

CARRERA:

Ingeniería de sistemas

ASIGNATURA:

Métodos numéricos

FECHA DE ENTREGA: 12/05/2023

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Para cada uno de los problemas, halla la solución del sistema de ecuaciones mediante:

1. Método de la inversa, de forma manual y con MatLab.

Problema 1

$$\begin{aligned} 10x_1 + x_2 + 2x_3 &= 3 \\ 4x_1 + 6x_2 - x_3 &= 9 \\ -2x_1 + 3x_2 + 8x_3 &= 51 \end{aligned}$$

The screenshot shows the MATLAB environment. The Editor window displays the following code:

```

1 clc, clear all;
2 fprintf('\t\tMETODO DE LA INVERSA\n')
3 fprintf('Los datos son:\n')
4 A = [10 1 2; 4 6 -1; -2 3 8]
5 B = [3; 9; 51]
6 %C = [5 4; 1 2]
7 %D = [3 2; -2 -5]
8 %X = C+D %suma de matrices
9 %X = C*D %multiplicacion de matrices
10 %trace(A)
11 %det(A)
12 %inv(A)
13 %poly(A)
14 %eig(A)
15 %RESULTADO = inv(A)*B
16 det_A = det(A)
17 if det_A==0
18     fprintf('El sistema no tiene solucion')
19 else
20     fprintf('La solucion es: \n')

```

The Command Window shows the output of the code:

```

10    1    2
 4    6   -1
-2    3    8

B =

     3
     9
    51

det_A =

    528

La solucion es:
   -1
     3
     5

```

```

METODO DE LA INVERSA
Los datos son:

A =

    10     1     2
     4     6    -1
    -2     3     8

B =

     3
     9
    51

det_A =

    528|

La solucion es:

    -1
     3
     5

```

2. Método de Gauss Jordan, de forma manual y con MatLab.

Problema 2

$$\begin{aligned}
 -3x_1 + 5x_2 + 2x_3 &= 7 \\
 -x_1 - 2x_2 + 3x_3 &= -4 \\
 9x_1 - 15x_2 - 6x_3 &= 0
 \end{aligned}$$

```
Shortcuts How to Add What's New
Editor - C:\Users\huasc\Desktop\metodojordanaautomatico.m
Command Window

METODO DE GAUSS JORDAN

Los datos son:

A =

-3     5     2
-1    -2     3
 9   -15    -6

B =

 7
 4
 0

AU =

-3     5     2     7
-1    -2     3     4
 9   -15    -6     0

El sistema presente varias soluciones o no tiene solucion>>
```

```
METODO DE GAUSS JORDAN

Los datos son:

A =

-3     5     2
-1    -2     3
 9   -15    -6

B =

 7
 4
 0

AU =

-3     5     2     7
-1    -2     3     4
 9   -15    -6     0

El sistema presente varias soluciones o no tiene solucion>>
```

3. Método de Jacobi, con un error menor a 0.01, con Excel y MatLab.

Problema 3

$$\begin{aligned} 10x_1 + x_2 + 2x_3 - x_4 &= -3 \\ -5x_1 + 4x_2 + 6x_3 - x_4 &= 9 \\ -2x_2 + 3x_3 + 8x_4 &= 2 \\ -5x_3 + 5x_4 &= -1 \end{aligned}$$

NOTA. No es ni es posible hacerse una matriz diagonalmente dominante para A[2,2], por lo que el proceso puede ser divergente. Por ende, no es recomendable usar métodos iterativos como Jacobi.

```

clc, clear all;
%Metodo jacobi
fprintf('Método de Jacobi para sistemas de ecuaciones\n')
fprintf('Damos\n')
A = [10 1 2 -1;-5 4 6 -1;0 0 -5 5;0 -2 3 8]
B = [-3;9;-1;2]
iter_max = 100;
errmax = 0.01;
n=size(A,1);
X = zeros(1,n);
err1 = inf;
err = 0;
iter = 0;
fprintf('e_std = %1.2f\n',errmax)
fprintf('iter   x_1   x_2   x_3   x_4   e_a\n')
fprintf('-----\n')
while err1>errmax && iter<iter_max
    X_old = X;
    X = zeros(1,n);
    for i=1:n
        X(i) = (B(i) - sum(A(i,:).*X_old))/A(i,i);
    end
    err1 = max(abs(X - X_old));
    iter = iter + 1;
    fprintf('%2.0f %8.4f %8.4f %8.4f %8.4f %8.2f%%\n',iter,X,X_old,err1,errmax)
end

