

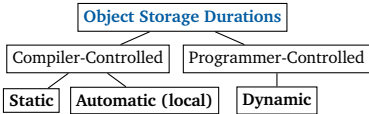
## Fundamentals and Machine Model

### Machine/Memory Model and the Function Call Stack

**Object:** a piece of data that's stored at a particular location in memory during runtime.

**Variable:** a *name* in source code that is associated with an object at compile time.

- Not all objects are associated with variables; e.g. dynamically-stored objects and string literals are not.
- The value stored by a variable's memory object may change, but the association between a variable and an object itself can only change when the variable goes out of **scope**.



**Atomic (primitive) types:** objects that can't be subdivided into smaller objects; includes `int`, `double`, `bool`, `float`, `char`, and all pointer types. Atomic objects are default-initialized to undefined values.

An **lvalue** is an object at some address in memory; an **rvalue** is a *value* with no meaningful address. The memory allocated to store a function's parameters and local variables during runtime is called a **stack frame** or activation record. The memory frame for the most-recently called function is added to the "top" of the **function call stack** and is destroyed when the function returns ("Last In First Out" ordering).

### Procedural Abstraction and Program Design

**Procedural Abstraction** involves using functions to break down a complex procedure into sub-tasks and separate the interface of a procedure (what it does) from implementation (how it works).

**Interface examples:** declarations in `.h` files, valid/invalid inputs, RME statements, *signature* (function name and parameter types), return type, and ADT representation invariants.

**Implementation examples:** definitions in `.cpp` files and code/comments inside function bodies.

## Pointers, Arrays and References

A **pointer** is a type of object that stores another object's memory address as its value.

- An `int*` pointer can *only* point to an `int`; an `int**` pointer can *only* point to an `int*`; and so on. (Trying to, for example, make an `int*` pointer point to a `double` will cause a compile error.)

**Dereferencing:** getting the object at an address. Note that the `*` operator is used both to declare pointers and to dereference them (and the `&` operator is used both to get an object's address and to declare references).

- Printing a non-`char` pointer prints an address. (`char` pointers get printed as C-strings.)
- A reference to a reference is really another reference for the "original" object.

**Null pointer:** a pointer that holds address `0x0` (which no object can be located at) and implicitly converts to `false`. Any pointer can be nulled by setting it equal to `nullptr` (or `0`, or `NULL`).

### Common Pointer/Reference Errors

- Dereferencing an uninitialized pointer results in undefined behavior, as (like all atomic objects) pointers that aren't explicitly initialized are default-initialized to an undefined value (*not* `nullptr`).
- Dereferencing a null pointer also leads to undefined behavior (almost always a program crash).
- An uninitialized reference or a reference-to-non-`const` that's bound to an rvalue won't compile.
- If a function returns a pointer or reference to one of its local variables (which die when the function returns), dereferencing that pointer or using that reference produces undefined behavior.

```
1 int* danglingPtr(int x) { return &x; } // BUG
2 int& danglingRef(int x) { return x; } // BUG
```

### Pointers vs References

References and pointers both enable working between stack frames (scopes) and indirection. Some ways they're different:

- References are simply aliases for existing objects, while pointers are distinct objects with distinct values.
- Pointers must be dereferenced to access the objects they point at, while references are used "as-is".
- You can change what a (non-`const`) pointer points to, but a reference's binding to an object can't be changed.

### Arrays and Pointer Arithmetic

**Arrays:** fixed-size containers that store objects of the same type (and same size) in contiguous memory.

```
int A[3] = {1,2}; // {1,2,0}
int B[3] = {}; // {0,0,0}
int C[] = {1,2}; // size = 2
int D[1][2] = {1,2,3}; // {{1,2},{3,0}}
int E[1][3] = {1,2,3}; // {{1,2,3}}
int F[3]; // CAUTION: uninitialized!
int G[]; // ERROR: unclear size
int H[2][1] = {1,2,3,4}; // Same
int I[] = {}; // Same
```

**Array decay:** using an array in a context where a value is required causes the compiler to convert the array into a pointer to its first element. Array decay is why it's necessary to pass an array's size separately from the array to a function (or to indicate the end of an array with a *sentinel character* like C-strings do).

