# Zero-inflated models: Beta-Binomial

#### Parameterisation

There is support for a further zero-inflated model of type 2 (see zero-inflated.pdf), the zero-inflated beta-binomial. It is only defined for type 2.

## Type 2

The likelihood is defined as

$$Prob(y \mid ...) = p \times 1_{[y=0]} + (1-p) \times Beta-binomial(y)$$

where:

$$p = 1 - \left(\frac{\exp(x)}{1 + \exp(x)}\right)^{\alpha}$$

### Link-function

As for the Binomial (see Zero-inflated.pdf).

## Hyperparameters

The Beta-binomial distribution has two arguments ( $\beta_1 \& \beta_2$ ) which we assume are a (specific) function of an underlying hyperparameter ( $\delta$ ) & x. There is a further hyperparameter,  $\alpha$ , governing zero-inflation where:

The parameter controlling the degree of overdispersion,  $\delta$ , is represented as

$$\theta_1 = \log(\delta)$$

and the prior is defined on  $\theta_1$ .

The zero-inflation parameter  $\alpha$ , is represented as

$$\theta_2 = \log(\alpha)$$

and the prior and initial value is is given for  $\theta_2$ .

# **Specification**

- family = zeroinflatedbetabinomial2
- Required arguments: As for the zero-inflated-nbinomial likelihood.

## Hyperparameter spesification and default values

### hyper

#### theta1

name log alpha short.name a initial 0.693147180559945 fixed FALSE prior gaussian

```
param 0.693147180559945 1
          to.theta
          from.theta
     theta2
          name beta
          short.name b
          initial 0
          fixed FALSE
          prior gaussian
          param 01
          to.theta
          from.theta
survival FALSE
discrete FALSE
link default logit probit cloglog
pdf zeroinflated
Example
In the following we estimate the parameters in a simulated example.
Example-zero-inflated-beta-binomial2.R
nx = 1000
                           # number of x's to consider
n.trial = 20
                           # size of each binomial trial
x = rnorm(nx)
                           # generating x
delta = 10
                              #hyperparameter 1
p = \exp(1+x)/(1+\exp(1+x))
                              #hyperparameter 2
alpha = 2
                                #ZI parameter
q = p^alpha
                                #prob presence
beta_1=delta*p
                                   #beta-bin parameter 1
beta_2=delta*(1-p)
                                   #beta-bin parameter 2
rb = rbeta(nx, beta_1, beta_2, ncp = 0)
y = rep(0,nx)
                                     #generating data
abs.pres = rbinom(nx,1,q)
y[abs.pres==1] = rbinom( sum(abs.pres>0), n.trial, rb[abs.pres==1])
formula = y \sim x + 1
r = inla(formula, data = data.frame(x,y), family = "zeroinflatedbetabinomial2",
        control.data = list(hyper=list(a = list(prior = "flat", param=numeric(0)),
                                        b = list(prior = "flat", param=numeric(0)))),
        Ntrials = rep(n.trial, nx),
```

verbose=TRUE)