

# Deep Learning Tomography

Lecture 9b

# Outline

- Optical Diffraction Tomography Introduction (ODT)
- Machine Learning for ODT
  - 1. TomoNet
    - accounts for the missing cone problem
  - 2. MaxwellNet
    - physics informed neural network
- Microfluidic Implementation

# 3D rendering

- <https://www.chaos.com/blog/what-is-3d-rendering-guide-to-3d-visualization>

# 3D rendering versus 3D inverse scattering

- Rendering:              Realistic 2D projections from 3D computer model
- Inverse scattering:    3D reconstruction from 2D measurements

# First step: to digitize the “Archivio di Stato”



Two main challenges:

- ★ Huge amount of manuscripts  
80 km of documents

- ★ Birth and death records
- ★ Testaments
- ★ Tax declarations
- ★ Commercial transactions
- ★ Work contracts ...

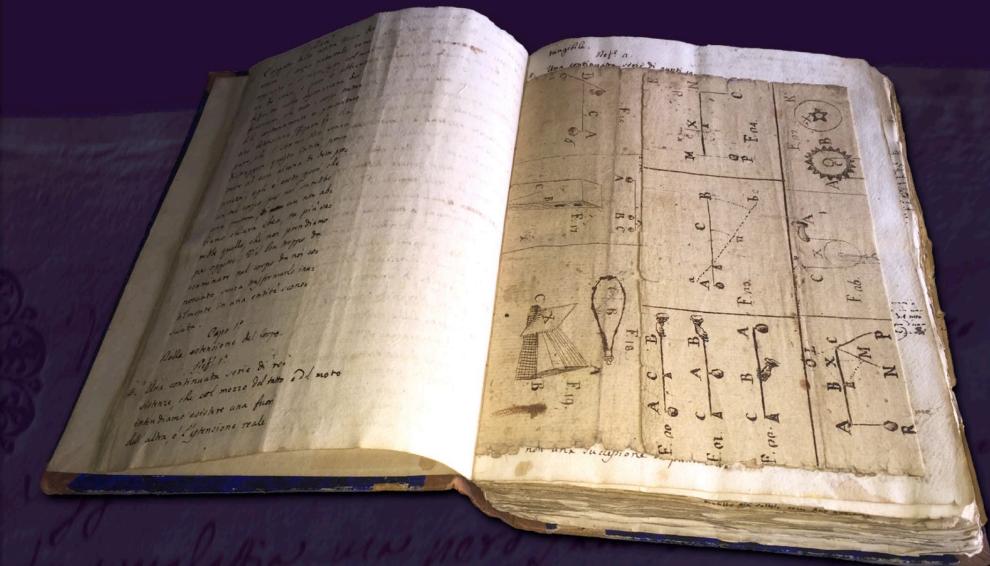
- ★ A variety of formats

- ★ Single sheets
- ★ Bounded volumes
- ★ Closed testaments
- ★ Scrolls

# Milestones :

Book

3D Imaging of a  
XIX century Physics Book



★ Handwritten book

★ Large size object

★ Text

★ Drawings

★ 20 x 25 cm

★ 200 pages

# Milestones :

Book

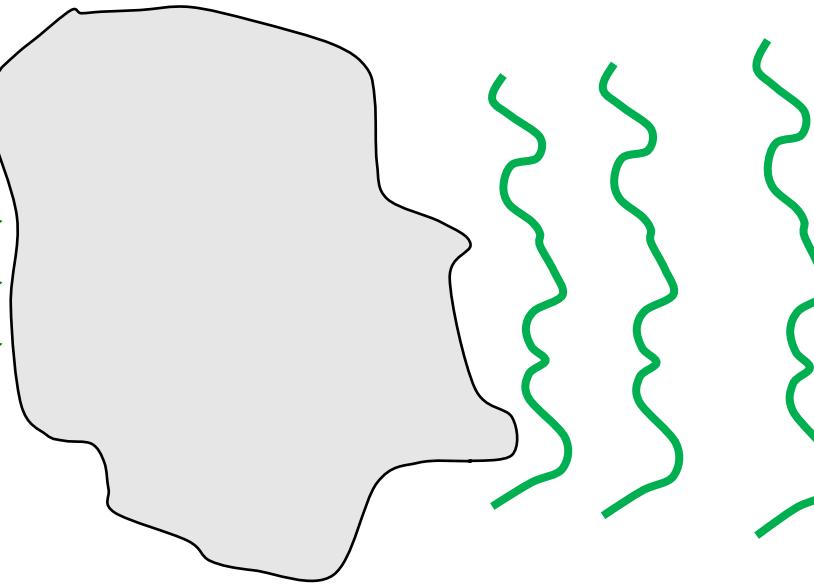
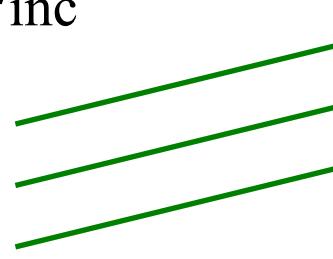
3D Imaging of a  
XIX century Physics Book



# Optical Tomography

Illumination

$E_{\text{inc}}$

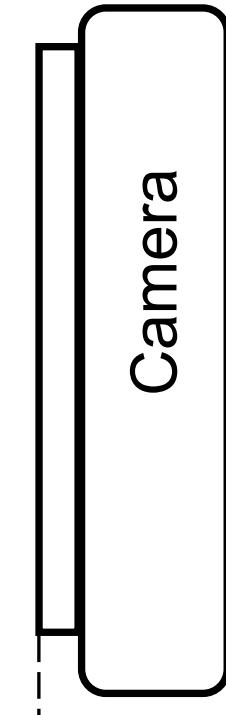
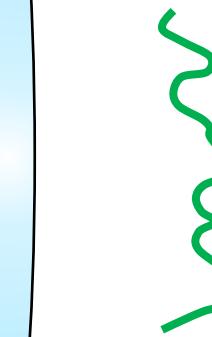


