

# In situ evidence of resonant interactions between energetic electrons and whistler waves in magnetopause reconnection

Zhi Li<sup>1,2</sup>, QuanMing Lu<sup>1,2\*</sup>, RongSheng Wang, XinLiang Gao, and HuaYue Chen<sup>1,2</sup>

<sup>1</sup>Chinese Academy Sciences Key Laboratory of Geospace Environment, Department of Geophysics and Planetary Science, University of Science and Technology of China, Hefei 230026, China;

<sup>2</sup>Chinese Academy Sciences Center for Excellence in Comparative Planetology, Hefei 230026, China

**Abstract:** In this paper, we analyze one reconnection event observed by the Magnetospheric Multiscale (MMS) mission at the earth's magnetopause. In this event, the spacecraft crossed the reconnection current sheet from the magnetospheric side to the magnetosheath side, and whistler waves were observed on both the magnetospheric and magnetosheath sides. On the magnetospheric side, the whistler waves propagated quasi-parallel to the magnetic field and toward the X-line, while on the magnetosheath side they propagated almost anti-parallel to the magnetic field and away from the X-line. Associated with the enhancement of the whistler waves, we find that the fluxes of energetic electrons are concentrated around the pitch angle 90° when their energies are higher than the minimum energy that is necessary for the resonant interactions between the energetic electrons and whistler waves. This observation provides *in situ* observational evidence of resonant interactions between energetic electrons and whistler waves in the magnetic reconnection.

**Keywords:** magnetic reconnection; whistler waves; magnetosphere; energetic electrons

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## 1. Introduction

Magnetic reconnection is a fundamental physical process occurring when two plasmas with different magnetic field topologies interact to change the magnetic structure. This process can efficiently convert magnetic energy into plasma kinetic energy (Priest and Forbes, 2000; Fu HS et al., 2015; Treumann and Baumjohann, 2015; Yamada et al., 2010; Lu S et al., 2019), and is considered to be responsible for explosive energy releases in space environments, such as solar flares (Ciaravella and Raymond, 2008) and substorms in the earth's magnetosphere (Russell and McPherron, 1973). During magnetic reconnection, the magnetic field lines reconnect in a small region called the diffusion region, which includes both the ion diffusion region on the ion inertial length scale and the electron diffusion region on the electron inertial length scale (Birn et al., 2001; Lu QM et al., 2010). In the ion diffusion region, electrons are frozen in the magnetic field and ions can cross the magnetic field lines. In the electron diffusion region (EDR), both ions and electrons are unmagnetized. Magnetic reconnection is considered to be initiated in the electron diffusion region and can then be extended to a large scale (Vasyliunas et al., 1975).

Various types of plasma waves have been found to be associated with magnetic reconnection. Plasma waves can transfer mo-

mentum and energy among particles, which results in anomalous resistivity and formation of energetic particles (Ji et al., 2004; Zhou et al., 2014). Among these plasma wave, whistler waves have received special attention. The first *in situ* observational evidence of whistler waves was identified by Deng XH and Matsumoto (2001) in the diffusion region of a magnetopause reconnection event, and then Wei et al. (2007) found enhancement of whistler waves in Cluster observations made during a magnetotail reconnection event. Particle-in-cell simulation of anti-parallel reconnection revealed that whistler waves can be excited in the downstream of the electron outflow by electron temperature anisotropy (Fujimoto and Sydora, 2008) and in the separatrix region by an electron beam (Fujimoto, 2014). With Cluster observations, Huang SY et al. (2016, 2017) confirmed the existence of whistler waves in both the downstream of the electron outflow and the separatrix region by statistically analyzing the reconnection events in the magnetotail. Characteristics of whistler waves in asymmetric reconnection have also been thoroughly studied when satellites cross the magnetopause. In asymmetric reconnection, whistler waves have been observed in the separatrix region (Graham et al., 2016; Wilder et al., 2016; Li et al., 2018; Burch et al., 2018), as well as in the electron diffusion region (Tang XW et al., 2013; Cao D et al., 2017). Recently, with the launching of the Magnetospheric Multiscale (MMS) mission, taking advantage of its high resolution electron plasma data, Cao D et al. (2017) indicated that the whistler waves observed in magnetic reconnection are excited by electron temperature anisotropy. In this paper, based on MMS mission observations of a magnetopause reconnection event, we analyze in detail the distributions of pitch angles of energetic

Correspondence to: Q. M. Lu, qmlu@ustc.edu.cn

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electrons at different energies. Our findings provide *in situ* evidence of resonant interactions of energetic electrons and whistler waves in the separatrix regions of both the magnetospheric and the magnetosheath sides.

