# Student-t

#### **Parametrization**

The Student-t likelihood is defined so that

$$\sqrt{w \ \tau}(y-\eta) \sim T_{\nu}$$

for continuous response y where

 $\tau\,$  : is the precision parameter

w: is a foxed weight w > 0

 $\eta$ : is the linear predictor

 $T_{\nu}$ : is a standardized Student-t with  $\nu$  degrees of freedom such that its variace is 1 for any value of  $\nu$ .

## **Link-function**

Identity

## Hyperparameters

This likelihood has to hyperparameters

$$\theta_1 = \log(\tau)$$

$$\theta_2 = \log(\nu - 2)$$

and the prior is defined on  $\theta = (\theta_1, \theta_2)$ .

# **Specification**

- family = T
- Required argument: y and w (keyword weights, default to 1).

## Hyperparameter spesification and default values

## hyper

### theta1

```
name log precision
short.name prec
initial 3
fixed FALSE
prior loggamma
param 1 5e-05
to.theta
from.theta
```

#### theta2

name log degrees of freedom
short.name dof

```
initial 0
          fixed FALSE
          prior loggamma
         param 1 0.5
         to.theta
          from.theta
survival FALSE
discrete FALSE
link default identity
pdf student-t
Example
#simulate data
n=100
phi=0.85
mu=0.5
eta=rep(0,n)
for(i in 2:n)
eta[i]=mu+phi*(eta[i-1]-mu)+rnorm(1)
nu=3
t=rt(n,df=nu)
y=eta+t/(sqrt(nu/(nu-2)))
data=list(y=y,z=seq(1:n))
#define the model and fit
formula=y~f(z,model="ar1")
result=inla(formula,family="T",data=data)
```

# Notes

None