

Lecture 4: Edge Based Vision

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Tuesday 10th March 2020

15:00pm – 16:00pm

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Overview:

- Why Edges Matter:
 - Edges in images correspond to physical events: edge of object, change in colour, change of surface orientation
- Edges and Derivatives
 - Convolution and filters (to detect changes)
- Edges and Scale
 - Physical edges persist across scales
- Edge Detection
 - Problem with noise, and accurate edge location
- Edge growing
 - Thresholding with hysteresis
 - Edge relaxation
- Hough Transform
 - Finding lines

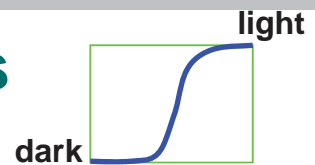
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Edges and Derivatives

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First-Derivative Edge Filters

- What is an edge?
- To detect: look at the slope



Discrete version of ∂_x ,
Central difference

?		?
-1	0	1
?		?

-1	0	1
-1	0	1
-1	0	1

Prewitt

-1	0	1
-2	0	2
-1	0	1

Sobel

1	0
0	-1

Roberts

$$S_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \otimes \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$$

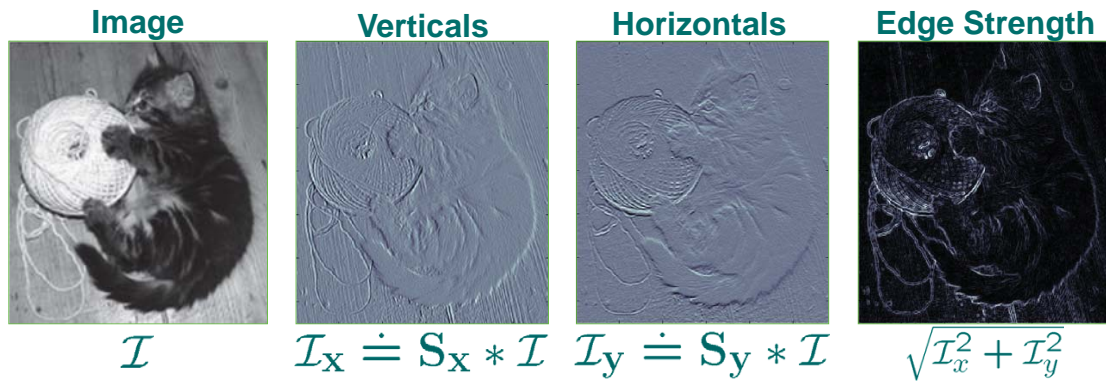
6 5 Multiplies and adds

Decomposable:
Exterior product

$$(a \otimes b) * \mathcal{I} \equiv a * (b * \mathcal{I})$$

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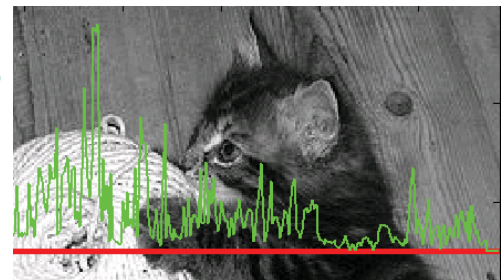
First Derivative Filters : Sobel



Edge strength: $g = |\vec{\nabla} I| = \sqrt{I_x^2 + I_y^2}$

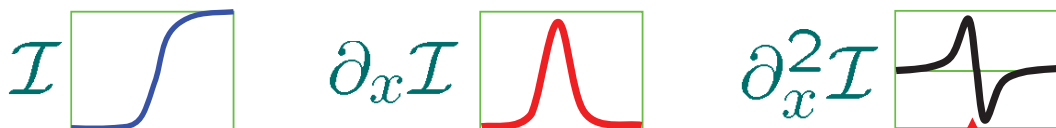
Ridges of g at edges, but noisy.

