# Generalised Extreme Value (GEV) distribution

## Parametrisation

The GEV distribution is defined through the cumulative distribution function

$$F(y; \eta, \tau, \xi) = \exp\left(-\left[1 + \xi\sqrt{\tau w}(y - \eta)\right]^{-1/\xi}\right)$$

for

$$1 + \xi \sqrt{\tau w}(y - \eta) > 0$$

and for a continuously response y where

 $\eta$ : is the linear predictor

 $\tau$ : is the "precision"

w: is a fixed weight, w > 0.

### Link-function

The linear predictor is given in the parameterisation of the GEV distribution.

## Hyperparameters

The GEV-models has two hyperparameters. The "precision" is represented as

$$\theta_1 = \log \tau$$

and the prior is defined on  $\theta_1$ . The shape parameter  $\xi$  is represented as

$$\xi = s\theta_2$$

where s > 0 is a chosen fixed scaling, and the prior is defined on  $\theta_2$ .

## Specification

- $\bullet$  family = gev
- Required arguments: y and w (keyword weights)
- The scaling s is given by the argument scale.xi.gev and is default set to 0.01, and provides an more appropriate scale for  $\theta_2$ .

The weights has default value 1.

## Hyperparameter spesification and default values

## hyper

#### theta1

name log precisionshort.name precinitial 4fixed FALSEprior loggamma

```
param 1 5e-05
to.theta function(x) log(x)
from.theta function(x) exp(x)
theta2
name gev parameter
short.name gev
initial 0
fixed FALSE
prior gaussian
param 0 6.25
to.theta function(x) x
from.theta function(x) x
survival FALSE
discrete FALSE
```

# Example

In the following example, we estimate the parameters of the GEV distribution on some simulated data

```
rgev = function(n=1, xi = 0, mu = 0.0, sd = 1.0) {
    u = runif(n)
    if (xi == 0) {
        x = -\log(-\log(u))
    } else {
        x = ((-log(u))^{-(-xi)} - 1.0)/xi
    return (x*sd + mu)
}
n = 100
z = rnorm(n)
sd.y = 0.5
xi = 0
y = 1+z + rgev(n, xi=xi, sd = sd.y)
formula = y ~ 1 + f(inla.group(z), model="rw1")
data = data.frame(y,z)
r = inla(formula, data = data, family = "gev",
        control.data = list(gev.scale.xi = 0.01,
                ## just to show how to set an initial value
                hyper = list(prec=list(initial=2))))
```

## Notes

None.