

# Autoregressive model of order 1 (AR1)

## Parametrization

The autoregressive model of order 1 (AR1) for the Gaussian vector  $\mathbf{x} = (x_1, \dots, x_n)$  is defined as:

$$\begin{aligned}x_1 &\sim \mathcal{N}(0, (\tau(1 - \phi^2))^{-1}) \\x_i &= \phi x_{i-1} + \epsilon_i; \quad \epsilon_i \sim \mathcal{N}(0, \tau^{-1}) \quad i = 2, \dots, n\end{aligned}$$

where

$$|\phi| < 1$$

## Hyperparameters

The precision parameter  $\tau$  is represented as

$$\theta_1 = \log(\tau)$$

and the parameter  $\phi$  is represented as

$$\theta_2 = \log\left(\frac{1 + \phi}{1 - \phi}\right)$$

and the prior is defined on  $\theta = (\theta_1, \theta_2)$ .

## Specification

The AR1 model is specified inside the `f()` function as

```
f(<whatever>, model="ar1", values=<values>, prior=c(<prior.model.theta1>, <prior.model.theta2>),
  param=c(<param.prior.theta1>, <param.prior.theta1>,
          <param.prior.theta2>, <param.prior.theta2>))
```

The (optional) argument `values` is a numeric or factor vector giving the values assumed by the covariate for which we want the effect to be estimated. See the example for RW1 for an application.

## Example

In this exaple we implement a `ar1` model where  $\theta_1$  has a log-Gamma prior with parameters 1 and 0.001 and  $\theta_2$  has a Gaussian prior with parameters 0 and 0.001

```
#simulate data
n=100
phi=0.8
prec=10
E=sample(c(5,4,10,12),size=n,replace=T)
eta = as.vector(arima.sim(list(order = c(1,0,0), ar = phi), n = n,sd=sqrt(1/prec)))
y=rpois(n,E*exp(eta))
data = list(y=y,z=1:n)

#fit the model
formula = y~f(z,model="ar1",prior=c("loggamma","gaussian"),param=c(1,0.001,0,0.001))
result = inla(formula,family="poisson")
```

## Notes

None