Normal to Edge: $\hat{n} = \frac{\vec{\nabla} I}{|\vec{\nabla} I|}$



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Second-Derivative Edge Filters

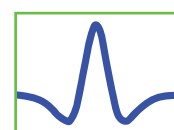


- Laplacian: **scalar** operator
 $\Delta = \nabla^2 = \partial_x^2 + \partial_y^2$
- Difference of Gaussian, Laplacian of Gaussian: includes gaussian smoother
- False edges: **every** peak/trough of gradient gives a zero-crossing, not just big peaks
- Doesn't tell us the direction of the edge (scalar operator)
- Tends to **create closed loops of edges** ('plate of spaghetti' effect)

zero crossing

-1	-1	-1
-1	8	-1
-1	-1	-1

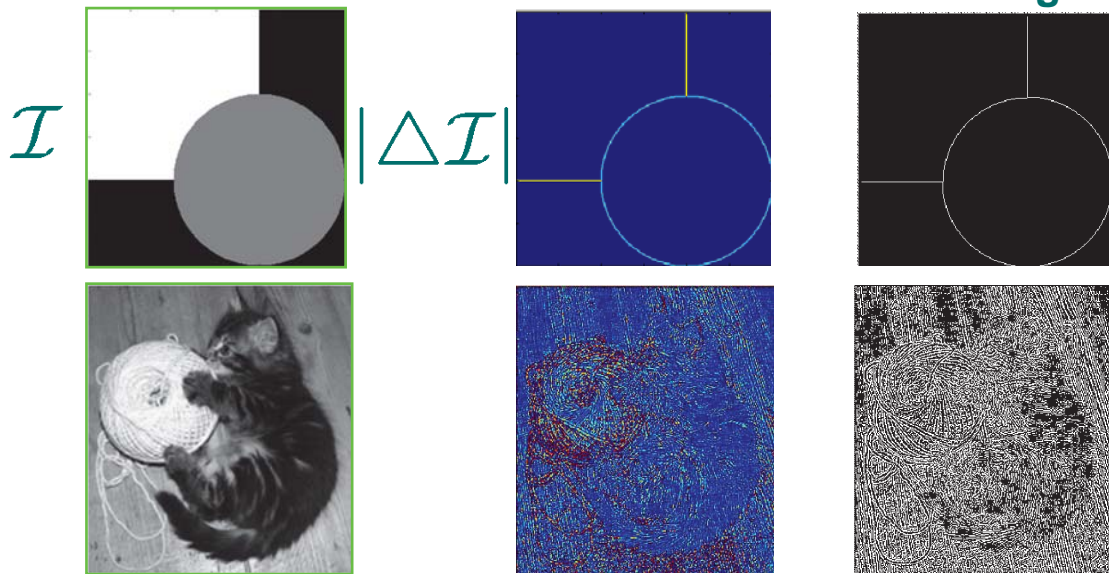
Laplacian



'mexican hat'

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Laplacian Filter



- Need to consider **smoothing** and **noise**
- Need to consider **scale**
- Need to consider **edge detection**

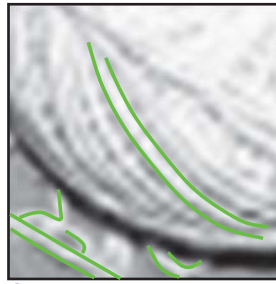
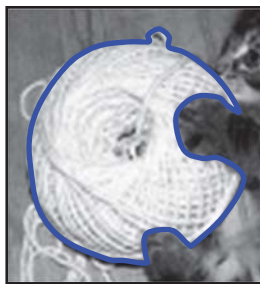
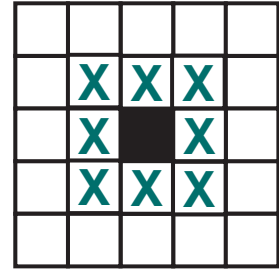
-1	-1	-1
-1	8	-1
-1	-1	-1

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Edges and Scale

Edges and Scale

- Edge filters enhance noise
- What is a 'real' edge and what noise?
- Edges exist at many different scales
- What scales matter depends on application
- Sensible approach: use many different scales
 - Edges persist across scales, allows fusion across scales
- Gaussian gives scale & **smoothing** separable filter

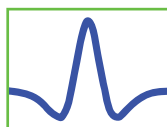


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Edges and Scale

Marr-Hildreth:

- Convolve with gaussian \mathcal{G}
- Take Laplacian ∇^2 of result:
 - **combine into single stage LoG**
- Edges at zero-crossings
- Edges move with scale if curved
- No information on direction
- 'Plate of spaghetti' problem



'mexican hat'

Canny:

- Convolve with gaussian \mathcal{G}
- Take gradient $\vec{\nabla}$ of result

$$\vec{\nabla}(\mathcal{G} * I), g = |\vec{\nabla}(\mathcal{G} * I)|$$
- Find gradient direction:

$$\hat{n} = \vec{\nabla}(\mathcal{G} * I) / g$$
- Create gaussian-smoothed derivative tuned to this direction
- Take another derivative in that direction to find local maximum, zero-crossing
- Stable across scales

