Zero-inflated models: Beta-Binomial

Parameterisation

There is support for a further zero-inflated model of type 2 (see zero-inflated.pdf), the zero-inflated beta-binomial. It is only defined for type 2.

Type 2

The likelihood is defined as

$$Prob(y \mid ...) = p \times 1_{[y=0]} + (1-p) \times Beta-binomial(y)$$

where:

$$p = 1 - \left(\frac{\exp(x)}{1 + \exp(x)}\right)^{\alpha}$$

Link-function

As for the Binomial (see Zero-inflated.pdf).

Hyperparameters

The Beta-binomial distribution has two arguments ($\beta_1 \& \beta_2$) which we assume are a (specific) function of an underlying hyperparameter (δ) & x. There is a further hyperparameter, α , governing zero-inflation where:

The parameter controlling the degree of overdispersion, δ , is represented as

$$\theta_1 = \log(\delta)$$

and the prior is defined on θ_1 .

The zero-inflation parameter α , is represented as

$$\theta_2 = \log(\alpha)$$

and the prior and initial value is is given for θ_2 .

Specification

- family = zeroinflatedbetabinomial2
- Required arguments: As for the zero-inflated-nbinomial2 likelihood.

Hyperparameter spesification and default values

hyper

theta1

name log alphashort.name ainitial 0.693147180559945fixed FALSEprior gaussian

```
param 0.693147180559945 1
          to.theta function(x) log(x)
          from.theta function(x) exp(x)
     theta2
          name beta
          short.name b
          initial 0
          fixed FALSE
          prior gaussian
          param 01
          to.theta function(x) log(x)
          from.theta function(x) exp(x)
survival FALSE
 discrete FALSE
link default logit probit cloglog
pdf zeroinflated
Example
In the following we estimate the parameters in a simulated example.
Example-zero-inflated-beta-binomial2.R
nx = 1000
                          # number of x's to consider
n.trial = 20
                          # size of each binomial trial
x = rnorm(nx)
                          # generating x
delta = 10
                              #hyperparameter 1
p = exp(1+x)/(1+exp(1+x))
                              #hyperparameter 2
alpha = 2
                                #ZI parameter
q = p^alpha
                                #prob presence
beta_1=delta*p
                                   #beta-bin parameter 1
                                   #beta-bin parameter 2
beta_2=delta*(1-p)
rb = rbeta(nx, beta_1, beta_2, ncp = 0)
y = rep(0, nx)
                                     #generating data
abs.pres = rbinom(nx,1,q)
y[abs.pres==1] = rbinom( sum(abs.pres>0), n.trial, rb[abs.pres==1])
formula = y \sim x + 1
r = inla(formula, data = data.frame(x,y), family = "zeroinflatedbetabinomial2",
        control.data = list(hyper=list(a = list(prior = "flat", param=numeric(0)),
                                        b = list(prior = "flat", param=numeric(0)))),
        Ntrials = rep(n.trial, nx),
```

verbose=TRUE)