- Dereferencing a pointer that goes past the bounds of an array results in undefined behavior. But merely *using* a pointer that goes just past the end of an array without dereferencing it is well-defined.

```
1 void reverseArray(int arr[], int size) {
2   for (int i = 0; i < (size / 2); ++i) {
3     int temp = arr[i]; // needed for swapping
4     arr[i] = arr[size - 1 - i]; // prints 3
5     arr[size - 1 - i] = temp; // prints 3
6   }
7 }
```

Passing an array by value passes a pointer to its first element by value, so functions with array parameters like this one actually have pointer parameters.

- The number of elements in an array `arr` is equal to `sizeof(arr) / sizeof(*arr)`.

```
1 cout << &arr[0],
2 cout << arr, and
3 cout << &arr
4 would all print
5 0x1008.
```

```
1 int foo = 7;
2 int& bar = foo; // value of bar is foo (7)
3 int* ptr = &foo;
4 int arr[3] = {4, 5, 9};
5 cout << arr << endl; // prints 0x1008 (decay)
6 cout << (arr + 2) << endl; // prints 0x1010
```

	0x1000	7	foo, bar
	0x1004	0x1008	ptr
	0x1008	4	arr[0]
	0x100c	5	arr[1]
	0x1010	9	arr[2]

**Pointer arithmetic:** adding an integer `n` to a pointer yields a pointer that is `n` objects forward in memory.

**Pointer subtraction:** Subtracting two pointers of the same type yields an integer (possibly a negative one) equal to the *number of objects* between them.

**Pointer comparison:** comparing pointers of the same type compares the addresses they store.

Using the `&` operator on an array produces a pointer to the entire array, not a pointer to the first element or a pointer to a pointer (`&` does not require a value, so it doesn't cause decay).

Static objects "live" for essentially a program's runtime. Local objects' lifetimes are tied to scope (e.g. a block of code or pair of curly braces). Dynamic objects are manually created/destroyed.

- Objects declared in a loop body (between the `{}`) are created/destroyed each time the loop repeats.

**Traversal By Pointer:** arrays can be traversed by pointer (mostly used with C-strings and iterators).

Traversal By Pointer: Pattern 1	Traversal by Pointer: Pattern 2 (C-String Sanitization)
<pre>1 int const SIZE = 3; 2 int arr[SIZE] = {-1, 7, 2}; 3 int* ptr = arr; 4 int* end = arr + SIZE; 5 // int* end is "1-past-the-end" of arr 6 while (ptr &lt; end) { 7   cout &lt;&lt; *ptr &lt;&lt; endl; 8   ++ptr; // "Walk" ptr across arr 9 } // Alternative to while loop below 1 for (; ptr &lt; end; ++ptr) { ... }</pre>	<pre>1 void sanitizeUsername(Account* acc, char to_remove) { 2   char* ptr1 = acc-&gt;username, *ptr2 = acc-&gt;username; 3   while (*ptr1 &amp;&amp; *ptr2) { // while not '\0' 4     if (*ptr2 != to_remove) { 5       *ptr1 = *ptr2; 6       ++ptr1; // ++ptr1 only when a char gets copied 7     } 8     ++ptr2; // ++ptr2 every time the loop executes 9   } 10  *ptr1 = '\0'; // null-terminate string when done 11 } // NOTE: '\0' is the only char that evaluates to false</pre>

## The const Keyword

The `const` type qualifier stops objects from being modified after initialization. Note: `const` scalars must be explicitly-initialized to compile, and `const` class-type objects must have their data members initialized.

**const pointers:** pointers that can modify what they point at but cannot be re-pointed to different objects.

**Pointer-to-const:** read-only pointers; pointers that can be re-bound but can't modify what they point at.

- A `const` pointer must be initialized to compile, but a pointer-to-`const` doesn't need to be.

**Reference-to-const:** a read-only alias.

**const array:** an array of `const` elements. Note that the placement of `const` matters for arrays of pointers.

```
const int* A[] = { ... }; // pointer-to-const array
int* const B[] = { ... }; // const pointer array
```

### const Conversions and Passing

The compiler treats every pointer-to-`const` as if they point to a `const` object and every reference-to-`const` as if they're aliased to a `const` object. It won't allow conversions that could bypass existing `const` protections (so, e.g., you can assign a `const` pointer to a pointer-to-`const`, but the converse is *not* true).