```

32	-0.4686	0.9798	0.5044	0.3043	0.44%
33	-0.4684	0.9838	0.5043	0.3058	0.49%
34	-0.4687	0.9844	0.5058	0.3068	0.33%
35	-0.4689	0.9822	0.5068	0.3064	0.23%
36	-0.4689	0.9802	0.5064	0.3055	0.31%
37	-0.4688	0.9806	0.5055	0.3051	0.19%
38	-0.4686	0.9821	0.5051	0.3056	0.16%
39	-0.4687	0.9829	0.5056	0.3061	0.17%
40	-0.4688	0.9823	0.5061	0.3061	0.10%
41	-0.4688	0.9814	0.5061	0.3058	0.11%
42	-0.4688	0.9812	0.5058	0.3056	0.08%
43	-0.4687	0.9817	0.5056	0.3056	0.05%
44	-0.4687	0.9822	0.5056	0.3058	0.07%
45	-0.4688	0.9821	0.5058	0.3059	0.04%
46	-0.4688	0.9818	0.5059	0.3058	0.04%
47	-0.4688	0.9816	0.5058	0.3057	0.04%
48	-0.4688	0.9817	0.5057	0.3057	0.02%
49	-0.4687	0.9819	0.5057	0.3058	0.03%
50	-0.4688	0.9820	0.5058	0.3058	0.02%
51	-0.4688	0.9818	0.5058	0.3058	0.01%
52	-0.4688	0.9817	0.5058	0.3058	0.02%
53	-0.4688	0.9817	0.5058	0.3058	0.01%

Método de Jacobi para sistemas de ecuaciones

Datos

A =

10	1	2	-1
-5	4	6	-1
0	0	-5	5
0	-2	3	8

B =

-3
9
-1
2

e_std = 0.01

iter	x_1	x_2	x_3	x_4	e_a
0	0.0000	0.0000	0.0000	0.0000	Inf%
1	-0.3000	2.2500	0.2000	0.2500	100.00%
2	-0.5400	1.6375	0.4500	0.7375	66.10%
3	-0.4800	1.0844	0.9375	0.4906	52.00%
4	-0.5469	0.3664	0.6906	0.1695	195.95%
5	-0.4578	0.5729	0.3695	0.0826	105.20%
6	-0.4229	1.1441	0.2826	0.2546	67.56%
7	-0.4455	1.3611	0.4546	0.4300	40.79%
8	-0.4840	1.1187	0.6300	0.4198	27.84%
9	-0.4959	0.8048	0.6198	0.2934	43.07%
10	-0.4751	0.7738	0.4934	0.2188	34.10%
11	-0.4542	0.9707	0.4188	0.2584	20.28%
12	-0.4550	1.1187	0.4584	0.3356	23.00%
13	-0.4700	1.0775	0.5356	0.3578	14.41%
14	-0.4791	0.9485	0.5578	0.3185	13.60%
15	-0.4746	0.8941	0.5185	0.2780	14.59%
16	-0.4653	0.9485	0.4780	0.2791	8.49%
17	-0.4625	1.0212	0.4791	0.3079	9.36%
18	-0.4671	1.0302	0.5079	0.3256	5.67%
19	-0.4720	0.9856	0.5256	0.3171	4.52%
20	-0.4720	0.9508	0.5171	0.2993	5.94%
21	-0.4686	0.9592	0.4993	0.2938	3.56%
22	-0.4664	0.9888	0.4938	0.3026	2.99%
23	-0.4674	1.0020	0.5026	0.3120	3.03%

