Fundamentals and Machine Model

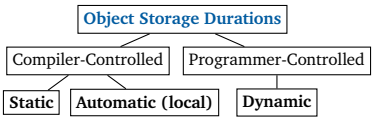
Machine/Memory Model and the Function Call Stack

Object: a piece of data that's stored at a particular location in memory during runtime.

Variable: a *name* in source code that is associated with an object at compile time.

ℹ Not all objects are associated with variables; e.g. dynamically-stored objects and string literals are not.

❗ The value stored by a variable's memory object may change, but the association between a variable and an object itself can only change when the variable goes out of **scope**.



Static objects "live" for essentially a program's runtime. Local objects' lifetimes are tied to scope (e.g. a block of code or pair of curly braces). Dynamic objects are manually created/destroyed.

ℹ Objects declared in a loop body (between the {}) are created/destroyed each time the loop repeats.

Atomic (primitive) types: types whose objects can't be subdivided into smaller objects; includes `int`, `double`, `bool`, `float`, `char`, and all pointer types. Atomic objects are default-initialized to undefined values.

```
// Four different ways to initialize an int to 5
int a = 5; int b(5); int c{5}; int d = {5};
```

```
// Explicitly cast an int 'd' to a double 'e'
double e = static_cast<double>(d);
```

The memory allocated to store a function's parameters and local variables during runtime is called a **stack frame** or activation record. The memory frame for the most-recently called function is added to the "top" of the **function call stack** and is destroyed when the function returns ("Last In First Out" ordering).

Procedural Abstraction and Program Design

Procedural Abstraction involves using functions to break down a complex procedure into sub-tasks and separate the interface of a procedure (what it does) from implementation (how it works).

Interface examples: declarations in `.h` files, valid/invalid inputs, RME statements, *signature* (function name and parameter types), return type, and ADT representation invariants.

Implementation examples: definitions in `.cpp` files and code/comments inside function bodies.

Pointers, Arrays and References

A **pointer** is a type of object that stores another object's memory address as its value.

❗ An `int*` pointer variable can *only* point to an `int`; an `int**` pointer variable can *only* point to an `int*`; and so on. (E.g. attempting to make an `int*` pointer point to a `double` will lead to a compile error.)

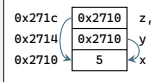
Dereferencing a pointer: getting the object at an address. Note that the star `*` operator is used both to declare pointers and to dereference them (and the `&` operator is used both to get an object's address and to declare a reference).

```
int x = 3; int y = 4;
int* p1 = &x; // p1 initialized to x's address
int* p2; // p2 initialized to undefined value
p2 = p1; // copies the address stored by p1 to p2
p1 = &y; // no star...assigns y's address to p1
*p1 = 6; // dereferences p1, now y == 6
*p2 = 2; // p2 still points to x, so now x == 2
```

ℹ Printing a non-`char` pointer will print an address. (`char` pointers are special and get printed as C-strings.)

ℹ A reference to a reference is really another reference for the "original" object.

```
int x = 5;
int* y = &x; // creates pointer to x
int* z = y; // creates another pointer to x
int* &b = z; // creates reference b to pointer z
cout << *b << endl; // Prints 5
cout << &y << endl; // prints 0x2714
cout << y << endl; // prints 0x2710
cout << &(*z) << endl; // equiv. to cout << &x
cout << *(&z) << endl; // equiv. to cout << z
```



Null pointer: a pointer that holds address `0x0` (which no object can be located at) and implicitly converts to `false`. Any pointer can nulled; to do so, set it equal to `nullptr` (`0` or `NULL` also work but are bad style).

Common Pointer/Reference Errors

⚠ Dereferencing an uninitialized pointer results in undefined behavior, as (like all atomic objects) pointers that aren't explicitly initialized are default-initialized to an undefined value (*not* `nullptr`).

⚠ Dereferencing a null pointer also leads to undefined behavior (almost always a program crash).

❗ Uninitialized references or references-to-non-`const` that are bound to "literal" values won't compile.