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998
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- C-Style Struct vs C++ Class**
- 1 The compiler implicitly creates a default ctor iff there are no user-defined ctors (same for dtors).
  - 2 The order in which members are declared in a class body is *always* the order they're initialized in.
  - 3 Initialization values from a member init. list take precedence over initializations made at declaration.
  - 4 You can't initialize members within a constructor body—attempting to do so actually performs default-initialization followed by assignment.
  - 5 A delegating ctor must contain a call to the other ctor (and nothing else) in its member init. list.

```
1 class Animal {
2 private: string name;
3 public:
4   Animal(const string& name_in)
5     : name(name_in) {}
6   Animal(): Animal("Blank") {} // Default ctor
7 }; // Default ctor delegates to other ctor
8
9 class Bird : public Animal {
10 private: bool can_fly;
11 public: Bird(string name_in, bool fly_in)
12       : Animal(name_in), can_fly(fly_in) {}
13 }; // Derived class ctors must call a base ctor
14
15 class Duck : public Bird {
16 private: int age;
17 public:
18   Duck(string name_in, bool fly_in, int age_in)
19     : Bird(name_in, fly_in), age(age_in) {}
20 }; // Calling Bird ctor also calls Animal ctor
21
22 // This is how to define a ctor OUTSIDE of body
23 Bird::Bird(string name_in, bool fly_in)
24   : Animal(name_in), can_fly(fly_in) {}
```

```
ADT Function Definition
1 // C-Style Struct
2 void Triangle::scale(Triangle *t, double s) {
3   t->a *= s; // ">" is necessary here
4 }
5
6 // C++ Class (Inside Body)
7 class Triangle { // "this->" optional
8   void scale(double s) { this->a *= s; }
9   }; // this-> implicit iff no name conflicts
10
11 // C++ Class (Outside Body)
12 void Triangle::scale(double s) { ... }
```

```
Object Creation/Manipulation
1 // C-Style Struct
2 Triangle t1;
3 Triangle_init(&t1, 3, 4, 5);
4
5 // C++ Class
6 Triangle t1; // Calls default ctor
7 Triangle t2(3,4,5); // calls 3-argument ctor
8 Triangle t3 = Triangle(3,4,5); // ditto
9
10 // Syntax for classes AND structs:
11 Triangle t4(3, 4, 5);
12 Triangle t5 = {3, 4, 5};
13 Triangle t6 = Triangle{3, 4, 5};
```

```
const Function Definition
1 // C-Style Struct
2 double area(const Triangle *t) { ... }
3 // const goes inside argument list
4
5 // C++ Class (Inside Body)
6 class Triangle {
7   double area() const { ... }
8   }; // const comes after signature
9
10 // C++ Class (Outside Body)
11 double Triangle::area() const { ... }
```

## Inheritance and Polymorphism

### Function Overloading (Ad Hoc Polymorphism) and Operator Overloading

**Function Overloading:** using one name for functions with *different signatures*. Functions can only be overloaded in the same scope (otherwise the "closer" scope takes priority). Note: `const/non-const` passing only alters the signature if a function has pointer/reference parameters (or implicit `this->` pointers).

**Operator Overloading:** operators like `+`, `*`, `<<`, etc. must be "overloaded" either as a top-level or class member function to work properly with custom classes (at least 1 operand must be of class-type).

- 1 An operator must be overloaded as a top level function if the first operand is an atomic type or a class type whose definition we can't access (e.g. `ostream`). Also, the `=`, `()`, `[]` and `->` operators can only be overloaded as member functions (along with overloads that need to access `private` members).

```
[ ] Overload Example (Member)
1 class IntSet {
2 ... // contains() is also a member function
3 public:
4   bool operator[](int v) const;
5 };
6
7 bool IntSet::operator[](int v) const {
8   return contains(v);
9 }
```

```
<< and == Overload Examples (Top-Level)
1 class Line { ... }; // start/end are public members
2
3 ostream& operator<<(ostream& os, Line line) {
4   return os << line.start << line.end;
5 } // os needs to be passed by non-const ref here
6
7 bool operator==(const Line &a, const Line &b) {
8   return (a.start == b.start && a.end == b.end);
9 } // Don't pass by non-const ref here
```

### Inheritance and Derived Classes

All base class members (EXCEPT ctors and dtors) become implicit members of derived classes. So you can call any non-private base class function on a derived class object or access non-private inherited data members via `.`/`->`.

