

1 ADDITIONAL EXPERIMENTS

1.1 EFFECT OF PRIVACY RADIUS ON MLDP-KDE

Table 1: MSEs of MLDP-KDE on each dataset when the privacy radius r is the maximum of the 10% percentile distance of a point to its neighbors, compared to the results in the original settings. We highlight results with increases of more than $10\times$ in the MSE in **bold**.

| Dataset | r | MSE | | | r | MSE | | |
|----------------|---------|--------------------------------|---------------------------------|----------------------------------|-------|-------------------|-------------------|--------------------|
| | | $\varepsilon = 1$ | $\varepsilon = 5$ | $\varepsilon = 20$ | | $\varepsilon = 1$ | $\varepsilon = 5$ | $\varepsilon = 20$ |
| CodRNA | 0.8494 | 0.0268 (12.7 \times) | 0.00174 (2.9 \times) | 0.0009 (3.0 \times) | 0.01 | 0.0021 | 0.0006 | 0.0003 |
| CovType | 1.7803 | 0.0520 (173 \times) | 0.00853 (42.7 \times) | 0.001155 (19.2 \times) | 0.01 | 0.0003 | 0.0002 | 6e-05 |
| RCV1 | 0.8565 | 0.0131 (16.4 \times) | 0.00131 (2.2 \times) | 0.000759 (3.8 \times) | 0.01 | 0.0008 | 0.0006 | 0.0002 |
| Yelp | 8.4035 | 0.0295 (36.9 \times) | 0.0154 (45.3 \times) | 0.0101 (56.1 \times) | 0.001 | 0.0008 | 0.00034 | 0.00018 |
| SYN | 11.2314 | 0.0082 (2.4 \times) | 0.00377 (14.0 \times) | 0.00242 (24.2 \times) | 0.072 | 0.0034 | 0.00027 | 0.0001 |

Table 2: MSEs of MLDP-KDE on each dataset by varying the privacy radius r as the average distance from a point to its t -nearest neighbors for $t \in \{1, 10, 100, 1000, 10000\}$ (rounded up to the nearest decimals of up to three digits). For $t = \{10, 100, 1000, 10000\}$, we highlight results with over $5\times$ increases in the MSE compared to that for $t = 1$ in **bold**.

| Datasets | t | r | MSE | | |
|----------------|--------|---------|--------------------------------|-------------------|--------------------|
| | | | $\varepsilon = 1$ | $\varepsilon = 5$ | $\varepsilon = 20$ |
| CodRNA | 1 | 0.01 | 0.0021 | 0.0006 | 0.0003 |
| | 10 | 0.055 | 0.0018 | 0.0007 | 0.0003 |
| | 100 | 0.1 | 0.0016 | 0.0009 | 0.0005 |
| | 1,000 | 0.15 | 0.0044 | 0.00095 | 0.0006 |
| | 10,000 | 0.2 | 0.0044 | 0.00142 | 0.0006 |
| CovType | 1 | 0.01 | 0.0003 | 0.0002 | 6e-05 |
| | 10 | 0.06 | 0.0003 | 0.0001 | 8e-05 |
| | 100 | 0.1 | 0.0023 (7.7 \times) | 0.0001 | 8e-05 |
| | 1,000 | 0.3 | 0.0065 (21.7 \times) | 0.0004 | 0.0001 |
| | 10,000 | 0.5 | 0.0144 (48 \times) | 0.0005 | 0.0001 |
| RCV1 | 1 | 0.01 | 0.0008 | 0.0006 | 0.0002 |
| | 10 | 0.057 | 0.0013 | 0.0007 | 0.0002 |
| | 100 | 0.2 | 0.0058 (7.3 \times) | 0.0008 | 0.0006 |
| | 1,000 | 0.35 | 0.006 (7.5 \times) | 0.0008 | 0.0006 |
| | 10,000 | 0.5 | 0.022 (27.5 \times) | 0.0013 | 0.0007 |
| Yelp | 1 | 0.001 | 0.0008 | 0.00034 | 0.00018 |
| | 10 | 0.00175 | 0.0014 | 0.00038 | 7e-05 |
| | 100 | 0.0025 | 0.0016 | 0.00056 | 7e-05 |
| | 1,000 | 0.00375 | 0.0013 | 0.00041 | 8e-05 |
| | 10,000 | 0.005 | 0.0015 | 0.00073 | 0.0001 |
| SYN | 1 | 0.072 | 0.0034 | 0.00027 | 0.0001 |
| | 10 | 0.088 | 0.0036 | 0.00035 | 0.0001 |
| | 100 | 0.107 | 0.0037 | 0.0008 | 0.0001 |
| | 1,000 | 0.142 | 0.0036 | 0.0008 | 0.0001 |
| | 10,000 | 0.177 | 0.0037 | 0.0004 | 0.0001 |

