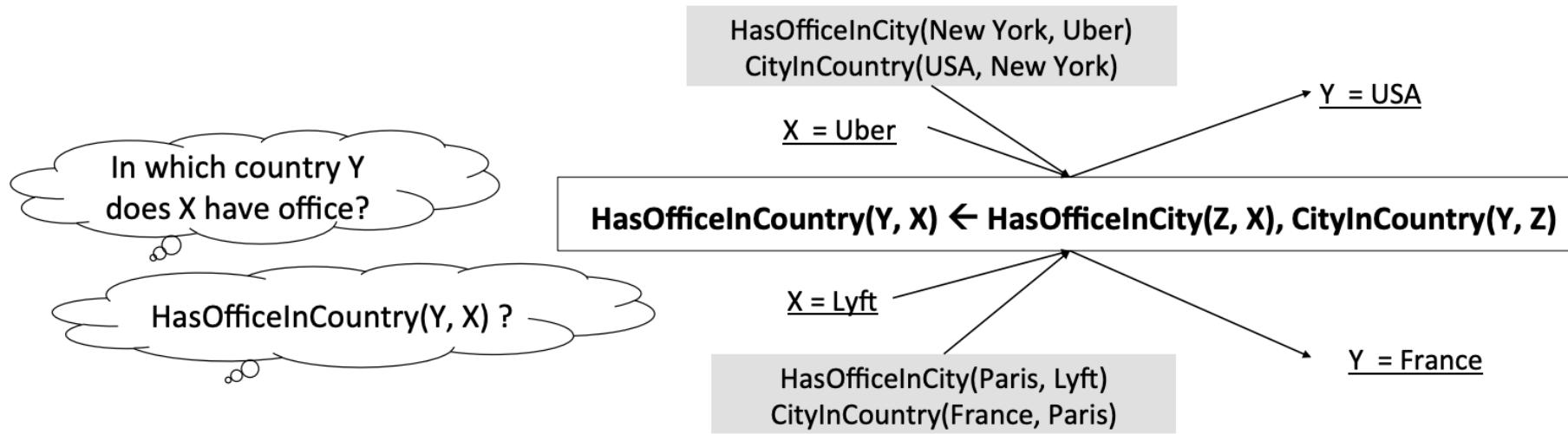
Differentiable, so you can now optimize wrt  $p(A_1 \vee A_2)$  and  $p(A_1 \wedge A_2)$

[Gokhale et al., VQA-LOL: Visual Question Answering Under the Lens of Logic. ECCV 2020]

# Logical Inference Challenges

Open challenges

Many open directions



Differentiable knowledge base reasoning

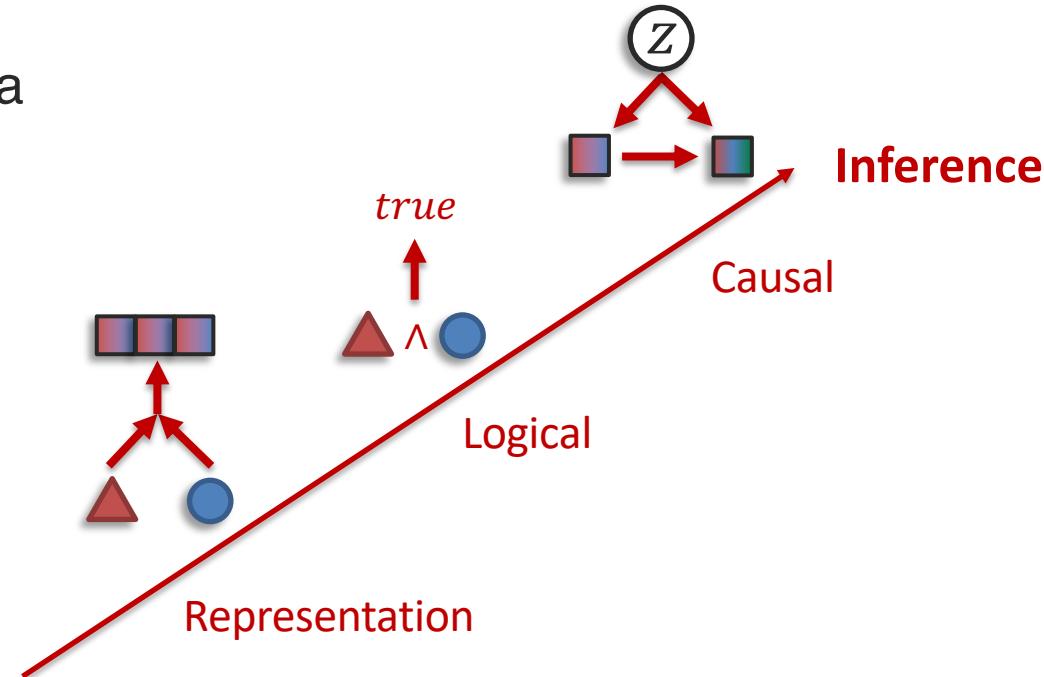
[Yang et al., Differentiable Learning of Logical Rules for Knowledge Base Reasoning. NeurIPS 2017]

## Sub-Challenge 3c: Inference Paradigm

**Definition:** How increasingly abstract concepts are inferred from individual multimodal evidences.

**Towards explicit inference paradigms:**

1. Logical inference
2. Causal inference: how can one determine the actual **causal** effect of a variable in a larger system?



# Causal Inference

---

## Association vs causation

**Example:** How does class size impact student outcomes?

Why can't we just compare student outcomes among different class sizes?

- Poorer districts may have larger class sizes.
- Students in poorer districts may have access to fewer resources, more difficult family circumstances, etc.
- All of these factors may impact student outcomes.

Association describes how things are. Causation describes how things would have been under different circumstances.

(side note: correlation is a specific type of linear association)

[Slides from Victoria Lin]



Language Technologies Institute

# Causal Inference

---

## Association vs causation

### Simple linear regression

Consider the simple linear regression model

$$Y = \beta_0 + \beta_1 X_1 + \dots + \beta_p X_p + \epsilon$$

[Slides from Victoria Lin]



# Causal Inference

---

## Association vs causation

### Simple linear regression

Consider the simple linear regression model

$$Y = \beta_0 + \beta_1 X_1 + \dots + \beta_p X_p + \epsilon$$

How do we interpret the coefficient  $\beta_1$ ?

- Commonly: The expected change in outcome  $Y$  if covariate  $X_1$  were increased by one, holding all other covariates constant
- Correctly: The expected difference in outcome for two data points who *happen to have* the same covariate values for  $(X_2, \dots, X_p)$  and whose values for  $X_1$  *happen to differ* by one

*The first interpretation is in fact causal and requires extra assumptions!*

[Slides from Victoria Lin]



Language Technologies Institute

# Causal Inference

---

## Intervention

Causal inference is reliant on the idea of interventions —what outcome might have occurred if X happened (an intervention), possibly contrary to observed data.

