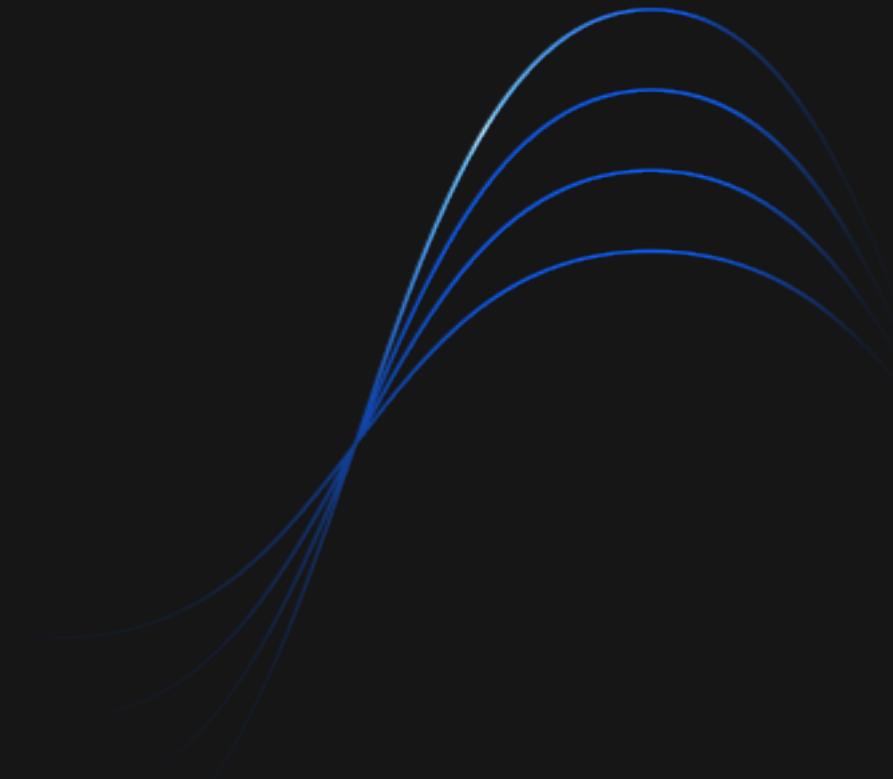


# Introduction to Quantum Computing @ SUTD

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Huang Junye  
Quantum Developer Advocate



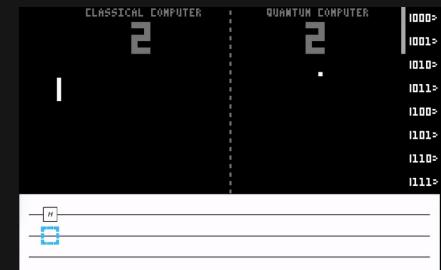
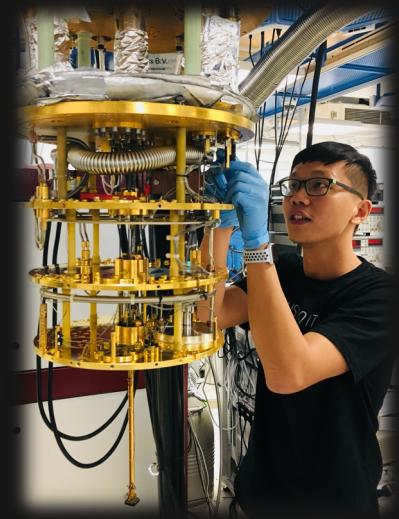
# Huang Junye

- Quantum developer advocate focusing on quantum education
- Leads Qiskit advocate program, supporting most active members of the Qiskit community through events, networking and mentorship.
- Led a team of 40+ for IBM Quantum Challenge 2021 for celebration of 5th anniversary of IBM Quantum and 40 years of quantum computing.
- Outstanding Accomplishment (highest level of recognition) from IBM Research for supporting Qiskit Global Summer School 2020.
- Co-creator of quantum games: QPong, QPong Arcade, QiskitBlocks, ...
- Graduate research in experimental low temperature physics at NUS

Connect with the  
**advocates** from within  
the Qiskit community

IBM Quantum Challenge generates  
better solutions than challenge  
creators thought possible

From May 20 to 26, 1,431 people from 76 countries participated in the IBM Quantum Challenge 2021, a celebration for 5-year anniversary of IBM Quantum and 40 years of quantum computing. Not only was the event a blast, but participants devised a more-efficient solution to one quantum computing problem than the problem's authors even thought possible.



# Agenda

Date	Start	End	Subject
26 Aug	15:00	17:00	Quantum Computing Lab
27 Aug	9:30	14:00	Quantum Algorithms

# Quantum Algorithms

IBM Quantum

Start	End	Duration	Subject
9:45	10:00	0:15	Overview and Recap
10:00	10:30	0:30	Deutsch-Jozsa algorithm + hands-on implementations
10:30	10:45	0:15	Break
10:45	11:20	0:35	Grover's algorithm + + hands-on implementations
11:20	12:00	0:40	Shor's algorithm + hands-on implementations
12:00	13:00	1:00	Lunch Break
13:00	13:30	0:30	Near-term algorithms and applications

# Deutsch- Jozsa algorithm

# Deutsch-Jozsa Problem

IBM Quantum

$$f(\{x_0, x_1, x_2, \dots\}) \rightarrow 0 \text{ or } 1, \text{ where } x_n \text{ is } 0 \text{ or } 1$$

Determine a hidden function to be constant or balanced.