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Marr-Hildreth vs Canny

- Both involve pre-smoothing with gaussian
- Both involve second-derivative BUT:

Marr-Hildreth:

- **No information on direction**
- By adding second-derivative in other direction, increases effect of **noise**

Canny:

- Create tuned derivative given **estimated gradient direction**
- Only compute second derivative in gradient direction
- Check that it really is local maximum of edge strength in that direction (see non-maximum suppression)

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Marr-Hildreth Edge Detection

 $\sigma = 2 \quad \sigma = 3 \quad \sigma = 4$

zero crossings $\text{LOG} > 0$ LOG



white, all 3 scales

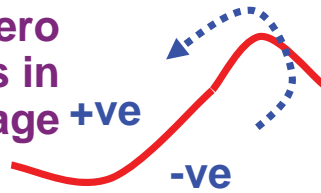


Marr-Hildreth Edge Detection

$\sigma = 10$

- Some edges not well localized
- 'Plate of spaghetti' effects

Trace zero crossings in image +ve



Keeps going until meets edge or closes the loop



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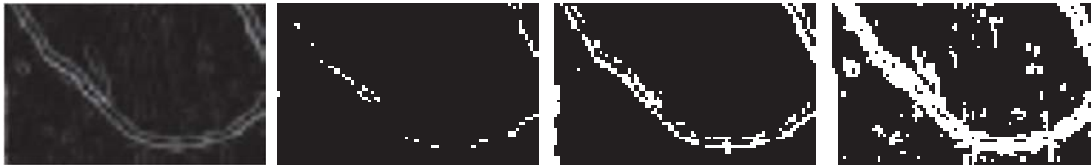
Edge Detection

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Edge Detection: First Derivatives



- Position of maximum can be difficult to locate:
 - second-derivative, zero crossing more precise
- Simple **threshold**:
 - thick edges, need to apply thinning
 - missed edges, streaking (see thresholding with hysteresis)



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Edge Detection:

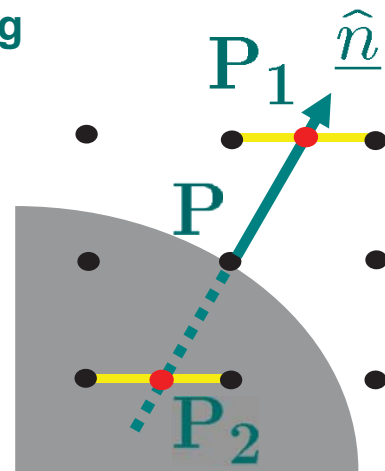
- Zero-crossing more precisely located than maximum
 - Sub-pixel accuracy?
- Thresholding in Marr-Hildreth (LoG):
 - Threshold at ~zero, but what about noise?
 - Doesn't use directional information
 - Other second derivative increases noise
- 'Plate of spaghetti':
 - continuity => closed loops or meets boundary
- Thresholding & Thinning 1st Derivative
 - Incorporates neighbourhood information
 - Still doesn't use all available information
- If we had the edge direction as well.....



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Non-Maximum Suppression

- Start from edge-strength signal g
- Locate possible edge point P
- Identify gradient direction \hat{n}
- Interpolate g at P_1 and P_2
- P is local maximum provided:
 $g(P) > g(P_1) \text{ \& } g(P) > g(P_2)$
- Only accepts as edge if proper **maximum**, rejects if not
- In practise, only allow a set of discrete possible directions