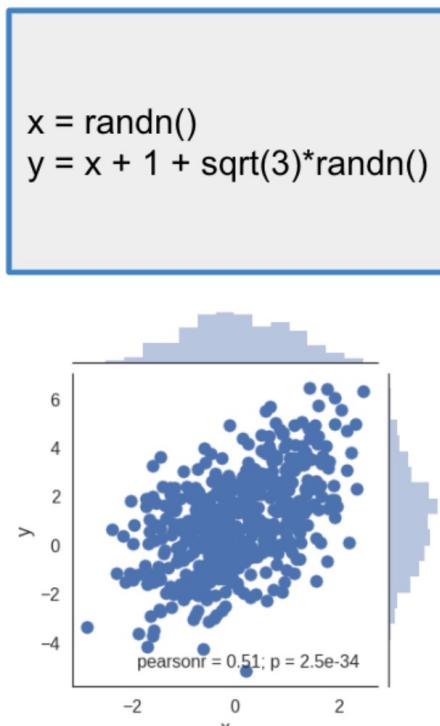
[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

---

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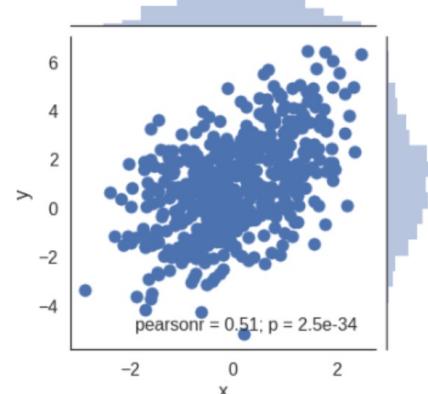
[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

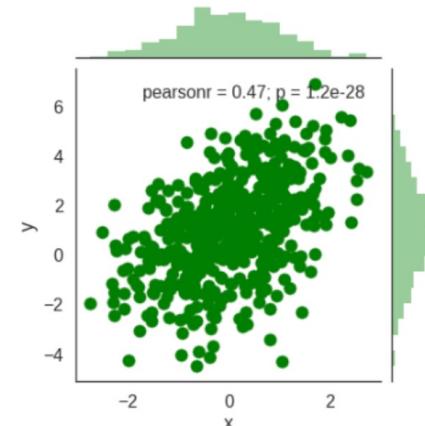
## Intervention

Causal inference is reliant on the idea of interventions —what outcome might have occurred if X happened (an intervention), possibly contrary to observed data.

```
x = randn()
y = x + 1 + sqrt(3)*randn()
```



```
y = 1 + 2*randn()
x = (y-1)/4 + sqrt(3)*randn()/2
```



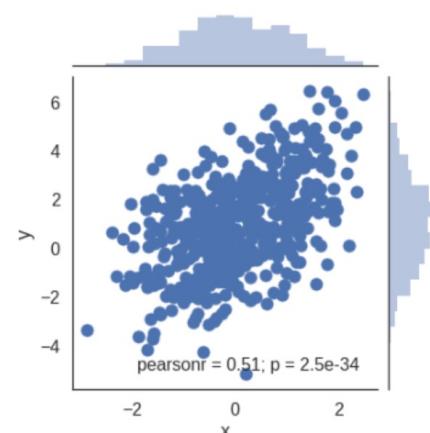
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# Causal Inference

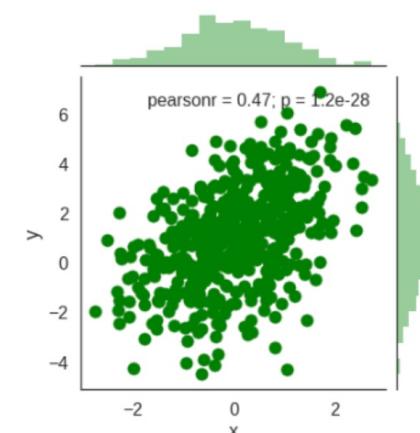
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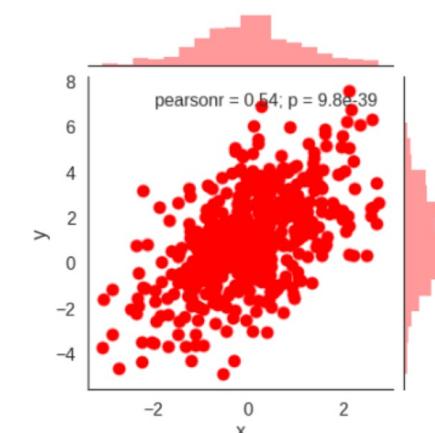
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y = x + 1 + sqrt(3)*randn()
```



```
y = 1 + 2*randn()
x = (y-1)/4 + sqrt(3)*randn()/2
```



```
z = randn()
y = z + 1 + sqrt(3)*randn()
x = z
```



[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

---

## Intervention

Let's say I really want to set the value of  $x$  to 3.

```
x = randn()  
x = 3  
y = x + 1 + sqrt(3)*randn()  
x = 3
```

```
y = 1 + 2*randn()  
x = 3  
x = (y-1)/4 + sqrt(3)*randn()/2  
x = 3
```

```
z = randn()  
x = 3  
x = z  
x = 3  
y = z + 1 + sqrt(3)*randn()  
x = 3
```

[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

## Intervention

Let's say I really want to set the value of  $x$  to 3. What happens to  $y$ ?

```
x = randn()
```

```
x = 3
```

```
y = x + 1 + sqrt(3)*randn()
```

```
x = 3
```

```
y = 1 + 2*randn()
```

```
x = 3
```

```
x = (y-1)/4 + sqrt(3)*randn()/2
```

```
x = 3
```

```
z = randn()
```

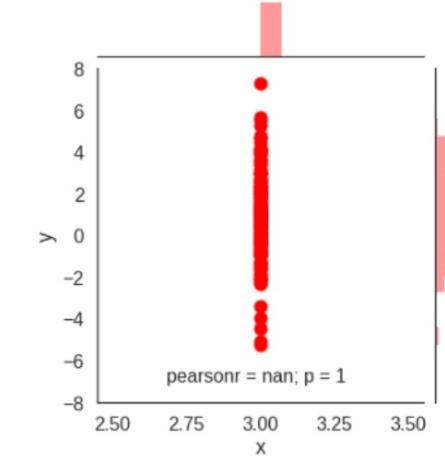
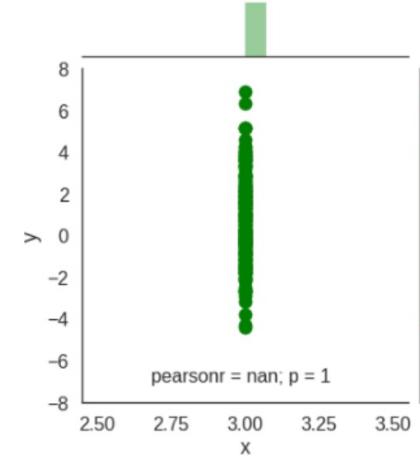
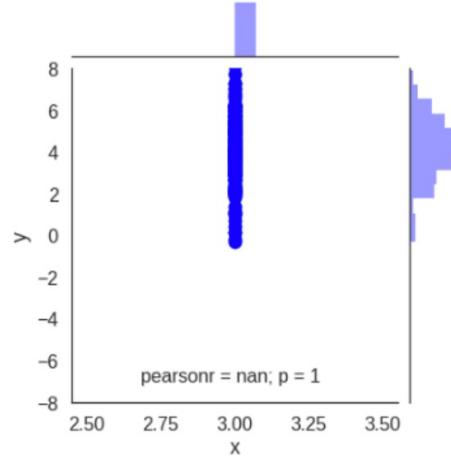
```
x = 3
```