1.2 EXPERIMENTS WITH REVISED PRIVACY PARAMETER AND RADIUS

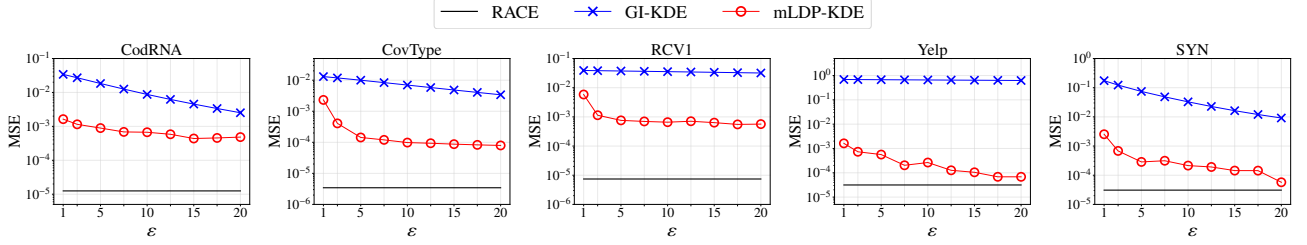


Figure 1: MSEs for KDE under mLDP with varying privacy budget $\varepsilon \in \{1, 2.5, 5, \dots, 20\}$, where r is set to be the average distance from a point to its 100-nearest neighbors in each dataset.

1.3 ADDITIONAL VISUALIZED RESULTS

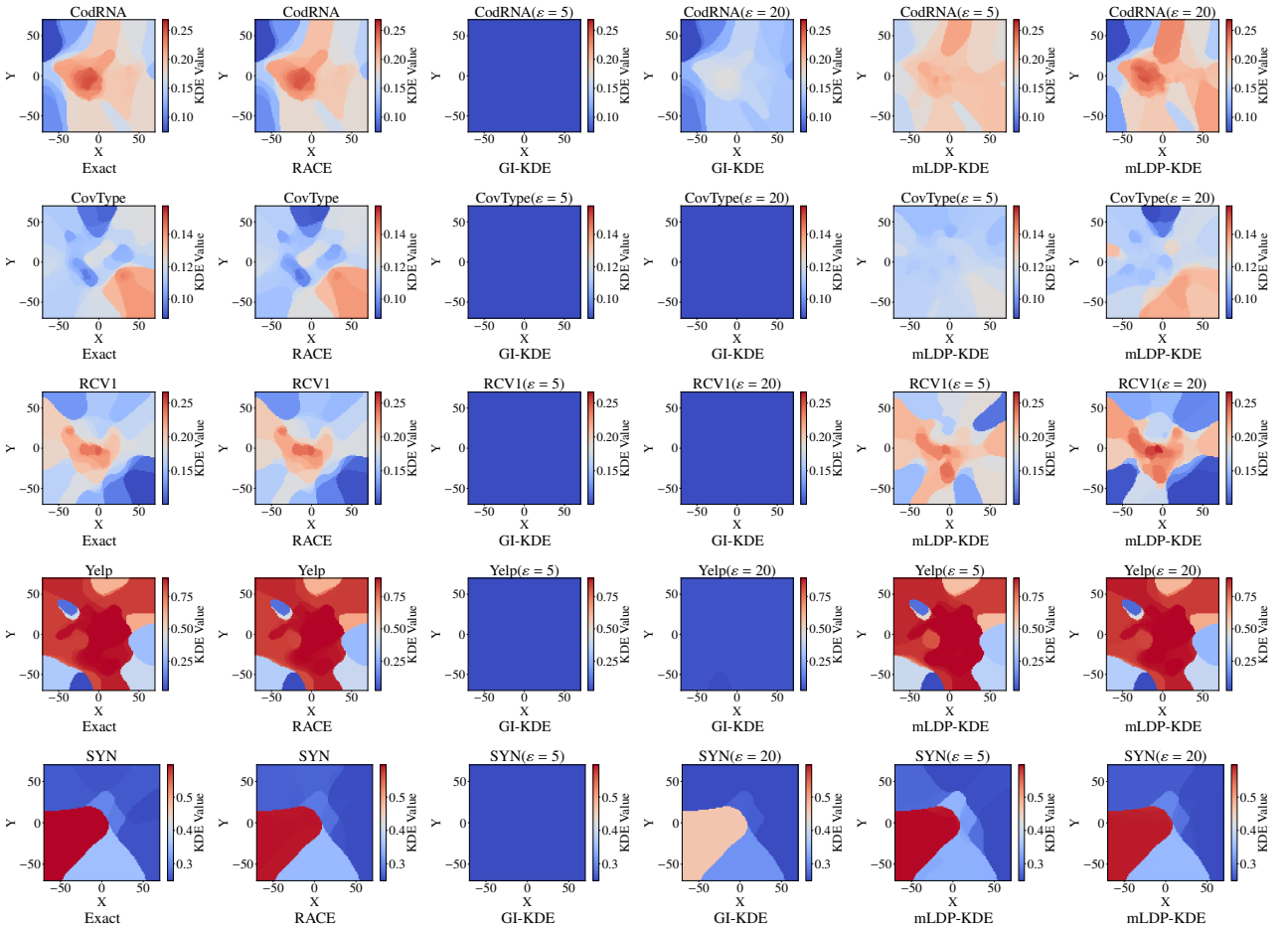


Figure 2: 2D heat maps for the KDE distributions provided by different methods on each dataset, where t-SNE is used for dimensionality reduction. For GI-KDE and mLDP-KDE, we present the results for $\varepsilon = 5$ and 20. We set r as the average distance from a point to its 100-nearest neighbors in each dataset. We observe that GI-KDE completely fails to preserve the exact KDE distributions in all cases, but mLDP-KDE generally preserves the exact KDE distributions in most cases when $\varepsilon = 5$ and always does when $\varepsilon = 20$.