# Computing for Mathematics: Week 1

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$$\begin{pmatrix} (0,0) & (-1,1) & (1,-1) \\ (1,-1) & (0,0) & (-1,1) \\ (1,-1) & (-1,1) & (0,0) \end{pmatrix}$$

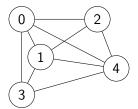
http://thefightclub.herokuapp.com/

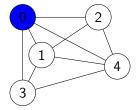
http://jayrobertvos.pythonanywhere.com/

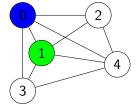
### Programming and Mathematics

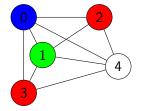
There are various areas in which computers are of major importance to Mathematicians:

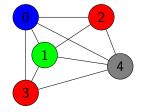
- Computer assisted proofs;
- Implementation of mathematics;
- Computer generated proofs;
- Everyday mathematics.



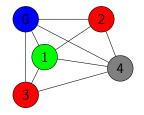








→ '4 colour theorem': Any map can be coloured using 4 colours.



- '4 colour theorem': Any map can be coloured using 4 colours.
- ► Proved in 1976 by Kenneth Appel and Wolfgang Haken:

  Used computers to check 1936 particular cases.

#### Risk boards



How to pack 3 dimensional spheres?

- ▶ In 1611 Kepler conjectured the best possible way.
- Proof in 1998 by Hales which involved a computer to minimize a function of 150 variables (100,000 times).
- Also involved a 100 page paper for the 'non computer assisted aspects'.

#### How to pack 3 dimensional spheres?

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- ▶ Proof in 1998 by Hales which involved a computer to minimize a function of 150 variables (100,000 times).
- ► **Also** involved a 100 page paper for the 'non computer assisted aspects'.
- ▶ Referees are 99% sure.

### Implementation of mathematics

Here at Cardiff Dr Leanne Smith studied the best way to locate ambulances in Wales. This took in to account:

- Queues;
- Survival probabilities of patients;
- ► Time of the day...

Once the mathematics was done a computer program was built to be able to demonstrate to the Welsh Ambulance Trust.

Timothy Gowers

#### Timothy Gowers

Theorem: Let X and Y be sets, let  $f: X \to Y$  be an injection and let A and B be subsetsof X. Then  $f(A) \cap f(B) \subset f(A \cap B)$ .

#### Timothy Gowers

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Proof: Take  $x \in f(A) \cap f(B)$ . So there is some  $y \in A$  and  $z \in B$  such that f(y) = f(z) = x. As f is injective, y and z are equal. So  $y \in A \cap B$ . So  $x = f(y) \in f(A \cap B)$ .

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The above is an example of a computer generated proof. You do not need to know any of this!

# **Everyday mathematics**

Everyday mathematicians might need to calculate an integral for a bigger project. This is some Sage code to calculate an integral:

1 integrate 
$$(x ^3, x)$$

which returns:

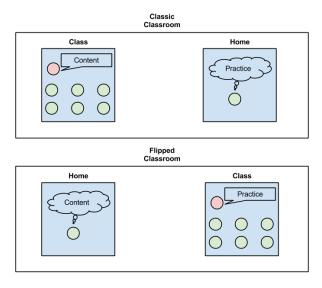
$$\frac{x^4}{4}$$

#### What we will learn

- ▶ Python: general purpose programming language (Weeks 1-5).
- ► Sage: mathematics package (based on Python) (Weeks 5-9).
- ► LATEX: a package for writing mathematics (Week 10).

# Flipped classrooms

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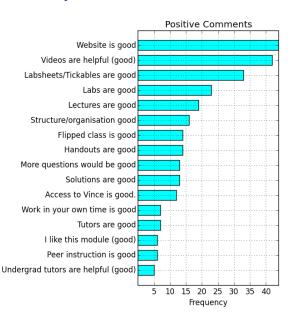
#### Labs and 'Tickables'

- Every week you have 2 computer lab sessions.
- ➤ You have until the end of the second lab session to complete all exercises marked as 'TICKABLE'.
- ▶ You will need to work on these outside of the lab sessions.

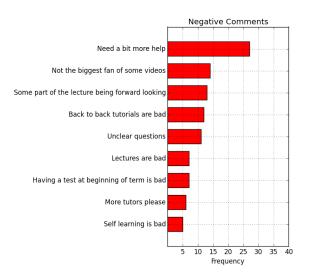
#### Resources

http://vknight.org/Computing\_for\_mathematics/

#### Feedback from last year



### Feedback from last year



"No matter how difficult the lab sheets are, it always feels like there is sufficient support, either from Vince or from various online resources."

"Only one video tutorial is given providing only one angle"	

"Would like to know about all assessment from the start, class test was only recently revealed and don't know much about the remaining 45%"

- ► Class test: Week 6 40%
- ► Individual Coursework: Week 11 30%

► Group Coursework: Spring semester - 30%

http://cardiffmathematicscodeclub.github.io/