Constant example

x	f(x)
0	0
1	0
2	0
3	0

Balanced example

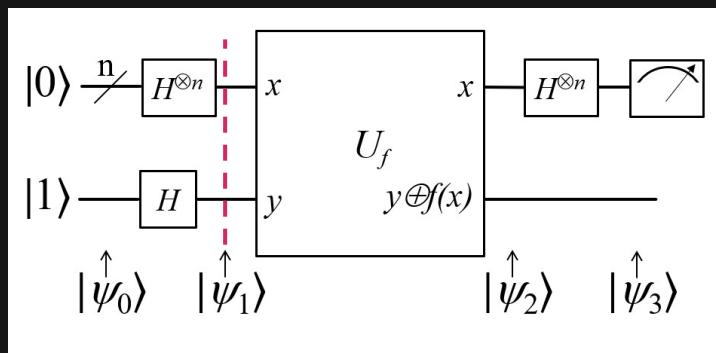
x	f(x)
0	0
1	1
2	1
3	0

Classical:  $2^{n-1} + 1$

Quantum: 1

# DJ Step 1

IBM Quantum

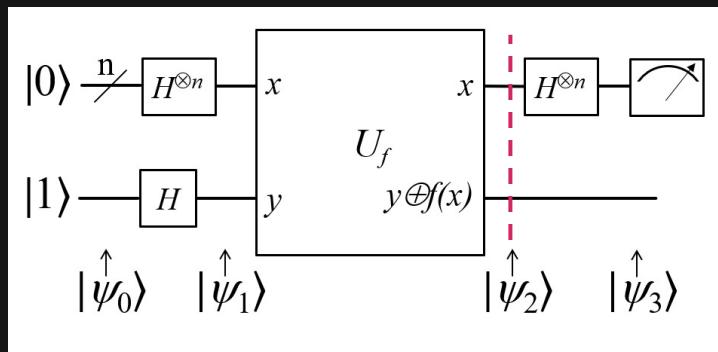


$$\frac{1}{\sqrt{2^{n+1}}} \sum_{x=0}^{2^n-1} |x\rangle (|0\rangle - |1\rangle)$$

# DJ Step 2

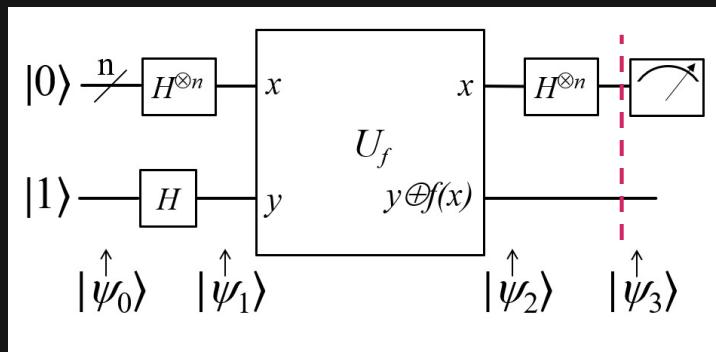
IBM Quantum

$$\frac{1}{\sqrt{2^{n+1}}} \sum_{x=0}^{2^n-1} |x\rangle (|f(x)\rangle - |1 \oplus f(x)\rangle)$$



$$= \frac{1}{\sqrt{2^{n+1}}} \sum_{x=0}^{2^n-1} (-1)^{f(x)} |x\rangle (|0\rangle - |1\rangle)$$

$$= \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} (-1)^{f(x)} |x\rangle$$



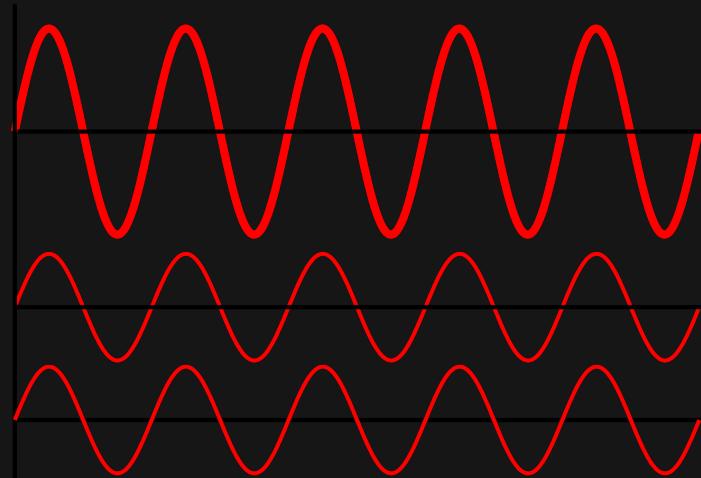
$$\begin{aligned}
 & \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} (-1)^{f(x)} \left[ \frac{1}{\sqrt{2^n}} \sum_{y=0}^{2^n-1} (-1)^{x \cdot y} |y\rangle \right] \\
 & = \frac{1}{2^n} \sum_{y=0}^{2^n-1} \left[ \sum_{x=0}^{2^n-1} (-1)^{f(x)} (-1)^{x \cdot y} \right] |y\rangle
 \end{aligned}$$

Probability of measuring  $|0\rangle^{\otimes n}$  :  $\left| \frac{1}{2^n} \sum_{x=0}^{2^n-1} (-1)^{f(x)} \right|^2 \rightarrow$