⚠ If a function returns a pointer or reference to one of its local variables (which die when the function returns), dereferencing that pointer or using that reference produces undefined behavior.

```
int* danglingPtr(int x) // BUG
  { return &x; }
```

```
int& danglingRef(int x) // BUG
  { return x; }
```

```
int* returnPtr(int &x )
  { return &x; } // Ok
```

Pointers vs References

References and pointers both enable working between stack frames (scopes) and indirection. Some ways they're different:

- References are simply aliases for existing objects, while pointers are themselves distinct objects with distinct values.
- Pointers must be dereferenced to access the objects they point at, while references are used "as-is".
- You can change the object that a (non-`const`) pointer points to, while a reference's binding to an object can't be changed.

Number Swap Function

```
void swap_nums(int *x, int *y) {
  int tmp = *x;
  *x = *y;
  *y = tmp;
}

int main() {
  int a = 1216, b = 1261;
  swap_nums(&a, &b);
}
```

Arrays and Pointer Arithmetic

Arrays: fixed-size containers that store objects of the same type (and same size) in contiguous memory.

```
// Valid array declarations
int arr[3] = {1,2}; // {1,2,0}
int zeroArr[3] = {}; // {0,0,0}
```

```
// Valid array declarations
int arr[] = {4,5,6};
int mat[][2] = {1,2,3,4};
```

```
// INVALID array declarations
int junk[4]; // Undefined items
int err2[][] = {5,6,7,8}; // No
```

Array decay: using an array in a context where a value is required causes the compiler to convert the array into a pointer to its first element. Array decay is why it's necessary to pass an array's size separately from the array to a function (or to indicate the end of an array with a *sentinel character* like C-strings do).

⚠ Dereferencing a pointer that goes past the bounds of an array results in undefined behavior. But merely *using* a pointer that goes just past the end of an array without dereferencing it is well-defined.

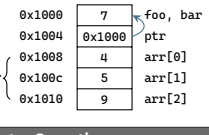
```
void add_five(int arr[], int size) {
  for (int i = 0; i < size; i++) { arr[i] += 5; }
} // arr[i] += 5 is equiv. to *(arr + i) += 5

int main() {
  int arr[] = { 10, 20, 30 };
  add_five(arr, (sizeof(arr) / sizeof(*arr)));
  cout << arr[1] << endl; // prints 25
} // 1[arr] is equiv. to arr[1], but bad style
```

Passing `arr` by value passes a pointer to `arr[0]` by value. Also, `arr[i]` is shorthand for pointer arithmetic followed by a dereference, i.e., `arr[i] = *(arr + i)`.

ℹ The `sizeof` operator returns the size of an object *in bytes*. In this example, `sizeof(arr)` alone would return 12, not 3.

ℹ `cout << &arr[0]`, `cout << arr`, and `cout << &arr` would all print `0x1008`.

```
int foo = 7;
int& bar = foo; // value of bar is foo (7)
int* ptr = &foo;
int arr[3] = { 4, 5, 9 };
cout << arr << endl; // prints 0x1008 (decay)
cout << (arr + 2) << endl; // prints 0x1010
cout << (&foo + 1) << endl; // prints 0x1004
```



Pointer arithmetic: adding an integer `n` to a pointer yields a pointer that is `n` *objects* forward in memory.

Pointer subtraction: Subtracting two pointers of the same type yields an integer (possibly a negative one) equal to the *number of objects* between them.

Pointer comparison: comparing pointers of the same type compares the addresses they store.

Pointer Operations

```
// Mainly for pointers into the same array
double arr[4] = { 2.5, 5.0, 8.0, 7.0 };
double* ptr1 = &arr[0], *ptr2 = &arr[3];
cout << *arr << endl; // prints 2.5
cout << (ptr2 - ptr1) << endl; // prints 3
cout << (ptr1 - ptr2) << endl; // prints -3
(ptr1 > ptr2); // equates to false (0)
ptr1 += 2; // ptr1 now points at arr[2]
```

Using the `&` operator on an array produces a pointer to the entire array, not a pointer to the first element or a pointer to a pointer (`&` does not require a value, so it doesn't cause decay).

```
int arr[4] = { 1, 2, 3, 4 };
int (*arr_ptr)[4] = &arr; // pointer to entire array
cout << (*arr_ptr)[2] << endl; // prints 3
// ++arr_ptr would increment by the size of 4 ints
```

Traversal By Pointer: arrays can be traversed by pointer (mostly used with C-strings and iterators).