24	-0.4695	0.9899	0.5120	0.3120	1.85%
25	-0.4702	0.9731	0.5120	0.3055	2.15%
26	-0.4692	0.9706	0.5055	0.3013	1.40%
27	-0.4680	0.9806	0.5013	0.3031	1.03%
28	-0.4680	0.9889	0.5031	0.3072	1.33%
29	-0.4688	0.9871	0.5072	0.3086	0.81%
30	-0.4693	0.9804	0.5086	0.3066	0.69%
31	-0.4691	0.9772	0.5066	0.3044	0.72%
32	-0.4686	0.9798	0.5044	0.3043	0.44%
33	-0.4684	0.9838	0.5043	0.3058	0.49%
34	-0.4687	0.9844	0.5058	0.3068	0.33%
35	-0.4689	0.9822	0.5068	0.3064	0.23%
36	-0.4689	0.9802	0.5064	0.3055	0.31%
37	-0.4688	0.9806	0.5055	0.3051	0.19%
38	-0.4686	0.9821	0.5051	0.3056	0.16%
39	-0.4687	0.9829	0.5056	0.3061	0.17%
40	-0.4688	0.9823	0.5061	0.3061	0.10%
41	-0.4688	0.9814	0.5061	0.3058	0.11%
42	-0.4688	0.9812	0.5058	0.3056	0.08%
43	-0.4687	0.9817	0.5056	0.3056	0.05%
44	-0.4687	0.9822	0.5056	0.3058	0.07%
45	-0.4688	0.9821	0.5058	0.3059	0.04%
46	-0.4688	0.9818	0.5059	0.3058	0.04%
47	-0.4688	0.9816	0.5058	0.3057	0.04%
48	-0.4688	0.9817	0.5057	0.3057	0.02%
49	-0.4687	0.9819	0.5057	0.3058	0.03%
50	-0.4688	0.9820	0.5058	0.3058	0.02%
51	-0.4688	0.9818	0.5058	0.3058	0.01%
52	-0.4688	0.9817	0.5058	0.3058	0.02%
53	-0.4688	0.9817	0.5058	0.3058	0.01%

Los rasultados son:

X_1: -0.4688

X_2: 0.9817

X_3: 0.5058

X_4: 0.3058>>

Método de Jacobi									
Datos									
$10x_1$	$+x_2$	$+2x_3$	$-x_4 = -3$	$x_1 =$	$(-3-1*x_2-2*x_3+x_4)/10$		C.S.=		4
$-5x_1$	$+4x_2$	$+6x_3$	$-x_4 = 9$	$x_2 =$	$(9-4*x_1-6*x_3+1*x_4)/-5$		e_std=		0.01%
$0x_1$	$+0x_2$	$-5x_3$	$+5x_4 = -1$	$x_3 =$	$(-1-0*x_1-0*x_2-5*x_4)/-5$				
$0x_1$	$-2x_2$	$+3x_3$	$+8x_4 = 2$	$x_4 =$	$(2+0*x_1+2*x_2-3*x_3)/8$				
[A] no es estrictamente diagonal dominante por la fila 2, verificada por nosotros									

