

# MFE 409 LECTURE 6

## LIQUIDITY RISK

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Spring 2019



# LECTURE OBJECTIVES

- Market liquidity
- Funding liquidity
- How to measure them?
- Liquidity crises

# LIQUIDITY

- Liquidity: ability to make payments when they are due
- Two dimensions to liquidity:
  - ① **Market liquidity**, or trading liquidity
  - ② **Funding liquidity**
- The two dimensions interact

# OUTLINE

① MARKET LIQUIDITY

② FUNDING LIQUIDITY

③ LIQUIDITY CRISES

# MARKET LIQUIDITY

- **Market liquidity:** Ability to sell an asset on short notice
- Price received for an asset depends on:
  - ▶ Mid-market price

# MARKET LIQUIDITY

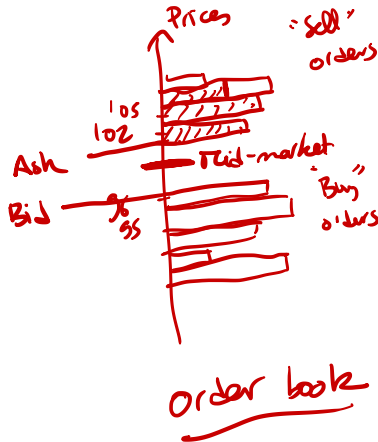
- **Market liquidity:** Ability to sell an asset on short notice
- Price received for an asset depends on:
  - ▶ Mid-market price
  - ▶ How much is to be sold
  - ▶ How quickly it is to be sold
  - ▶ The economic environment

# BID-ASK SPREAD

$Ask > Bid$

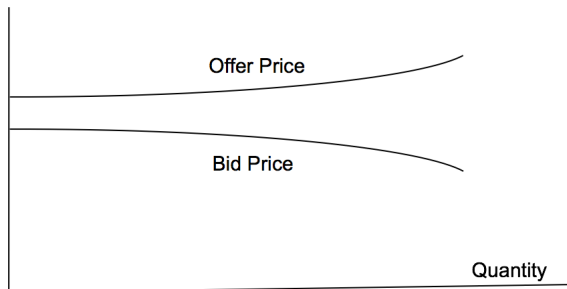
- Ask price (or offer price): price at which one can buy
- Bid price: price at which one can sell

limit orders  
market orders



# BID-ASK SPREAD

- Ask price (or offer price): price at which one can buy
- Bid price: price at which one can sell
- Role of *size*





# COST OF LIQUIDATION

- Proportional bid-ask spread:

$$s = \frac{\text{Ask Price} - \text{Bid Price}}{\text{Mid-market Price}}$$

$= \frac{\text{Bid} + \text{Ask}}{2}$

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$$\sum_{i=1}^n \frac{1}{2} |\alpha_i| s_i$$

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- Stressed conditions: replace  $s_i$  by extreme historical value, e.g. 1% largest

- *Liquidity-adjusted VaR*: If portfolio is likely liquidated in extreme bad performance, add liquidation cost to VaR calculation

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- Role of *time*

- ▶ Example: selling a house tomorrow vs over the next month

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- Trade-off for executing a trade:

- ▶ Selling slowly avoids large trading costs
- ▶ Selling slowly increases the risk of adverse price movement

# OPTIMAL EXECUTION

- You want to sell  $S$  shares over the next  $n$  days
- The bid-ask difference is  $p(q)$  where  $q$  is the quantity sold on that day
- The daily standard deviation of ~~returns~~ <sup>change in price</sup> is  $\sigma$
- Formalize the problem of optimal execution

$$\min_{\{q_t\}_{t=1}^n} \sum_{t=1}^n p(q_t) |q_t| + \lambda \sqrt{\sum_{t=1}^n x_t^2 \sigma^2}$$