Traversal By Pointer: Pattern 1

```
int const SIZE = 3;
int arr[SIZE] = {-1, 7, 2};
int *ptr = arr;
int *end = arr + SIZE;
// int* end is just past the end of arr
while (ptr < end) {
  cout << *ptr << endl;
  ++ptr; // "Walk" ptr across arr
} // Alternative to while loop below
```

```
for (; ptr < end; ++ptr) { ... }
```

Traversal by Pointer: Pattern 2 (C-String Sanitization)

```
void sanitize_username(Account *acc, char to_remove) {
  char *ptr_a = acc->username, *ptr_b = acc->username;
  while (*ptr_a && *ptr_b) { // while not '\0'
    if (*ptr_b != to_remove) {
      *ptr_a = *ptr_b;
      ++ptr_a; // ++ptr_a only when a char gets copied
    }
    ++ptr_b; // ++ptr_b every time the loop executes
  }
  *ptr_a = '\0'; // null-terminate string when done
}
```

The `const` Keyword

The `const` type qualifier stops objects from being modified after initialization. Note: `const` scalars must be explicitly-initialized to compile, and `const` class-type objects must have their data members initialized.

`const` pointers: pointers that can modify what they point at but cannot be re-pointed to different objects.

Pointer-to-`const`: read-only pointers; pointers that can be re-bound but can't modify what they point at.

❗ A `const` pointer must be initialized to compile, but a pointer-to-`const` doesn't need to be.

Reference-to-`const`: a read-only alias.

`const` array: an array of `const` elements. Note that the placement of `const` matters for arrays of pointers.

Special `const` Type Syntax

```
int x = 5;
int * const ptr_a = &x; // const pointer
const int * ptr_b = &x; // pointer-to-const
int const * ptr_c = &x; // pointer-to-const
const int * const ptr_d = &x; // both
int const * const ptr_e = &x; // both

const int &ref_a = x; // reference-to-const
int const &ref_b = 42; // reference-to-const
const int arr_a[2] = {1, 2}; // array of consts
int const arr_b[2] = {3, 4}; // array of consts
```

```
const int* A[] = { ... }; // ptr-to-const array
```

```
int* const B[] = { ... }; // const pointer array
```

`const` Conversions and Passing

The compiler treats every pointer-to-`const` as if they point to a `const` object and every reference-to-`const` as if they're aliased to a `const` object. It won't allow conversions that could bypass existing `const` protections (so, for example, you can assign a `const` pointer to a pointer-to-`const`, but the converse is *not* true).

```
int foo(int* a) { ... }
int bar(int b) { ... }
int func(const int* c) { ... }
const int x = 3;
bar(x); func(&x); // both ok
foo(&x); // ERROR
```

```
const int x = 3;
int y = x; // Ok
const int* cptr = &x; // Ok
const int& cref = x; // Ok
int* ptr = cptr; // ERROR 1
int& ref = cref; // ERROR 2
```

```
int x = 2, y = 5;
const int *x_ptr = &x;
int *y_ptr = &y;
*y_ptr = *x_ptr; // Ok
y_ptr = x_ptr; /* ERROR (even
though x isn't const) */
```

- **Pass by pointer/reference**: if you need to modify the original object (as opposed to a local copy).
- **Pass by value**: if an object is small (e.g., an `int`) and you can't/don't need to modify the original.
- **Pass by pointer/reference-to-`const`**: if you want to pass a large object without modifying it.