iter	x_1	x_2	x_3	x_4	E_a	E_a<E_std	e_a	e_a<e_std
0	0.0000	0.0000	0.0000	0.0000				
1	-0.3000	2.2500	0.2000	0.2500	2.2500	sigla iterando	100.000%	sigla iterando
2	-0.5400	1.6375	0.4500	0.7375	0.6610	sigla iterando	66.102%	sigla iterando
3	-0.4800	1.0844	0.9375	0.4906	0.5200	sigla iterando	52.000%	sigla iterando
4	-0.5469	0.3664	0.6906	0.1695	1.9595	sigla iterando	195.949%	sigla iterando
5	-0.4578	0.5729	0.3695	0.0826	1.0520	sigla iterando	105.201%	sigla iterando
6	-0.4229	1.1441	0.2826	0.2546	0.6756	sigla iterando	67.555%	sigla iterando
7	-0.4455	1.3611	0.4546	0.4300	0.4079	sigla iterando	40.787%	sigla iterando
8	-0.4840	1.1187	0.6300	0.4198	0.2784	sigla iterando	27.840%	sigla iterando
9	-0.4959	0.8048	0.6198	0.2934	0.4307	sigla iterando	43.067%	sigla iterando
10	-0.4751	0.7738	0.4934	0.2188	0.3410	sigla iterando	34.105%	sigla iterando
11	-0.4542	0.9707	0.4188	0.2584	0.2028	sigla iterando	20.284%	sigla iterando
12	-0.4550	1.1187	0.4584	0.3356	0.2300	sigla iterando	23.004%	sigla iterando
13	-0.4700	1.0775	0.5356	0.3578	0.1441	sigla iterando	14.414%	sigla iterando
14	-0.4791	0.9485	0.5578	0.3185	0.1360	sigla iterando	13.603%	sigla iterando
15	-0.4746	0.8941	0.5185	0.2780	0.1459	sigla iterando	14.591%	sigla iterando
16	-0.4653	0.9485	0.4780	0.2791	0.0849	sigla iterando	8.485%	sigla iterando
17	-0.4625	1.0212	0.4791	0.3079	0.0936	sigla iterando	9.358%	sigla iterando
18	-0.4671	1.0302	0.5079	0.3256	0.0567	sigla iterando	5.673%	sigla iterando
19	-0.4720	0.9856	0.5256	0.3171	0.0452	sigla iterando	4.519%	sigla iterando
20	-0.4720	0.9508	0.5171	0.2993	0.0594	sigla iterando	5.944%	sigla iterando
21	-0.4686	0.9592	0.4993	0.2938	0.0356	sigla iterando	3.563%	sigla iterando
22	-0.4664	0.9888	0.4938	0.3026	0.0299	sigla iterando	2.991%	sigla iterando
23	-0.4674	1.0020	0.5026	0.3120	0.0303	sigla iterando	3.032%	sigla iterando
24	-0.4695	0.9899	0.5120	0.3120	0.0185	sigla iterando	1.848%	sigla iterando
25	-0.4702	0.9731	0.5120	0.3055	0.0215	sigla iterando	2.146%	sigla iterando
26	-0.4692	0.9706	0.5055	0.3013	0.0140	sigla iterando	1.398%	sigla iterando
27	-0.4680	0.9806	0.5013	0.3031	0.0103	sigla iterando	1.027%	sigla iterando
28	-0.4680	0.9889	0.5031	0.3072	0.0133	sigla iterando	1.333%	sigla iterando
29	-0.4688	0.9871	0.5072	0.3086	0.0081	sigla iterando	0.808%	sigla iterando
30	-0.4693	0.9804	0.5086	0.3066	0.0069	sigla iterando	0.691%	sigla iterando
31	-0.4691	0.9772	0.5066	0.3044	0.0072	sigla iterando	0.724%	sigla iterando
32	-0.4686	0.9798	0.5044	0.3043	0.0044	sigla iterando	0.437%	sigla iterando
33	-0.4684	0.9838	0.5043	0.3058	0.0049	sigla iterando	0.487%	sigla iterando
34	-0.4687	0.9844	0.5058	0.3068	0.0033	sigla iterando	0.325%	sigla iterando
35	-0.4689	0.9822	0.5068	0.3064	0.0023	sigla iterando	0.231%	sigla iterando
36	-0.4689	0.9802	0.5064	0.3055	0.0031	sigla iterando	0.308%	sigla iterando
37	-0.4688	0.9806	0.5055	0.3051	0.0019	sigla iterando	0.186%	sigla iterando
38	-0.4686	0.9821	0.5051	0.3056	0.0016	sigla iterando	0.158%	sigla iterando
39	-0.4687	0.9829	0.5056	0.3061	0.0017	sigla iterando	0.168%	sigla iterando
40	-0.4688	0.9823	0.5061	0.3061	0.0010	sigla iterando	0.101%	sigla iterando
41	-0.4688	0.9814	0.5061	0.3058	0.0011	sigla iterando	0.111%	sigla iterando
42	-0.4688	0.9812	0.5058	0.3056	0.0008	sigla iterando	0.077%	sigla iterando
43	-0.4687	0.9817	0.5056	0.3056	0.0005	sigla iterando	0.052%	sigla iterando
44	-0.4687	0.9822	0.5056	0.3058	0.0007	sigla iterando	0.071%	sigla iterando
45	-0.4688	0.9821	0.5058	0.3059	0.0004	sigla iterando	0.043%	sigla iterando
46	-0.4688	0.9818	0.5059	0.3058	0.0004	sigla iterando	0.036%	sigla iterando
47	-0.4688	0.9816	0.5058	0.3057	0.0004	sigla iterando	0.039%	sigla iterando
48	-0.4688	0.9817	0.5057	0.3057	0.0002	sigla iterando	0.024%	sigla iterando
49	-0.4687	0.9819	0.5057	0.3058	0.0003	sigla iterando	0.025%	sigla iterando
50	-0.4688	0.9820	0.5058	0.3058	0.0002	sigla iterando	0.018%	sigla iterando
51	-0.4688	0.9818	0.5058	0.3058	0.0001	sigla iterando	0.012%	sigla iterando
52	-0.4688	0.9817	0.5058	0.3058	0.0002	sigla iterando	0.016%	sigla iterando
53	-0.4688	0.9817	0.5058	0.3058	0.0001	valor verdadero	0.010%	valor verdadero
54	-0.4688	0.9818	0.5058	0.3058	0.0001	valor verdadero	0.008%	valor verdadero
55	-0.4688	0.9819	0.5058	0.3058	0.0001	valor verdadero	0.009%	valor verdadero

