# Model for seasonal variation

#### Parametrization

A model for seasonal variation with periodicity m for the random vector  $\S = (x_1, \dots, x_n), n > m$  is obtained assuming that the sums  $x_i + x_{i+1} + \dots + x_{i+m-1}$  are independent Gaussian with preciosion  $\tau$ .

The density for  $\mathbf{x}$  is derived from the n-m+1 increments as

$$\pi(\mathbf{x}|\tau) \propto \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{\tau}{2}\sum (x_i + x_{i+1} + \dots + x_{i+m-1})^2\right\}$$

$$= \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{1}{2}\mathbf{x}^T\mathbf{Q}\mathbf{x}\right\}$$
(2)

where  $\mathbf{Q} = \tau \mathbf{R}$  and  $\mathbf{R}$  is the structure matrix reflecting the neighbourhood structure of the model.

# Hyperparameters

The precision parameter  $\tau$  is represented as

$$\theta = \log \tau$$

and the prior is defined on  $\theta$ .

# **Specification**

```
The seasonal model is specified inside the f() function as
```

#### Hyperparameter spesification and default values

#### hyper

aug.constr

n.required FALSE

set.default.values FALSE

n.div.by

```
name log precision
short.name prec
prior loggamma
param 1 5e-05
initial 4
fixed FALSE
to.theta function(x) log(x)
from.theta function(x) exp(x)

constr FALSE
nrow.ncol FALSE
augmented FALSE
aug.factor 1
```

# Example

### Notes

The seasonal is intrinsic with rank deficiency m-1.