- 1 Creating a derived class object *always* calls a base class ctor. If you don't call one explicitly, the base class default ctor will be implicitly called. Also, a base class dtor is always called when a derived object dies.

**Member name lookup** begins in the *static type* of a receiver/object and moves up the inheritance hierarchy (to the base class) if no match is found. It stops at the first member with a matching *name* or the top of the hierarchy.

- 1 Access levels are only checked *after* name lookup ends.
- 2 Member name lookup searches by name. Virtual function resolution at runtime searches by signature.

```
1 class Base {
2 public:
3   void print() { cout << "B" << endl; }
4   ~Base() {} // custom dtor syntax
5   }; // Base::~Base() outside class body
6
7 class Derived : public Base {
8 public:
9   void print() { cout << "D" << endl; }
10  void printB() { Base::print(); }
11 };
12
13 Derived d;
14 d.print(); // prints "D"
15 d.printB(); // prints "B"
16 d.Base::print(); // prints "B"
17 Base b = d;
18 b->print(); // prints "B"
```

Access Modifier	Out-of-scope access	Derived class access
public	✓ Yes	✓ Yes
private	✗ No	✗ No
protected	✗ No	✓ Yes

```
class A {
public: // Base class
  AC { cout << "A_ctor "; }
  ~AC { cout << "A_dtor "; }
};

class B : public A {
public: // Derived class
  BC { cout << "B_ctor "; }
  ~BC { cout << "B_dtor "; }
};
```

```
1 int main() {
2   A obj_a; // Prints "A_ctor "
3   B obj_b; // Prints "A_ctor B_ctor "
4   A* b_ptr = &obj_b; // Doesn't print anything
5   }; // When main returns: "B_dtor A_dtor A_dtor "
```

### Subtype Polymorphism and Class Casting

**Subtype polymorphism** allows a publicly-derived class object to be used in place of a base class object; to do this, a base class reference or pointer to a derived class object must be created.

```
1 class Bird { }; // Base class
2 class Chicken : public Bird { };
3 class Duck : public Bird { };
4 Bird b; Chicken c; Duck d;
5 b = c; // Legal, but "slices" c's data
6 Bird* b_ptr = &c; // Good, no slicing
7 c = b; // ERROR (illegal assignment)
8 Chicken* c_ptr = &b; // ERROR (downcast)
9 Duck* d_ptr = &c; // ERROR
```

```
C++ allows implicit upcasts (i.e. base pointers/refs to publicly derived objects), but all downcasts must be explicit via static_cast or (less preferably) dynamic_cast.

1 // Be careful - validity not checked at runtime:
2 Chicken *cPtr_a = static_cast<Chicken*>(&bird_ptr);
3 // Bird needs at least 1 virtual function for this:
4 Chicken *cPtr_b = dynamic_cast<Chicken*>(&bird_ptr);
```

### Virtual Functions and the `override` Keyword

Here, the *receiver* of the call to `talk()` on line 13 has a **static type** known at compile time (`Bird`) and a **dynamic type** known at runtime (`Duck`). Member lookup starts in the static class, so `Duck::talk` won't hide `Bird::talk`. Instead, `Bird::talk` is declared as **virtual** to make it dynamically-bound.

Declare a function as **virtual** when a receiver's static and dynamic type are different and you want to use the dynamic version of the function.

```
1 class Bird {
2 ... // virtual can only be used in a class body
3   virtual void talk() const { cout << "tweet"; }
4 };
5 // Note: ctors can't be virtual, but dtors can
6 class Duck : public Bird {
7 ... // "virtual" is optional/implicit here
8   void talk() const override { cout << "Quack"; }
9 }; // override = an optional "sanity check"
10 // override always goes at end of signature
11 Duck duck;
12 Bird* duck_ptr = &duck;
13 duck_ptr->talk(); // prints "Quack"
14 // Scope resolution operator can suppress virtual
15 duck_ptr->Bird::talk(); // prints "tweet"
```

**override keyword:** tells the compiler to verify that a function overrides a base-class **virtual** function with a matching signature (if no override is found, **override** causes a compile error).