3D object

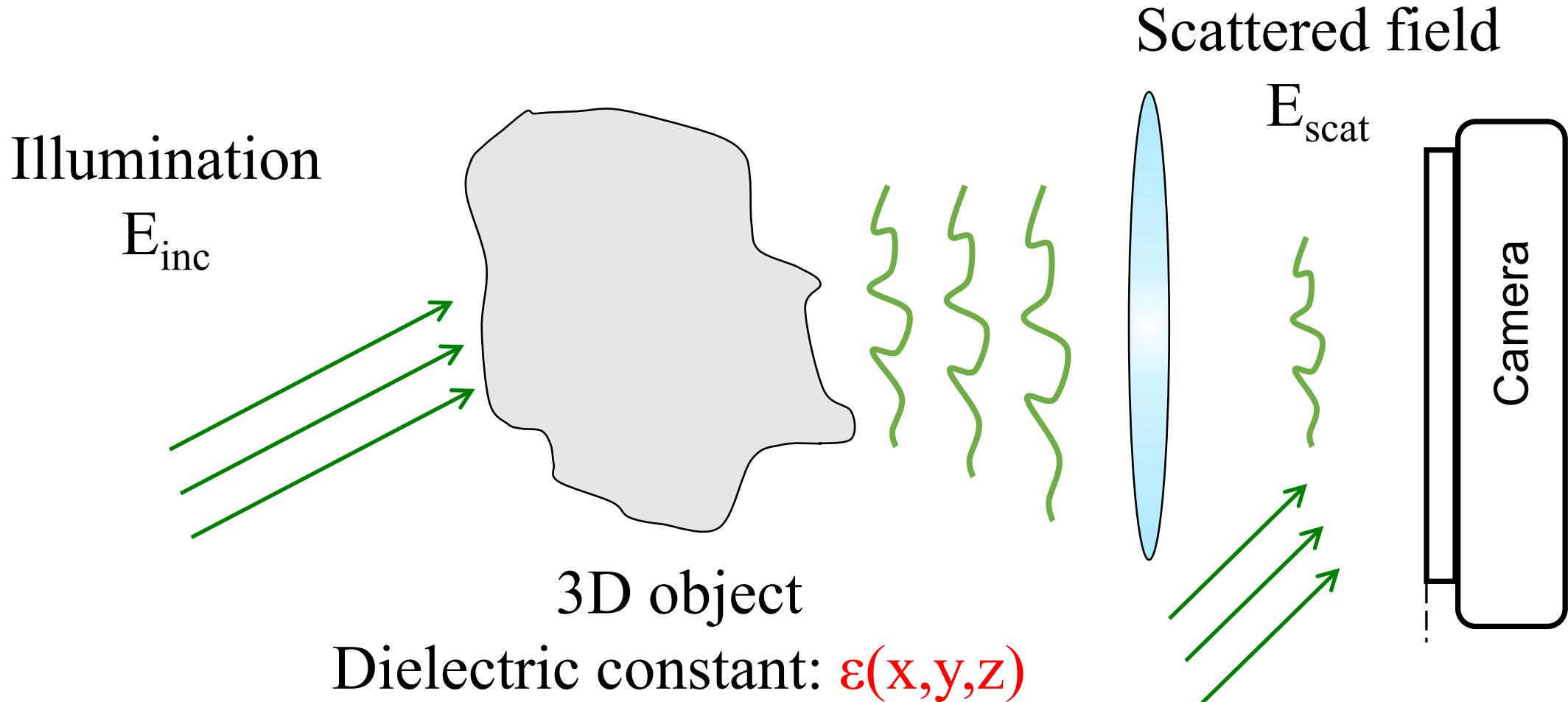
Dielectric constant:  $\epsilon(x,y,z)$

Scattered field

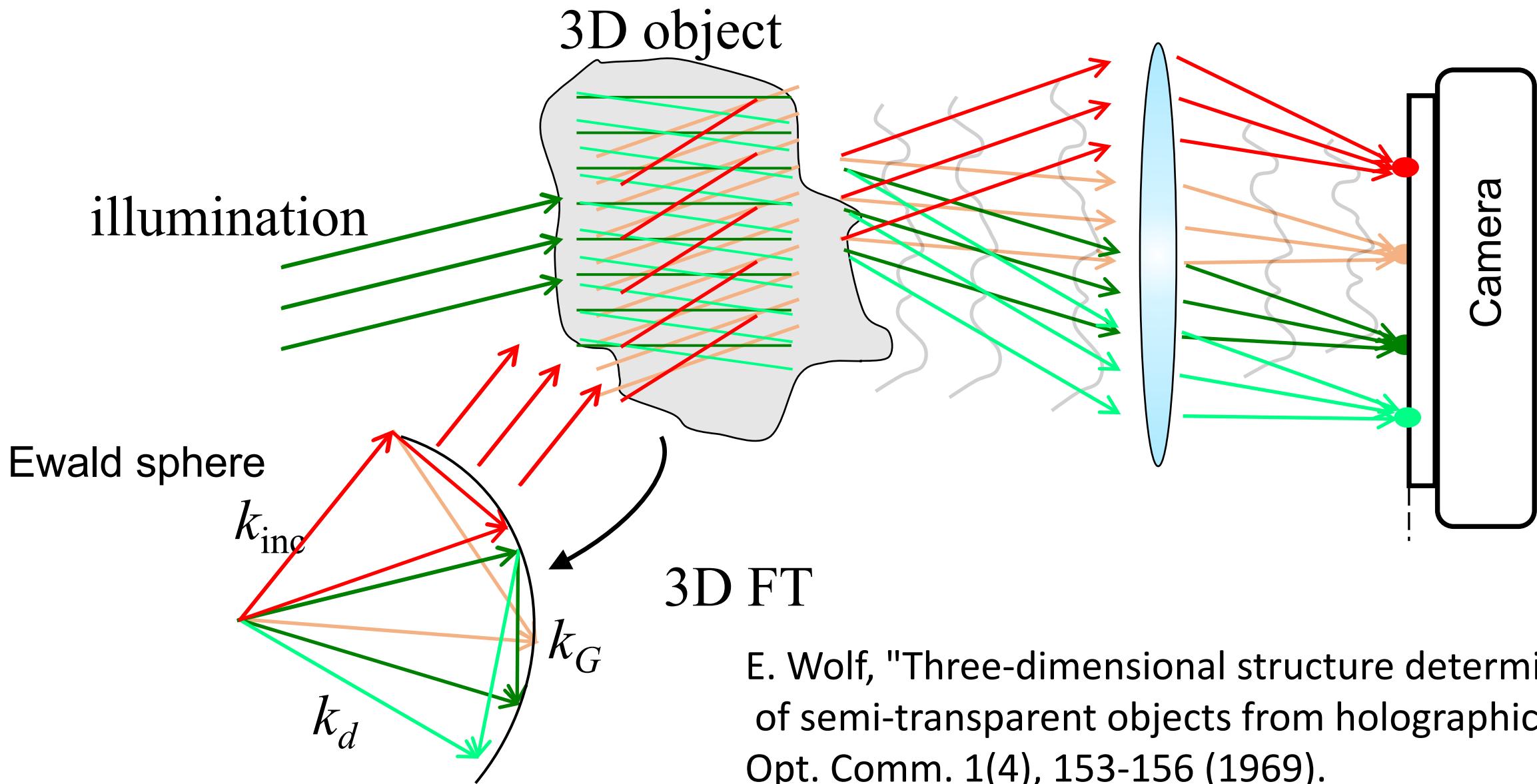
$E_{\text{scat}}$



# Optical Diffraction Tomography



# The *Wolf transform*

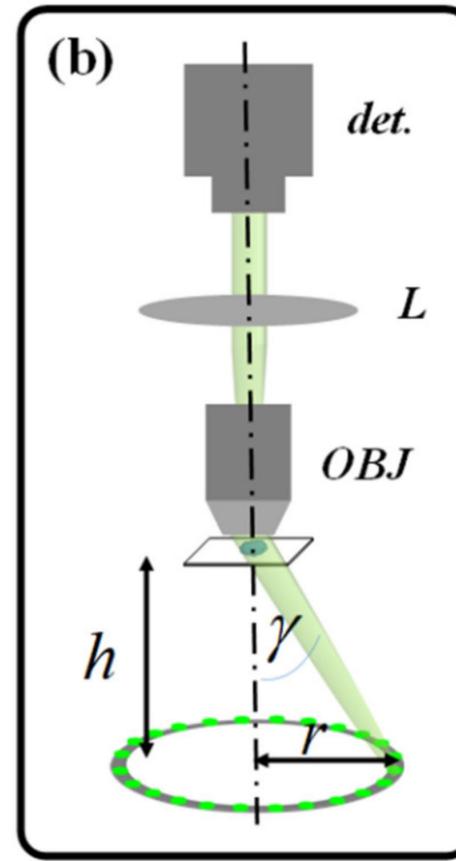


# Optical Diffraction Tomography with the LED ring

(a)



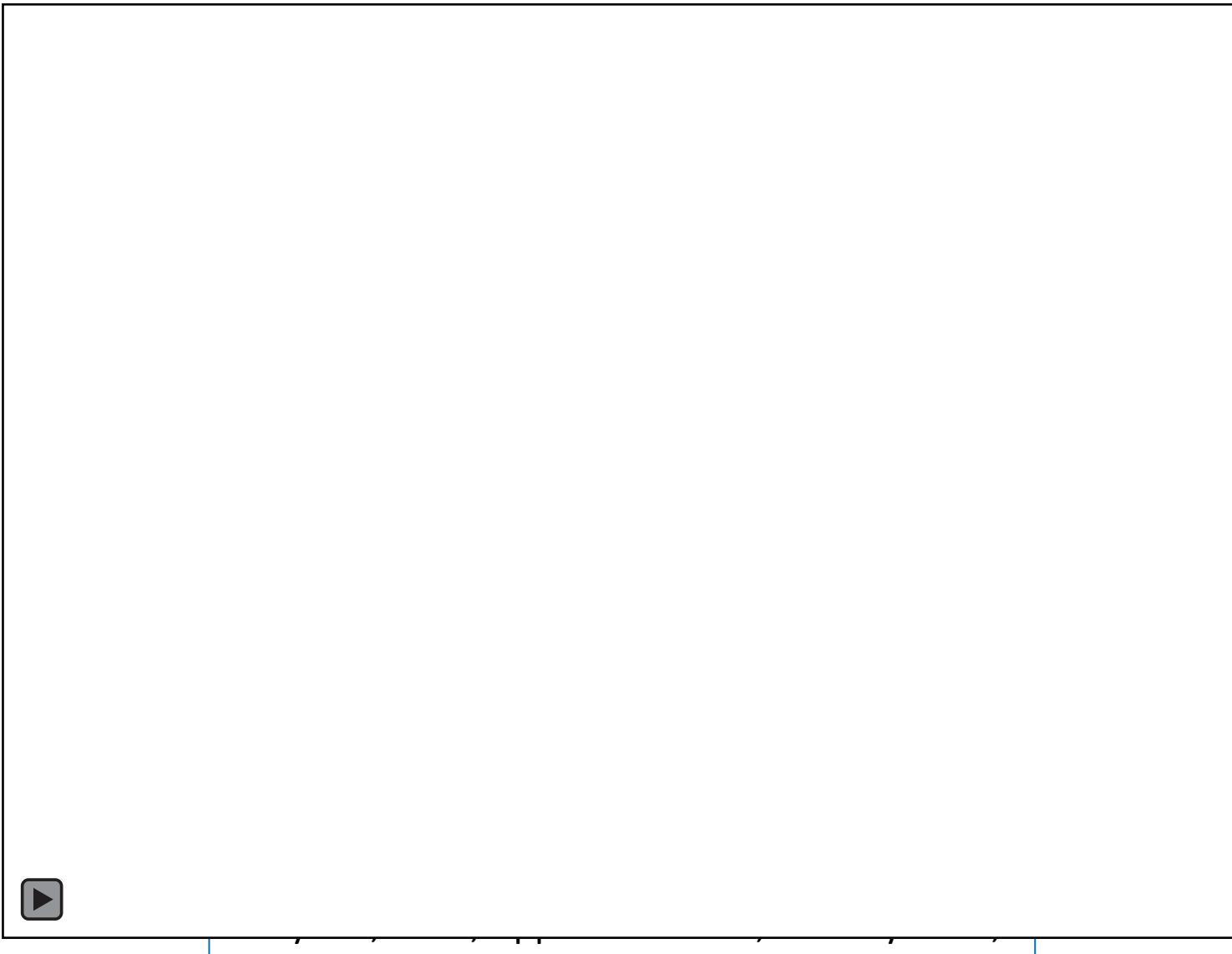
(b)



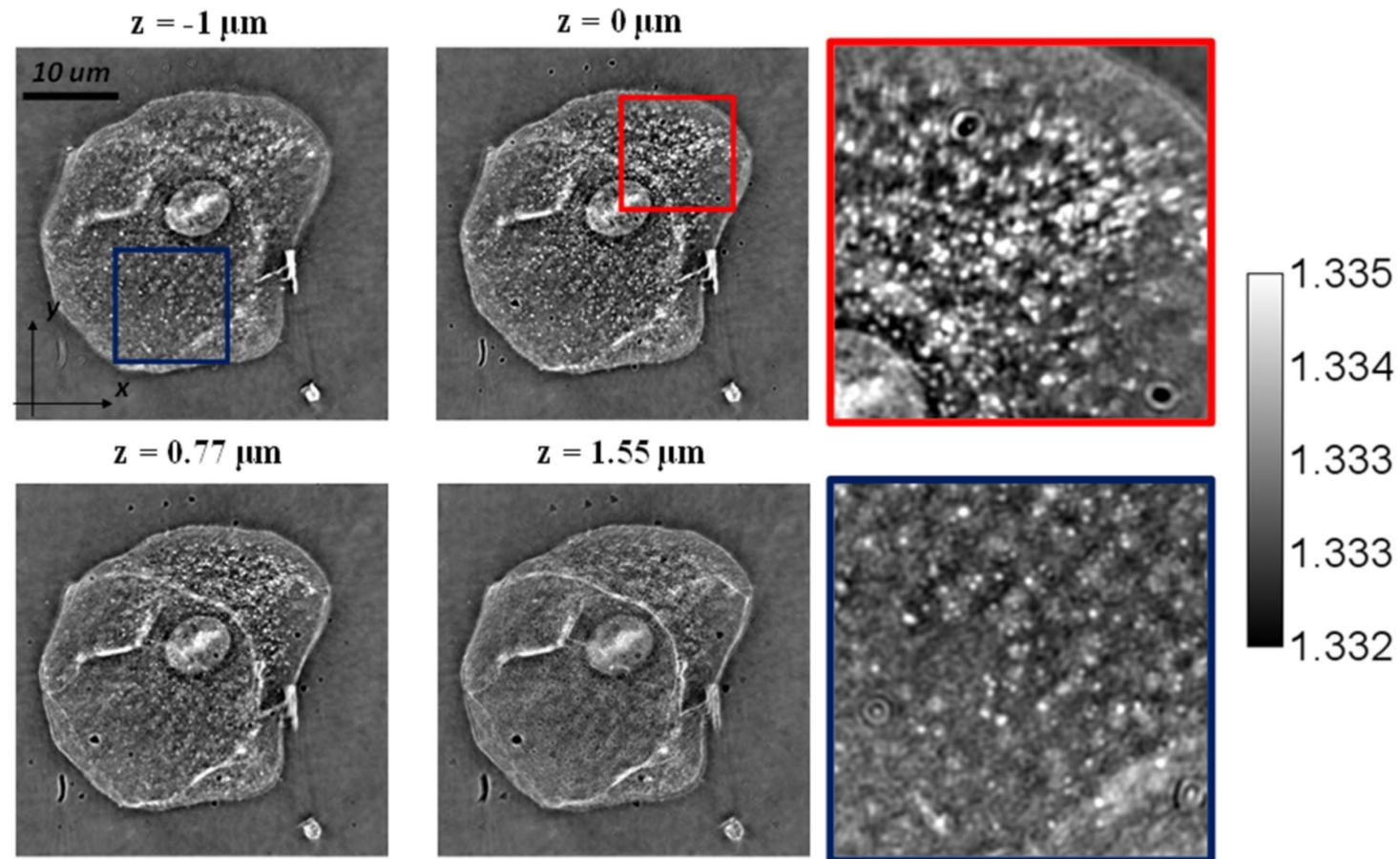
3D intensity and phase imaging from light field measurements in an LED array microscope, [Tian and Waller](#), Optica, 2015

Optical Diffraction Tomography using Nearly In-Line Holography with a Broadband LED Source, Ayoub, Roy and Psaltis, Applied Sciences, 2022.