Strings, Streams and I/O

Creating/Using C-Strings and Strings

```
const char* cstr = "abcd"; // Only works for string literals; use .c_str() on string variables
char color[] = "00274C"; // Create 7-element array (including \0) and copy a string literal to it
// Note: '\0' is the only char that evaluates to false (useful for traversal-by-pointer loops).
cout << cstr << " " << *cstr << " " << &cstr[0] << endl; // prints "abcd a abcd"
cout << (cstr + 1) << " " << *(cstr + 1) << " " << (*cstr + 1); // prints "bcd b 98" ('a' == 97)
string xyz = string(cstr); // Explicitly copy cstring to a string (implicit copy would work too)
```

	Length	Copy Value	Index	Concatenate	Compare
`<cstring>`	`strlen(cstr);`	`strcpy(cstr1, cstr2);`	`cstr[i];`	`strcat(cstr1, cstr2);`	`strcmp(cstr1, cstr2);`
`<string>`	`str.length();`	`str1 = str2;`	`str[i];`	`str1 += str2;`	`str1 != str2;`

Streams and File I/O

`stdin` redirection	`stdout` redirection	Pipeline	Combined redirection
`./main.exe < input.txt`	`./main.exe > output.txt`	`./output.exe | input.exe`	`./main.exe < input.in > output.out`

File I/O Ex 1: Print Lines From File

```
#include <fstream> // defines (if/of)stream objects
int main() {
  ifstream inFS;
  inFS.open("file.txt"); // valid way to open file
  if (!inFS.is_open()) { return 1; }
  string my_string; // initialized to empty string
  while (getline(inFS, my_string)) {
    cout << my_string << endl;
  } // could close inFS manually via inFS.close();
} // inFS also closes when scope ends/main returns
```

Ex 2: Copy One File's Contents to Another

```
#include <fstream>
int main() {
  ifstream inFS("input.txt"); // Also valid
  ofstream outFS("output.txt");
  string my_string;
  while (inFS >> my_string) {
    outFS << my_string << '\n';
// any whitespace works as a "separator"
  }
} // Note: file streams take C-strings too
```

`istringstream`: an object that "simulates" input with a string as its source. Note: an `istringstream`, an `ifstream` and `cin` can *all* be passed to a function with a `std::istream&` parameter.

`ostringstream`: an object that that captures output and stores it in a string. Note: an `ostringstream`, an `ofstream` and `cout` can *all* be passed to a function with a `std::ostream&` parameter.

```
#include <sstream> // defines stringstreams
void printPlusOne(istream& is, ostream& os) {
  int num = 0;
  while (is >> num) { os << (++num) << " "; }
} // Note: can't pass or return streams by value
...
istringstream inSS("1 3 5");
ostringstream outSS;
printPlusOne(inSS, outSS);
cout << outSS.str() << endl; // Prints "2 4 6"
```

Command-Line Arguments

`argc`: an `int` parameter of `main` representing the number of a command's arguments.

`argv`: an array of the arguments passed to a program. (Technically, `argv` is an array of pointers that each point to the start of a C-string—so `argv` is passed to `main` as a pointer to an array of pointers to C-strings).

```
#include <string> // defines stoi()/stod()
int main(int argc, char* argv[]) { // char** argv also OK
  if (string(argv[1]) == "add") {
    int sum = 0;
    for (int i = 2; i < argc; i++) {sum += stoi(argv[i]);}
    cout << "Sum: " << sum << ", argc: " << argc << endl;
  } // pay attention to where the "actual" arguments start
} // Also remember to use stoi()/string() when needed
```

```
Terminal
hugokim@ubuntu:~$ ./main.exe add 7 2
Sum: 9, argc: 4
hugokim@ubuntu:~$ ./main.exe add 1 2 3
Sum: 6, argc: 5
hugokim@ubuntu:~$ _
```

ADTs, Structs and Classes

C-Style Structs and ADTs

A `struct` is a class-type object composed of member subobjects (heterogeneous data). They're passed by value by default, and they support assignment and initialization via the `=` operator. A `struct` or `class` object can also be declared as `const`, which prevents it and all of its data members from being modified.

❗ You can't call non-`const` member functions on a `const` instance of a `class` or `struct`. Also, you can't call non-`const` member functions from within a `const` member function.

Arrow `->` operator: shorthand for pointer dereferencing followed by member access. `(*ptr).x == ptr->x;`

ℹ Without parentheses, the dot and arrow operators have greater precedence than dereferencing.

Abstract Data Type: a data type that separates its behavior and implementation. ADTs encompass both data and behaviors/functions that act upon it. Not all `structs` are ADTs, some are "plain old data".