```
x = z
```

```
x = 3
```

```
y = z + 1 + sqrt(3)*randn()
```

```
x = 3
```

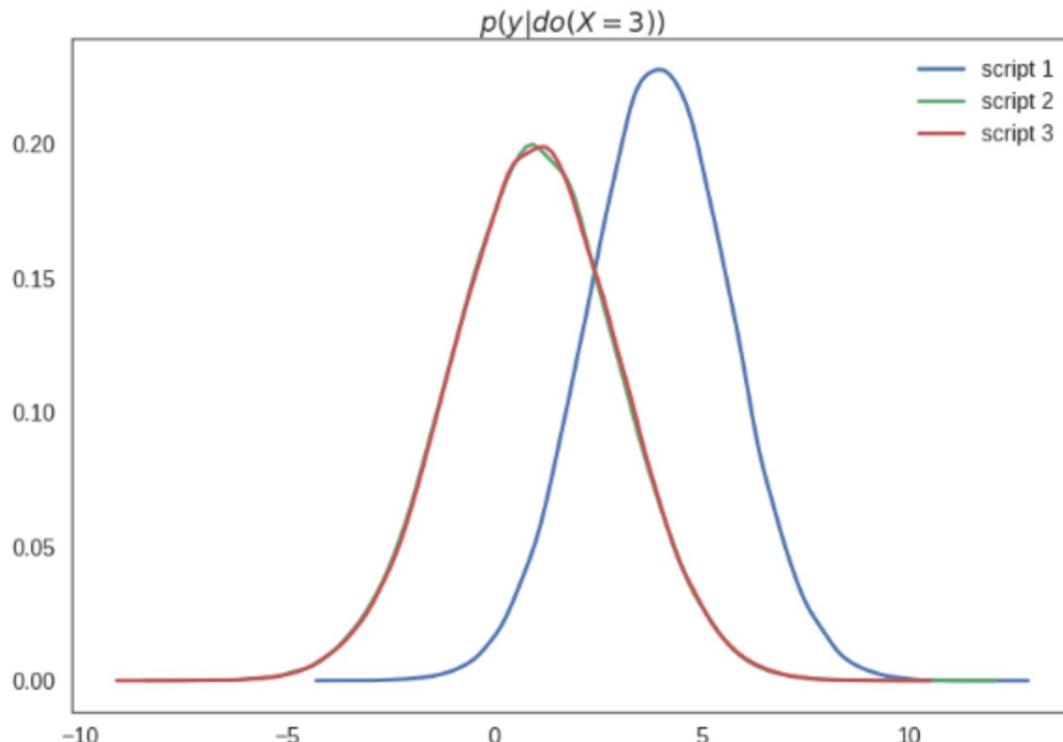


[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

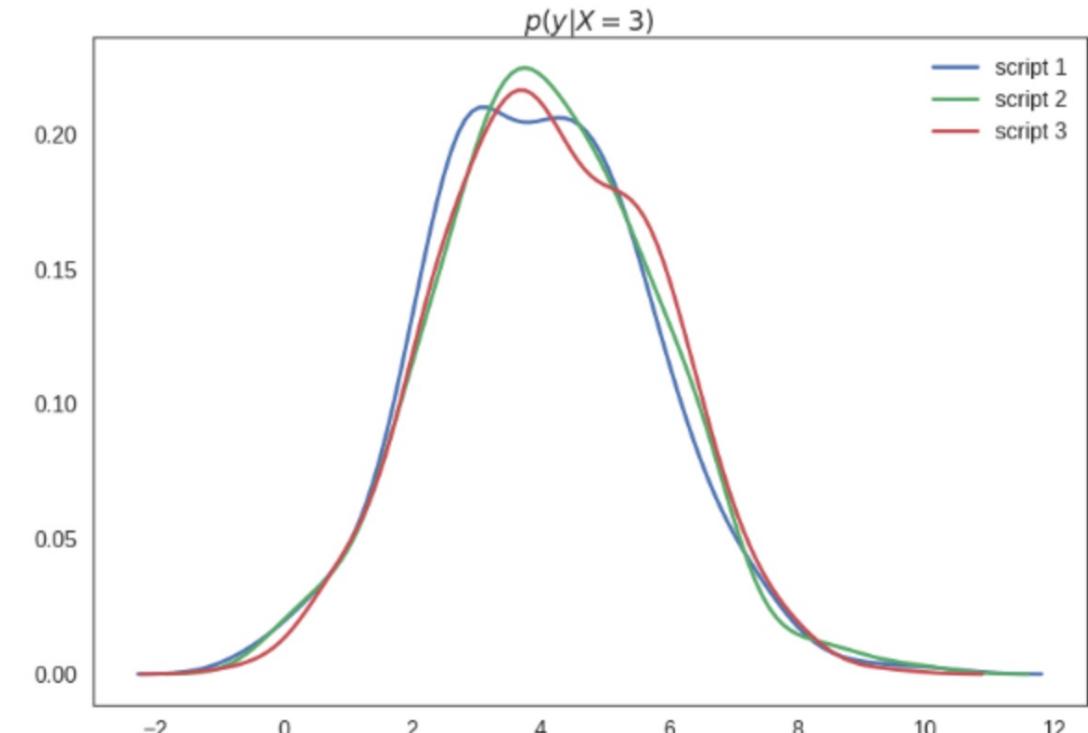
# Causal Inference

## Intervention

The marginal distribution of  $y$ :  $p(y | \text{do}(x=3))$ .



The marginal distribution of  $y$ :  $p(y | x=3)$ .



The joint distribution of data alone is insufficient to predict behavior under interventions.

[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

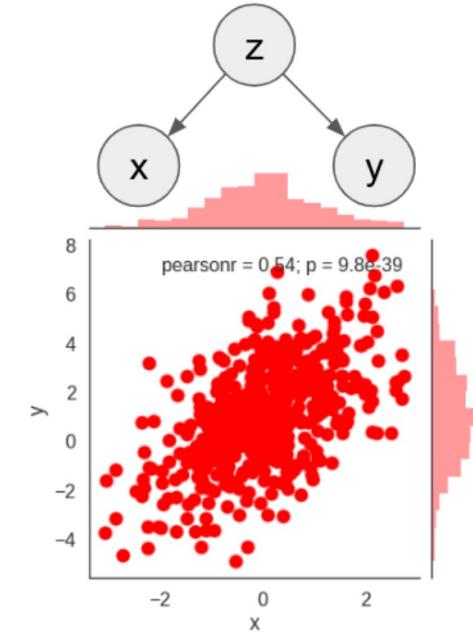
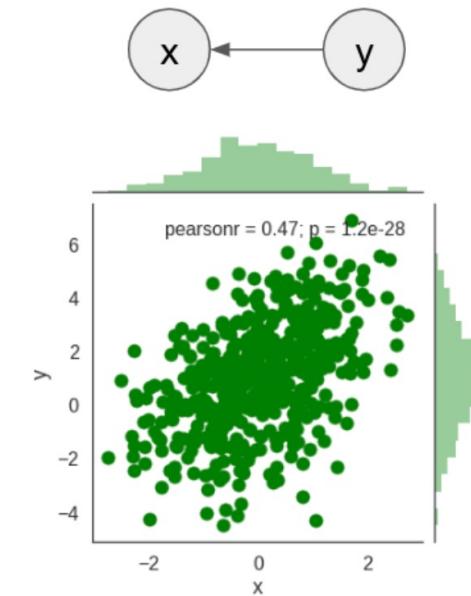
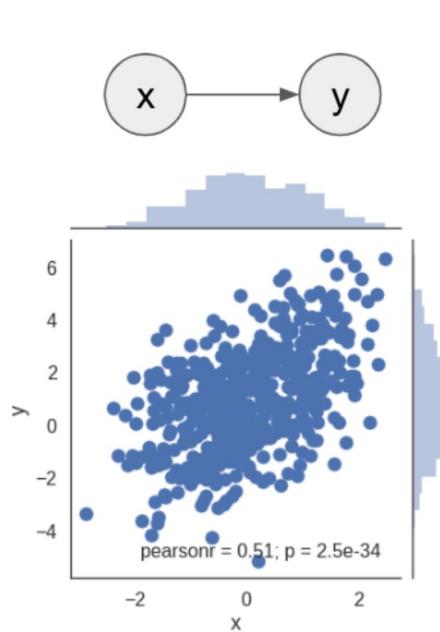
# Causal Inference

Causal diagrams: arrow pointing from cause to effect.