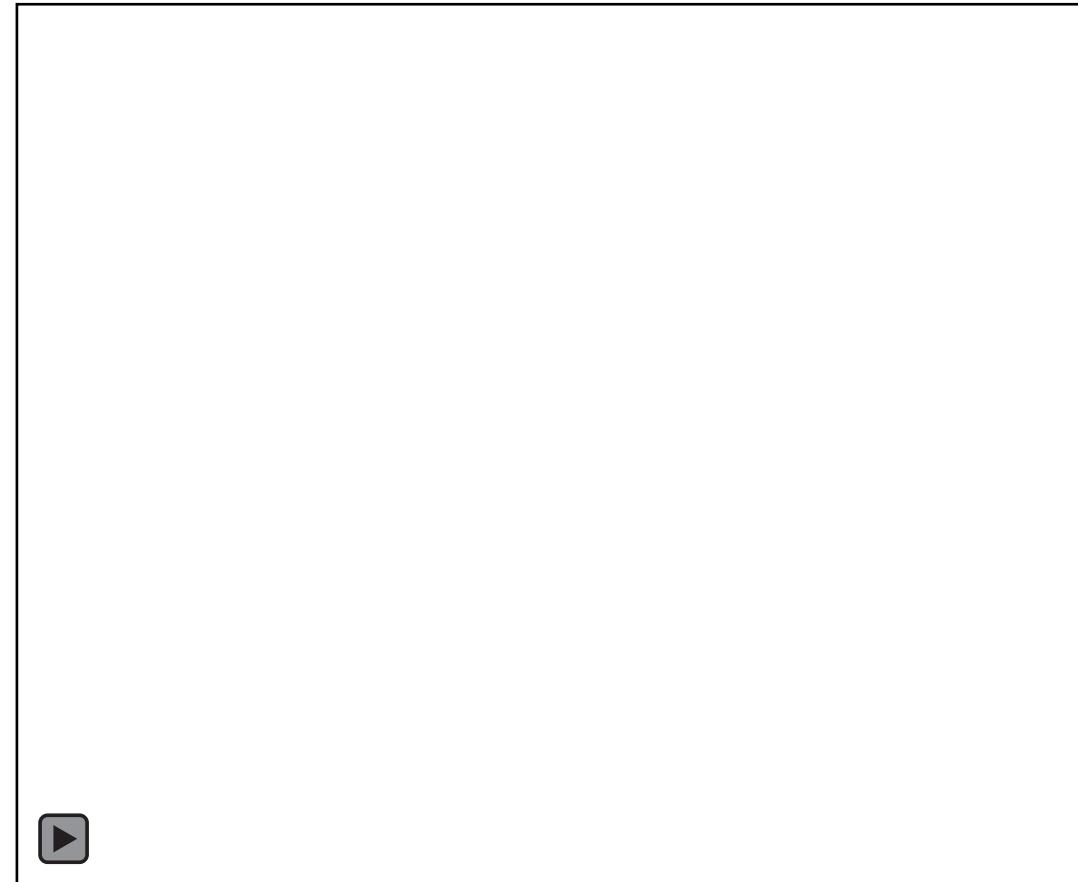
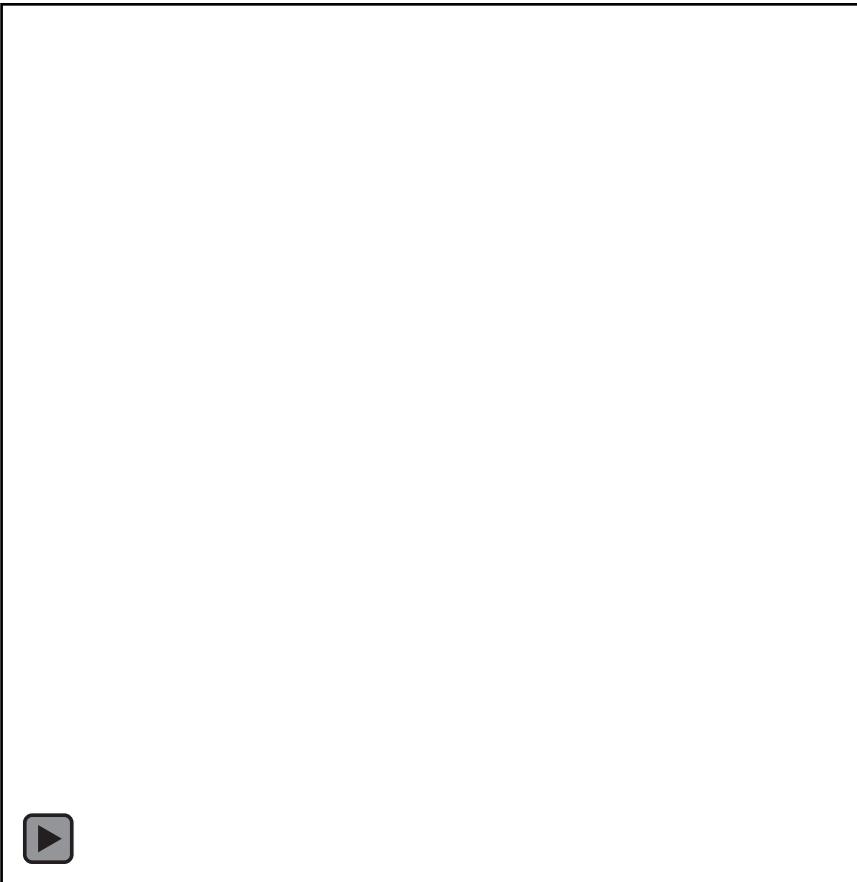
# Hologram of cheek cell and its 2D spectrum



# Cheek cell reconstruction



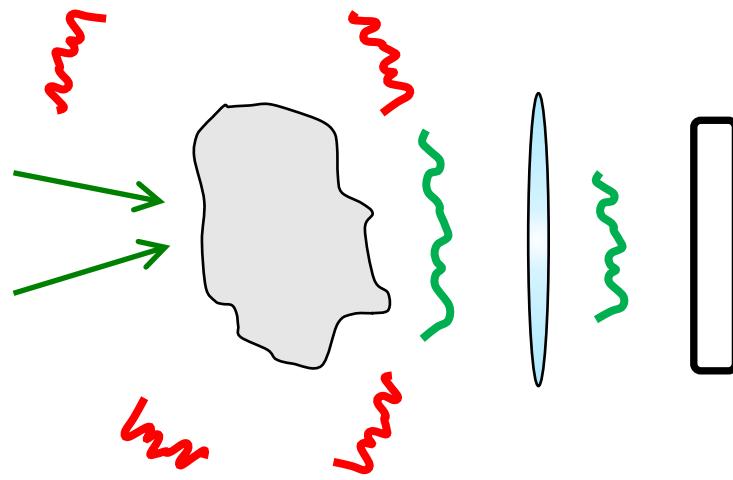
# 3D RI Reconstruction examples



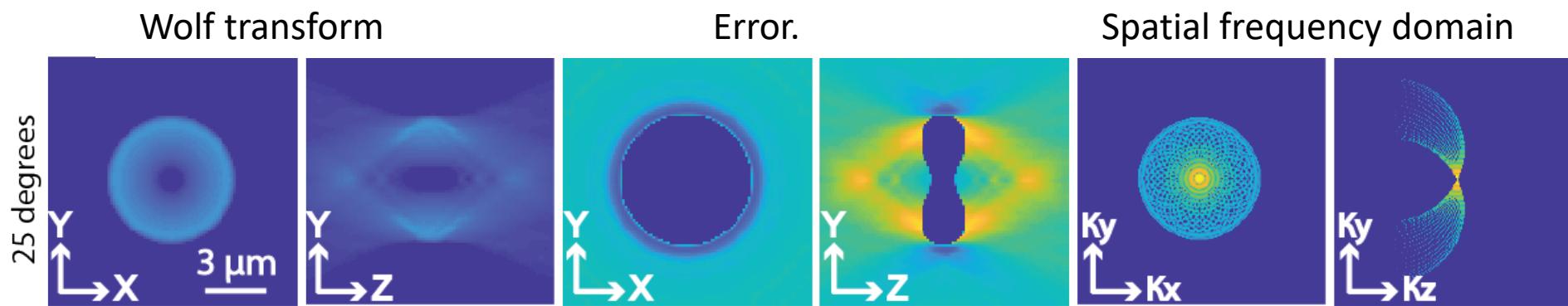
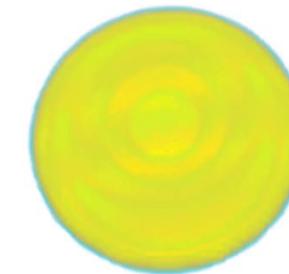
# Machine learning for ODT ?

1. Multiple scattering  
(e.g Reflections)
2. Limited Numerical Aperture  
(Missing cone problem)
3. Fast phase from intensity
4. Scalar approximation  
(Birefringent objects)
5. Optical Nonlinearities
6. Denoising  
(Speckle)