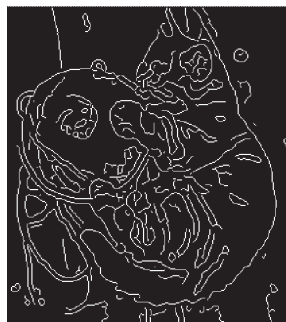
Object & pixel positions

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Canny Edge Detector

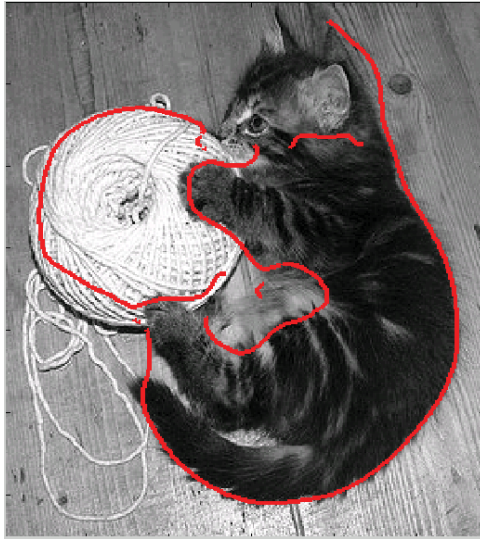
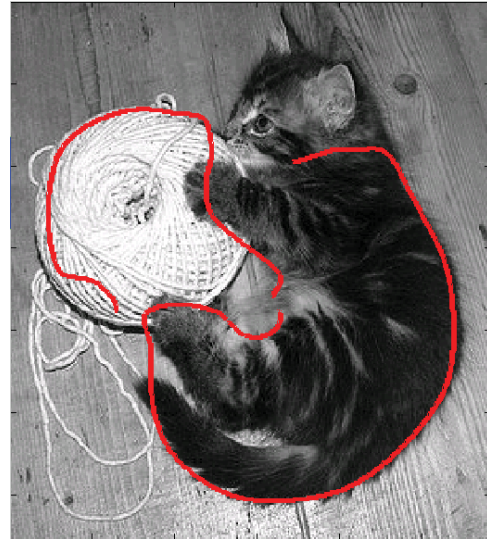
 $\sigma = 1$ $\sigma = 1.5$

white, all 3 scales

 $\sigma = 2$ 

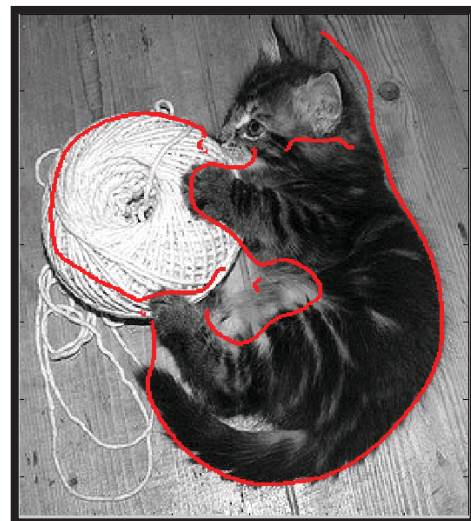
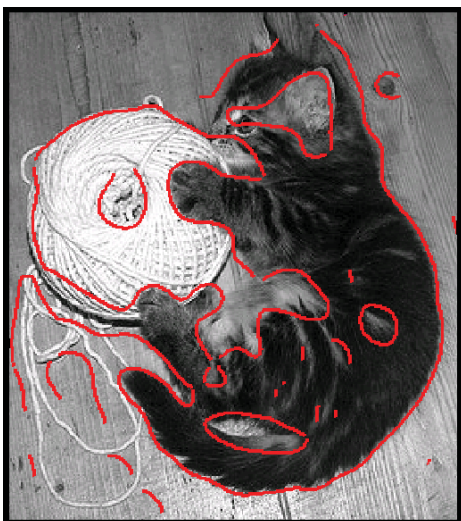
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Canny Edge Detector:

 $\sigma = 10$  $\sigma = 20$ 

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Marr-Hildreth vs Canny at $\sigma=10$



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From Edge Pixels to Edges

- Have candidate edge pixels
- Have information on edge direction and strength
- Want connected edges:

Edge growing

- Going from individual edge pixels, to entire, connected edges – curves that are boundaries of objects

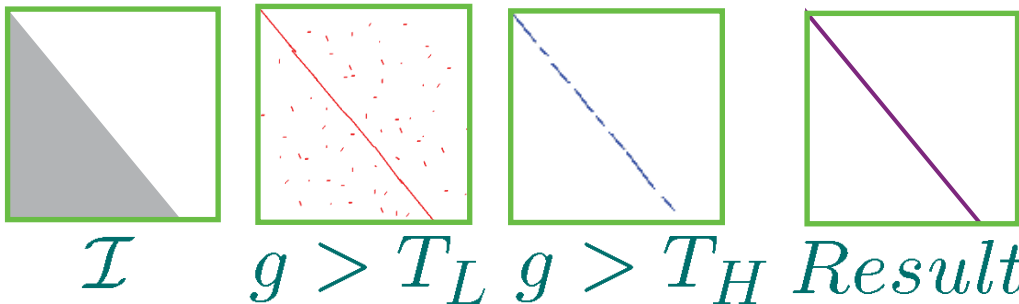
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Edge Growing

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Edge Thresholding with Hysteresis