$x_t$ : how much I hold at the beginning of date  $t$

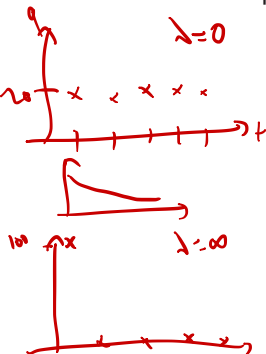
such that  $\sum_{t=1}^n q_t = S$

$$x_1 = S$$
$$x_{t+1} = x_t - q_t$$

- Solve it for  $p(q) = 0.1 + 0.05 \exp(0.03 \times q)$ ,  $S = 100$ ,  $n = 5$ ,  $\sigma = 0.1$

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$$\min_{\{q_t\}} \lambda \sqrt{\sum_{t=1}^n \sigma^2 x_t^2} + \sum_{t=1}^n \frac{1}{2} |q_t| p(q_t)$$

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- Fire sales are difficult to tell apart from justified low prices
  - ▶ Chodorow-Reich, Ghent, Haddad (2016): *Asset insulators*: Valuation of institutions that sit out the fire sale should not respond to the drop in prices

# OUTLINE

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- **Funding liquidity:** Ability to maintain sources of funding for running the firm's activities
- Sources of funding liquidity:
  - ▶ Cash and Treasury holdings
  - ▶ Ability to borrow
  - ▶ Retail and wholesale deposits
  - ▶ Central bank borrowing

# QUANTIFYING LIQUIDITY RISK

- Difficult to quantify liquidity risk
- Some measures from Basel III:
  - ▶ *Liquidity coverage ratio*: designed to make sure that the bank can survive a 30-day period of acute stress
  - ▶ *Net stable funding ratio*: a longer term measure designed to ensure that stability of funding sources is consistent with the permanence of the assets that have to be funded

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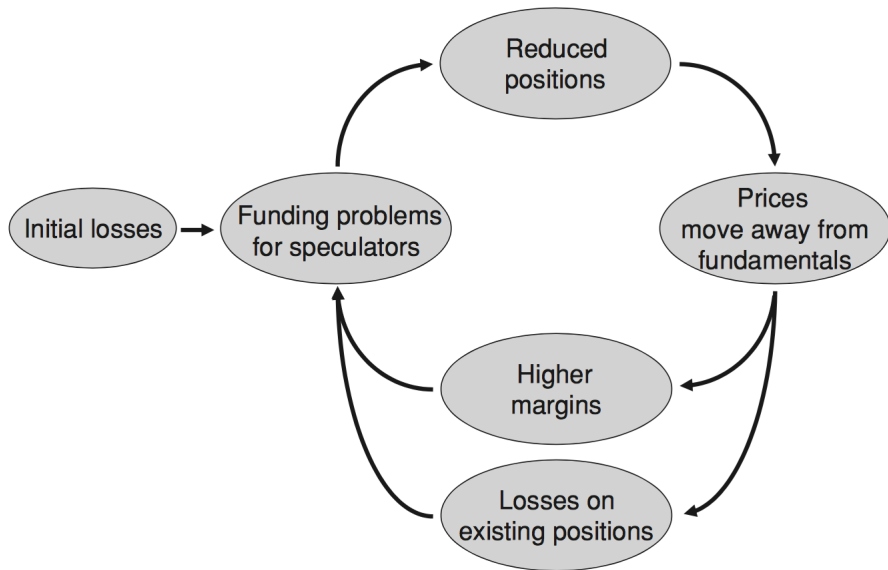
- In a simple view of markets, trading stabilizes prices
  - ▶ If somebody gets in trouble and has to liquidate some assets ...
  - ▶ Somebody else sees this as a buying opportunity
  - ▶ *Negative feedback trading*: price drop creates buying, which pushes price up



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- But market frictions can lead to unstable prices: positive feedback trading
  - ▶ Remember LTCM

# LIQUIDITY SPIRALS



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  - ▶ Understand behavior of other participants in the markets: if everybody does the same thing, everybody will fall at the same time

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- Even risk management regulations could generate liquidity crises!

# TAKEAWAYS

- Liquidity problems can prevent ability to run a strategy or a business
- Stem from limited ability to:
  - ▶ Sell assets: market liquidity
  - ▶ Borrow to finance trade: funding liquidity
  - ▶ Both
- Liquidity risk is difficult to quantify ...
- But being aware of sources of liquidity and market environment can help