- If  $f(x)$  is constant:  $p = 1$
- If  $f(x)$  is balanced:  $p = 0$

# How does it work? Interference!

IBM Quantum



Constant

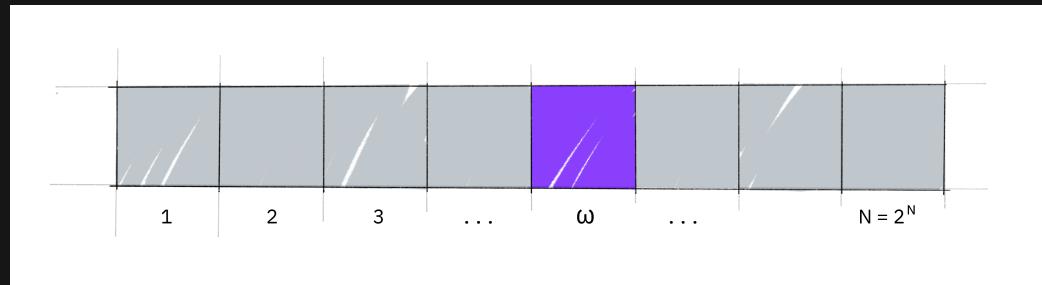


Balanced

# Grover's algorithm

# Unstructured search problem

IBM Quantum



Search for an element in an unstructured data base

Classical:  $O(N)$

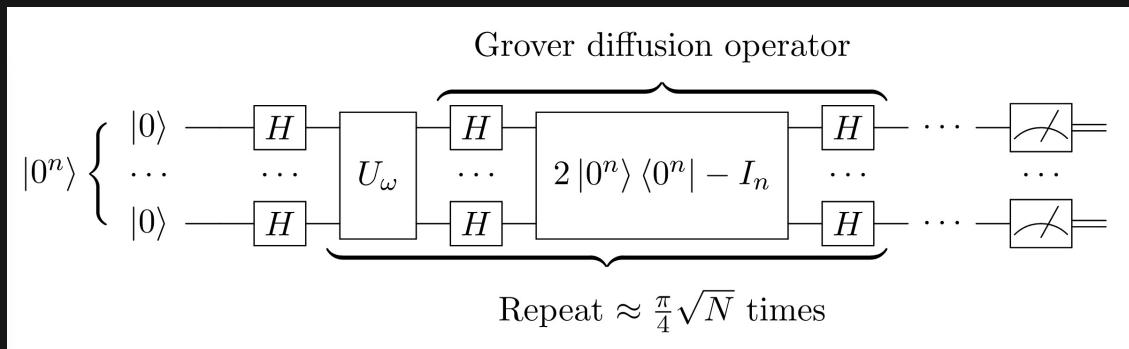
Quantum:  $O(\sqrt{N})$

# Grover's algorithm

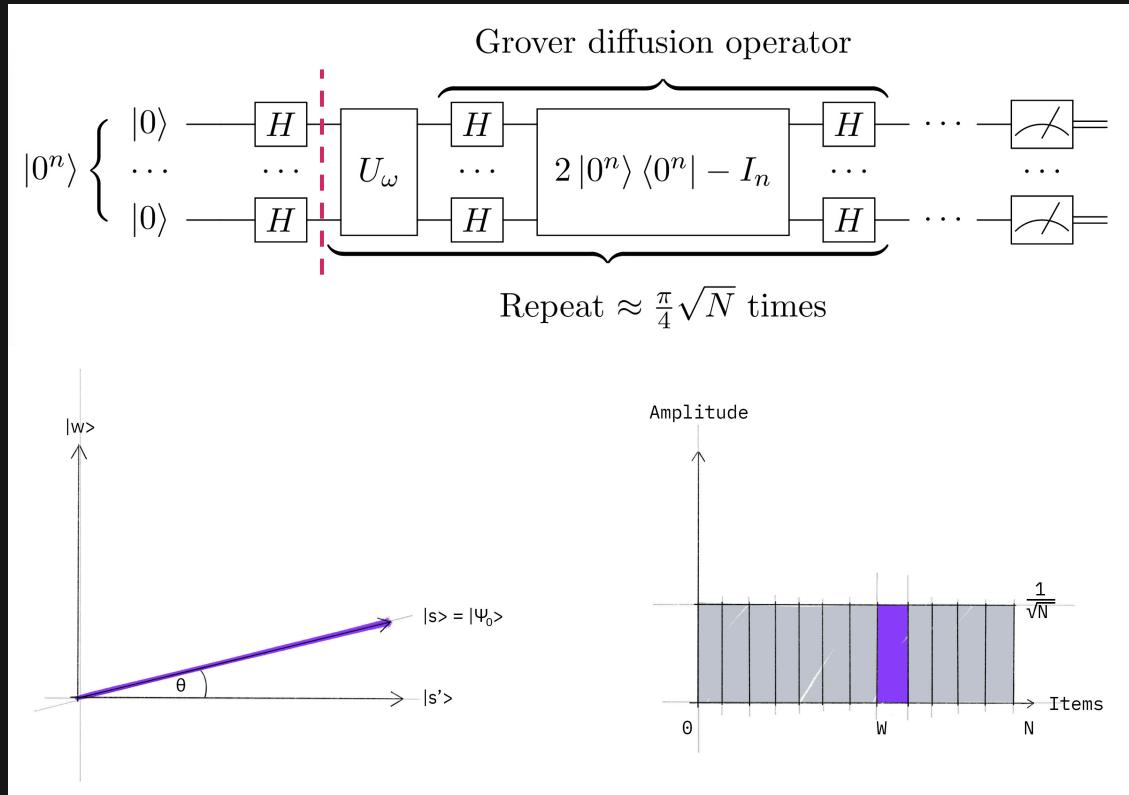
IBM Quantum

Algorithm:

1. Initialize the system to the uniform superposition over all states
2. Apply oracle  $U_w$
3. Apply diffusion operator
4. Repeat step 2 & 3
5. Measure



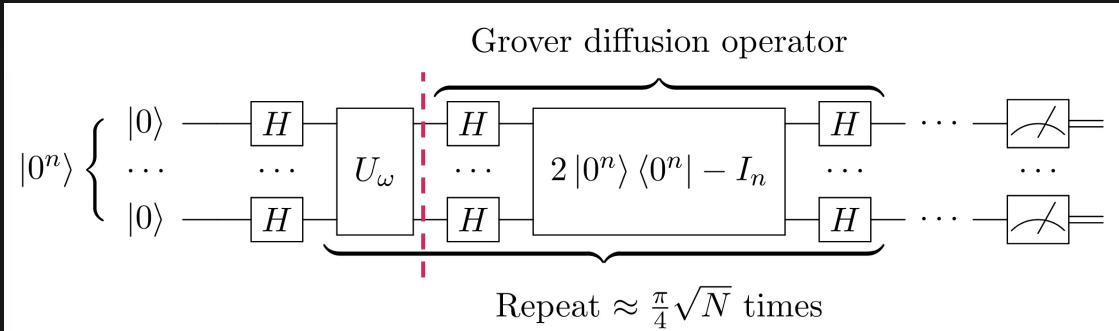
# Grover Step 1



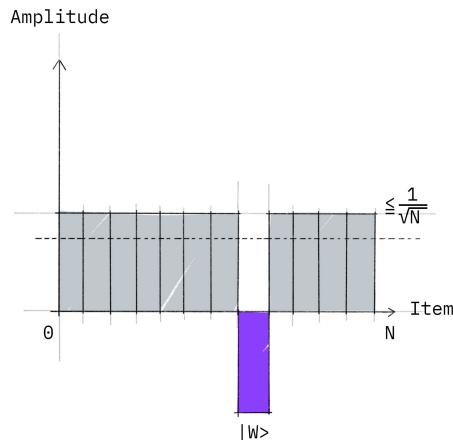
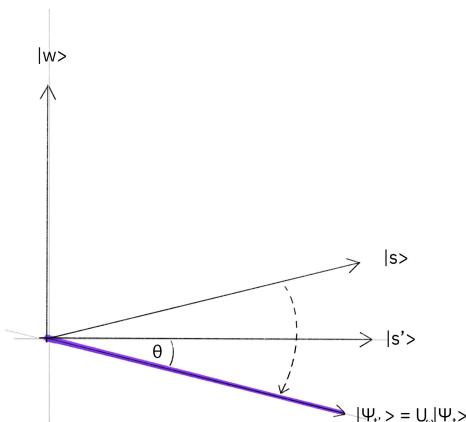
Step 1: Initialize the system to the uniform superposition over all states