4. Método de Gauss Seidel, con un error menor a 0.01, con Excel y MatLab.

Problema 4

$$\begin{aligned}x_1 + x_2 &= 3 \\ -2x_1 + 3x_2 - 4x_3 &= 3 \\ 3x_1 - x_2 + 2x_3 &= 3\end{aligned}$$

The screenshot shows a MATLAB script in the Editor window and its execution results in the Command Window.

Script Code:

```
clc,clear all;
fprintf('\n\t\t Método Gauss Seidel\n');
%Datos
fprintf('_____ \n')
fprintf('Datos:\n');
A=[3 -1 2;1 1 0;-2 3 -4]
B=[3;3;3]
iter_max=100;
e_max=0.0001;
fprintf('Error estandar: \tE_a = %.2f\n\n',e_max);
%inicializando
n=size(A,1);
x_new=zeros(1,n);
%x_new = [27 5 25 4]
iter = 0;
E_a = inf;%e absoluto
%Algoritmo
fprintf('_____ \n')

fprintf('La Solución es: \n')

while iter<iter_max && E_a>e_max
```

Command Window Output:

El método converge en 15 iteraciones.

y =

1.0000	1.0000	2.0000	0.2500	2.0000	100.0000
2.0000	1.5000	1.5000	-0.3750	0.6250	166.6667
3.0000	1.7500	1.2500	-0.6875	0.3125	45.4545
4.0000	1.8750	1.1250	-0.8438	0.1563	18.5185
5.0000	1.9375	1.0625	-0.9219	0.0781	8.4746
6.0000	1.9688	1.0313	-0.9609	0.0391	4.0650
7.0000	1.9844	1.0156	-0.9805	0.0195	1.9920
8.0000	1.9922	1.0078	-0.9902	0.0098	0.9862
9.0000	1.9961	1.0039	-0.9951	0.0049	0.4907
10.0000	1.9980	1.0020	-0.9976	0.0024	0.2447
11.0000	1.9990	1.0010	-0.9988	0.0012	0.1222
12.0000	1.9995	1.0005	-0.9994	0.0006	0.0611
13.0000	1.9998	1.0002	-0.9997	0.0003	0.0305
14.0000	1.9999	1.0001	-0.9998	0.0002	0.0153
15.0000	1.9999	1.0001	-0.9999	0.0001	0.0076