### Pure Virtual Functions and Abstract Classes

**Pure virtual function:** a **virtual** base-class function that has no meaning or implementation (their purpose is to specify the interface of derived classes). To declare one, add `= 0;` to the end of a function's signature.

**Abstract class:** a class with at least one pure virtual member function. Note that derived classes of an abstract class will also be abstract unless they override (i.e., implement) every pure virtual function they inherit.

**Interface (pure abstract class):** a class that contains nothing but pure virtual member functions.

```
1 class Abst { // Abstract Class
2 public: virtual void foo() = 0;
3 }; // Note the lack of empty braces
4
5 class Concrete : public Abst {
6 public: void foo() { cout << "foo"; }
7 }; // public/private doesn't matter here
8
9 Concrete c;
10 Abst* c_ptr = &c; Abst& c_ref = c; // ok
11 class Abst_obj { // COMPILER ERROR
12 c.Abst::foo(); // RUNTIME ERROR (or U.B.)
```

- 1 Don't call pure virtual functions or try to instantiate abstract classes.

## Containers, Templates and Array-Based Data Structures

### Container ADTs

**static keyword:** used to make one copy of a class data member "shared" between all instances of that class. A **static** data member has static storage duration but exists only within the scope of a class.

**stack:** a container that's designed to operate in a LIFO order.

**queue:** a container designed to operate in a first-in/first-out (FIFO) order.

- 1 An efficient way to implement a queue is to create a vector with free space at both ends (a **ring/circular buffer**). To do so, keep track of the data using head (inclusive) and tail (exclusive) variables.

Useful std::vector Functions					Operation				
	size()	v[i]	.push_back(val)	.pop_back()	.resize(n)	insert/remove	Unsorted Set	Sorted Set	Stack
	.front()	.back()	.at(i)	.empty()	.clear()	search	O(n)	O(n)	O(1) <sup>2</sup>
						access	O(1)	O(1)	O(n)

### C++ Standard Library Containers

**std::array:** Fixed-size containers that store elements in contiguous memory.

**std::vector:** resizable containers that store elements at the front and free space at the back.

**std::list:** a container whose elements are linked via pointers (i.e., in non-contiguous memory).

**std::map:** an associative array that maps unique keys to values. Keys act like indexes for a map.

**std::set:** an associative sorted container that only stores unique keys.

```
C++ Standard Library Containers
1 std::array<int, 4> arr = {-4, 0, 3, 6};
2 std::vector<int> vec = {4, 7, 2};
3 std::set<int> unique = {3,2,1}; // {1,2,3}
4 // Note: can't index into a std::list
5 std::list<int> values = {1, 2, 3};
6
7 // The elements of a map are <key, val> pairs
8 std::map<string, int> EECS = {{"Bill", 183}};
9 EECS["Emily"] = 203;
10 EECS.insert(pair<string, int>("James", 280));
11 cout << EECS["James"] << endl; // prints 280

Useful std::map functions
// Returns iterator to the pair with Key == k
// Returns .end() iterator if no such pair exists
iterator find(const Key_type& k) const;

// Inserts a pair of <key, T value> into a map
// Returns <iterator, false> if key in map already
pair<iterator, bool> insert(const Pair_type &val);

// Returns a reference to a key's associated value
// If it doesn't exist, enters it into the map
Value_type& operator[](const Key_type& key_val);
```

Container	Ordering	Default Sort	Sizing	Default-Construction	Allocation	Value Type	Duplicate Values
std::array	Sequential	Unsorted	Fixed-size	Undefined values	Contiguous	T	Yes
std::vector	Sequential	Unsorted	Dynamic	Empty container	Contiguous	T	Yes
std::list	Sequential	Unsorted	Dynamic	Empty container	Not Contiguous	T	Yes
std::map	Associative	Ascending (by key)	Dynamic	Empty container	Not Contiguous	pair<const Key, T>	No repeat keys
std::set	Associative	Ascending	Dynamic	Empty container	Not Contiguous	Key	No

### Templates (Parametric Polymorphism)

**Templates:** flexible models for producing code that take a data type as a parameter to create an object or call a function that works with that type. They help reduce code duplication in container ADT interfaces.