$$|s\rangle = \frac{1}{\sqrt{N}} \sum_{x=0}^{N-1} |x\rangle$$

# Grover Step 2

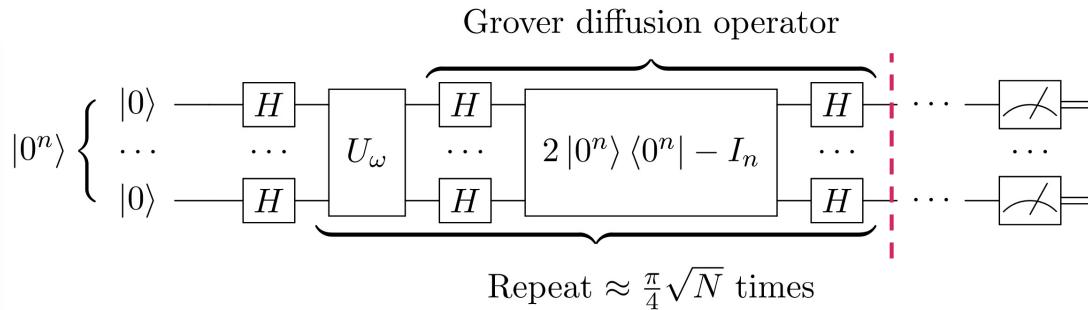


Step 2: Apply oracle  $U_w$



$$U_f|x\rangle = (-1)^{f(x)}|x\rangle$$

# Grover Step 3



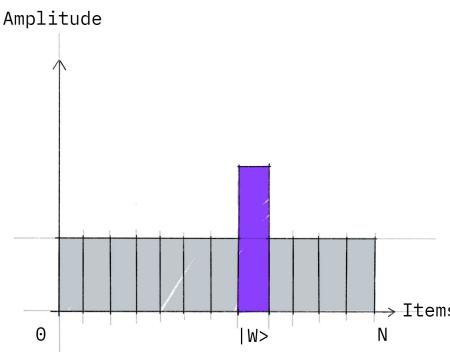
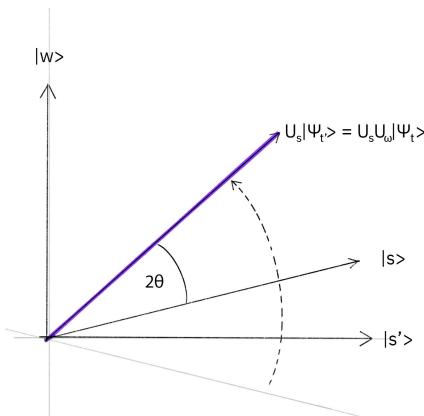
Step 2: Apply diffuser  $U_s$

$$U_s = 2|s\rangle\langle s| - 1$$

$$U_s U_w |x\rangle$$

Repeat  $r$  times

$$(U_s U_w)^r |x\rangle$$



# Shor's algorithm

# RSA encryption

- Widely used and assumed to be safe
- In 1994, Peter Shor proposed an algorithm which showed exponential speedup compared to the best-known classical algorithm
- Ignited the field

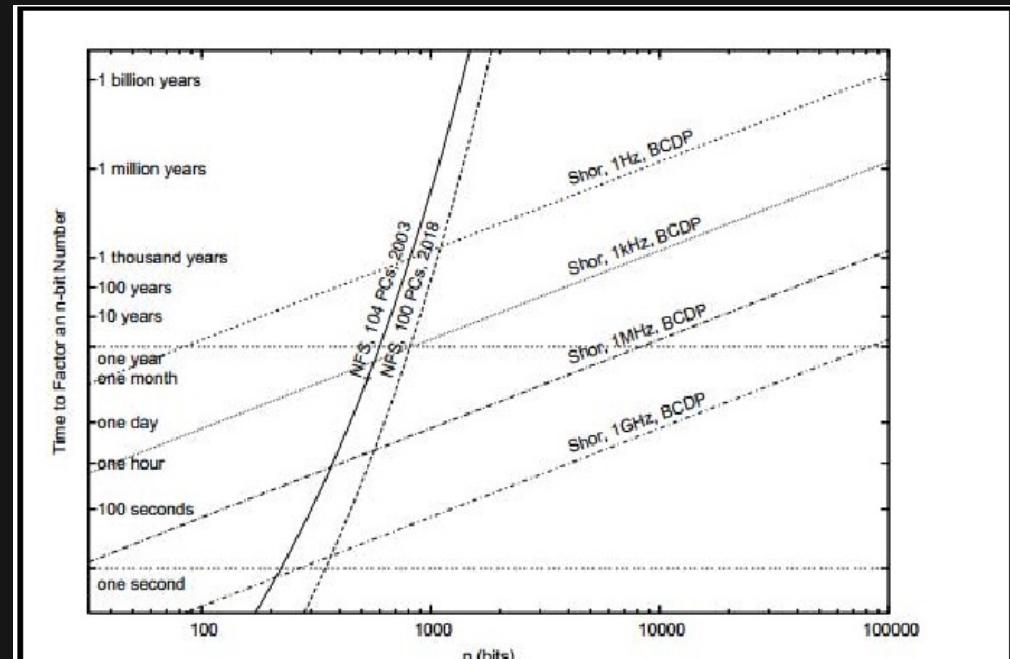


Fig. 1. Scaling of general number field sieve (GNFS) on classical computers and Shor's algorithm for factoring on a quantum computer, using BCDP modular exponentiation with various clock rates [14].

S. M. Hamdi, S. T. Zuhori, F. Mahmud and B. Pal, "A Compare between Shor's quantum factoring algorithm and General Number Field Sieve," *2014 International Conference on Electrical Engineering and Information & Communication Technology*, 2014, pp. 1-6, doi: 10.1109/ICEEICT.2014.6919115.

