## Zero-inflated models: Beta-Binomial

#### Parameterisation

There is support for a further zero-inflated model of type 2 (see zero-inflated.pdf), the zero-inflated beta-binomial. It is only defined for type 2.

### Type 2

The likelihood is defined as

$$Prob(y \mid ...) = p \times 1_{[y=0]} + (1-p) \times Beta-binomial(y)$$

where:

$$p = 1 - \left(\frac{\exp(x)}{1 + \exp(x)}\right)^{\alpha}$$

# Link-function

As for the Binomial (see Zero-inflated.pdf).

## Hyperparameters

The Beta-binomial distribution has two arguments ( $\beta_1 \& \beta_2$ ) which we assume are a (specific) function of an underlying hyperparameter ( $\delta$ ) & x. There is a further hyperparameter,  $\alpha$ , governing zero-inflation where:

The parameter controlling the degree of overdispersion,  $\delta$ , is represented as

$$\theta_1 = \log(\delta)$$

and the prior is defined on  $\theta_1$ .

The zero-inflation parameter  $\alpha$ , is represented as

$$\theta_2 = \log(\alpha)$$

and the prior and initial value is is given for  $\theta_2$ .

### Specification

- family = zeroinflatedbetabinomial2
- Required arguments: As for the zero-inflated-nbinomial2 likelihood.

### Example

In the following we estimate the parameters in a simulated example.

Example-zero-inflated-beta-binomial2.R

```
nx = 1000 # number of x's to consider

n.trial = 20 # size of each binomial trial

x = rnorm(nx) # generating x
```

```
delta = 10
                             #hyperparameter 1
p = \exp(1+x)/(1+\exp(1+x))
                             #hyperparameter 2
                               #ZI parameter
alpha = 2
q = p^alpha
                               #prob presence
beta_1=delta*p
                                  #beta-bin parameter 1
beta_2=delta*(1-p)
                                  #beta-bin parameter 2
rb = rbeta(nx, beta_1, beta_2, ncp = 0)
y = rep(0,nx)
                                    #generating data
abs.pres = rbinom(nx,1,q)
y[abs.pres==1] = rbinom( sum(abs.pres>0), n.trial, rb[abs.pres==1])
formula = y \sim x + 1
r = inla(formula, data = data.frame(x,y), family = "zeroinflatedbetabinomial2",
        control.data = list(prior = c("flat", "flat"),
                fixed = c(F,F)),
        Ntrials = rep(n.trial, nx),
        verbose=TRUE)
```