- 1 A template can accept an invalid type argument during instantiation (leading to a runtime error).

```
Class Template Syntax
1 template <typename T>
2 class UnsortedSet {
3 public:
4   void insert(T my_val);
5   bool contains(T my_val) const;
6   int size() const;
7 private:
8   T elts[ELTS_CAPACITY];
9   int elts_size;
10
11 }; // Syntax: UnsortedSet<type> s;

Function Template Syntax
1 template <typename T> // "T" = an arbitrary parameter name
2 // Note: "class" also works in place of "typename".
3 T maxVal(const T &valA, const T &valB) {
4   return (valB > valA) ? valB : valA; // "?" == conditional
5 } // This function returns the greater of valA and valB
6 // Syntax to call it: maxVal<int/double/etc>(...);

Templated Class Member Function Syntax
1 template <typename T> // Necessary if outside class body
2 void UnsortedSet<T>::insert(T my_val) { ... }
```

### Iterators, Traversal by Iterator and Range-Based Loops

**Iterators:** objects that have the same *interface* as pointers; they provide a general interface for traversing different types of container ADTs. To implement iterators for an ADT, define them as a nested class within the container's class and overload the `*` (dereference), `++`, `==`, and `!=` operators.

- 1 `std::begin()` returns an iterator to the start of an STL container. `std::end()` returns an iterator that's 1 past the end of an STL container (the iterator returned by `std::end()` should not be dereferenced).

- 1 Using an *invalidated* iterator (e.g. an iterator pointing at a deleted element) causes undefined behavior.

Container	std::array	std::vector	std::list	std::map	std::set
Iterator	Random Access	Random Access	Bidirectional	Bidirectional	Bidirectional
Operations	->, [], ++, --, ==, !=, *, +, +=	->, [], ++, --, ==, !=, *, +, +=	++, --, ==, !=, *, +, +=	++, --, ==, !=, *, +, +=	++, --, ==, !=, *, +, +=

**Traversal by iterator:** a more general form of traversing a container data type by pointer.

```
1 vector<int> v(3, -1); // this syntax initializes v to {-1,-1,-1}
2 for (vector<int>::iterator it = v.begin(); it != v.end(); ++it)
3   { cout << *it << endl; } // ::const_iterator if const vector
```

```
Range-Based For Loop (Works on Any Sequence Traversable by Iterator)
1 vector<int> v = {1, 2, 3, 4};
2 // for (<type> <variable> : <sequence>) { ... }
3 for (int item : v) { // works with arrays too
4   cout << item << endl;
5 } // could also declare item as const or a ref

1 // Compiler translation of range-based for loop
2 for (auto it = v.begin(); it != v.end(); ++it) {
3   int item = *it;
4   cout << item << endl;
5 }
```

Time Complexity									
O(1)	O(log n)	O(√n)	O(n)	O(n log n)	O(log(n!))	O(n <sup>2</sup> )	O(n <sup>3</sup> )	O(2 <sup>n</sup> )	O(3 <sup>n</sup> )
								O(n!)	O(n <sup>n</sup> )
									O(2 <sup>n<sup>2</sup></sup> )

- 1 Functions in the same complexity class should have growth rates that differ by a constant factor as  $n \rightarrow \infty$ . So  $O(2^n)$  and  $O(8^n)$  are NOT in the same complexity class, but  $O(\log_2 n)$  and  $O(\log_3 n)$  are.

**Determining Asymptotic/Big-O Complexity**

**Constant coefficients:** if they're not part of an exponent, ignore them. Ex:  $O(3n) = O(0.5n) = O(n)$ .

**Addition** (sequential procedures): the highest-complexity term dominates. Ex:  $O(n^2 + n + \log n) = O(n^2)$ .

**Multiplication:** multiply the individual terms' complexities. Ex:  $O(n \times \log n) = O(n \log n)$ .

**Non-nested loops:** *sum* the complexities of each operation *inside* the loop body and *multiply* that by the number of times the loop executes. Ex: a loop that runs from 0 to n with a  $O(\log n)$  body is  $O(n \log n)$ .

**Nested loops:** start at the innermost loop and work outwards (the individual complexities of the loops should multiply). Ex: two nested  $O(n)$  loops will do  $n$  work  $n$  times, so they're  $O(n^2)$ .

**Partitioning/repeated division:** procedures that divide the "remaining steps" by a constant number each time they execute (e.g. binary search, for-loops that double the loop counter) are usually  $O(\log n)$ .