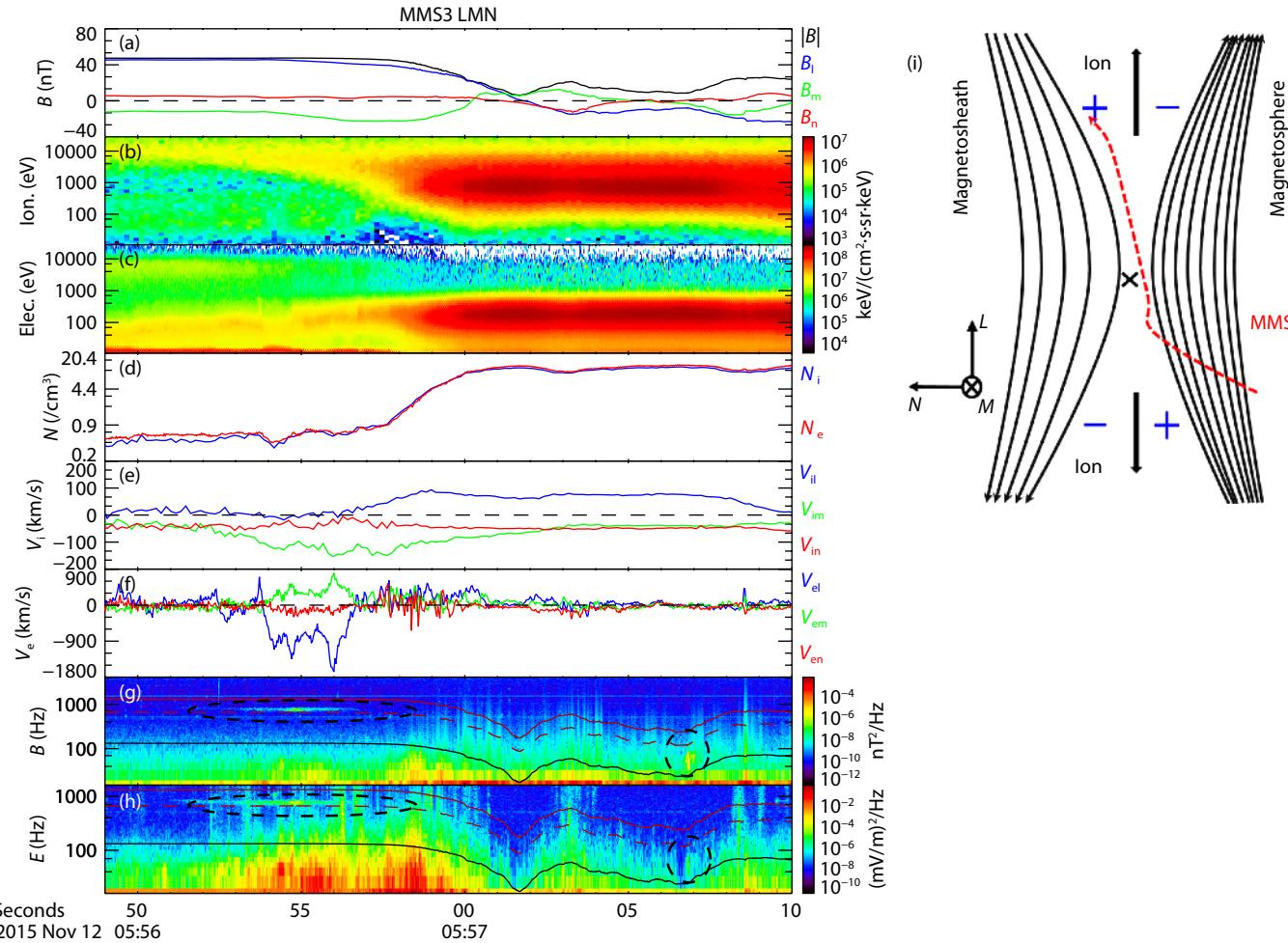
## 2. Observations of a Magnetopause Reconnection Event