# How to crack RSA?

1. Find prime factors  $g_1, g_2$  for  $N$  such that  $g_1 \times g_2 = N$

2. Same as finding

$$\begin{aligned}x^2 &\equiv 1 \pmod{N} \\(x+1)(x-1) &\equiv 0 \pmod{N}\end{aligned}$$

$$\begin{aligned}\gcd(x+1, N) &= g_1 \\ \gcd(x-1, N) &= g_2\end{aligned}$$

3. How to find  $x$ ? => pick a random number  $x$  in the range  $[0, N-1]$ , find  $r$  such that

$$\begin{array}{ll}x^0 & (x^{r/2})^2 \equiv 1 \pmod{N} \\x^1 & \gcd(x^{r/2} + 1) \\ \dots & \gcd(x^{r/2} - 1) \\x^r & \equiv 1 \pmod{N}\end{array}$$

4. How to find  $r$ ? => period finding => quantum Fourier transform

# Modular arithmetic

IBM Quantum

examples

$$3 \equiv 24 \pmod{21}$$

$$14 \equiv 35 \pmod{21}$$

$$1 \equiv -20 \pmod{21}$$

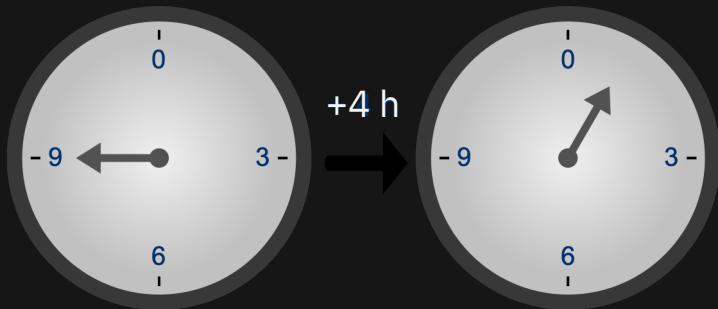
addition

$$\begin{aligned}24 + 35 &\pmod{21} \\&\equiv 3 + 14 \pmod{21} \\&\equiv 17 \pmod{21}\end{aligned}$$

multiplication

$$\begin{aligned}24 \times 30 &\pmod{21} \\&\equiv 3 \times 9 \pmod{21} \\&\equiv 27 \pmod{21} \\&\equiv 6 \pmod{21}\end{aligned}$$

Hours in a clock is modular 12



# Greatest common divisor

The largest positive integer that divides each of the integers

## Examples

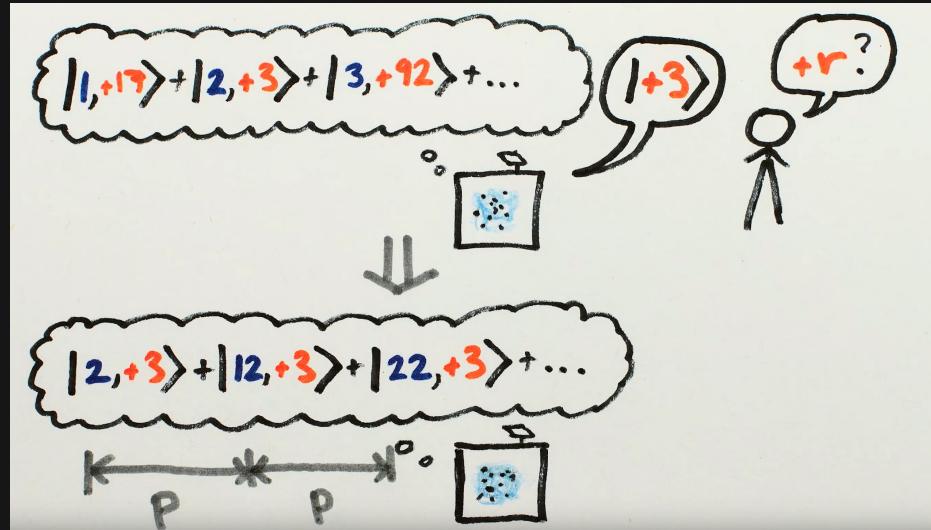
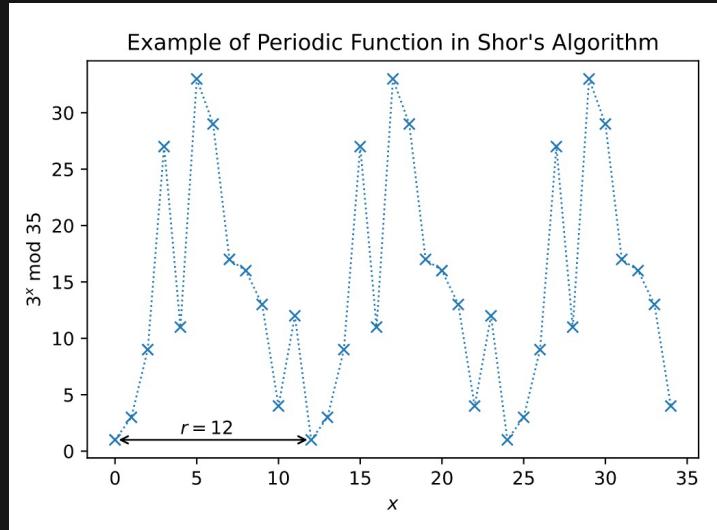
- $\text{gcd}(8,12) = 4$
- $\text{gcd}(54,24)=6$

2000-year-old efficient classical algorithm for finding gcd:  
Euclidean algorithm

# Period finding using QFT

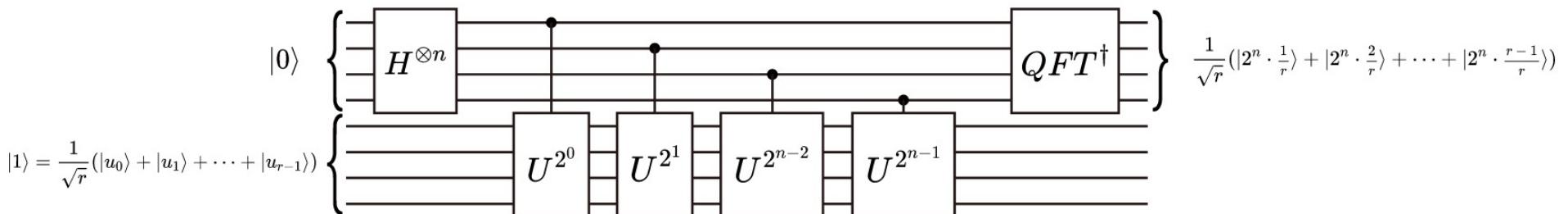
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This is the crust of Shor's algorithm