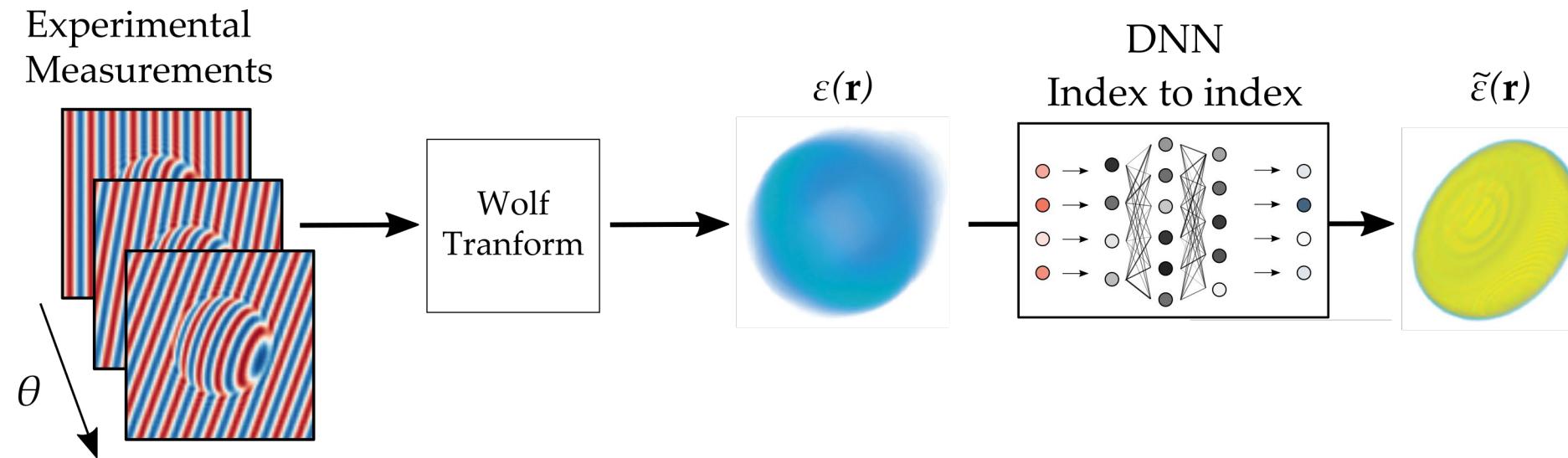
# The missing cone problem



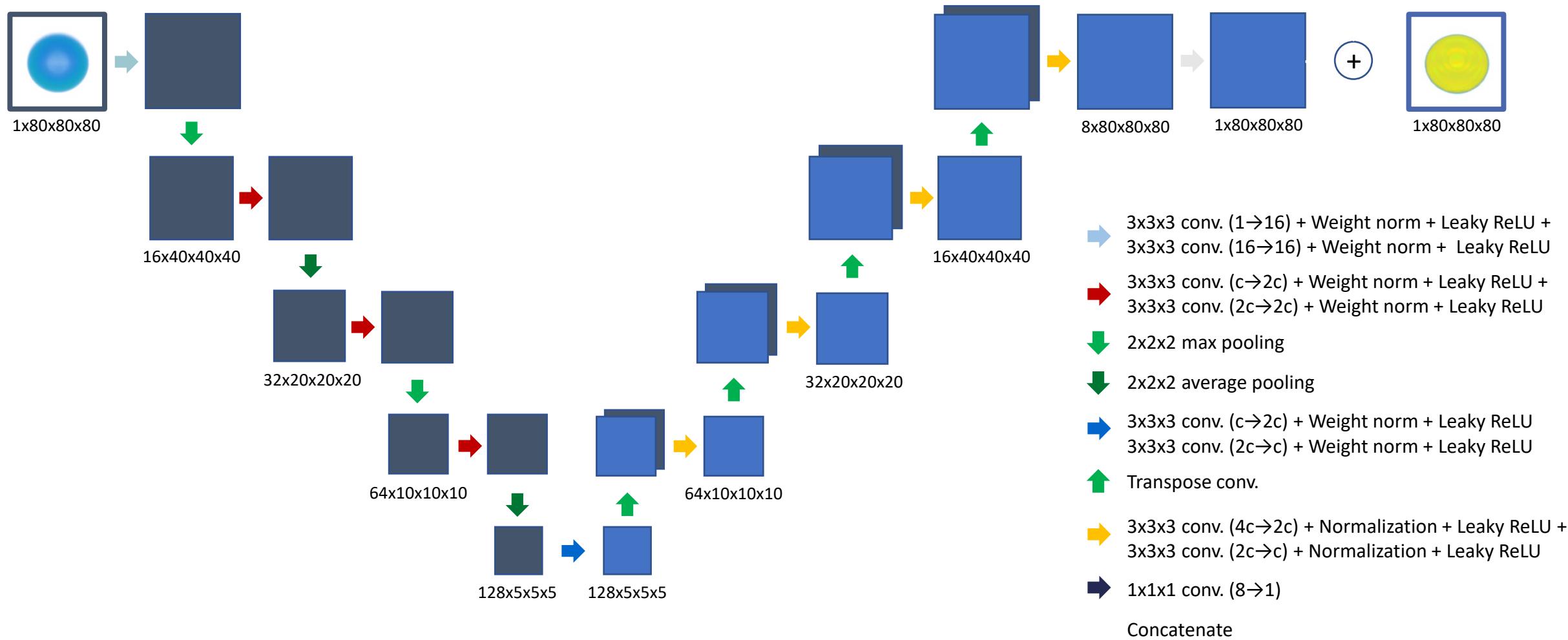
Red blood cell



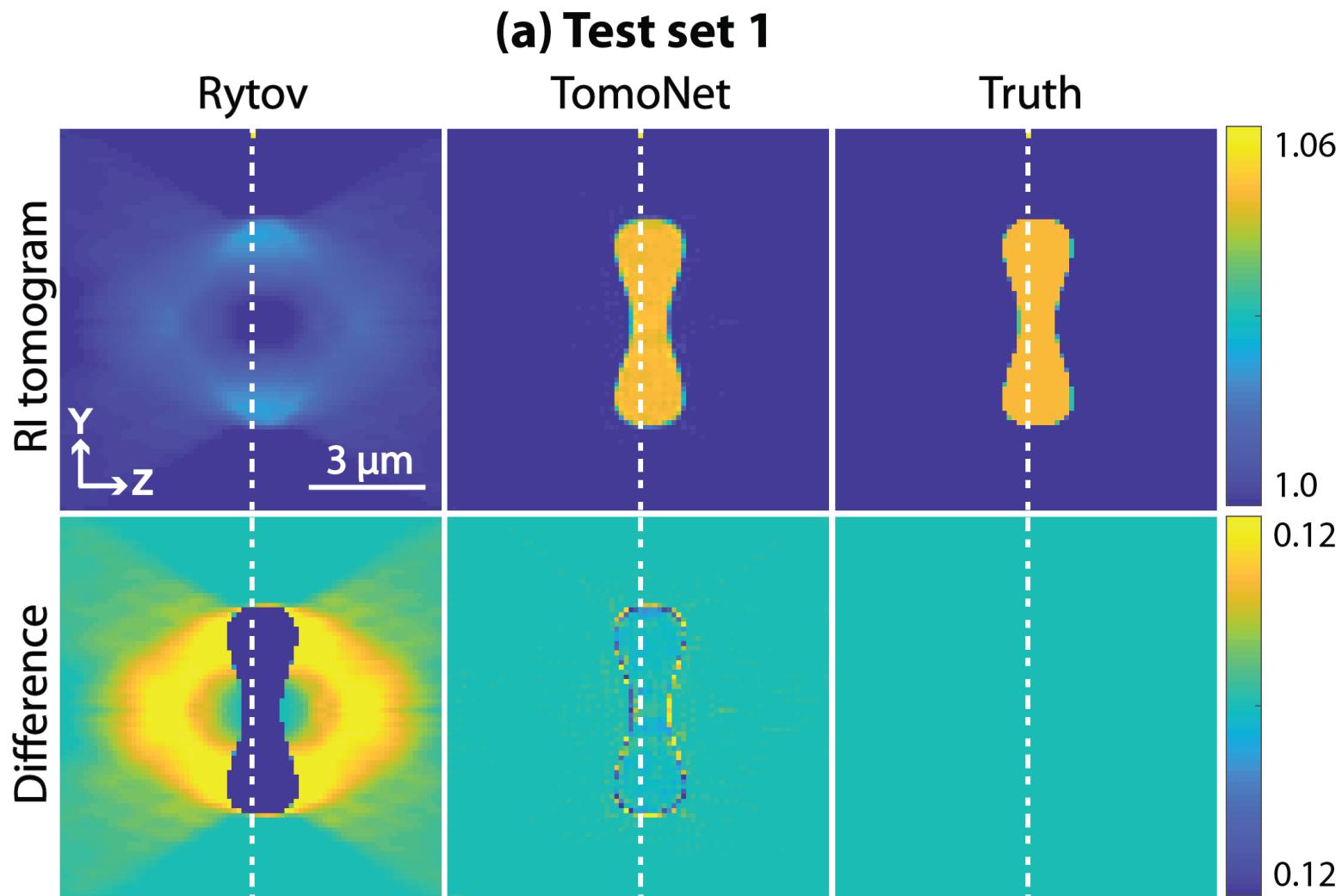
# Machine Learning for the missing cone problem



# TomoNet structure



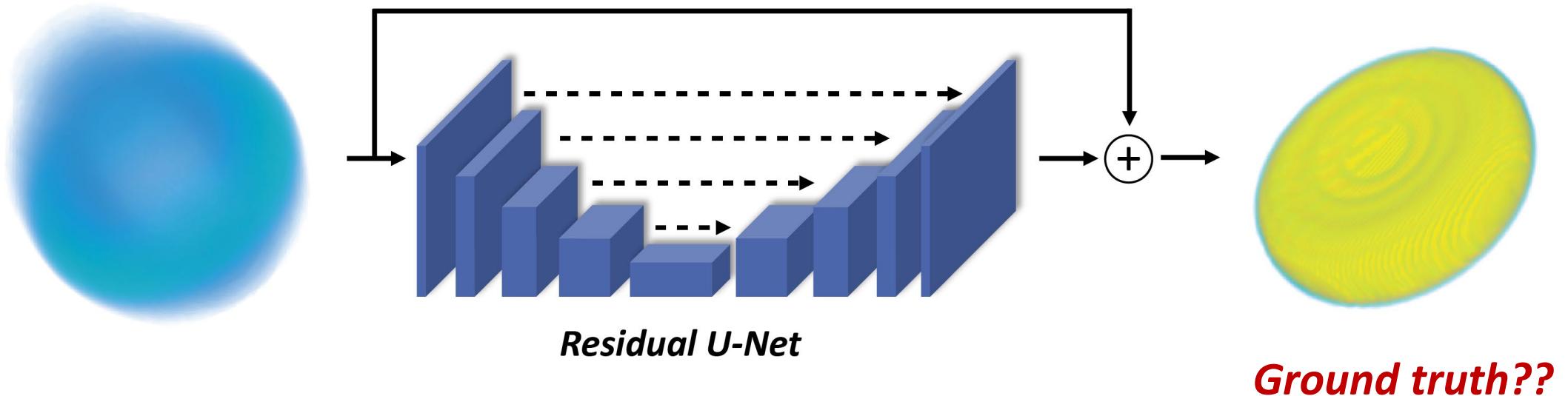
# Result on synthetic data



# Deep learning based correction for ODT

Rytov

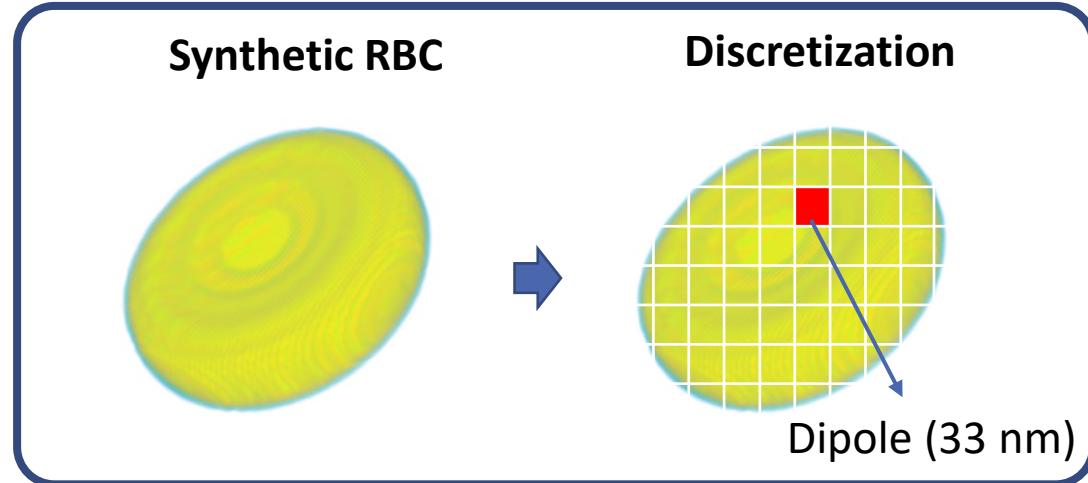
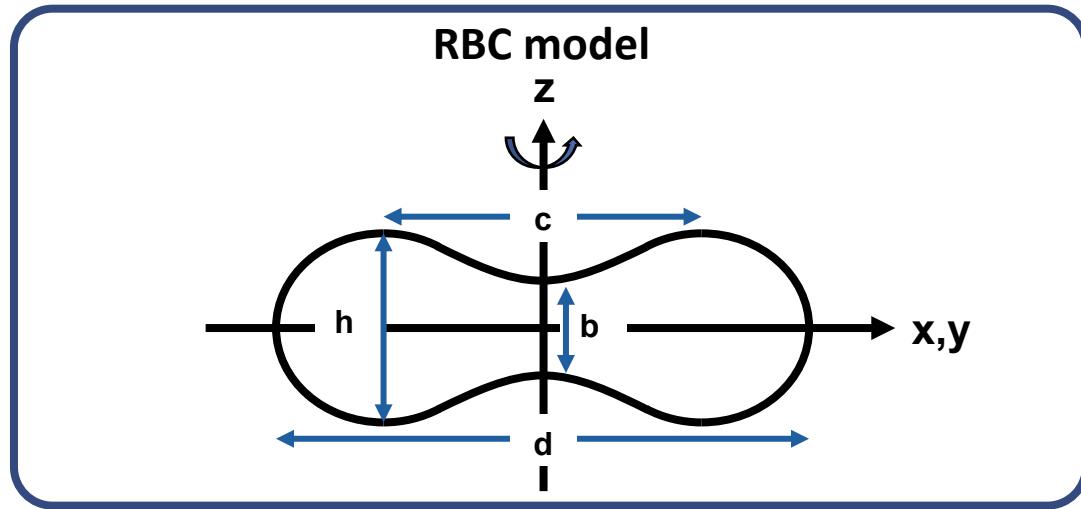
Truth



## Recent machine learning applications in Optics:

- **Virtual staining** : Rivenson, Yair, et al., *LSA* (2019), Borhani, Navid, et al., *BOE* (2019)
- **Phase retrieval** : Borhani, Navid, et al., *Optica* (2018), Xue, Yujia, et al. *Optica* (2019)
- **Classification / Segmentation** : Yoon, Jonghee, et al., *Sci. Rep.* (2017), Lee, Jimin, et al., *IEEE Access* (2019)
- + Many

# Discrete Dipole Approximation (DDA)



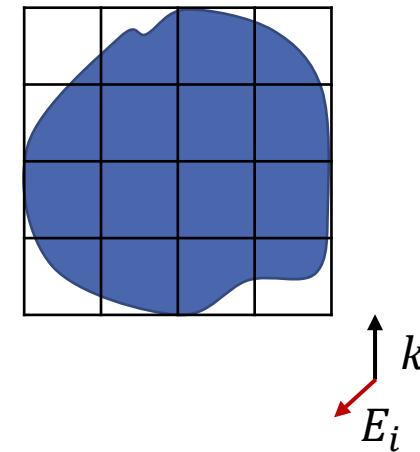
## Discrete Dipole Approximation (DDA) [1]