NASA's MMS mission was launched in March 2015; its main goal is to study magnetic reconnection on the electron scale (Burch et al., 2016). The mission includes four spacecraft in an approximate tetrahedral formation. Each spacecraft measures particle data, electric field, and so on, at high temporal resolution. The present study uses measurements of the electric and magnetic fields and wave and particle data from the comprehensive locations of instruments onboard the MMS spacecraft (Burch et al., 2016). The magnetic field is sampled by Fluxgate Magnetometers at 128/s in the burst mode and 16/s in the fast survey mode (Russell et al., 2016, Torbert et al., 2016). The electric field is sampled by Electric Double Probes at 8192/s in the burst mode and 32/s in the fast survey mode (Ergun et al., 2016, Lindqvist et al., 2016). The tem-

poral resolutions of electron and ion data measured by the Fast Plasma Instrument are 30 ms and 150 ms, respectively (Pollock et al., 2016). The ion and electron distributions electrons with 4.5 s resolution in the fast survey mode are also provided by Fast Plasma Instruments. The energy range of the Fast Plasma Instrument is from 10 eV to 30 keV for both electrons and ions. The three magnetic components of waves are measured at 8192/s by Search Coil Magnetometers and are used to study whistler wave characteristics (Le Contel et al., 2016).

A magnetic reconnection event was observed by MMS from 05:56:44 to 05:57:11 UT on 12 November 2015, when the spacecraft was located at [11.3, 1.7, -1.3] Earth radius ( $R_E$ ) in the geocentric solar magnetospheric (GSM) coordinate system. Since the spacecraft separation was about 20 km during this time period, observations of this event at all four spacecraft were similar; we use only data from MMS3.

Figures 1(a–h) show an overview of this magnetopause reconnection event. The data are given in a local current sheet (LMN) coordinate system, which is determined from Minimum Variance Analysis (Sonnerup and Scheible, 1998) applied to the ambient



**Figure 1.** Overview of MMS3 observations in the burst mode during 05:56:44–05:57:11 UT on 12 November 2015. (a) Magnetic field vector in the LMN coordinate, (b–c) ion and electron energy spectra, (d) ion and electron number density, (e) ion bulk velocity in the LMN coordinate, (f) electron bulk velocity in the LMN coordinate, (g–h) magnetic and electric field power spectral density; the black solid lines, red dashed lines, and red solid lines correspond to 0.1, 0.5, and 1.0 of the local electron gyrofrequency, (i) spacecraft trajectory crossing the magnetopause event.

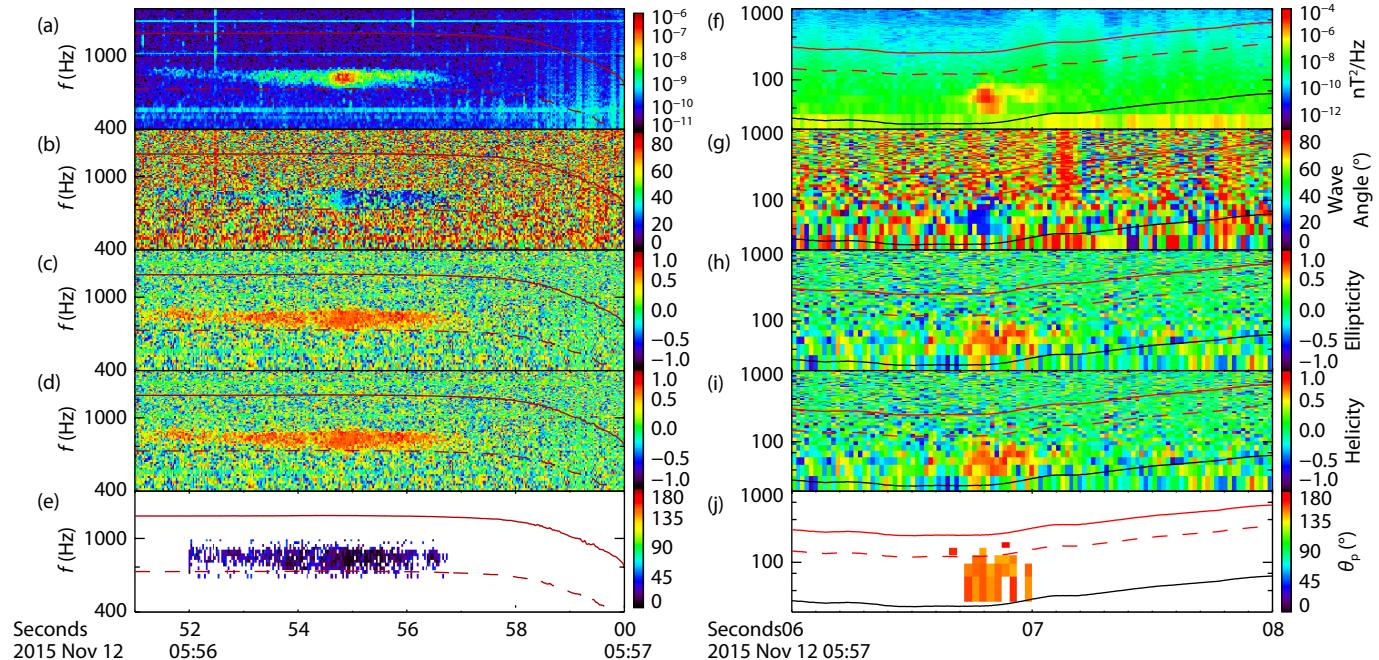
magnetic field during the current sheet crossing (05:56:53–05:57:00 UT). With respect to the GSM coordinates,  $M = (-0.207, 0.978, -0.015)$  mainly pointing to the dusk,  $N = (-0.933, -0.193, 0.302)$  is the boundary normal direction and almost identical to the  $X$ -axis in the GSM coordinates, and  $L = (0.293, 0.076, 0.953)$  completes the right-hand system.