# Shor's algorithm

IBM Quantum



# Near-term algorithms & applications

# Potential Use Cases for Quantum Computing

	<b>Chemicals and Petroleum</b>	<b>Distribution and Logistics</b>	<b>Financial Services</b>	<b>Health Care and Life Sciences</b>	<b>Manufacturing</b>
● Chemical Simulation	Chemical product design Surfactants, Catalysts			Drug Discovery Protein Structure Predictions	Materials Discovery Quantum Chemistry
■ Scenario Simulation		Disruption Management	Derivatives Pricing Investment Risk Analysis	Disease Risk Predictions	
▲ Optimization	Feedstock To Product Oil Shipping / Trucking Refining Processes	Distribution Supply Chain Network Optimization Vehicle Routing	Portfolio Management Transaction Settlement	Medical/Drug Supply Chain	Fabrication Optimization Manufacturing Supply Chain Process Planning
◆ AI/ML	Drilling Locations Seismic imaging	Consumer Offer Recommender Freight Forecasting Irregular Behaviors (ops)	Finance Offer Recommender Credit/Asset Scoring Irregular Behaviors (fraud)	Accelerated Diagnosis Genomic Analysis Clinical Trial Enhancements	Quality Control Structural Design & Fluid Dynamics

# Near-term algorithms and applications

IBM Quantum

Textbook algorithms are too stringent

Near term computers are noisy

Need shorter circuits

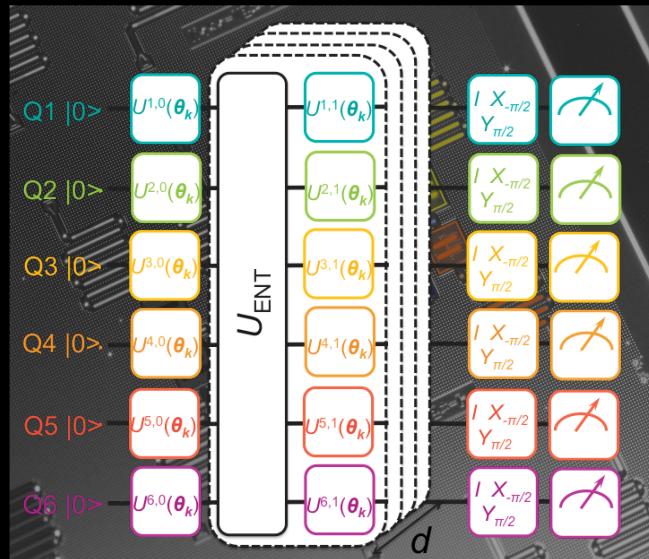
Quantum-classical hybrid algorithms

- Variational quantum eigensolver (VQE)
- Quantum approximate optimization algorithm (QAOA)

# Variational Quantum Eigensolver (VQE)

$$H = \sum_{\alpha} h_{\alpha} \sigma(\alpha)$$

Map problem onto Paulis



Prepare guess state  $|\psi_G(\vec{\theta})\rangle$

Measure its energy

$$E(\vec{\theta}) = \sum_{\alpha} h_{\alpha} \langle \psi_G(\vec{\theta}) | \sigma_{\alpha} | \psi_G(\vec{\theta}) \rangle$$

$$\begin{array}{c} E(\vec{\theta}) \\ \longrightarrow \\ \vec{\theta} \end{array}$$



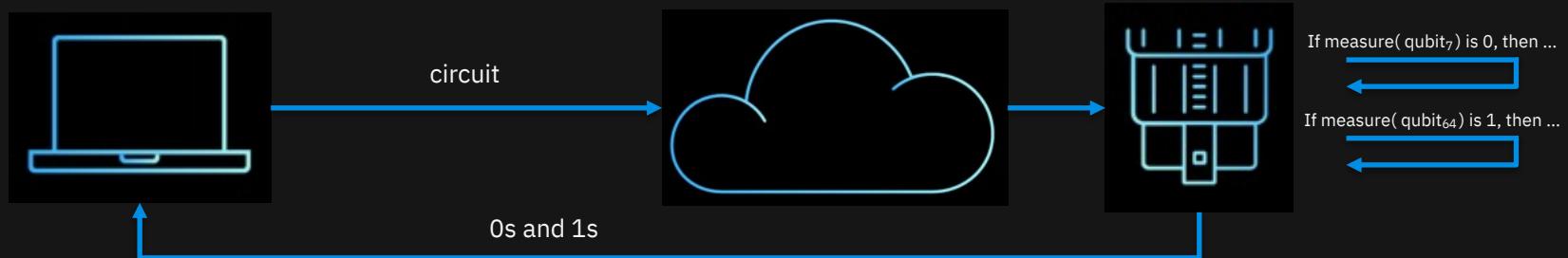
Use classical optimizer

Nat. Commun 5, 4213 (2014)  
Nature 549, 242-246 (2017)

A static circuit is run sequentially with the result returned to the user.



A dynamic circuit can measure qubits mid-circuit and change the flow of processing.



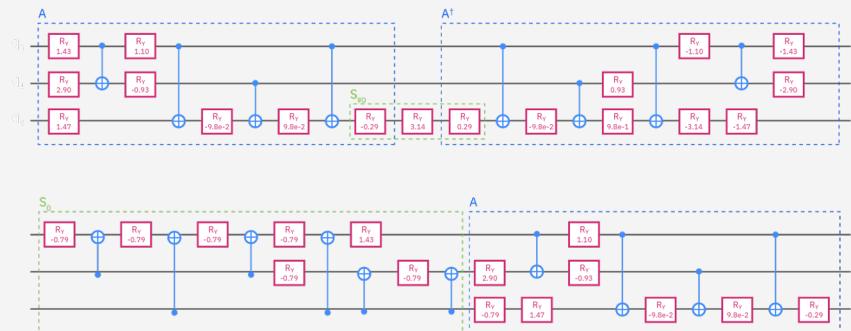
# JP Morgan Chase

## Quantum Computing for the Financial Services Industry

Recently, JPMC and IBM used Quantum Amplitude Estimation, a Monte Carlo-like sampling algorithm, to compute European option pricing, pricing path depend options, showing a quadratic speed-up versus a classical Monte Carlo approach.