- ✓ For particles of arbitrary geometry
- ✓ Representation of continuum target by discrete dipoles
- ✓ Integral solution of  $\nabla^2 \mathbf{E} + k^2 \mathbf{E} = 0$

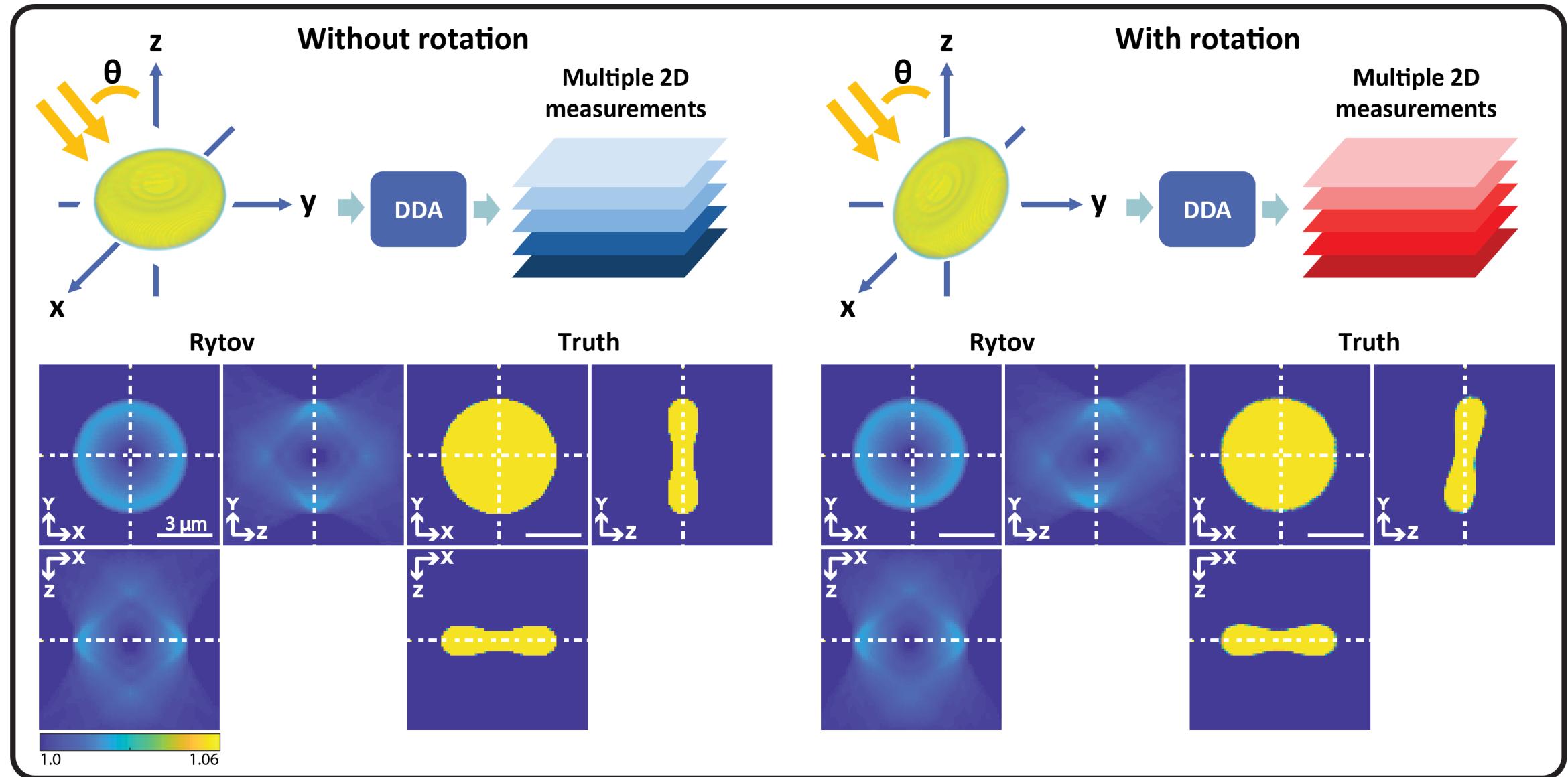
$$\mathbf{E}(\mathbf{r}) = \mathbf{E}^{inc}(\mathbf{r}) + \int_{V \setminus V_0} d^3\mathbf{r}' G(\mathbf{r}, \mathbf{r}') \chi(\mathbf{r}') \mathbf{E}(\mathbf{r}') + \mathbf{M}(V_0, \mathbf{r}) - \mathbf{L}(\partial V_0, \mathbf{r}) \chi(\mathbf{r}) \mathbf{E}(\mathbf{r})$$

- ✓ Discretization of the solution

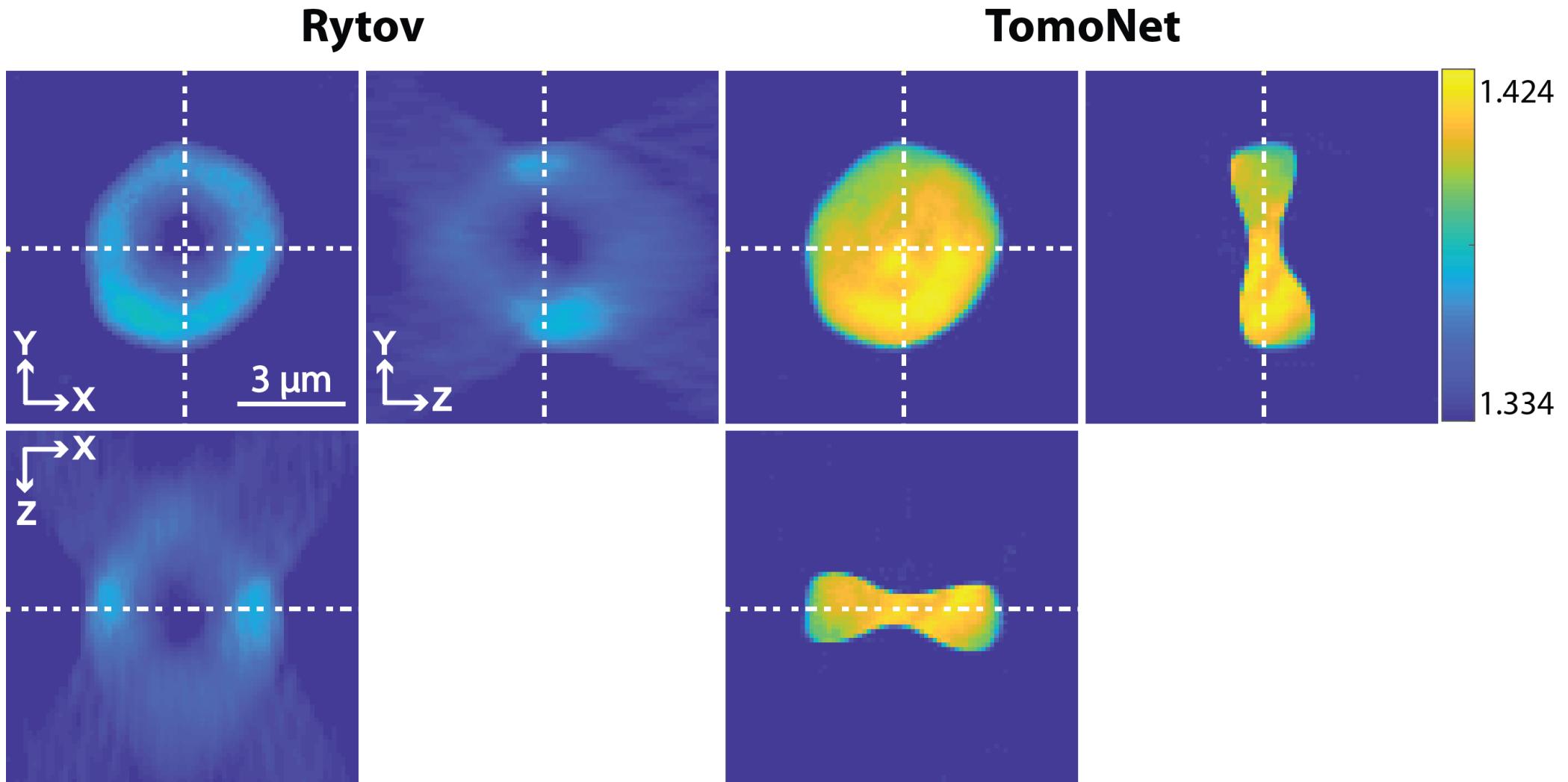
$$\mathbf{E}(\mathbf{r}) = \mathbf{E}^{inc}(\mathbf{r}) + \sum_{j \neq i} \int_{V_j} d^3\mathbf{r}' G(\mathbf{r}, \mathbf{r}') \chi(\mathbf{r}') \mathbf{E}(\mathbf{r}') + \mathbf{M}(V_i, \mathbf{r}) - \mathbf{L}(\partial V_i, \mathbf{r}) \chi(\mathbf{r}) \mathbf{E}(\mathbf{r})$$