In the beginning, the spacecraft was in the magnetosphere, identified by the stable and northward  $B_L$  ( $\sim 58$  nT, Figure 1a), and low-density plasma ( $< 1 \text{ cm}^{-3}$ , Figure 1d). From 05:56:54 to 05:56:57 UT, the electrons have a larger bulk velocity in the  $L$  direction, reaching a maximum value of  $-1600 \text{ km/s}$  (Figure 1f) in the outflow region. We also find that both the electrons and ions have an energetic component, of approximately 0.3 keV and 1.0 keV, respectively. These energetic components are generated during magnetic reconnection. At approximately 05:56:57.1 UT, MMS3 entered the magnetosheath, where the plasma density was high and the magnetic field  $B_L$  turned from northward to southward. The ions obtained a large bulk velocity in the  $L$  direction, and the spacecraft was in the northward outflow region. The spacecraft trajectory crossing the magnetopause reconnection event is plotted in Figure 1i. In this reconnection event, we can also observe high-frequency electromagnetic waves on both the magnetosphere and magnetosheath sides, circled by dashed lines in Figures 1g and 1h. Their frequencies are around 760 and 65 Hz, respectively, which are about 0.56 and 0.2 of the local electron gyrofrequency.

Figure 2 presents the characteristics of these electromagnetic waves. These wave characteristics are analyzed in the field-aligned coordinates (FAC) system, which is described as follows: the  $Z$ -axis is parallel to the mean magnetic field measured by the

Fluxgate Magnetometer at the burst data rate (128/s). The  $X$ -axis is perpendicular to the mean magnetic field and in the spacecraft spin plane, and the  $Y$ -axis completes the right-hand system. The polarization analysis is obtained from the spectral matrix computed using SCM waveforms (Samson and Olson, 1980), where the wave normal angle, the ellipticity, and the helicity are resolved. According to this method, the ellipticity and helicity of the right-hand polarized waves are equal to 1, and the waves have left-handed polarization when the ellipticity and helicity are equal to  $-1$ . Figures 2(a–e) plot the frequencies, wave normal angles, ellipticities, helicities, and angles between the Poynting fluxes and the magnetic field of the plasma waves on the magnetospheric sides. From about 05:56:53 UT to 05:56:57 UT, the enhancement of the plasma waves can be observed. Analysis of the magnetic spectra shows that the frequencies of the waves are about 0.56 of the local electron gyrofrequency. The ellipticity and helicity (Figures 2(c–d)) are approximately 1.0, and the magnetosospheric waves have right-hand polarization. Their wave normal angle is approximately  $25^\circ$ . Therefore, the observed electromagnetic waves on the magnetospheric sides are whistler waves. From the angle between the Poynting flux and magnetic field (Figure 2e), we conclude that the propagating angle of the magnetosospheric waves is about  $22^\circ$ , and they propagate toward the X-line.