```
x = randn()  
y = x + 1 + sqrt(3)*randn()
```

```
y = 1 + 2*randn()  
x = (y-1)/4 + sqrt(3)*randn()/2
```

```
z = randn()  
y = z + 1 + sqrt(3)*randn()  
x = z
```

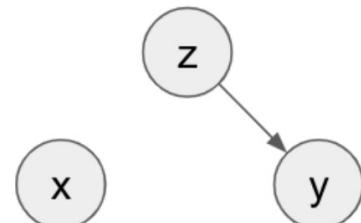
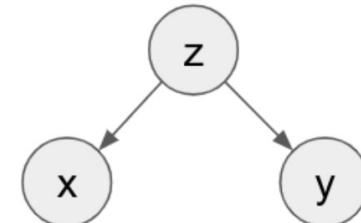


[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

---

**Intervention** mutilates the graph by removing all edges that point into the variable on which intervention is applied (in this case  $x$ ).



$$P(y|do(X)) = p(y|x)$$

$$P(y|do(X)) = p(y)$$

$$P(y|do(X)) = p(y)$$

[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

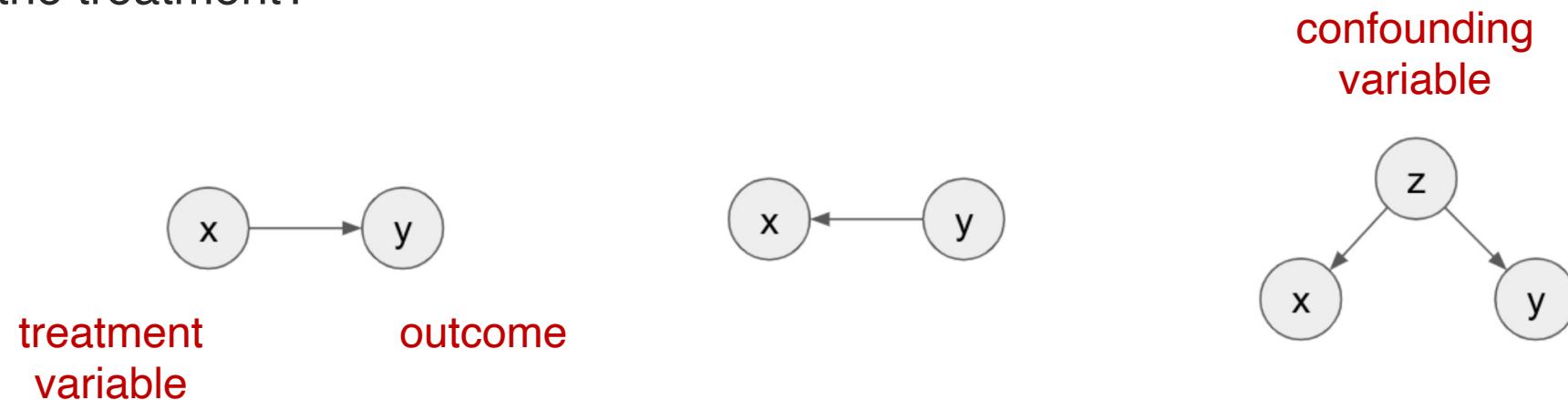
# Causal Inference

Intervention in real-life is typically very hard!

E.g., does treatment x treat disease y?

Can I estimate the intervention  $p(y|do(X=x))$ ?

Requires answering: all else being equal, what would be the patient's outcome if they had not taken the treatment?



Lots of work, see Judea Pearl, *The Book of Why*

[Example from Ferenc Huszár: <https://www.inference.vc/causal-inference-2-illustrating-interventions-in-a-toy-example/>]

# Causal Inference

---

**Causal VQA: does my multimodal model capture causation or correlation?**

## Covariant VQA

Target object in question

Q: How many zebras are there in the picture?

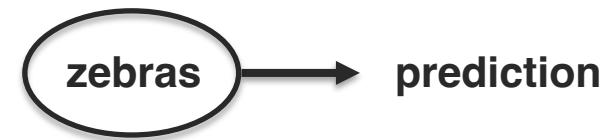
A: 2



Baselines:

**2**

i.e., treatment  
variable



BUT: correlation or causation?

[Agarwal et al., Towards Causal VQA: Revealing & Reducing Spurious Correlations by Invariant & Covariant Semantic Editing. CVPR 2020]

# Causal Inference

Recall error analysis!

## Causal VQA: does my multimodal model capture causation or correlation?

### Covariant VQA

Target object in question

Q: How many zebras are there in the picture?

A: 2

*zebra removed* A: 1

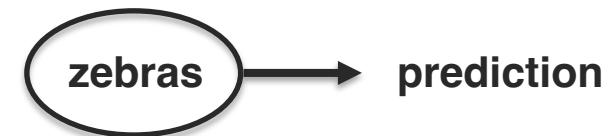