⚠ Avoid accessing the member data of an ADT directly (even in tests) because it breaks the interface.

C++ Classes

In C++, the only real difference between classes and structs are that classes have `private` member access and `private` inheritance by default while `structs` default to `public` access/inheritance.

Constructors

- The compiler implicitly creates a default ctor iff there are no user-defined ctors (same for dtors).
- The order in which members are declared in a class is *always* the order they're initialized in.
- Initialization values from a member init. list overwrite initializations made during declarations.
- Data members that aren't included in a ctor's member initializer list or initialized at declaration get default-initialized/constructed.
- A delegating ctor must contain a call to the other ctor (and nothing else) in its member init. list.

Constructor Definition Example

```
class Animal {
private: string name;
public:
  Animal(string name_in)  // Non-default ctor
    : name(name_in) {  }  // Member init. list
  Animal()  // Default ctor (no arguments)
    : Animal("Blank") {  } // ctor delegation
}; // Note the semicolon here!

class Bird : public Animal {
private: bool has_wings;
public: Bird(string name, bool wings_in)
      : Animal(name), has_wings(wings_in) {  }
}; // Derived class ctors must call base ctor

class Duck : public Bird {
private: string color;
public: Duck(string name, bool wings, string rgb)
      : Bird(name, wings), color(rgb) {  }
}; // Calling Bird ctor also calls Animal ctor
-------------------------------------------------
// This is how to define a ctor OUTSIDE of body
Duck::Duck(string name, bool wings, string rgb)
  : Bird(name, wings), color(rgb) {  }
```

C-Style Struct vs Class Syntax

ADT Function Definition

```
// C-Style Struct
void Triangle_scale(Triangle *t, double s) {
  t->a *= s; // "->" is necessary here
} // struct pointer is explicitly passed
-------------------------------------------------
// C++ Class (Inside Body)
class Triangle { // "this->" is optional here
  void scale(double s) { this->a *= s; }
}; // this-> implicit iff no name conflicts

// C++ Class (Outside Body)
void Triangle::scale(double s) { ... }
```

Object Creation/Manipulation

```
// C-Style Struct
Triangle t1;
Triangle_init(&t1, 3, 4, 5);
-------------------------------------------------
// C++ Class
Triangle t1; // Calls default ctor
Triangle t2(3,4,5); // calls 3-argument ctor
Triangle t3 = Triangle(3,4,5); // ditto
// Syntax that works for classes AND structs:
Triangle t4{3, 4, 5};
Triangle t5 = {3, 4, 5};
Triangle t6 = Triangle{3, 4, 5};
```

`const` Function Definition

```
// C-Style Struct
double area(const Triangle *t) { ... }
// const goes inside argument list
-------------------------------------------------
// C++ Class (Inside Body)
class Triangle {
  double area() const { ... }
}; // const comes after signature

// C++ Class (Outside Body)
double Triangle::area() const { ... }
```

Nested Classes and Constructors

To initialize a nested class object, initialize it with a valid argument for the nested class's ctor.

Nested class objects in a `const` class object are also `const`.

```
class Book {
public:
  Book(double price_in)
    : price(price_in) { }
// Note: no default Book ctor
private:
  double price;
};
```

```
class Person {
public:
  Person(string& n, double p)
    : name(n), favBook(p) { }
private:
  string name;
  Book favBook;
};
```

Inheritance and Polymorphism

Function Overloading (Ad Hoc Polymorphism) and Operator Overloading

Function Overloading: using one name to refer to functions with *different signatures*. Functions can only be overloaded in the same scope (otherwise the "closer" scope takes priority). Note: `const`/non-`const` passing only alters the signature of functions with pointer/reference parameters (or implicit `this->` pointers).

Operator Overloading: operators like `+`,`-`,`<<`, etc. must be "overloaded" either as a top-level or class member function to work properly with custom classes (at least 1 operand must be of class-type).

- An operator must be overloaded as a top level function if the first operand is an atomic type or a class type whose definition we can't access (e.g. `ostream`). Also, the `=`, `()`, `[]` and `->` operators can only be overloaded as member functions (along with overloads that need to access `private` members).

