Model for seasonal variation

Parametrization

A model for seasonal variation with periodicity m for the random vector $\S = (x_1, \dots, x_n), n > m$ is obtained assuming that the sums $x_i + x_{i+1} + \dots + x_{i+m-1}$ are independent Gaussian with preciosion τ .

The density for **x** is derived from the n-m+1 increments as

$$\pi(\mathbf{x}|\tau) \propto \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{\tau}{2} \sum_{i=1}^{\infty} (x_i + x_{i+1} + \dots + x_{i+m-1})^2\right\}$$
 (1)

$$= \tau^{\frac{(n-m+1)}{2}} \exp\left\{-\frac{1}{2}\mathbf{x}^T \mathbf{Q} \mathbf{x}\right\}$$
 (2)

where $\mathbf{Q} = \tau \mathbf{R}$ and \mathbf{R} is the structure matrix reflecting the neighbourhood structure of the model.

Hyperparameters

The precision parameter τ is represented as

$$\theta = \log \tau$$

and the prior is defined on θ .

Specification

The seasonal model is specified inside the f() function as

Example

```
n=204
n.seas=12

trend=seq(1:n)
seasonal=rep(1:n.seas,n/n.seas)

a=1
b=0.5
y = rnorm(n,a+b*trend,1)+rnorm(n,0.2*seasonal,1)

data=data.frame(y=y,trend=trend,seasonal=trend)
```

 $formula = y^{f}(trend, model="rw2") + f(seasonal, model="seasonal", season.length=n.seas, param=c(1,0) + f(seasonal, model="seasonal", season.length=n.sea$

Notes

The seasonal is a intrinsic random field with rank deficiency of m-1.