Baselines:

2

2

i.e., treatment variable



Interventional conditional:  $p(y|do(zebras = 1))$

Existing models struggle to adapt to targeted causal interventions.  
How can we make them more robust to spurious correlations?

# Causal Inference

**Causal VQA: does my multimodal model capture causation or correlation?**

## Invariant VQA

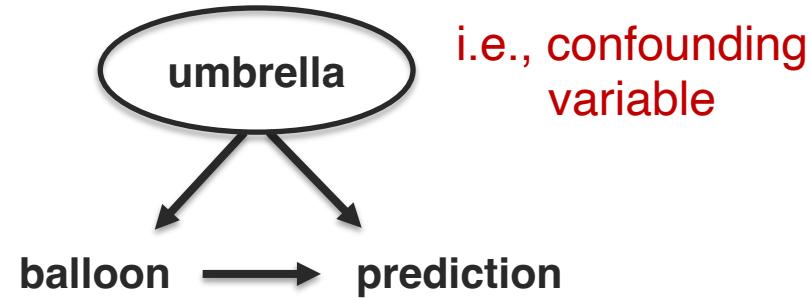
Target irrelevant object

Q: What color is the balloon?

A: red



Baselines: **pink**



Is my model picking up irrelevant objects?

[Agarwal et al., Towards Causal VQA: Revealing & Reducing Spurious Correlations by Invariant & Covariant Semantic Editing. CVPR 2020]

# Causal Inference

Recall error analysis!

Causal VQA: does my multimodal model capture causation or correlation?

## Invariant VQA

Target irrelevant object

Q: What color is the balloon?

A: red

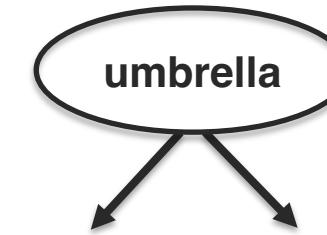
*umbrellas removed*; A: red



Baselines:

**pink**

**red**



i.e., confounding variable

balloon → prediction

Interventional conditional:  $p(y|do(\text{no umbrella}))$

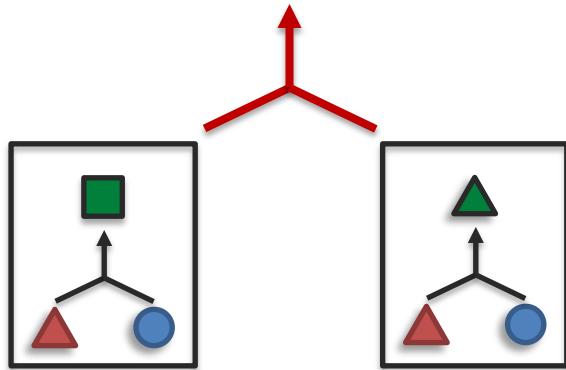
Existing models struggle to adapt to targeted causal interventions.  
How can we make them more robust to spurious correlations?

[Agarwal et al., Towards Causal VQA: Revealing & Reducing Spurious Correlations by Invariant & Covariant Semantic Editing. CVPR 2020]

# Causal Inference

## Causal inference via data augmentation

**Covariance**  
(targeted changes to answer)



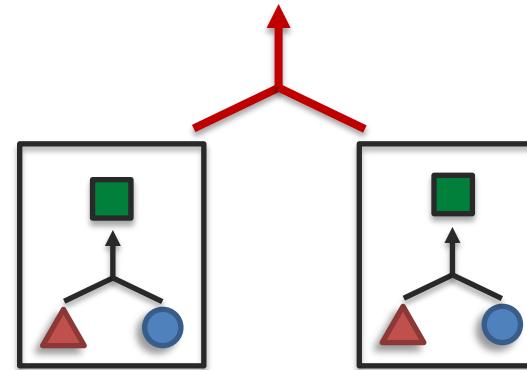
Q: How many zebras are there in the picture?  
A: 2      *zebra removed* A: 1



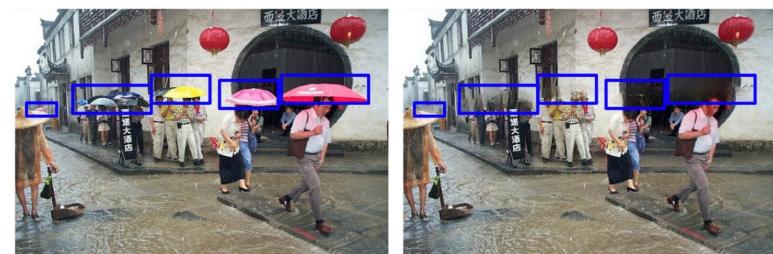
With  
relevant object

Without  
relevant object

**Invariance**  
(answer stays the same)



Q: What color is the balloon?  
A: red      *umbrellas removed*; A: red