- Edge strength image, two thresholds T_H & T_L
- Only edges have points $g > T_H$
- Edges have all points $g > T_L$
- Start at point $g > T_H$, and trace connected points with $g > T_L$



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Edge Relaxation

- Use context to resolve ambiguity (as in segmentation)

$g(i)$: Edge strength at pixel i

$\underline{e}(i)$: Edge direction at pixel i

Normalise edge strengths $g(i) \Rightarrow P(\underline{e}, i) \leq 1$

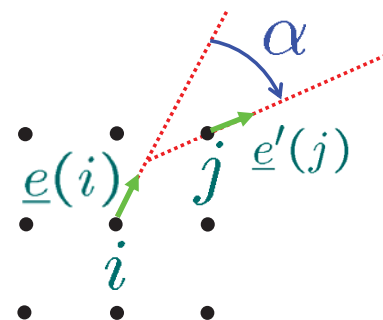
- Compatibility

Pixels i and j ,

edge directions \underline{e} and \underline{e}' :

$c_{i,j}(\underline{e}, \underline{e}') = 0$ not neighbours

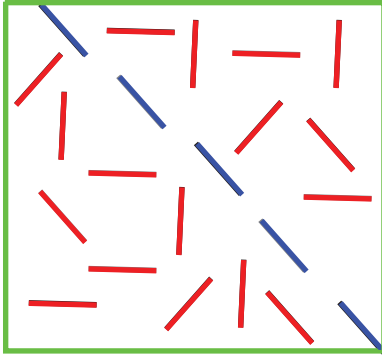
$c_{i,j}(\underline{e}, \underline{e}') = |\cos(\alpha)|$



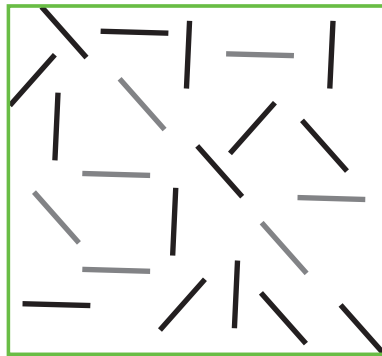
- As before, update probabilities based on support

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Edge Relaxation

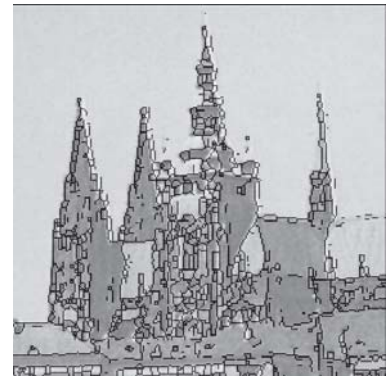
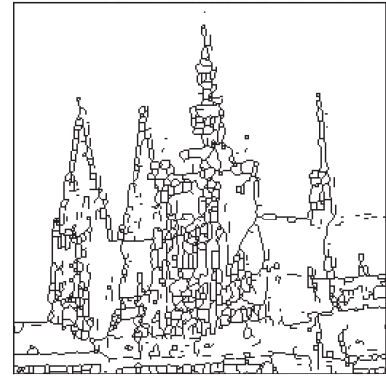


weak and strong edges



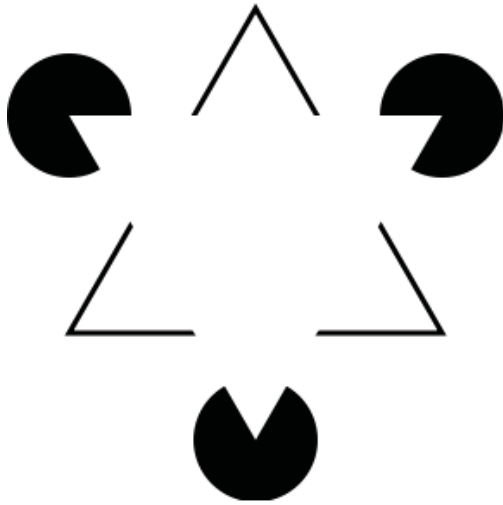
- Supporting each other
- Many refinements and alternatives in the literature, but all applying same basic ideas

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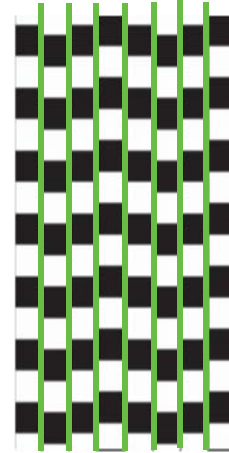


Hough Transform

Aside: Lines in human vision



See lines where we have only minimal information



Actually straight, but we don't see them as that!