# Data generation



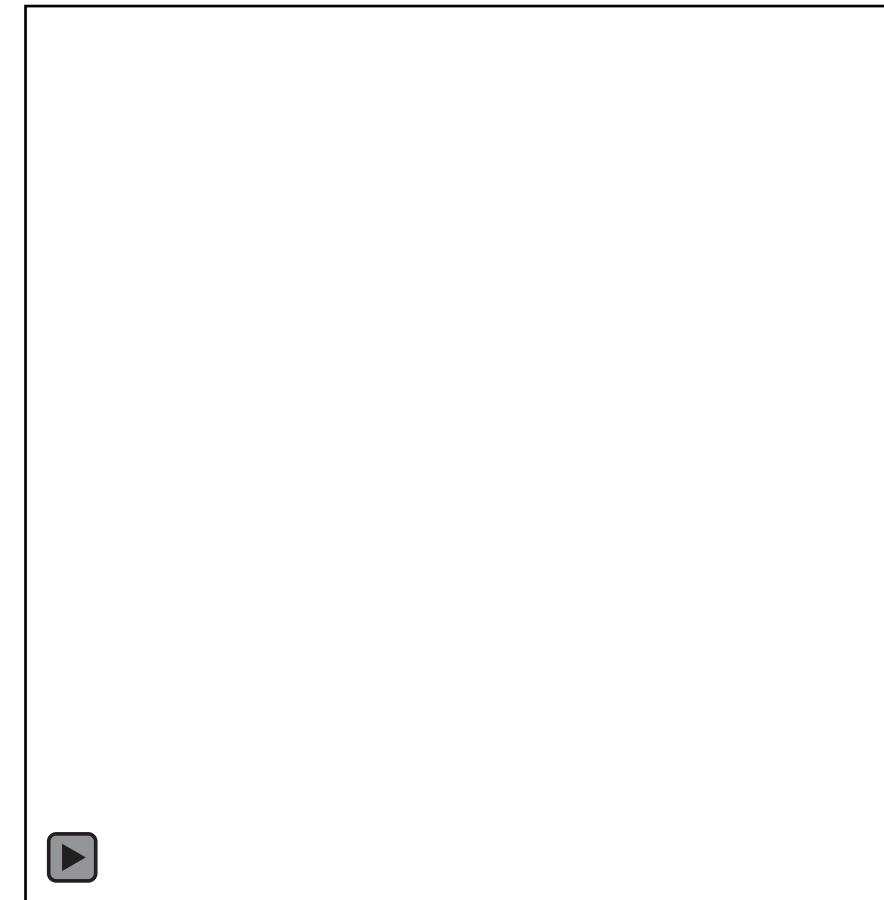
# Experimental result



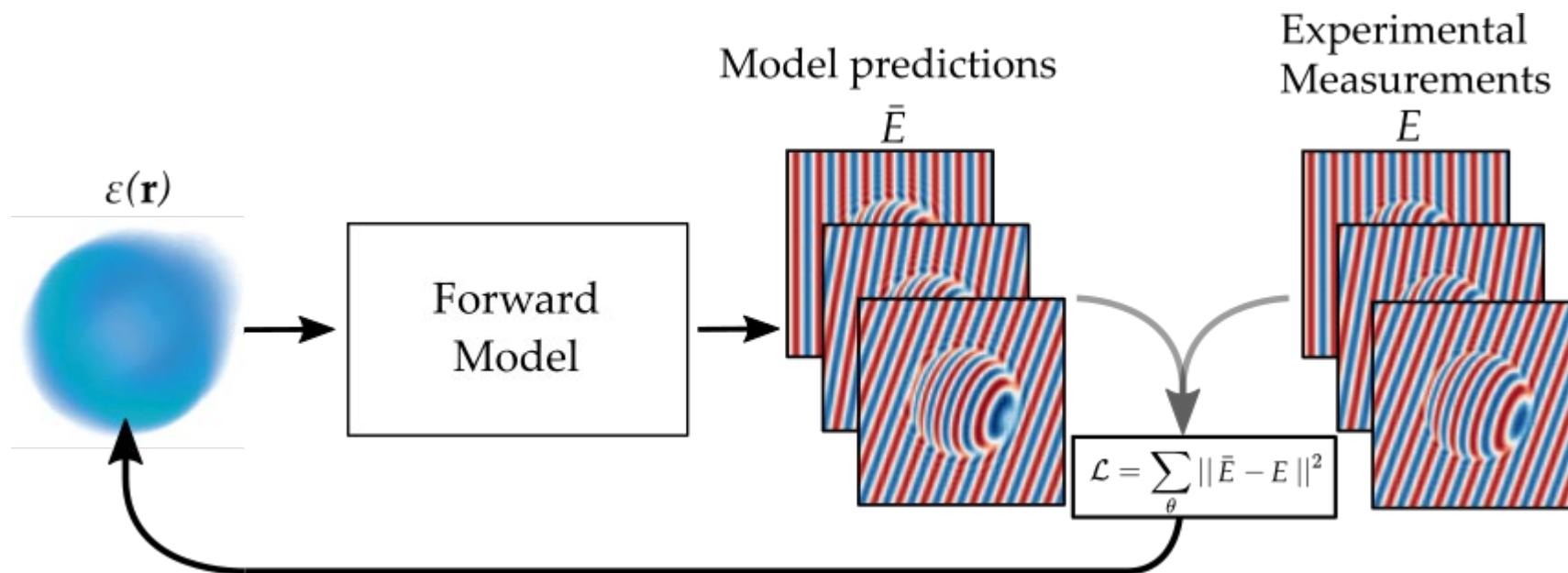
**Wolf transform**



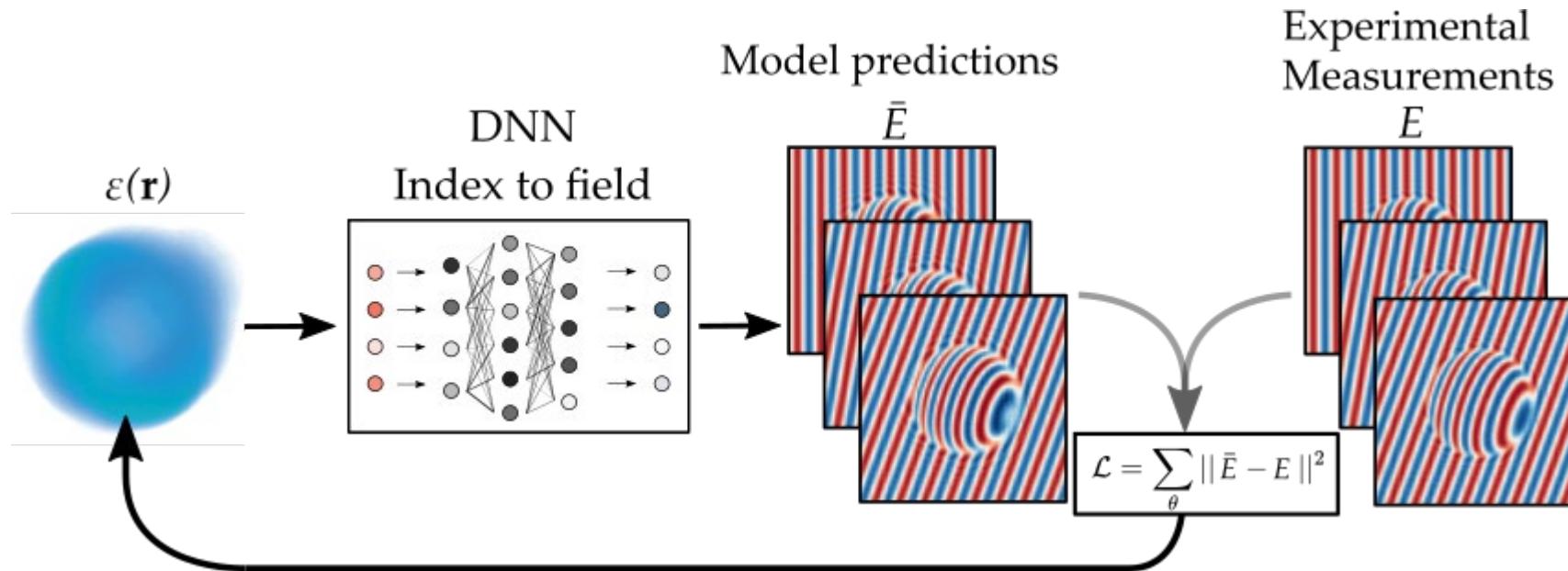
**TomoNet**



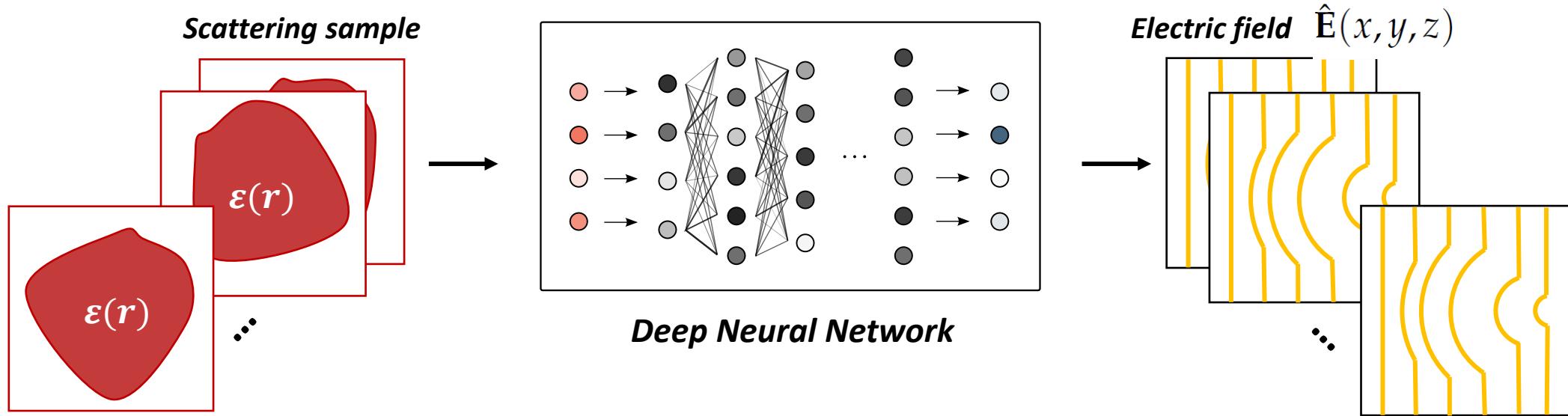
# Iterative ODT reconstruction



# Neural Network forward Model

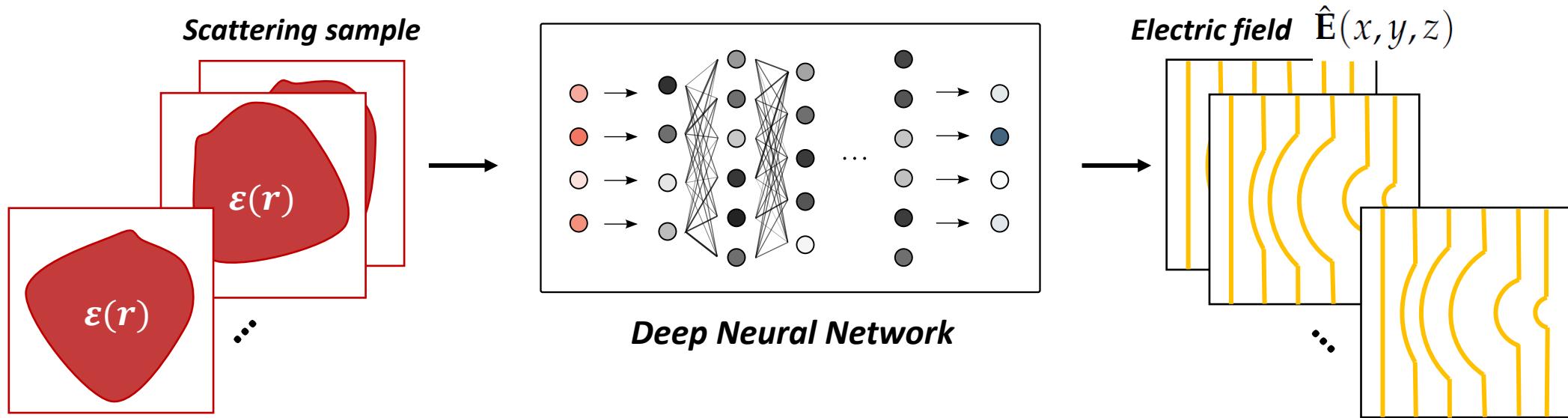


# Data-driven neural network



$$\mathcal{L} = \sum_i \|\hat{\mathbf{E}}(x_i, y_i, z_i) - \mathbf{E}(x_i, y_i, z_i)\|^2$$