Los resultados son:

```
X_1: 1.9999
X_2: 1.0001
```

Método Gauss Seidel

Datos:

A =

3	-1	2
1	1	0
-2	3	-4

B =

3
3
3

Error estandar: E_a = 0.00

La Solución es:

El Método converge en 15 iteraciones.

y =

1.0000	1.0000	2.0000	0.2500	2.0000	100.0000
2.0000	1.5000	1.5000	-0.3750	0.6250	166.6667
3.0000	1.7500	1.2500	-0.6875	0.3125	45.4545
4.0000	1.8750	1.1250	-0.8438	0.1563	18.5185
5.0000	1.9375	1.0625	-0.9219	0.0781	8.4746
6.0000	1.9688	1.0313	-0.9609	0.0391	4.0650
7.0000	1.9844	1.0156	-0.9805	0.0195	1.9920
8.0000	1.9922	1.0078	-0.9902	0.0098	0.9862
9.0000	1.9961	1.0039	-0.9951	0.0049	0.4907
10.0000	1.9980	1.0020	-0.9976	0.0024	0.2447
11.0000	1.9990	1.0010	-0.9988	0.0012	0.1222
12.0000	1.9995	1.0005	-0.9994	0.0006	0.0611
13.0000	1.9998	1.0002	-0.9997	0.0003	0.0305
14.0000	1.9999	1.0001	-0.9998	0.0002	0.0153
15.0000	1.9999	1.0001	-0.9999	0.0001	0.0076

Los resultados son:

x_1: 1.9999

x_2: 1.0001

x_3: -0.9999

>> |

Método de Gauss Eidel									
Datos									
$3x_1$	$-x_2$	$+2x_3$	$= 3$	$x_1=$	$(3+1*x_2-2*x_3)/3$		C.S.=		4
x_1	$+x_2$	$+0x_3$	$= 3$	$x_2=$	$(3-1*x_1-0*x_3)/1$		e_std=		0.01%
$-2x_1$	$+3x_2$	$-4x_3$	$= 3$	$x_3=$	$(3+2*x_1-3*x_2)/-4$				

[A] es diagonal dominante verificada por nosotros

iter	x_1	x_2	x_3	E_a	E_a<E_std	e_a	e_a<e_std
0	0.0000	0.0000	0.0000				
1	1.0000	2.0000	0.2500	2.0000	siguiterando	100.000%	siguiterando
2	1.5000	1.5000	-0.3750	0.6250	siguiterando	166.667%	siguiterando
3	1.7500	1.2500	-0.6875	0.3125	siguiterando	45.455%	siguiterando
4	1.8750	1.1250	-0.8438	0.1563	siguiterando	18.519%	siguiterando
5	1.9375	1.0625	-0.9219	0.0781	siguiterando	8.475%	siguiterando
6	1.9688	1.0313	-0.9609	0.0391	siguiterando	4.065%	siguiterando
7	1.9844	1.0156	-0.9805	0.0195	siguiterando	1.992%	siguiterando
8	1.9922	1.0078	-0.9902	0.0098	siguiterando	0.986%	siguiterando
9	1.9961	1.0039	-0.9951	0.0049	siguiterando	0.491%	siguiterando
10	1.9980	1.0020	-0.9976	0.0024	siguiterando	0.245%	siguiterando
11	1.9990	1.0010	-0.9988	0.0012	siguiterando	0.122%	siguiterando
12	1.9995	1.0005	-0.9994	0.0006	siguiterando	0.061%	siguiterando
13	1.9998	1.0002	-0.9997	0.0003	siguiterando	0.031%	siguiterando
14	1.9999	1.0001	-0.9998	0.0002	siguiterando	0.015%	siguiterando
15	1.9999	1.0001	-0.9999	0.0001	valor verdad	0.008%	valor verdad