

# Generalised Extreme Value (GEV) distribution

## Parametrisation

The GEV distribution is defined through the cummulative distribution function

$$F(y; \eta, \tau, \xi) = \exp \left( - \left[ 1 + \xi \sqrt{\tau w} (y - \eta) \right]^{-1/\xi} \right)$$

for

$$1 + \xi \sqrt{\tau w} (y - \eta) > 0$$

and for a continuously response  $y$  where

$\eta$ : is the linear predictor

$\tau$ : is the “precision”

$w$ : is a fixed weight,  $w > 0$ .

## Link-function

The linear predictor is given in the parameterisation of the GEV distribution.

## Hyperparameters

The GEV-models has two hyperparameters. The “precision” is represented as

$$\theta_1 = \log \tau$$

and the prior is defined on  $\theta_1$ . The shape parameter  $\xi$  is represented as

$$\xi = s\theta_2$$

where  $s > 0$  is a chosen fixed scaling, and the prior is defined on  $\theta_2$ .

## Specification

- family = **gev**
- Required arguments:  $y$  and  $w$  (keyword **weights**)
- The scaling  $s$  is given by the argument **scale.xi.gev** and is default set to 0.01, and provides an more appropriate scale for  $\theta_2$ .

The weights has default value 1.

## Example

In the following example, we estimate the parameters of the GEV distribution on some simulated data.

```
rgev = function(n=1, xi = 0, mu = 0.0, sd = 1.0) {  
  u = runif(n)  
  if (xi == 0) {  
    x = -log(-log(u))  
  } else {  
    x = ((-log(u))^-xi - 1.0)/xi  
  }  
}
```

```

    }
    return (x*sd + mu)
}

n = 100
z = rnorm(n)
sd.y = 0.5
xi = 0
y = 1+z + rgev(n, xi=xi, sd = sd.y)

formula = y ~ 1 + f(inla.group(z), model="rw1")
data = data.frame(y,z)

r = inla(formula, data = data, family = "gev",
         control.data = list(gev.scale.xi = 0.01))

```

## Notes

None.