European derivative pricing circuit

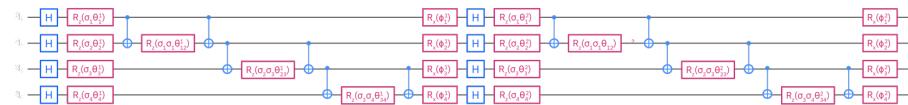


## Quantum Computing for Materials Discovery and Manufacturing Optimization

Daimler and IBM have recently published a series of papers demonstrating progress toward using quantum computers to model material systems including Lithium-sulfur that are relevant to advancing the performance of batteries. The teams have also demonstrated applications in manufacturing defect analysis and product recommendation.



Energy of binary crystalline materials circuit.



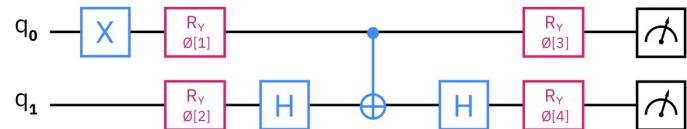
# ExxonMobil

## Quantum Computing as a Tool for Chemistry and Engineering

Working together, ExxonMobil and IBM recently demonstrated advancements in using quantum computers to accurately calculate thermodynamic observables, demonstrating how quantum can be the next generation tool for chemists and chemical engineers developing advanced energy solutions.



Accurate thermodynamic observables calculation circuit



# What are the next steps?

# Deutsch-Jozsa algorithm

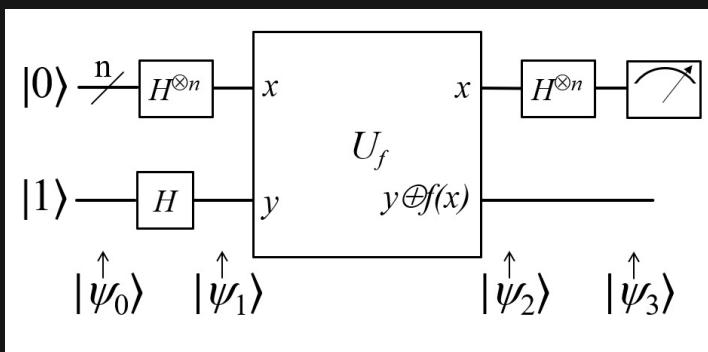
IBM Quantum

## Deutsch-Jozsa problem

$f(\{x_0, x_1, x_2, \dots\}) \rightarrow 0 \text{ or } 1$ , where  $x_n$  is 0 or 1

Determine a hidden function to be constant or balanced.

## Deutsch-Jozsa algorithm



[Qiskit textbook chapter](#)



[Circuit composer demo](#)



[Qiskit notebook demo](#)



[Qiskit GSS lecture](#)

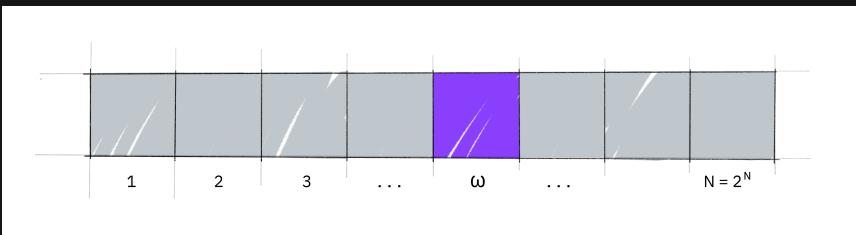


[Lecture note](#)

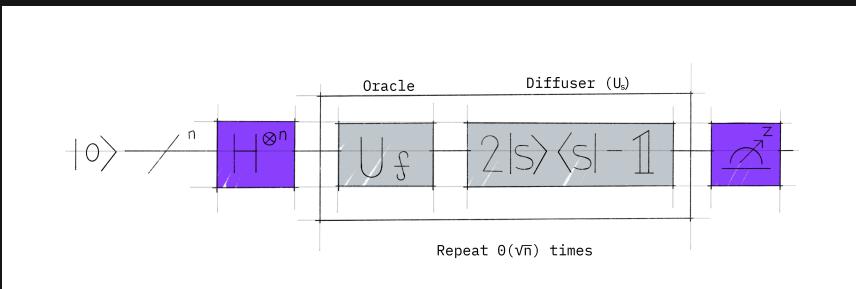
# Grover's algorithm

IBM Quantum

## Unstructured search problem



## Grover's algorithm



[Qiskit textbook chapter](#)



[Circuit composer demo](#)



[Qiskit notebook demo](#)



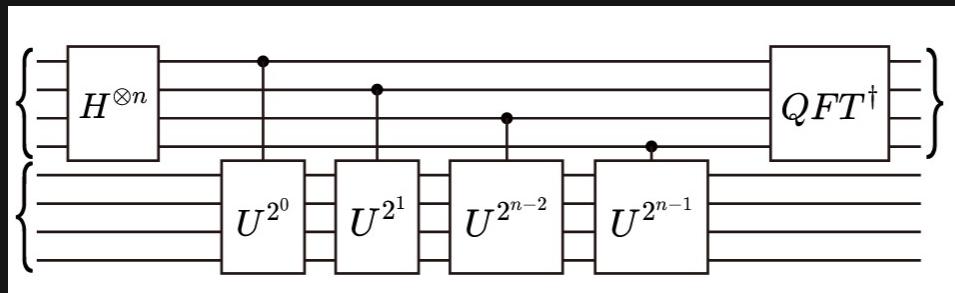
[Qiskit GSS lecture](#)



[Lecture note](#)

# Shor's algorithm

IBM Quantum



[Qiskit textbook chapter](#)



[Circuit composer demo\\*](#)



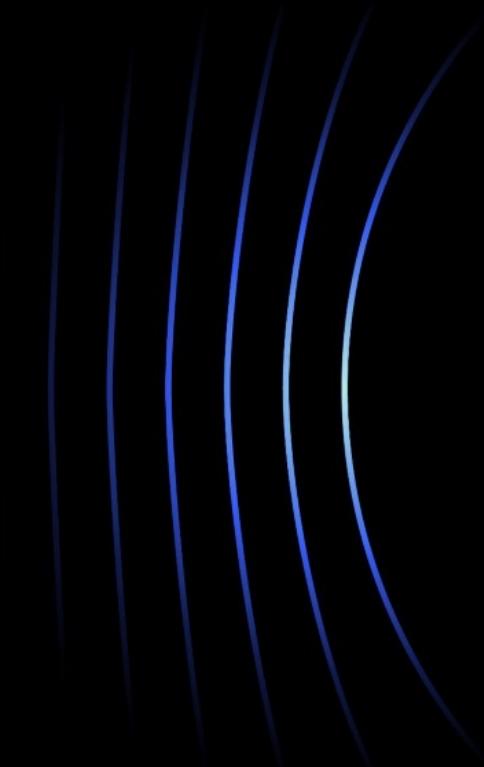
[Qiskit notebook demo](#)



[Qiskit GSS lecture](#)



Lecture note [1](#) and [2](#)



# IBM Quantum Challenge Africa 2021

The IBM Research Lab in South Africa and Wits University have developed a quantum computing challenge showcasing how the technology can be used in the fields of medicine, finance, and logistics.