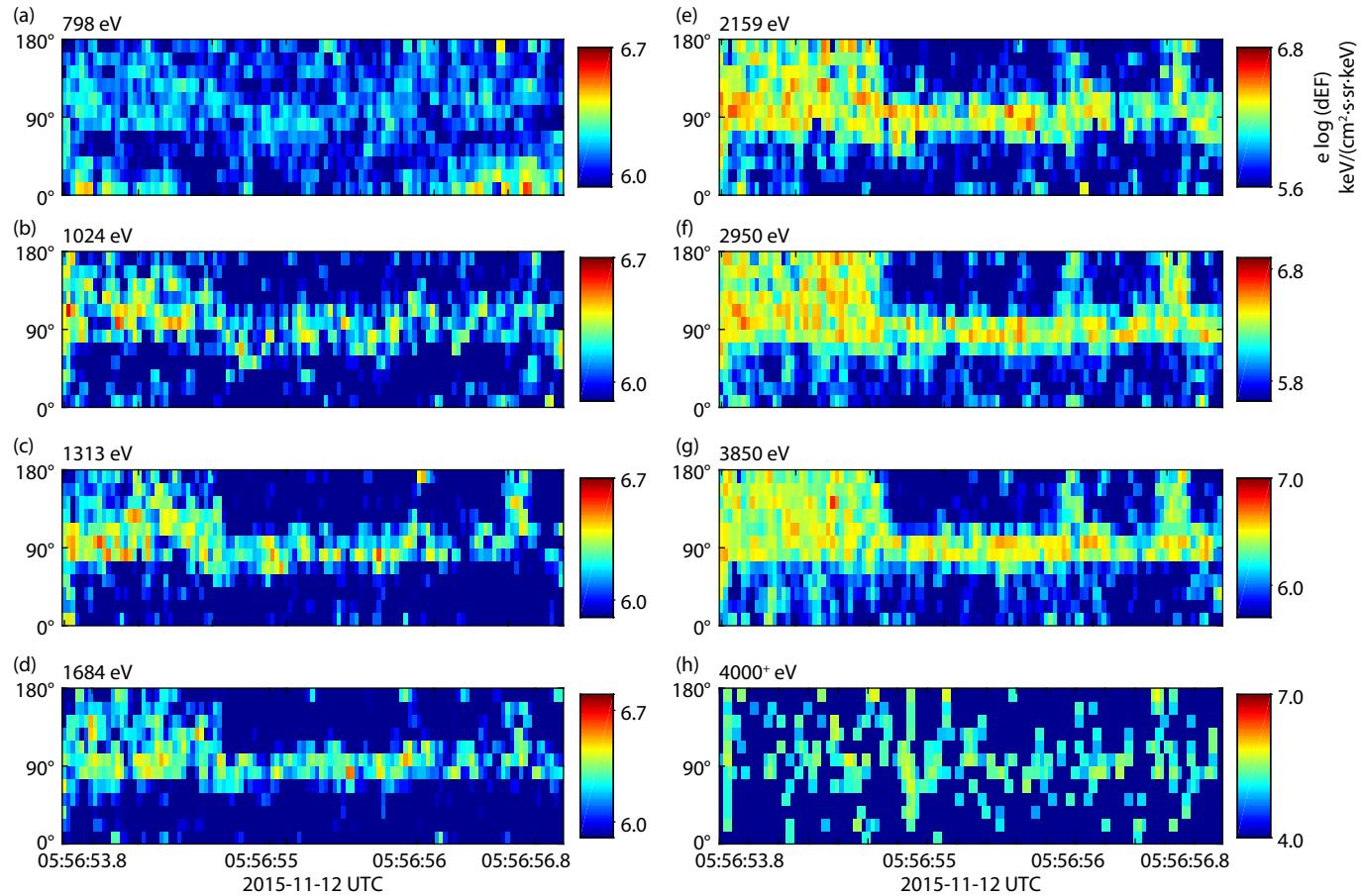
Figures 2(f–j) present the frequencies, wave number angles, ellipticities, helicities, and angles between the Poynting fluxes and magnetic field of the magnetosheath waves. We can observe obvious enhancement of plasma waves from 05:57:06.7 UT to 05:57:07 UT. Analysis of magnetic spectra shows that waves with frequencies from 0.1 and 0.5 of the local electron gyrofrequency are right-hand circularly polarized. The wave normal angle is



**Figure 2.** Characteristics of the electromagnetic waves on magnetospheric and magnetosheath sides. (a)–(e) plot characteristics of magnetospheric waves: (a) magnetic field power spectrogram, (b) wave angle, (c) ellipticity (+1 denotes right-handed circular polarization,  $-1$  denotes left-handed circular polarization), (d) helicity similar to ellipticity and (e) the angle between the wave Poynting flux and magnetic field. (f)–(j) plot the corresponding characteristics of magnetosheath waves.

