# SWERC NoteBook

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# 1 Parcours de graphes

- 1.1 Implémentation des graphes
- 1.1.1 C/C++
- 1.1.2 Python
- 1.2 DFS Depth First Search
- 1.3 BFS Breadth First Search
- 1.4 Topological Sort
- 1.5 Composantes connexes
- 1.6 Composantes bi-connexe
- 1.7 Composantes fortement connexe
- 1.8 2-SAT
- 1.9 Postier Chinois
- 1.10 Chemin eulérien
- 1.11 Chemin le plus court
- 1.11.1 Poids positif ou nul Dijkstra
- 1.11.2 Poids arbitraire Bellman-Ford
- 1.11.3 Floyd-Warshall

# 2 Points et polygones

- 2.1 Points
- **2.1.1** Points

```
1  class Point:
2    def __init__(self, x, y):
3        self.x = x
4        self.y = y
5    def subtract(self, p):
6        return Point(self.x - p.x, self.y - p.y)
7    def __str__(self):
8        return '(' + str(self.x) + ', ' + str(self.y) + ')'
```

### 2.1.2 Cross-product

```
1 def cross_product(p1, p2):
2    return p1.x * p2.y - p2.x * p1.y
```

#### 2.1.3 Direction

```
1
   def direction(p1, p2, p3):
     return cross_product(p3.subtract(p1), p2.subtract(p1))
 3 # checks if p3 makes left turn at p2
 4 def left(p1, p2, p3):
     return direction(p1, p2, p3) < 0</pre>
 5
 6 # checks if p3 makes right turn at p2
   def right(p1, p2, p3):
 7
     return direction(p1, p2, p3) > 0
8
9\, # checks if p1, p2 and p3 are collinear
10
   def collinear(p1, p2, p3):
11
     return direction(p1, p2, p3) == 0
```

### 2.2 Enveloppe convexe

#### 2.2.1 Marche de Jarvis

```
def jarvis_march(points):
 1
 2
       a = min(points, key = lambda point: point.x)
 3
       index = points.index(a)
 4
       1 = index
 5
       result = []
 6
       result.append(a)
 7
       while (True):
 8
           q = (1 + 1) \% len(points)
9
           for i in range(len(points)):
10
               if i == 1:
11
                   continue
12
               d = direction(points[1], points[i], points[q])
13
               if d > 0 or (d == 0 and distance_sq(points[i], points[l]) > distance_sq(points[q], points[l
                   ])):
14
                   q = i
15
           1 = q
16
           if 1 == index:
17
               break
18
           result.append(points[q])
19
       return result
```

- 2.2.2 Graham Scan
- 2.3 Aire d'un polygone
- 2.4 Paire de points les plus proches
- 3 Ensembles
- 3.1 Rendu de monnaie
- 3.2 Sac à dos
- 3.3 k-somme
- 4 Calculs
- 4.1 PGCD

```
def pgcd(a,b):
    return a if b == 0 else pgcd(b,a%b)
```

### 4.2 Coefficients de Bézout

```
def bezout(a,b):
1
2
      if b == 0:
3
          return (1,0)
4
      else:
5
          u,v = bezout(b,a%b)
6
          return (v, u - (a//b) *v)
7
  def inv(a,p):
8
      return bezout(a,p)[0]%p
```

## 4.3 Coefficients binomiaux

```
def binom(n,k,p):
    prod = 1
    for i in range(k):
        prod = (prod * (n-i)) // (i+1) %p
    return prod
    #Enlever le p et mod p pour sans modulo
```