`[]` Overload Example (Member)

```
class IntSet {
... // contains() is also a member function
public:
  bool operator[](int v) const;
};

bool IntSet::operator[](int v) const {
    return contains(v);
}
```

`<<` and `==` Overload Examples (Top-Level)

```
class Line {...}; // start/end are public members

ostream& operator<<(ostream& os, Line line) {
  return os << line.start << line.end;
} // os needs to be passed by non-const ref here

bool operator==(const Line &a, const Line &b) {
  return (a.start == b.start && a.end == b.end);
} // Don't pass by non-const ref here
```

Inheritance and Derived Classes

All base class members (EXCEPT ctors and dtors) become implicit members of derived classes. So you can call any non-private base class function on a derived class object or access non-private inherited data members via `(.)/->`

- Creating a derived class object *always* calls a base class ctor. If you don't call one explicitly, the base class default ctor will be implicitly called (causing a compile error if it doesn't exist or isn't accessible). Also, a base class dtor is always called when a derived object dies.

Member name lookup via `(.)/->` starts in the "first" class scope; if no match is found, the base class scope (if one exists) is searched. Lookup stops at the first match; member access levels are checked after name lookup finishes.

```
class Base {
public:
  void print() { cout << "B" << endl; }
  ~Base() { } // custom dtor syntax
// Base::~Base() { } outside class body
};

class Derived : public Base {
public: // Hiding Base::Print()
  void print() { cout << "D" << endl; }
  void print_b() { Base::print(); }
};

Derived d;
d.print(); // prints "D"
d.print_b(); // prints "B"
d.Base::print(); // prints "B"
Base* b = &d; // another way to un-hide
b->print(); // prints "B"
```

- Attempting to overload functions inherited from a base class will "hide" them, not overload them.

Indirect Access of Inherited Privates

```
class Base {
private:
  int x = 5;
public:
  int* x_ptr = &x;
  int get_x() const { return x; };
};
class Derived : public Base { };
```

```
  Derived d; // cannot directly access x
  cout << *(d.x_ptr) << endl; // prints 5
  cout << d.get_x() << endl; // prints 5
```

Summary: how access modifiers affect *direct* access

Modifier	Accessible to derived classes	Accessible out of scope
`public`	✔ Yes	✔ Yes
`private`	✖ No	✖ No
`protected`	✔ Yes	✖ No

Destructors: special functions that are invoked when a class object's lifetime ends (e.g. when you `delete` a dynamic object or when a local object goes out of scope). They look like ctors with `~` before their name.

- For derived class objects, constructors follow *top-down* behavior (i.e., the base class ctor is called first), while destructors are *bottom-up* (the derived class dtor is called first, and the base dtor is called last). Also, in general, objects are destroyed in the *opposite* order that they were created in.

Subtype Polymorphism and Class Casting

Subtype polymorphism allows a publicly-derived class object to be used in place of a base class object; to do this, a base class reference or pointer to a derived class object must be created.

```
class Bird { }; // Base class
class Chicken : public Bird { };
class Duck : public Bird { };
Bird b; Chicken c; Duck d;
b = c; // Legal, but "slices" c's data
Bird* b_ptr = &c; // Good, no slicing
c = b; // ERROR (illegal assignment)
Chicken* c_ptr = &b; // ERROR (downcast)
Duck* d_ptr = &c; // ERROR
```

C++ allows implicit **upcasts** (i.e. base pointers/refs to publicly derived objects), but all downcasts must be explicit via `static_cast` or (less preferably) `dynamic_cast`.

```
// Be careful - validity not checked at runtime:
Chicken *cPtr_a = static_cast<Chicken *>(bird_ptr);
// Bird needs at least 1 virtual function for this:
Chicken *cPtr_b = dynamic_cast<Chicken *>(bird_ptr);
```

Virtual Functions and the `override` Keyword

Here, the *receiver* of the call to `talk()` on line 13 has a **static type** known at compile time (`Bird`) and a **dynamic type** known at runtime (`Duck`). Member lookup starts in the static class, so `Duck::talk` won't hide `Bird::talk`. Instead, `Bird::talk` is declared as `virtual` to make it dynamically-bound.