about 20°, and the waves propagate in a direction quasi-parallel to the magnetic field. All these features suggest that these wave trains are also whistler waves. From the angle between the Poynting fluxes and magnetic field (Figures 2j), we can conclude that the propagating angle of the magnetosospheric waves is 165°, which means that magnetosheath waves are almost antiparallel to the magnetic field. Since the reconnection site is determined to be located at the southward of the spacecraft on the magnetosheath side, the magnetosheath waves propagate away from the X-line.

Figure 3 illustrates the time evolution of the electron differential fluxes (from 798 to 4000 eV) at different pitch angles from 05:56:53.8 to 05:56:58.8 UT, when the spacecraft was on the magnetospheric side. As shown in Figure 2, the electromagnetic waves begin to be enhanced at about 05:56:53 UT on the magnetospheric side. We find that these waves can scatter electrons with energy higher than about 1024 eV, and the pitch angles of these electrons are concentrated around 90°. This is seen more clearly in Figure 4, which shows the electron energy fluxes in the parallel, anti-parallel, and perpendicular directions at 05:56:51.7 UT (a) and 05:56:55.1 UT (b). Consistent with Figure 3, with the enhancement of the whistler waves (Figure 4b), the energy flux in the perpendicular direction is much larger than fluxes in the parallel and anti-parallel directions.



**Figure 3.** Time evolution of the electron differential energy fluxes (dEF) (from 798 to 4000 eV) at different pitch angles, from 05:56:53.8 to 05:56:58.8 UT, when the spacecraft was on the magnetospheric side.

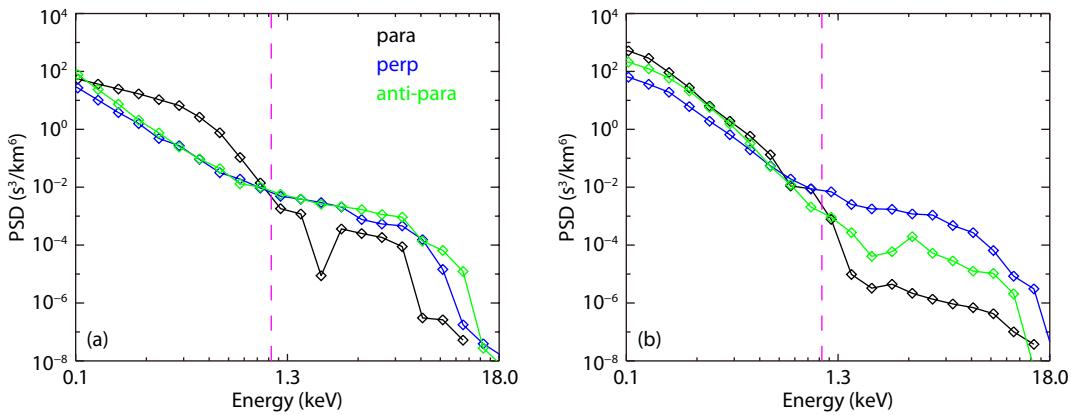
Figure 5 plots the time evolution of the electron differential fluxes (from 52 to 1024 eV) at different pitch angles from 05:57:06.2 to 05:57:07.1 UT, when the spacecraft was on the magnetosheath side. As shown in Figure 2, the electromagnetic waves begin to be enhanced at about 05:57:06.7 UT on the magnetospheric side. We note that when the electron energy is less than about 140 eV, the pitch angles of electrons are concentrated around 0° and 180°. However, for electrons with energy higher than 140 eV, their pitch angles begin to be concentrated around 90° with the enhancement of the whistler waves. This pattern can be also be identified in Figure 6, which plots electron energy fluxes in the parallel, anti-parallel and perpendicular directions at 05:57:06.1 UT (a) and 05:57:06.73 UT (b). It is clear that the enhanced whistler waves can scatter electrons with energy higher than about 140 eV, and that the energy flux in the perpendicular direction is much larger than fluxes in the parallel and anti-parallel directions.