With  
irrelevant object

Without  
irrelevant object

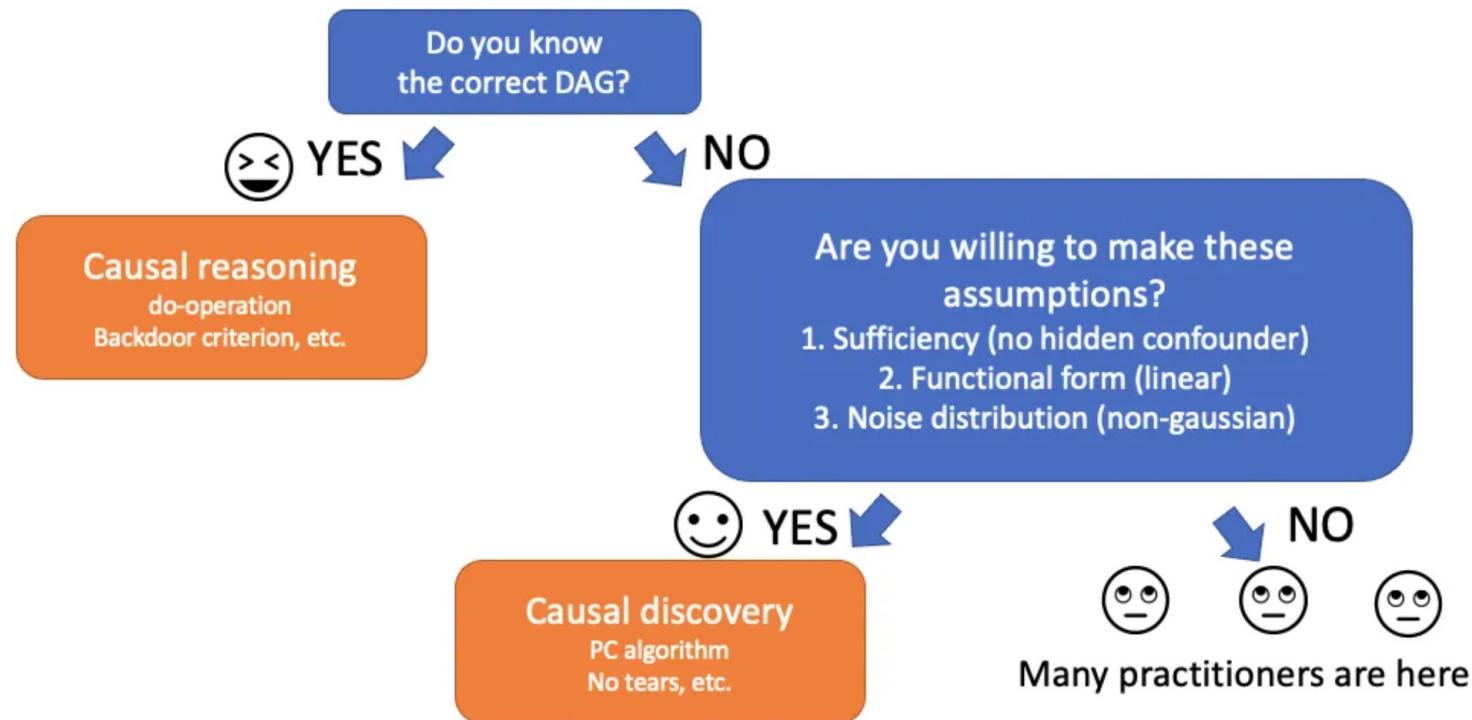
[Agarwal et al., Towards Causal VQA: Revealing & Reducing Spurious Correlations by Invariant & Covariant Semantic Editing. CVPR 2020]

# Causal Inference Challenges

Open challenges

Many open directions

## Application of causality – current state

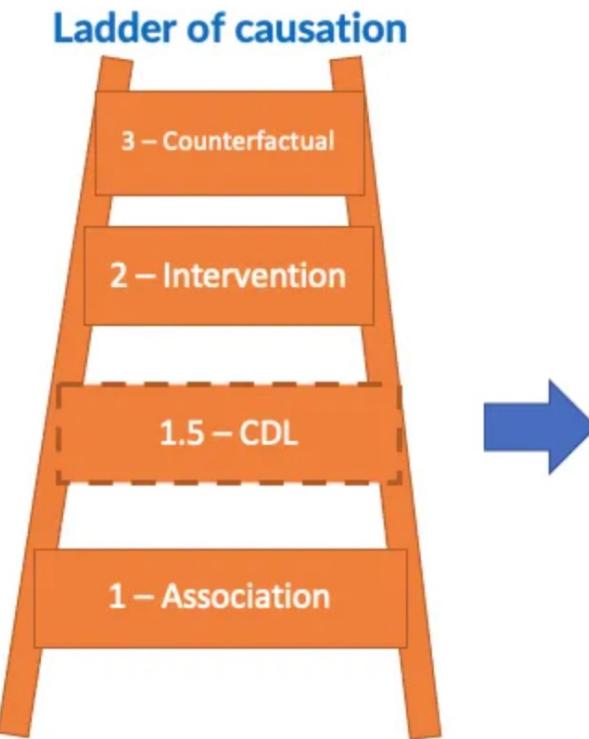


Causal deep learning, see <https://www.vanderschaar-lab.com/causal-deep-learning/>

# Causal Inference Challenges

Open challenges

Many open directions



The space between association and intervention

Many interesting ML problems lie in Rung 1.5

- Robustness
  - Distribution shift
  - Adversarial attack
- Generalization
  - Domain adaptation
  - Transfer learning
  - Meta-learning
  - Few-shot learning
- Other potential areas
  - Fairness
  - Data augmentation
  - Etc.

1. Empirically verifiable
2. “Good enough”

Causal deep learning, see <https://www.vanderschaar-lab.com/causal-deep-learning/>

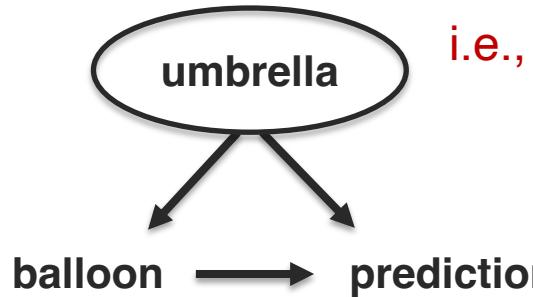
## Sub-Challenge 3c: Inference Paradigm

**Definition:** How increasingly abstract concepts are inferred from individual multimodal evidences.

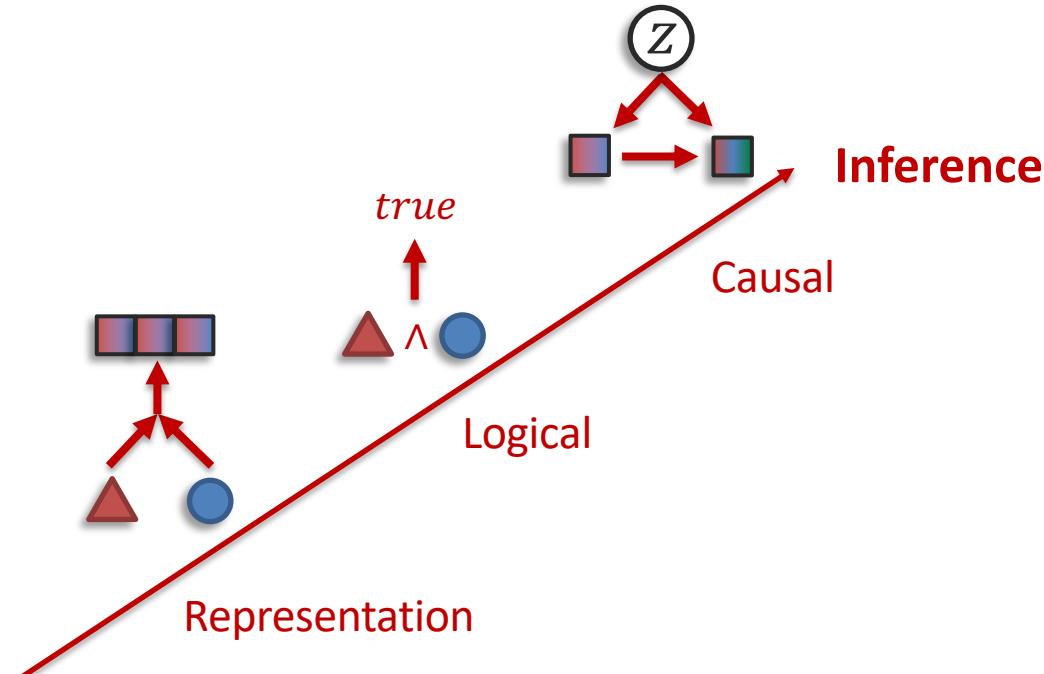
**Towards explicit inference paradigms:**

1. Logical inference
2. Causal inference

Nice, but you don't get these for free!

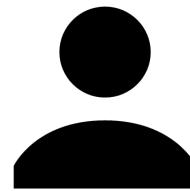


i.e., confounding variable

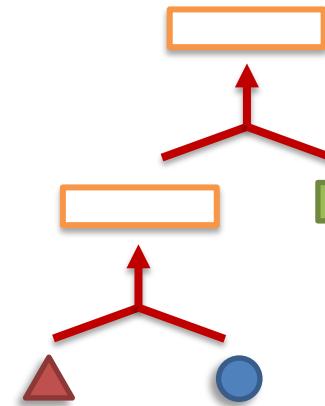


## Sub-Challenge 3d: Knowledge

**Definition:** The derivation of knowledge in the study of inference, structure, and reasoning.



Domain knowledge

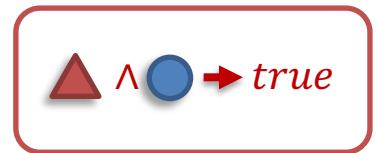
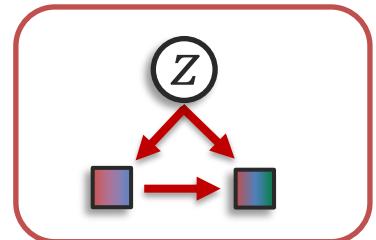


words

or

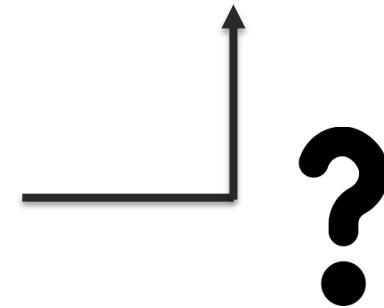


or



Knowledge graphs

Knowledge in other unstructured formats