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Hough Transform (1)

- Have some set of points, parts of edges etc
- Want to put them together into continuous lines
- Strategy:
 - Transform to parameter space
 - Let points vote for lines that could pass through them
 - Look for clusters
- Finding the right parameter space
- Can be extended if you can find such a space for shape of interest

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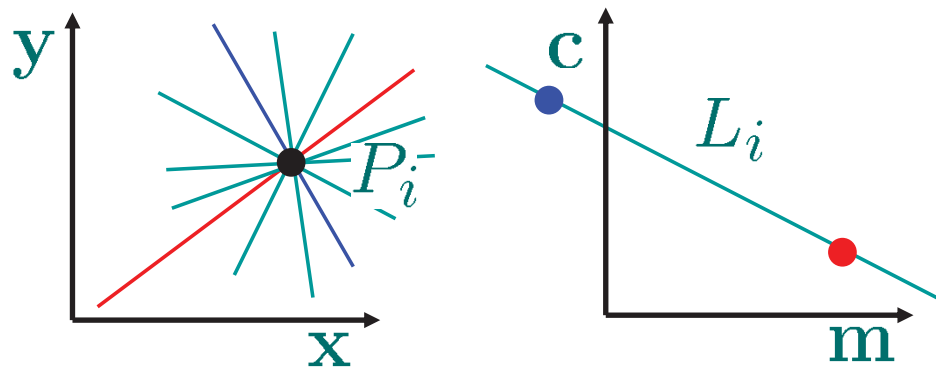
Hough Transform (2)

Set of points $\{P_i = (x_i, y_i)\}$ in image plane.

Any and all straight lines thro' P_i :

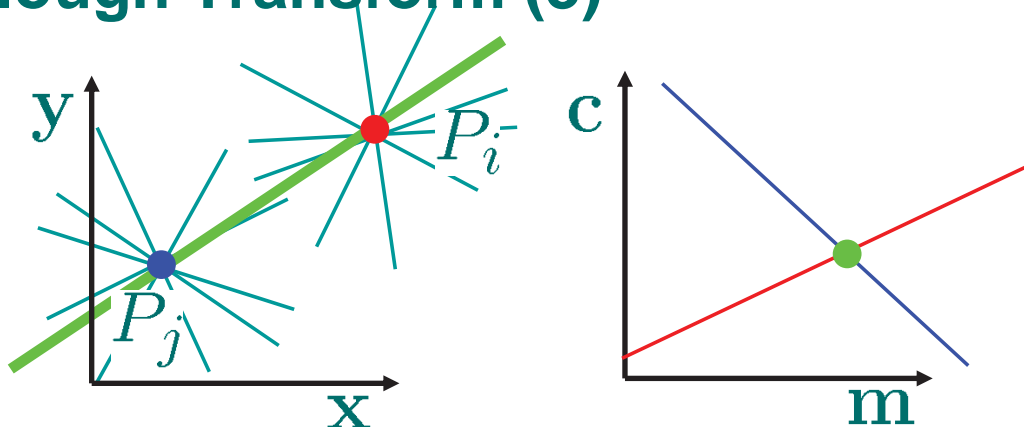
$$y_i = mx_i + c \Rightarrow c = -x_i m + y_i$$

L_i : line in (c, m) plane, intercept y_i , gradient $-x_i$



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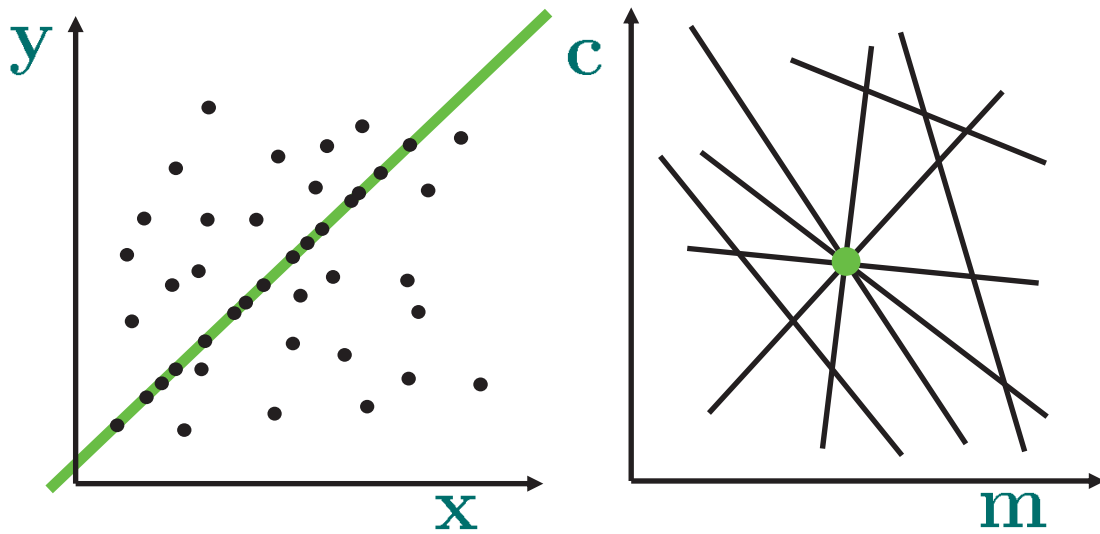
Hough Transform (3)