### 3. Discussion and Conclusions

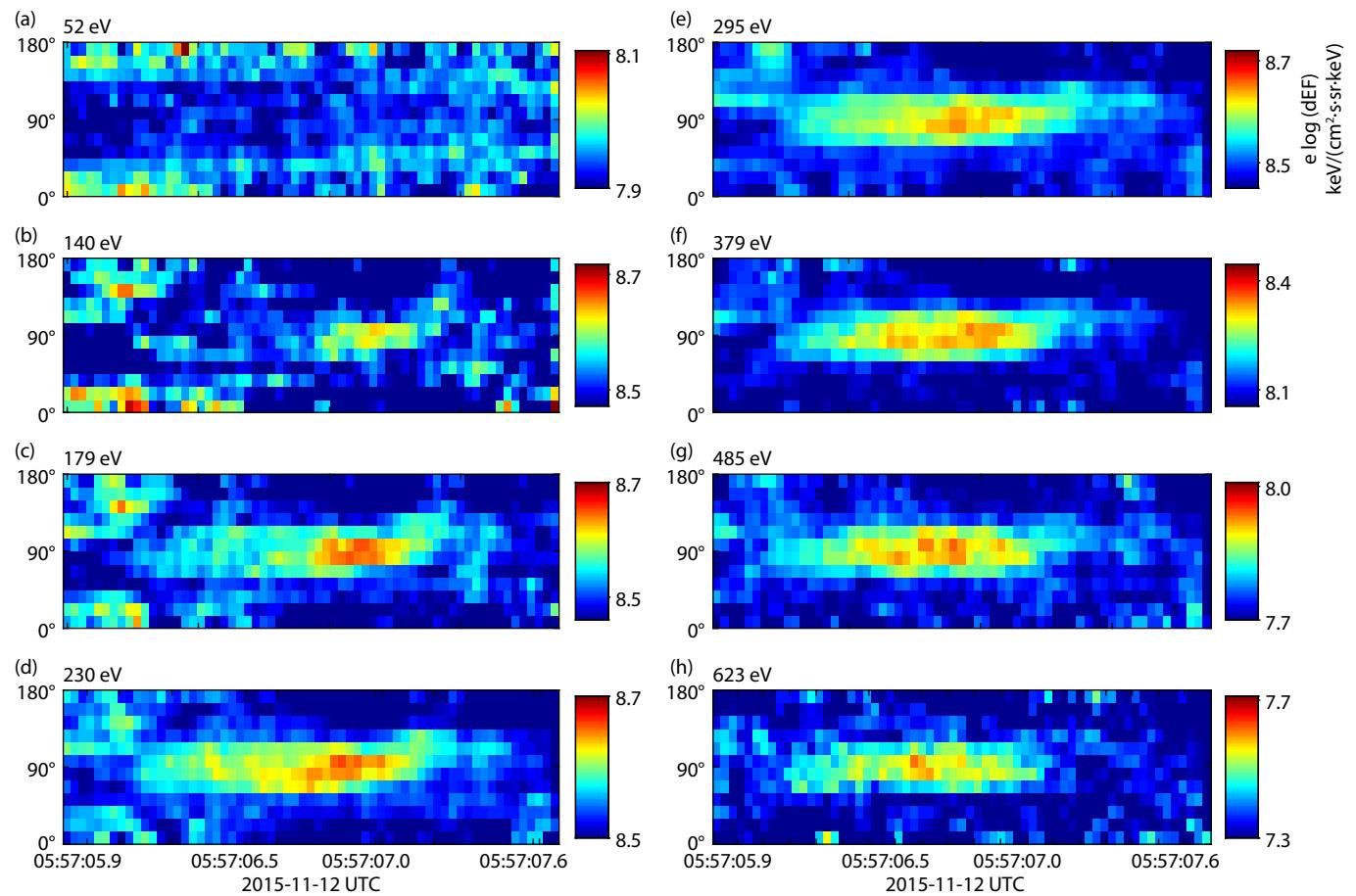
Based on Faraday equation in Fourier space, we can obtain

$$\mathbf{k} \times \delta\mathbf{E}(\omega, \mathbf{k}) = \omega \delta\mathbf{B}(\omega, \mathbf{k}), \quad (1)$$

where  $\delta\mathbf{E}(\omega, \mathbf{k})$  and  $\delta\mathbf{B}(\omega, \mathbf{k})$  are the electric and magnetic fluctuations in Fourier space, obtained by fast Fourier transformation of the electric and magnetic field data. If the plasma waves have a dominant wave mode, such as the observed whistler waves in this



**Figure 4.** Electron energy fluxes in the parallel, anti-parallel and perpendicular directions at (a) 05:56:51.7 UT and (b) 05:56:55.1 UT, when the spacecraft was on the magnetospheric side. The vertical lines correspond to electrons with at least 1100 eV.