# External Knowledge: Multimodal Knowledge Graphs

---

Knowledge can also be gained from external sources



*What kind of  
board is this?*

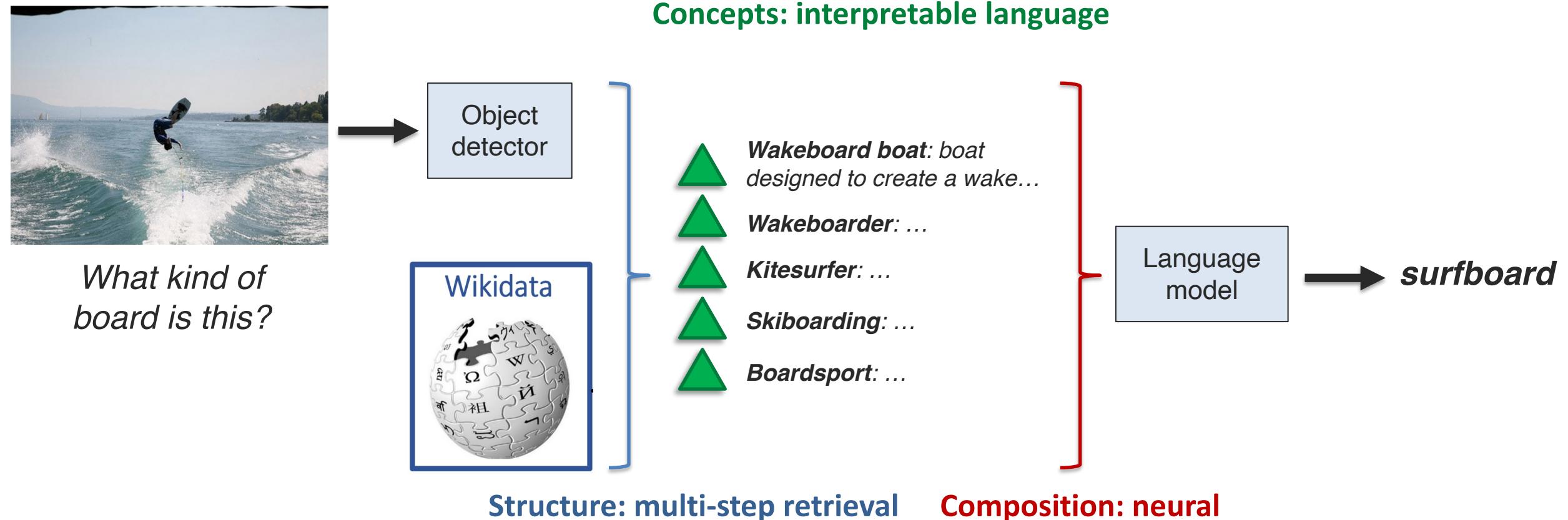
*Requires knowledge of water  
sports, sports equipment, etc.*

Existing models struggle when external knowledge is needed.  
How can we leverage external knowledge?

[Marino et al., OK-VQA: A visual question answering benchmark requiring external knowledge. CVPR 2019]

# External Knowledge: Multimodal Knowledge Graphs

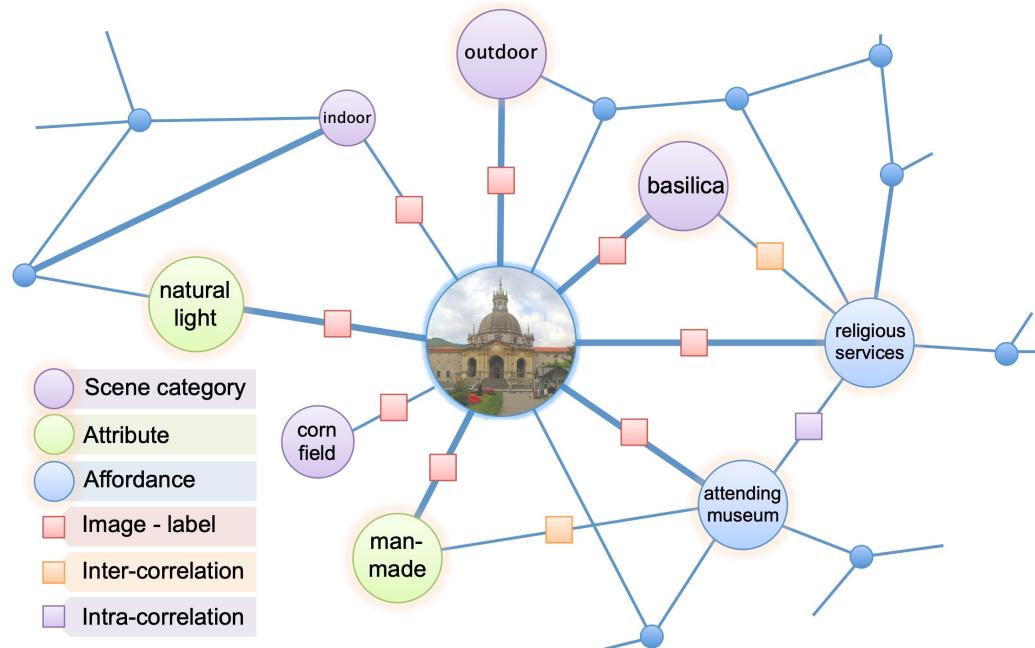
Knowledge can also be gained from external sources



[Gui et al., KAT: A Knowledge Augmented Transformer for Vision-and-Language. NAACL 2022]

# External Knowledge: Multimodal Knowledge Graphs

Knowledge can also be gained from external sources



Class



auditorium

community and social work, taking class for personal interest, religious practices, waiting, attending the performing arts

Affordances

congregating, indoor lighting, spectating, enclosed area, glossy

Attributes

Concepts: interpretable

Structure: multi-step inference

Composition: graph-based

# External Knowledge Challenges

Open challenges

## Yejin Choi

Brett Helsel Professor  
Office: 578 Allen Center  
Fax: 206-685-2969  
email: yejin@cs.washington.edu

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University of Washington  
Box 352350  
185 E Stevens Way NE  
Seattle, WA 98195-2350

Allen Institute for Artificial Intelligence  
2157 N Northlake Way, Suite 110  
Seattle, WA 98103



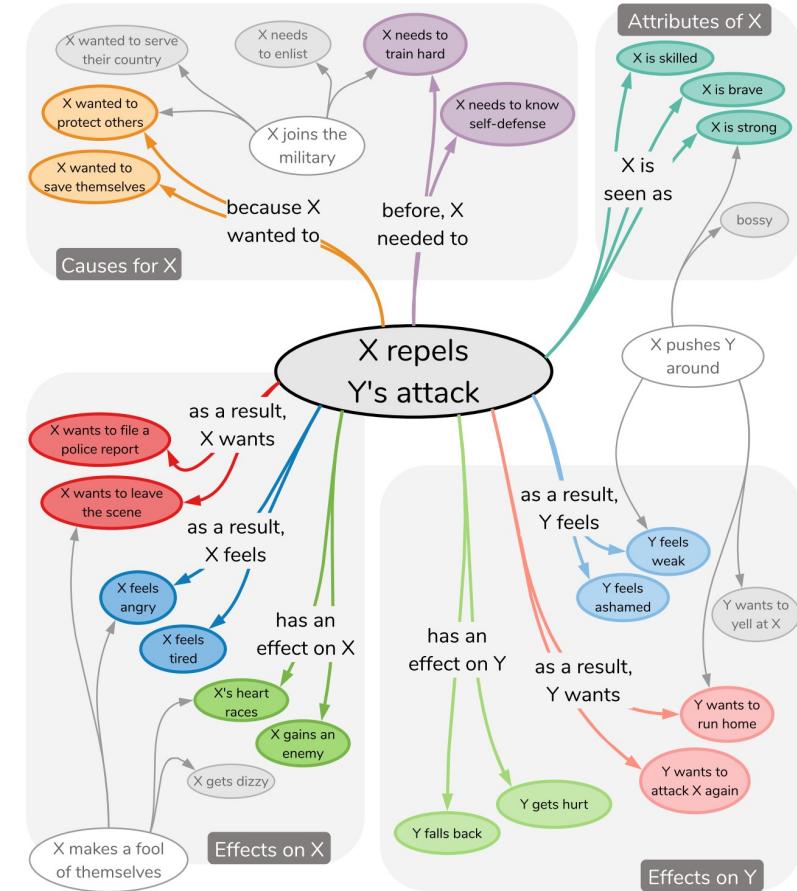
Photo credit:  
Bruce Hemingway

## News:

- Outstanding Paper Award at ICML 2022
- Best Paper Award at NAACL 2022
- Keynote at ACL: "**2082: An ACL Odyssey: The Dark Matter of Language and Intelligence**" along with a fireside chat on "*The Trajectory of ACL and the Next 60 years*"
