Model for seasonal variation

Parametrization

A model for seasonal variation with periodicity m for the random vector $\S = (x_1, \ldots, x_n)$, $n > m$ is obtained assuming that the sums $x_i + x_{i+1} + \ldots + x_{i+m-1}$ are independent Gaussian with preciosion τ.

The density for $\mathbf{x}$ is derived from the $n - m + 1$ increments as

$$
\pi(\mathbf{x}|\tau) \quad \propto \quad \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{\tau}{2} \sum (x_i + x_{i+1} + \ldots + x_{i+m-1})^2\right\} \tag{1}
$$

$$
= \quad \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{1}{2}\mathbf{x}^T \mathbf{Q} \mathbf{x}\right\} \tag{2}
$$

where $\mathbf{Q} = \tau\mathbf{R}$ and $\mathbf{R}$ is the structure matrix reflecting the neighbourhood structure of the model.

Hyperparameters

The precision parameter τ is represented as

$$
\theta = \log \tau
$$

and the prior is defined on θ.

Specification

The seasonal model is specified inside the `f()` function as

```
 f(<whatever>,model="seasonal",season.length=<season.length>,
             hyper = <hyper>)
```

Hyperparameter spesification and defaults

hyper

> **theta**
>> **name**   precision
>> **short.name**   prec
>> **initial**   4
>> **fixed**   FALSE
>> **prior**   loggamma
>> **param**   c(1, 1e-04)

constr   FALSE

nrow.ncol   FALSE

augmented   FALSE

aug.factor   1

aug.constr   NULL

n.div.by   NULL

n.required   FALSE

set.default.values   FALSE

Example

```
n=203
n.seas=12
trend=seq(1:n)
seasonal=rep(1:n.seas, ceiling(n/n.seas))[1:n]

a=1
b=0.5
y = rnorm(n,a+b*trend,1)+rnorm(n,0.2*seasonal,1)

data=data.frame(y=y,trend=trend,seasonal=trend)

formula = y~f(trend,model="rw2")+f(seasonal,model="seasonal",
              season.length=n.seas)
result=inla(formula,family="gaussian",data=data)
```

Notes

The seasonal is intrinsic with rank deficiency $m - 1$.