- Repeat for all points $\{P_i = (x_i, y_i)\}$ in image plane
- Look for points in (c, m) plane where lots of lines cross
- Lines which pass thro' lots of points in image plane

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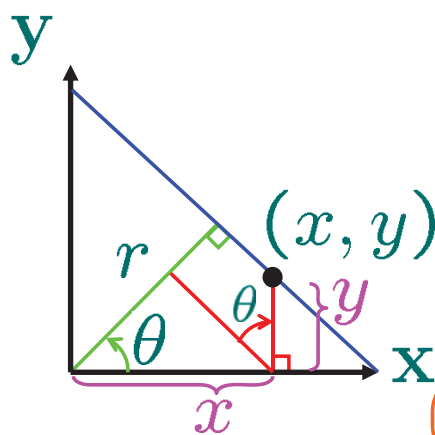
Hough Transform (4)



- **Verticals, m is infinite! Need better parameter space**

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Hough Transform (5)



$$y = mx + c$$

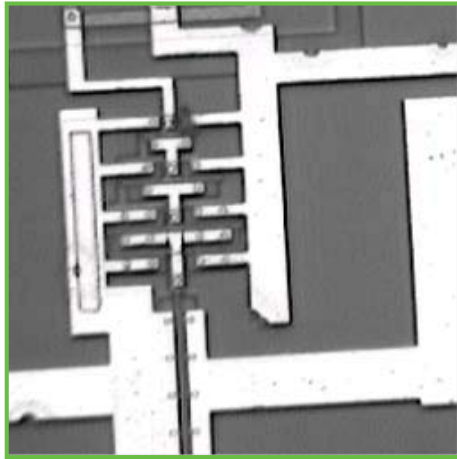
$$(c, m) \Rightarrow (r, \theta)$$

$$r = x \cos \theta + y \sin \theta$$

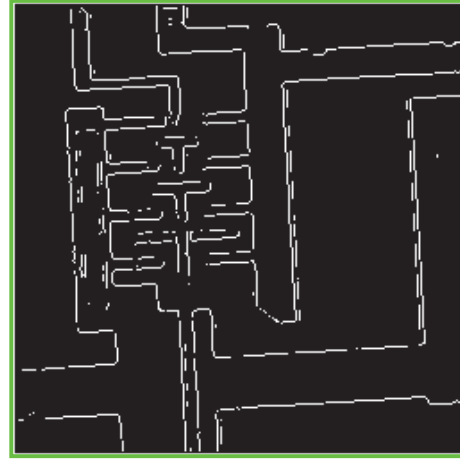
- Single point $P_i = (x_i, y_i)$
- All possible θ : allowed values of r , sinusoid curve
- Extend to other than lines, generalised Hough transform