Declare a function as `virtual` when a receiver's static and dynamic type are different and you want to use the dynamic version of the function.

```
class Bird {
... // virtual can only be used in a class body
  virtual void talk() const { cout << "tweet"; }
};
// Note: ctors can't be virtual, but dtors can
class Duck : public Bird {
... // "virtual" is optional/implicit here
  void talk() const override { cout << "Quack"; }
}; // override = an optional "sanity check"
// override always goes at end of signature
Duck duck;
Bird* duck_ptr = &duck;
duck_ptr->talk(); // prints "Quack"
// Scope resolution operator can suppress virtual
duck_ptr->Bird::talk(); // prints "tweet"
```

`override` keyword: tells the compiler to verify that the function overrides a base-class virtual function with a matching signature (if no override is found, `override` causes a compile error).

Pure Virtual Functions and Abstract Classes

Pure virtual function: a `virtual` base-class function that has no meaning or implementation; they simply make up part of the interface for derived classes. To declare one, add `= 0;` to the end of a function's signature.

Abstract class: a class with at least one pure virtual member function. Note that derived classes of an abstract class will also be abstract unless they override (define) every pure virtual function they inherit.

Interface (pure abstract class): a class that contains nothing but pure virtual member functions.

```
class Abst { // Abstract Class
public: virtual void foo() = 0;
}; // Note the lack of empty braces

class Concrete : public Abst {
public: void foo() { cout << "foo"; }
}; // public/private doesn't matter here

Concrete c;
Abst* c_ptr = &c; Abst& c_ref = c; // ok
Abst abst_object; // COMPILE ERROR
c.Abst::foo(); // RUNTIME ERROR (or U.B)
```

- Don't call pure virtual functions or try to instantiate abstract classes.

Container ADTs and Templates (Array-Based Data Structures)

Container ADTs

`static` keyword: used to make one copy of a class data member "shared" between all instances of that class. A `static` data member has static storage duration but exists only within the scope of a class.

Vectors: resizable array-based container ADTs that store elements at the front and free space at the back.

stack: a container that's designed to operate in a LIFO order.

queue: a container designed to operate in a first-in/first-out (FIFO) order.

Container	Interface Operations - Optimal Implementations are All O(1)					
Stack	empty	size	back/top (next)		push_back	pop_back
Queue	empty	size	front (next)	back (last)	push_back	pop_front

- An efficient way to implement a queue is to create a vector with free space at both ends (a **ring/circular buffer**). To do so, keep track of the data using head (inclusive) and tail (exclusive) variables.

Useful `<vector>` Functions				
`.size()`	`v[i]`	`.push_back(val)`	`.pop_back()`	`.resize(n)`
`.front()`	`.back()`	`.at(i)`	`.empty()`	`.clear()`

Operation	Unsorted Set	Sorted Set	Stack	Queue	Array
`insert, remove`	$O(n)$	$O(n)$	$O(1)^*$	$O(1)^*$	$O(n)$
`contains`	$O(n)$	$O(\log n)$	$O(n)$	$O(n)$	$O(n)$
`access`	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(1)$

`SortedIntSet::remove()` Implementation

```
void remove(int v) {
  int i = indexOf(v); // indexOf() is a member
  if (i == -1) { return; }
  for (; i < elts_size - 1; ++i) {
    elts[i] = elts[i + 1];
  }
  --elts_size; // elts_size == cardinality
}
```

`SortedIntSet::insert()` Implementation

```
void insert(int v) {
  if (indexOf(v) != -1) { return; }
  int i = elts_size;
  for (; (i > 0) && (elts[(i-1)] > v); i--)
    { elts[i] = elts[(i - 1)]; }
  elts[i] = v;
  ++elts_size;
}
```

Templates (Parametric Polymorphism)

Templates: flexible models for producing code that take a data type as a parameter to create an object or call a function that works with that type. They help reduce code duplication in container ADT interfaces.

- A template can accept an invalid type argument during instantiation (leading to a runtime error).