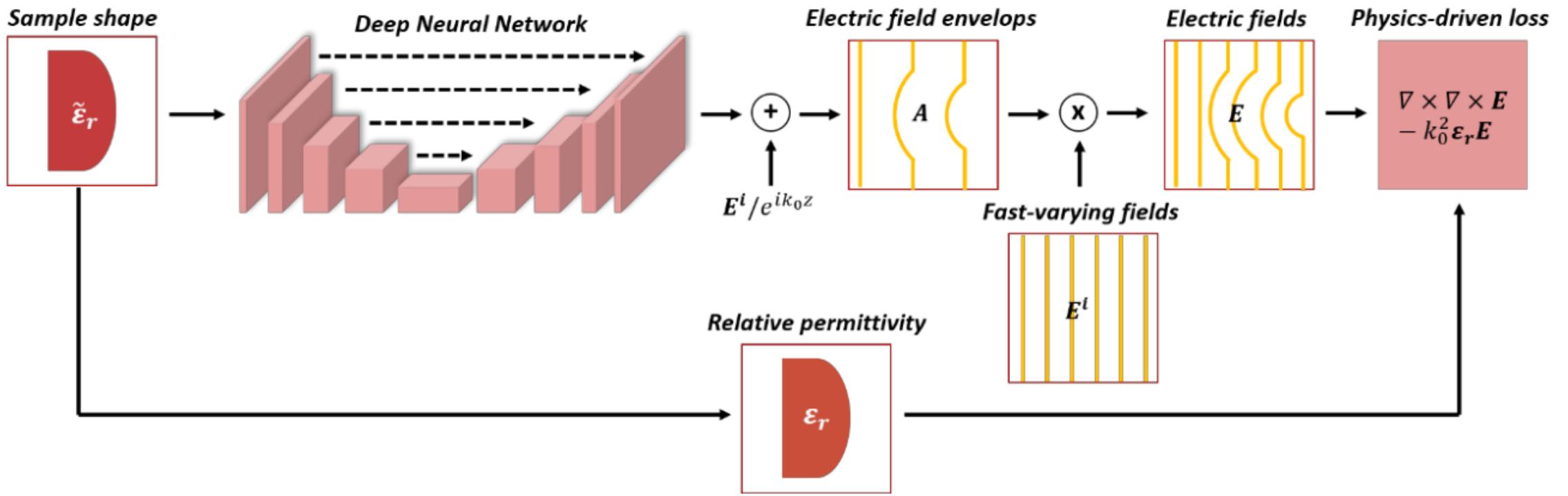
# Physics informed neural network



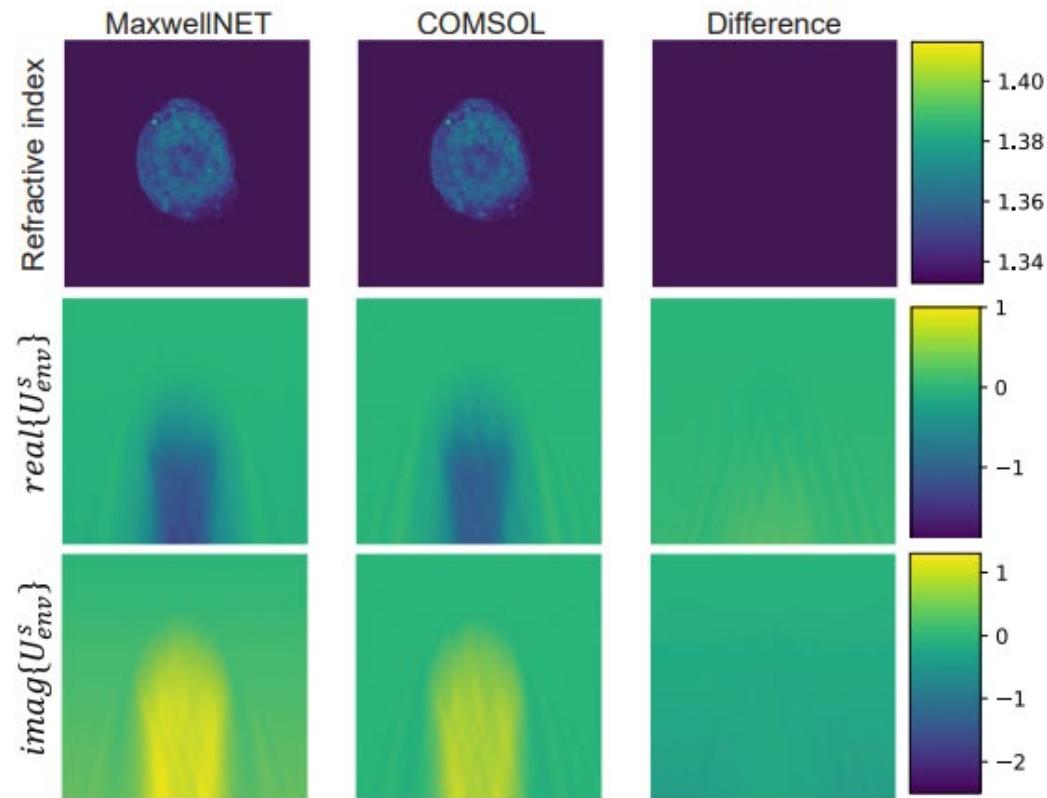
$$\mathcal{L} = \sum_i \left| \nabla \times \nabla \times \hat{\mathbf{E}}(x, y, z) - \frac{\omega^2}{c^2} \epsilon(x, y, z) \hat{\mathbf{E}}(x, y, z) \right|_{x_i, y_i, z_i}^2$$

- How to numerically discretize physical loss
- Which is the best network structure to accomplish this task

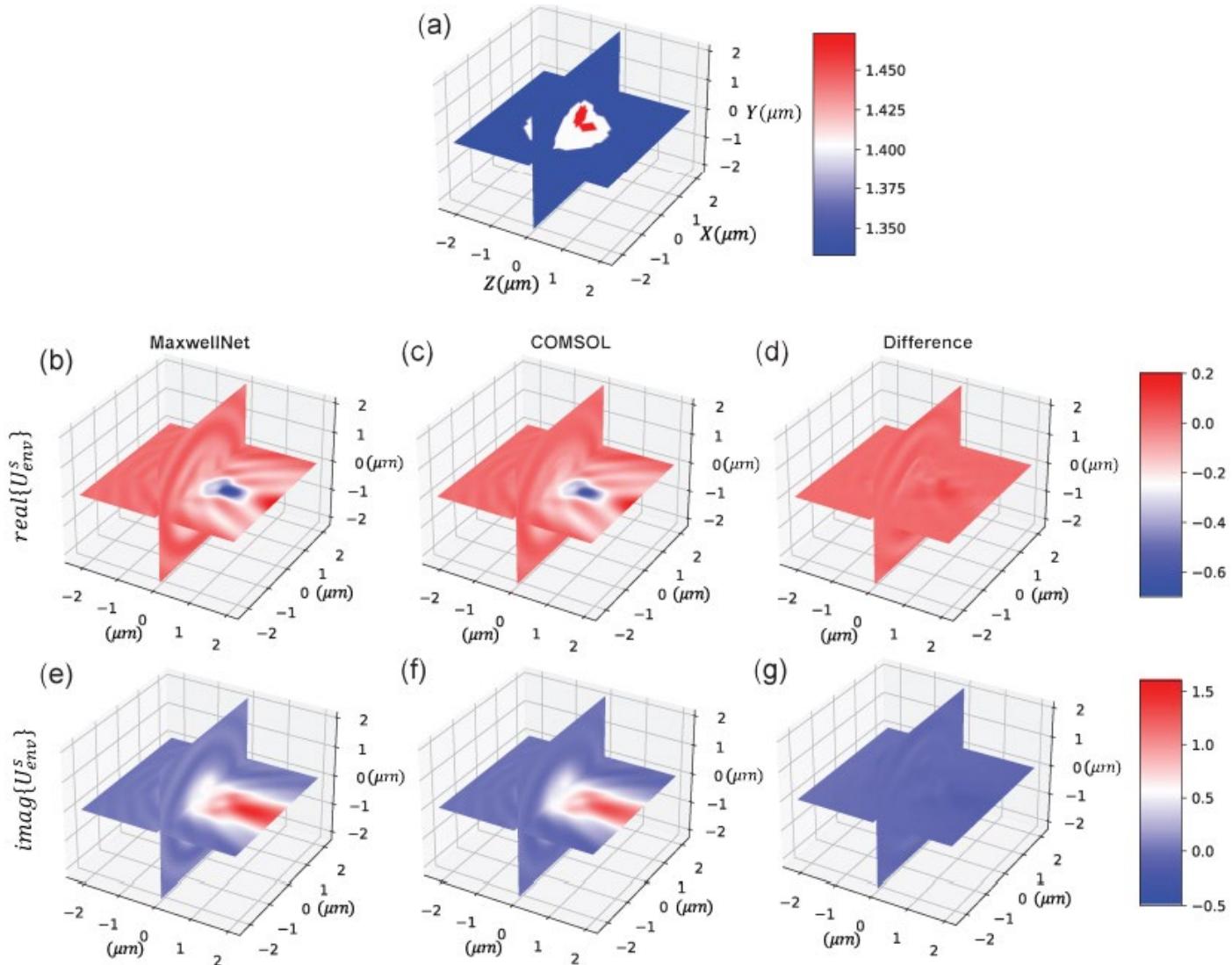
# Maxwell equations based loss function



## Results-HCT Cancer Cells



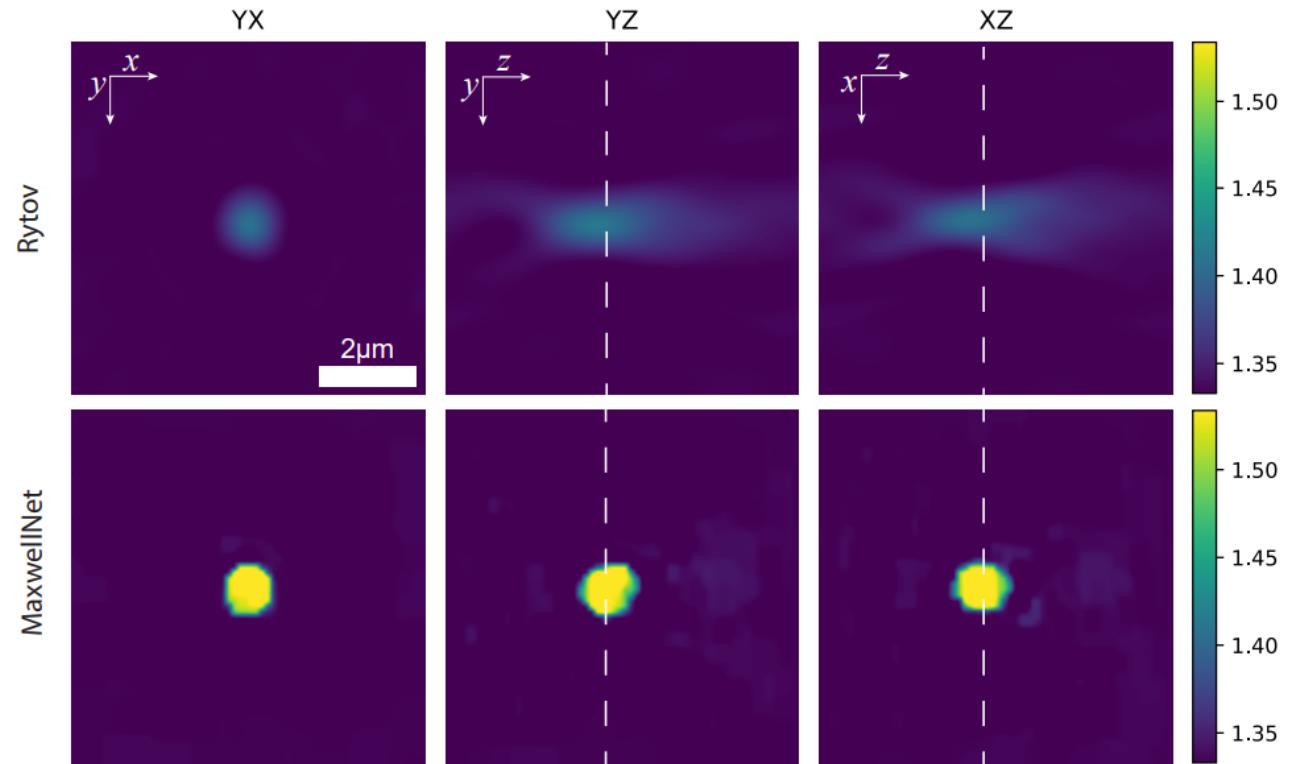
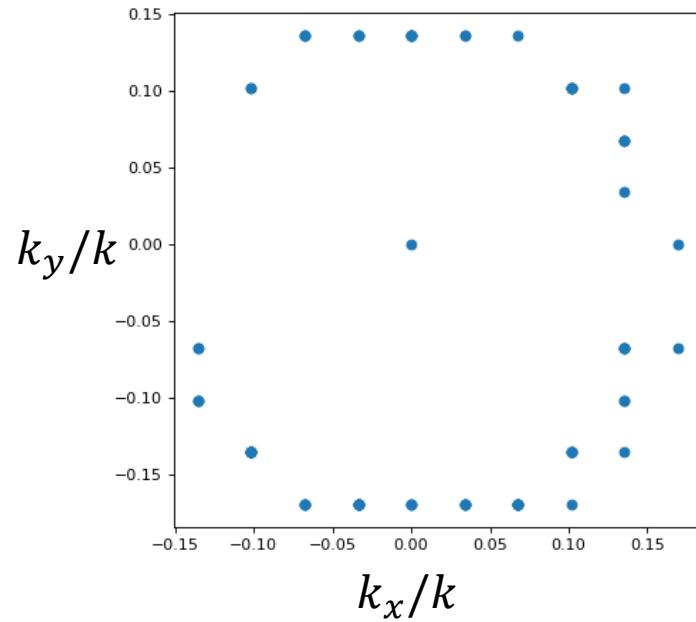
# MaxwellNet 3D:



# Diffraction Tomography using MaxwellNet

## Tomographic Results: Experiment

Polystyrene microsphere in water

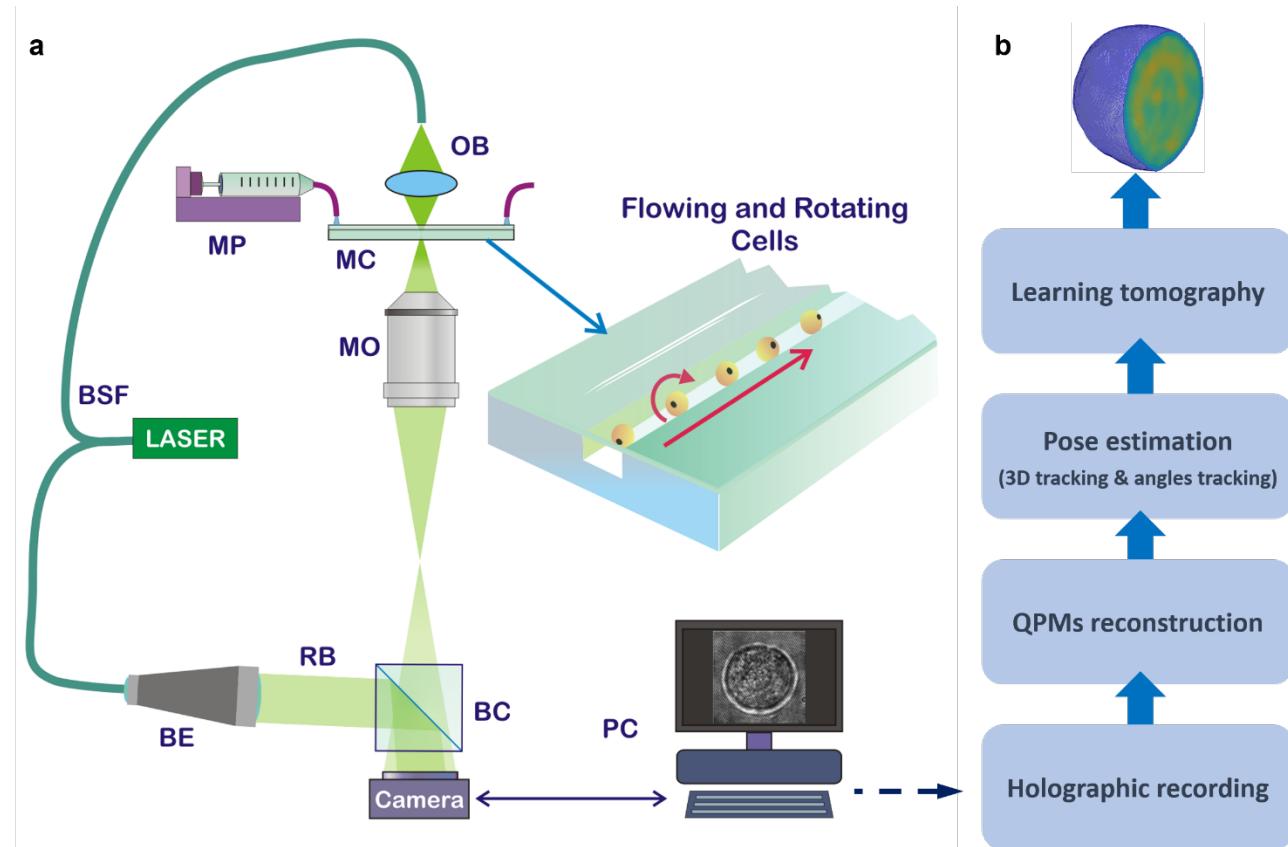


## Computation time

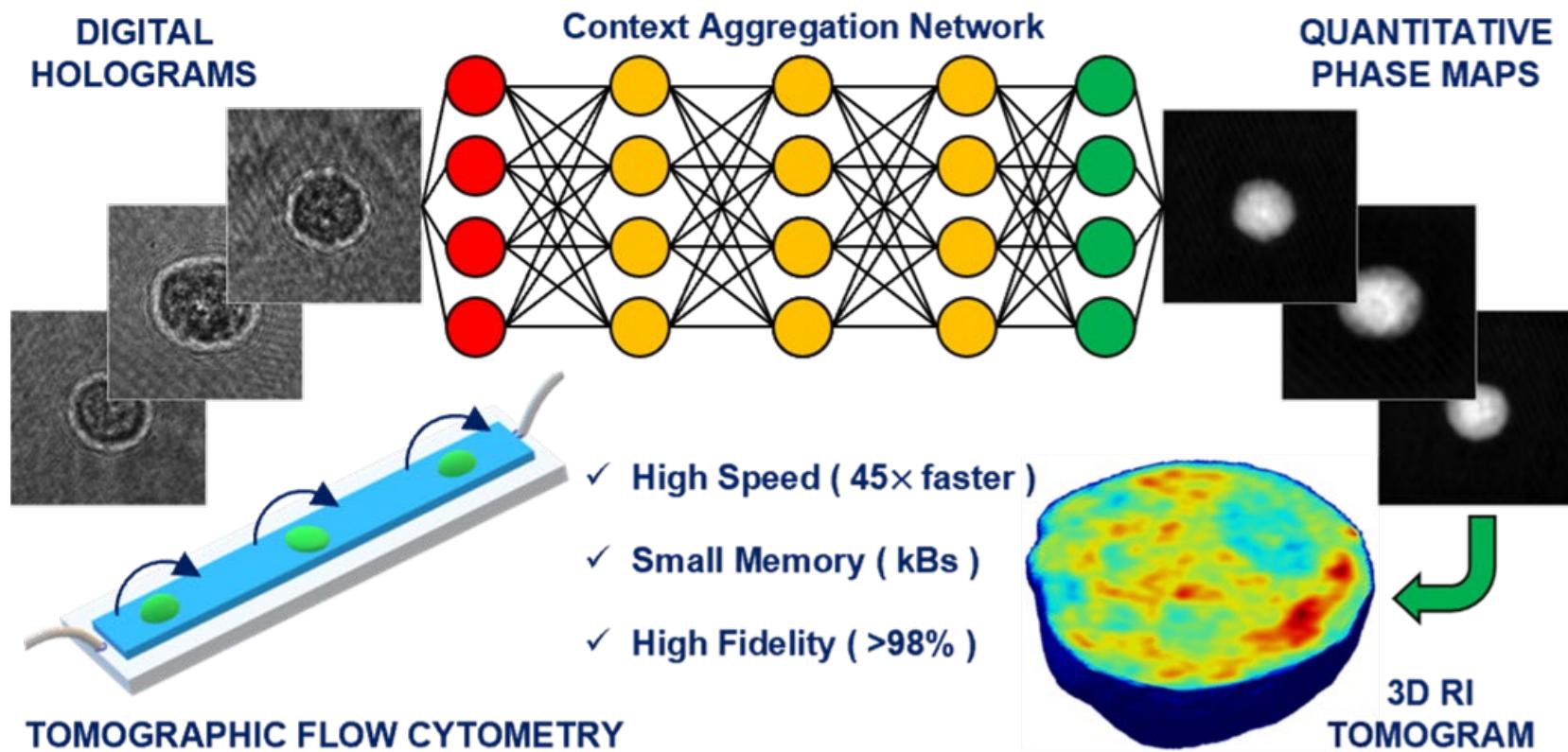
**Table 1** Computation time comparison

Dataset	2D Phantoms	2D HCT-116	3D Phantoms
MaxwellNET training/fine-tuning	30.5h	0.18h	15.5h
MaxwellNET inference	17.0ms	17.0ms	44.9ms
COMSOL	13s	13s	2472s

# TomoFlow



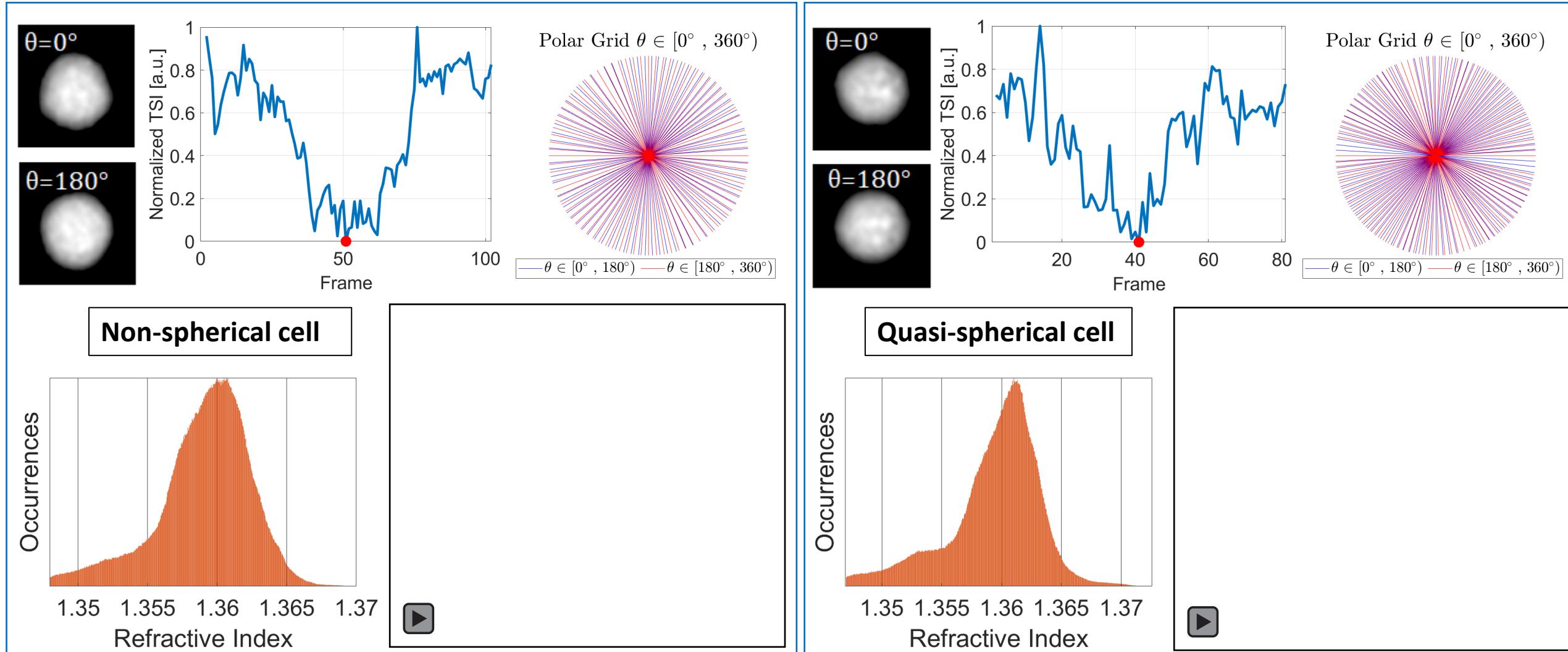
# Deep Learning for TomoFlow



# Nucleus Identification for Breast and Neuroblastoma Cancer Cells



# Breast cancer cells by TomoFlow



# Advantages of label-free 3D imaging

- Avoid photobleaching
- Avoid blinking
- Avoid chemical modification
- In vivo imaging
- Flexibility in wavelength selection
- Generally simpler light sources
- etc