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Example: Integrated Circuit



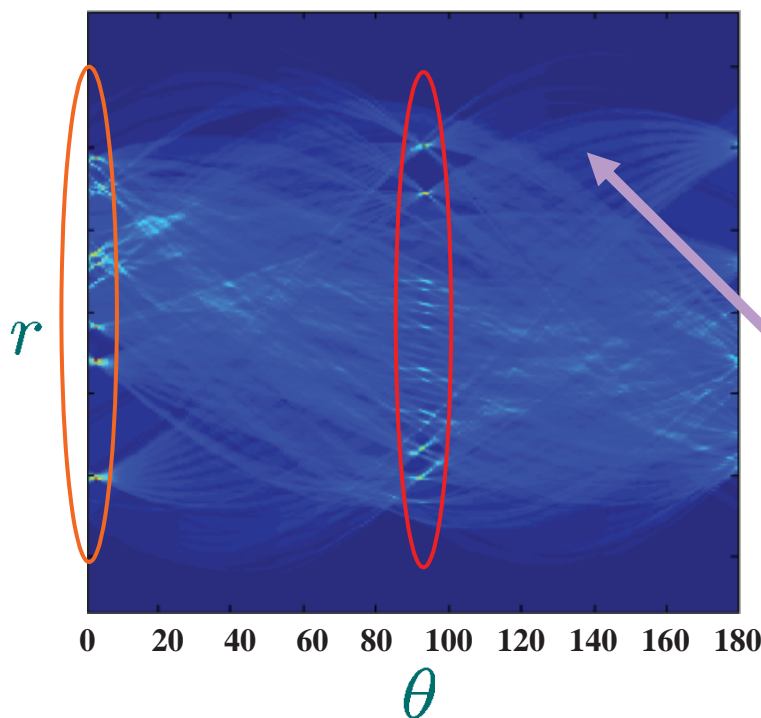
Image



Edge Pixels

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Example: Integrated Circuit



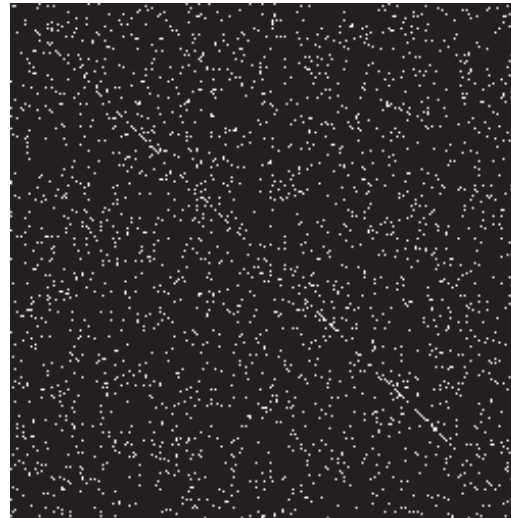
Each edge pixel
= 1 sinusoid
Each peak
= 1 line in image
Set of peaks at
approx 90°
Another at
approx 0°

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Example: Finding Lines under Noise



Broken Line

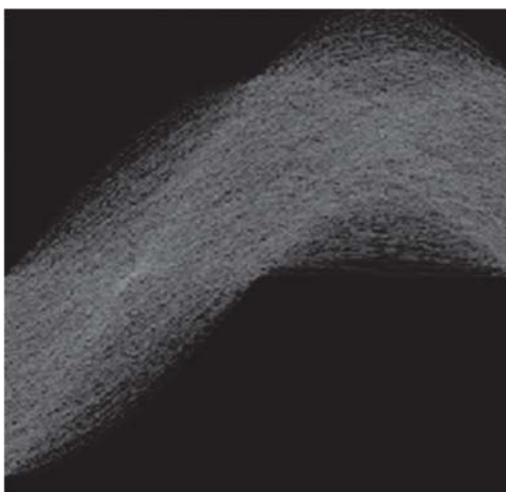


Hidden under noise

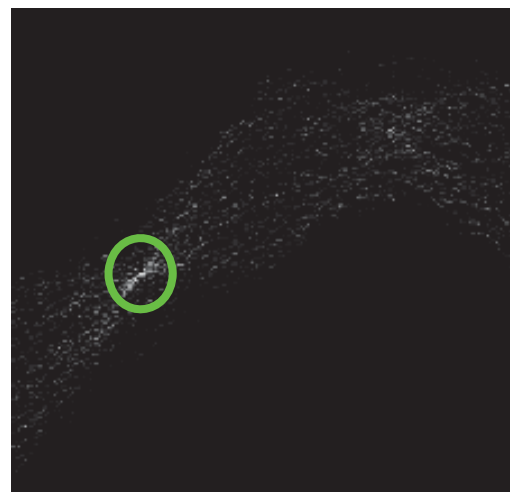
Edge Strength Image

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Example: Finding Lines under Noise



Hough Space



...thresholded

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Summary:

● Edges and Derivatives

- Convolution and filters (first & second derivatives, **gaussians**)

● Edges and Scale

- Physical edges persist across scales

● Edge Detection

- Problems with noise, and **accurate edge location**
- Non-maximum suppression

● Edge Growing

- **Thresholding** with hysteresis
- **Edge relaxation**

● Hough Transform

- Finding lines/circles etc even when occluded

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