With a focus on problems relevant to Africa for African learners, students, and industry members; the challenge highlights the amazing opportunities available to grow the necessary expertise and communities on the continent.



9 September (07:00 UTC) -  
20 September (23:00 UTC)

Learn more at [ibm.co/ibmQuantumAfrica21](https://ibm.co/ibmQuantumAfrica21)

# Qiskit Developer Certification

IBM Quantum



Quantum industry's first developer certificate

A requirement for becoming a Qiskit advocate

# IBM Quantum Resources – Self-learning

## [IBM Quantum Composer and IBM Quantum Lab](#)

Cloud applications for  
programming real  
quantum hardware and  
high performance  
simulators

## [Qiskit Online Open Source Textbook](#)

Interactive advanced text  
on quantum algorithms  
and computation based on  
Qiskit

## [Qiskit Youtube Channel](#)

- [Coding with Qiskit Series](#): learn to program quantum computers with Qiskit
- [Qiskit Live](#): livestream of public lecture series
- [SuperPosition Series](#): explores how individuals became Qiskit developers
- [1 Minute Qiskit](#): Qiskit tips & tricks

## [Qiskit.org](#)

Open-source quantum  
computing software  
development

- [Documentation, Tutorials, Events, Education](#)
- [Metal](#) - quantum device design
- [OpenQASM 3.0](#)

# Qiskit on Social Networks

Follow @Qiskit



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[Medium](#)

Coding with Qiskit



1 minute Qiskit (every Monday)



SuperPosition



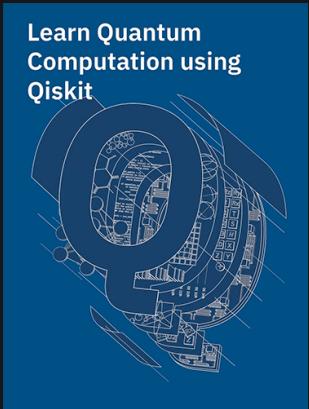
Qiskit Live (every Wednesday and Friday)



Charlie Bennett  
Seminar Series



# Qiskit Learning Resources

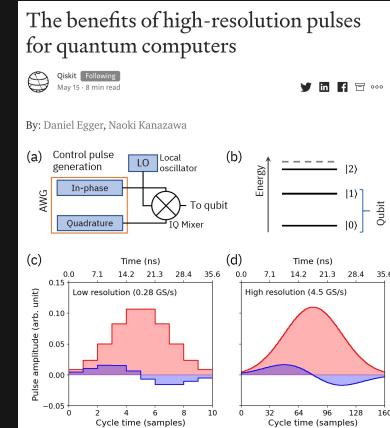


Qiskit textbook

Qiskit tutorials

IQX documentation

Qiskit documentation

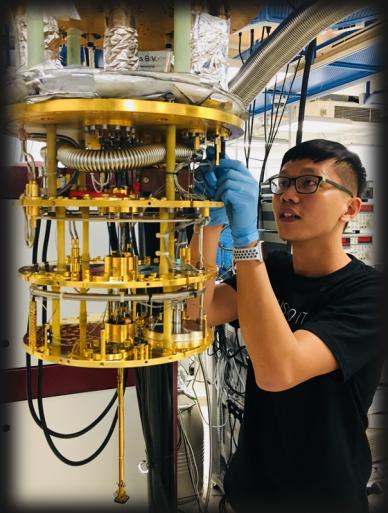


Qiskit Medium

IBM Research Blog

# Contacts

IBM Quantum



Huang Junye



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[@Huang Junye](https://www.linkedin.com/in/HuangJunye)



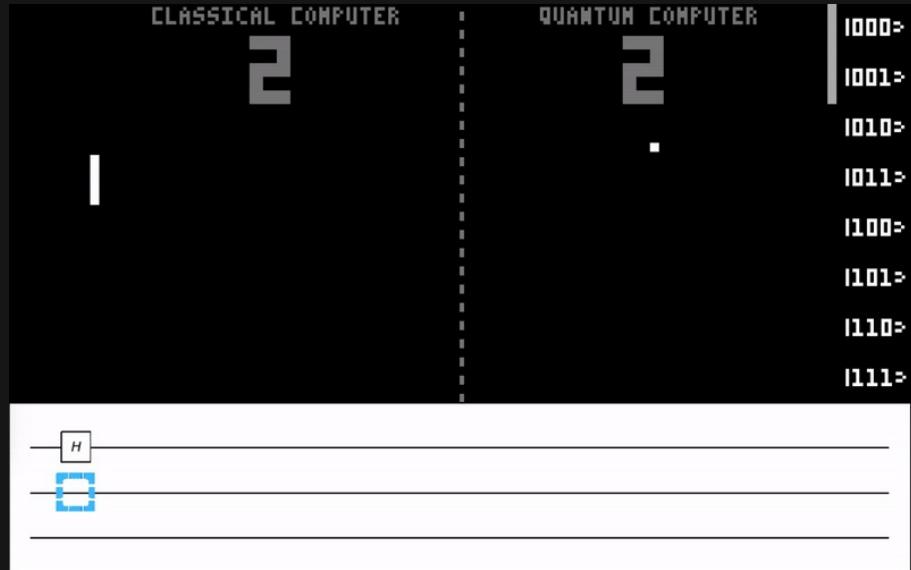
[@Junye](https://github.com/Junye)



[junye.huang@ibm.com](mailto:junye.huang@ibm.com)

# QPong

IBM Quantum



# IBM Quantum

<https://quantum-computing.ibm.com>