

Hash Table

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→ Used for fast data retrieval

↳ Efficient in lookups / insertions / deletions

↳ Depends on the $O(1)$ collisions

Hash table \approx Hash map → maps keys to values

↳ Achieve fast lookup by using hash functions to compute an index / look for a key
↳ Constant time complexity $O(1)$

2. Key Concepts

- **Hash Function:** A function that takes an input (key) and returns an integer (hash code). This hash code is typically converted into an array index where the value is stored.
- **Collision:** Two different keys may generate the same hash code, leading to a conflict. Hash tables must handle collisions to maintain efficiency.
- **Buckets:** The array used by the hash table to store key-value pairs. Each bucket can hold multiple items in case of collisions.

B1	V1	V2
B2	V1	
B3	V1	V2
B4	V1	V2

3. Collision Handling Techniques

- ① **Separate Chaining:** Each bucket is a linked list (or another data structure). When collisions occur, multiple elements are stored in the same bucket by chaining them together.
- **Open Addressing:** Instead of using linked lists, open addressing probes (searches) for the next available slot when a collision occurs.
 - **Linear Probing:** If a collision occurs, the algorithm checks the next slot (linearly) until an empty slot is found.
 - **Quadratic Probing:** Instead of linearly searching for the next slot, this method uses a quadratic function to find the next available position.
 - **Double Hashing:** Uses a second hash function to determine the step size for probing.

→ Values are not stored in a sorted order

→ ① Implemented with an array of linked lists

↳ Map the key to a index in the array using hash functions

↳ Then, add the value to the linked list at the position

map the key to a value in the array using some function

↳ Then, add the value to the linked list at the position

→ Use good hash functions to ensure that the keys are well distributed and reduce the number of collisions

↳ We'll have collisions !!!

→ Large amount of data

→ thread safe

→ Not sorted

→ Implemented as unordered_map <>

↳ Cache information for fast retrieval

Load Factor (LF)

$$\text{Ratio} \rightarrow \left(LF = \frac{\text{N}^{\circ} \text{ of elements in the hash table}}{\text{N}^{\circ} \text{ of available buckets}} \right)$$

High LF → More likely to have collisions

↳ When cross a threshold → Resize the hash table

6. Time Complexity

- Insert: $O(1)$ on average, $O(n)$ in the worst case (when many collisions occur).
- Lookup: $O(1)$ on average, $O(n)$ in the worst case.
- Delete: $O(1)$ on average, $O(n)$ in the worst case.

5. Hash Table Operations in C++

In C++, hash tables can be implemented using `std::unordered_map`, which provides the basic functionality of a hash table with separate chaining for collision resolution.

Example:

cpp

Copy code

```
#include <iostream>
#include <unordered_map>

int main() {
    std::unordered_map<std::string, int> hashTable;

    // Insert key-value pairs
    hashTable["apple"] = 1;
    hashTable["banana"] = 2;
    hashTable["orange"] = 3;

    // Access elements
    std::cout << "apple: " << hashTable["apple"] << std::endl;

    // Check if a key exists
    if (hashTable.find("banana") != hashTable.end()) {
        std::cout << "banana exists" << std::endl;
    }

    // Delete a key
    hashTable.erase("orange");

    return 0;
}
```

May to access the value using the key

Super important before any access points

Just need to pass the key

→ Difference between `map()` \approx `unordered-map()`

Map → Keys in incremental order → search / Insertion → $O(\log N)$
↳ Uses a BST → Self Balanced Binary Search
↳ Used when order is important

`unordered-map()` → Implemented using hash table (no order)
↳ search / Insertion $O(1)$
↳ Used for where data that order is not important.

• ... , insertion ...

→ Used to store data that ordering is not important

→ Implement not using unordered-map

→ Class definition →

{	Insert
	Remove
	Get

• How to define a hash function?

↳ Traces a fixed size output used to index a data structure

↳ Deterministic → same input same output

↳ Efficiently → fast to calculate

↳ Uniformly → Distribute the values evenly

↳ Define this hash function as a private method

↳ Don't want to expose it as public