Class Template Syntax

```
template <typename T>
class UnsortedSet {
public:
  void insert(T my_val);
  bool contains(T my_val) const;
  int size() const;
private:
  T elts[ELTS_CAPACITY];
  int elts_size;
  ...
}; // Syntax: UnsortedSet<type> s;
```

Function Template Syntax

```
template <typename T> // "T" = an arbitrary parameter name
// Note: "class" also works in place of "typename".
T maxValue(const T &valA, const T &valB) {
  return valB > valA ? valB : valA; // Note: "?" = ternary
} // This function returns the greater of valA and valB
// Syntax to call it: maxValue<int/double/etc>(...);
```

Templated Class Member Function Syntax

```
template <typename T> // Necessary if outside class body
void UnsortedSet<T>::insert(T my_val) {...}
```

Iterators, Traversal By Iterator, and Range-Based Loops

Iterators: objects that have the same *interface* as pointers; they provide a general interface for traversing different types of container ADTs. To implement an iterator for a particular ADT, define them as a nested class within the container's class and overload the `*` (dereference), `++`, `==`, `!=` operators.

- `std::begin()` returns an iterator to the start of an STL container. `std::end()` returns an iterator that's *1 past* the end of an STL container (the iterator returned by `std::end()` should not be dereferenced).
- Using an *invalidated* iterator (e.g. an iterator pointing at a deleted element) causes undefined behavior.

Traversal By Iterator: a more general form of traversing a container data type by pointer.

```
vector<int> v(3, -1); // this syntax initializes v to {-1,-1,-1}
for (vector<int>::iterator it = v.begin(); it != v.end(); ++it)
  { cout << *it << endl; } // ::const_iterator if const vector
```

Range-Based For Loop (Works on Any Sequence Traversible by Iterator)

```
vector<int> v = { 1, 2, 3, 4 };
// for (<type> <variable> : <sequence>) {...}
for (int item : v) { // works with arrays too
  cout << item << endl;
} // could also declare item as const or a ref
```

```
// Compiler translation of range-based for loop
for (auto it = v.begin(); it != v.end(); ++it) {
  int item = *it;
  cout << item << endl;
}
```

Time Complexity

We define **runtime complexity** in terms of *number of steps*, not literal runtime. Big-O notation represents an *upper-bound* of the magnitude of a function's growth rate with respect to input size (thus, all $O(n)$ functions are also $O(n^2)$, $O(n^3)$, etc). Big-Θ and Big-Ω represent average and lower bounds, respectively.

$O(1)$	$O(\log n)$	$O(\sqrt{n})$	$O(n)$	$O(n \log n)$, $O(\log(n!))$	$O(n^2)$	$O(n^3)$	$O(2^n)$	$O(n!)$	$O(n^n)$	$O(2^{2^n})$

- Functions in the same complexity class should have growth rates that differ by a constant factor as $n \to \infty$. So $O(2^n)$ and $O(8^n)$ are NOT in the same complexity class, but $O(\log_2 n)$ and $O(\log_3 n)$ are.

Determining Asymptotic/Big-O Complexity

Constant coefficients: if they're not part of an exponent, ignore them. Ex: $O(3n) = O(0.5n) = O(n)$.

Addition (sequential procedures): the highest-complexity term dominates. Ex: $O(n^2 + n + \log n) = O(n^2)$.

Multiplication: multiply the individual terms' complexities. Ex: $O(n \times \log n) = O(n \log n)$.

Non-nested loops: *sum* the complexities of each operation *inside* the loop body, and then *multiply* that by the number of times the loop executes. Ex: a loop that runs from `0` to `n` with a $O(\log n)$ body is $O(n \log n)$.

Nested loops: start at the innermost loop and work outwards (the individual complexities of the loops should multiply). Ex: two nested $O(n)$ loops will do n work n times, so they're $O(n^2)$.

Partitioning/repeated division: procedures that divide the "remaining steps" by a constant number each time they execute (e.g. binary search, for-loops that double the loop counter) are usually $O(\log n)$.

$\log(xy) = \log(x) + \log(y)$	$\log\left(\frac{x}{y}\right) = \log(x) - \log(y)$	$\log(x^n) = n \log(x)$	$\log_b(x) = \frac{\log_a(x)}{\log_a(b)} = \frac{1}{\log_x(b)}$