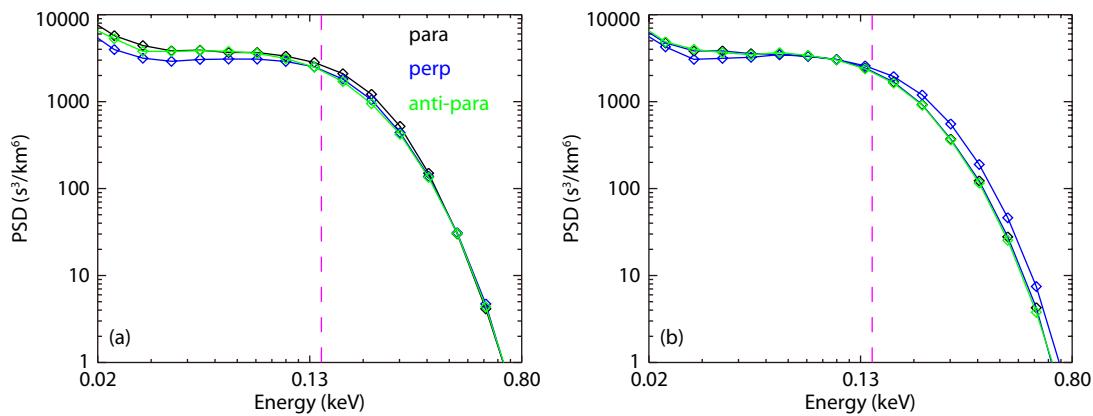


**Figure 5.** Time evolution of the electron differential energy fluxes (dEF) (from 52 to 1024 eV) at different pitch angles from 05:57:06.2 to 05:57:07.1 UT, when the spacecraft was on the magnetosheath side.

event, we can calculate the corresponding wave number  $k$  according to Equation (1). Then, after the wave normal angle is determined, we can estimate the resonant velocity  $v_{||}$  based on the cyclotron resonant condition  $\omega - k_{||}v_{||} = \pm 2\pi f_{ce}$  (where  $f_{ce} = eB/(2\pi m_e)$  is the electron gyrofrequency, and + and - are used for right- and left-hand polarized waves, respectively). The minimum energy of the electrons that can be scattered by the electromagnetic waves is  $\epsilon_{\min} = 0.5m_e v_{||}^2$  (Kenne and Petschek,

1966). In other words, only electrons with energy higher than  $\epsilon_{\min}$  can resonantly interact with the electromagnetic waves.

In this reconnection event in the magnetopause, we observe whistler waves on both the magnetospheric and magnetosheath sides. On the magnetospheric side, according to Equation (1), we calculate the wave number of the dominant whistler wave mode to be  $k_{||} = 3 \times 10^{-5} \text{ m}^{-1}$ . It follows that the minimum energy of electrons able to interact resonantly with the whistler waves is ap-



**Figure 6.** Electron energy fluxes in the parallel, anti-parallel, and perpendicular directions at (a) 05:57:06.1 UT and (b) 05:57:06.73 UT, when the spacecraft was on the magnetospheric side. The vertical lines correspond to the electrons with at least 142 eV.

proximately 1100 eV. As described in Figure 3, associated with the enhancement of the whistler waves between 05:56:52 UT to 05:56:57 UT, the electron fluxes with energy higher than 1100 eV increase at pitch angles close to 90°. We attribute this observation to resonant interactions with the whistler waves.

On the magnetosheath side, we calculate the wave number of the dominant whistler mode wave to be  $k_{\parallel} = 1 \times 10^{-5} m^{-1}$ , and the minimum energy of the electrons scattered by the whistler waves to be about 142 eV. This is consistent with the demonstration of Figure 5 that the electrons with energy higher than 142 eV can resonantly interact with the whistler waves and exhibit pitch angles concentrated around 90°.

In summary, by analyzing a magnetopause reconnection event, we identify whistler waves on both the magnetospheric and magnetosheath sides. Associated with these whistler waves, fluxes of electrons with energies higher than the minimum energy are enhanced around the 90° pitch angle through resonant interactions with the whistler waves. This analysis provides *in situ* observational evidence for resonant interactions between energetic electrons and whistler waves.

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