THIS IS NOT IN USE

Negative Binomial

Parametrization

The negative Binomial distribution is

$$\text{Prob}(y) = \frac{\Gamma(y+n)}{\Gamma(n)\Gamma(y+1)} p^n (1-p)^y$$

for responses $y = 0, 1, 2, \ldots$, where:

n : number of successful trials, or dispersion parameter. Must be strictly positive, need not be integer.

p : probability of success in each trial.

Link-function

The mean and variance of y are given as

$$\mu = n\frac{1-p}{p} \qquad \text{and} \qquad \sigma^2 = \mu(1+\frac{\mu}{n})$$

and the mean is linked to the linear predictor by

$$\mu = E\exp(\eta)$$

where the hyperparameter n (or the *size*) plays the role of an overdispersion parameter. E represents known constant and $\log(E)$ is the offset of η.

Hyperparameters

The overdispersion parameter n is represented as

$$\theta = \log(n)$$

and the prior is defined on θ.

Specification

- family = `nbinomial`
- Required argument: y and E (default $E = 1$).

Example

In the following example we specify the likelihood to be negative binomial, and assign the hyperparameter θ a Gaussian prior with mean 0 and standard deviation 0.01

```
n=100
a = 1
b = 1
E = rep(1,n)
z = rnorm(n)
```

```
eta = a + b*z
mu = E*exp(eta)
siz = 15
p = siz/(siz + mu)
y = rnbinom(n, size=siz, prob = p)

data = list(y=y,z=z)
formula = y ~ 1+z
result = inla(formula, family = "nbinomial", data = data, E=E,
              control.data = list(prior="gaussian", param = c(0,0.01)))
summary(result)
```

Notes

As $n \to \infty$, the negative Binomial converges to the Poisson distribution. For numerical reasons, if n is too large:

$$\frac{\mu}{n} < 10^{-4},$$

then the Poisson limit is used.