- An invited article, "*The Curious Case of Commonsense Intelligence*" for the Daedalus's special issue on AI & Society
- A podcast interview with the Gradient on commonsense and morality



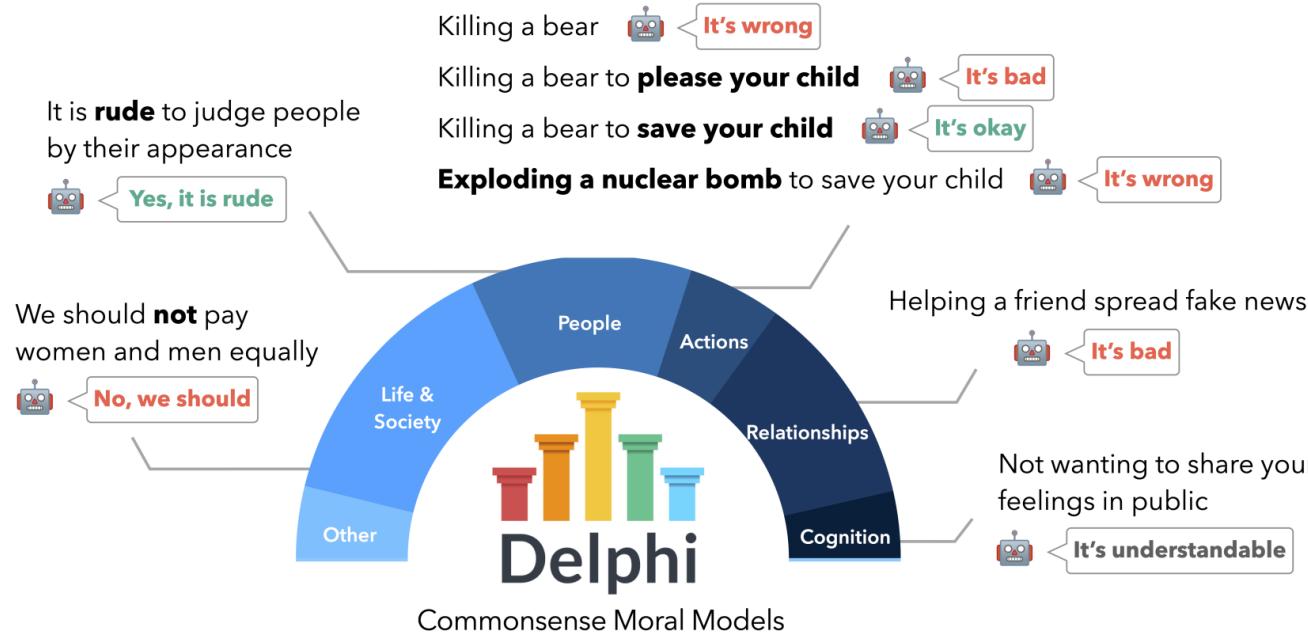
MOSAIC  
COMMONSENSE



## Atomic: If-then commonsense

[Sap et al., Atomic: An Atlas of Machine Commonsense for If-Then Reasoning. AAAI 2019]

# External Knowledge Challenges



Delphi: Moral commonsense



Social Chemistry: Social commonsense

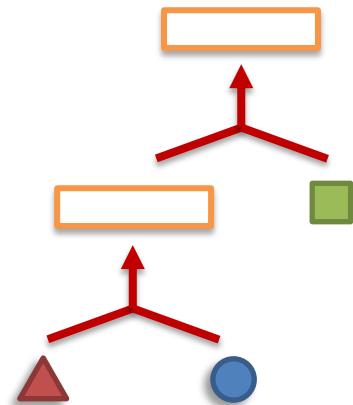
[Jiang et al., Can Machines Learn Morality? The Delphi Experiment. arXiv 2021]

[Forbes et al., Social Chemistry 101: Learning to Reason about Social and Moral Norms. EMNLP 2020]

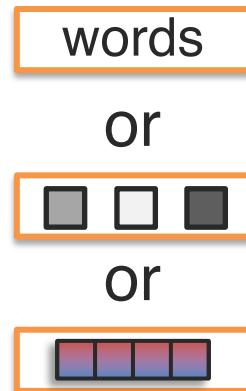
# Summary: Reasoning

**Definition:** Combining knowledge, usually through multiple inferential steps, exploiting multimodal alignment and problem structure.

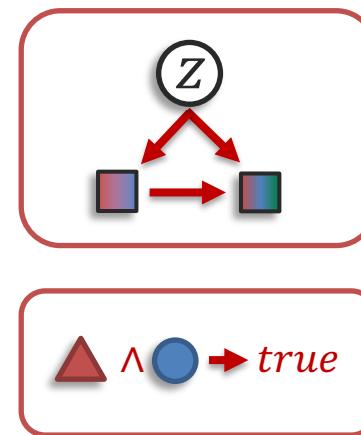
(A) Structure modeling



(B) Intermediate concepts



(C) Inference paradigm



(D) External knowledge



# Summary: Reasoning

**Definition:** Combining knowledge, usually through multiple inferential steps, exploiting multimodal alignment and problem structure.

(A) Structure modeling

(B) Intermediate concepts

(C) Inference paradigm

(D) External knowledge

Last Thursday

Temporal  
Hierarchical

Continuous

Tuesday

Interactive

Today

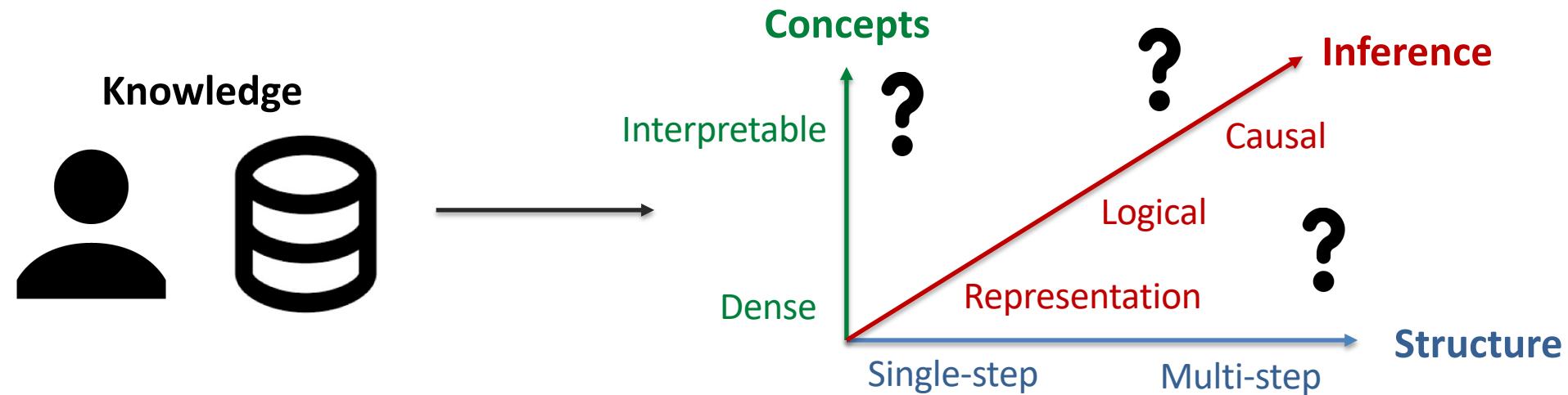
Discovery

Discrete

Causal  
Logical

Knowledge  
Commonsense

# More Reasoning



## Open challenges:

- Structure: multi-step inference
- Concepts: interpretable + differentiable representations
- Composition: explicit, logical, causal...
- Knowledge: integrating explicit knowledge with pretrained models
- Probing pretraining models for reasoning capabilities