

Methods and strategies for overvoltage prevention in low voltage distribution systems with PV

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Abstract: The rapid development of photovoltaic (PV) systems in electrical grids brings new challenges in the control and operation of power systems. A considerable share of already installed PV units is small-scale units, usually connected to low-voltage (LV) distribution systems that were not designed to handle a high share of PV power. This study provides an in-depth review of methods and strategies proposed to prevent overvoltage in LV grids with PV and discusses the effectiveness, advantages, and disadvantages of them in detail. On the basis of the mathematical framework presented in this study, the overvoltage caused by high PV penetration is described, solutions to facilitate higher PV penetration are classified, and their effectiveness, advantages, and disadvantages are illustrated. The investigated solutions include the grid reinforcement, electrical energy storage application, reactive power absorption by PV inverters, application of active medium-voltage to LV transformers, active power curtailment, and demand response. Coordination between voltage control units by localised, distributed, and centralised voltage control methods is compared using the voltage sensitivity analysis. On the basis of the analysis, a combination of overvoltage prevention methods and coordination between voltage control units can provide an efficient solution to increase the PV hosting capacity of LV grids.

1 Introduction

The adoption of photovoltaic (PV) in electrical energy systems is increasing and current trends suggest that the installation of PV will increase during the coming years. At the end of 2000, the cumulative capacity of the PV units installed worldwide was around 1 GW, and by the end of 2010, this capacity had increased to around 40 GW. In 2011 and 2012, more than 30 GW of PV units were installed annually, and the cumulative PV capacity reached 100 GW at the end of 2012. More than 38 GW of PV units were installed annually in 2013 and 2014, and this capacity was more than 50 GW in 2015. By the end of 2015, the worldwide cumulative capacity had reached 229.3 GW. The global annual installations and the global PV cumulative installed capacity from 2001 to 2015, as well as the minimum and the maximum values forecasted for PV installation from 2016 to 2020 are shown in Fig. 1 [1–5].

PV systems can also be split into distributed systems and centralised systems. Distributed systems are usually installed to

provide power to nearby customers whether or not their owners, while centralised PV systems act similarly to the power stations and are usually connected to higher voltage than the voltage level of low-voltage (LV) grids [2, 3]. The majority of already installed PVs are small-scale units, which are usually connected to LV distribution systems [3–5] and have a capacity of <10 kW [2]. According to the European Photovoltaic Industry Association, rooftop PV systems were the most prevalent in 2012, with around 12 GW in net power generation capacities added into the 27 European countries' electricity grid, while utility-scale PV systems, generating around 4.7 GW, took fourth place after onshore wind and gas power plants [3]. In 2012, in countries such as the Netherlands, Belgium, the UK, and the Czech Republic more than 50% of new PV installations were residential PVs. This percentage for Denmark was around 100% in 2012 where around 378 MW residential PVs were installed [4]. Around 20 GW rooftop PV units were installed annually in 2013, 2014, and 2015. Although the PV market is a policy-driven market, the trends suggest that decentralised PV installation will increase during the coming years.

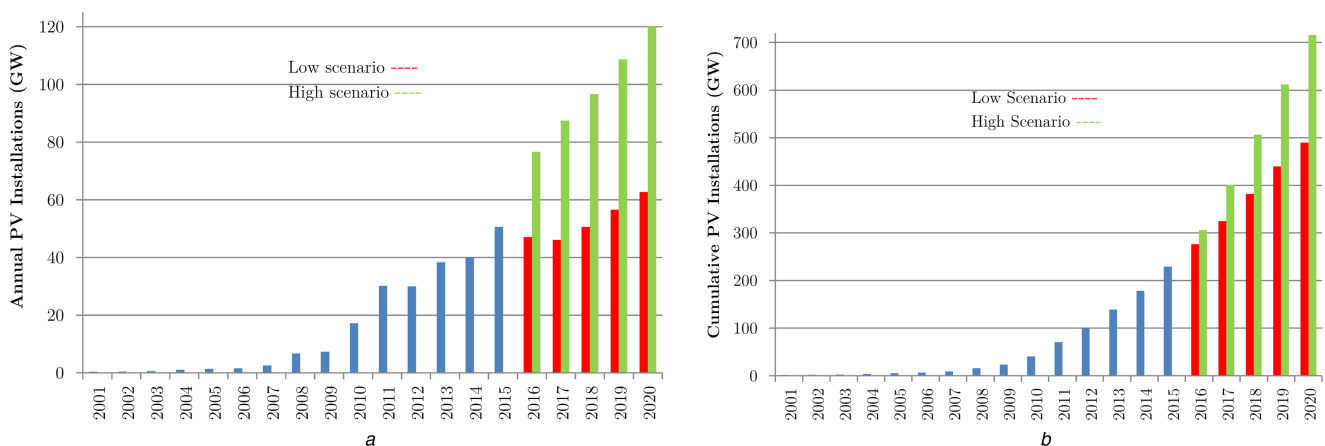


Fig. 1 Global PV installations from 2001 to 2015, and the minimum and the maximum values forecasted for PV installation from 2016 to 2020, according to [1–5]

(a) Annual, (b) Cumulative

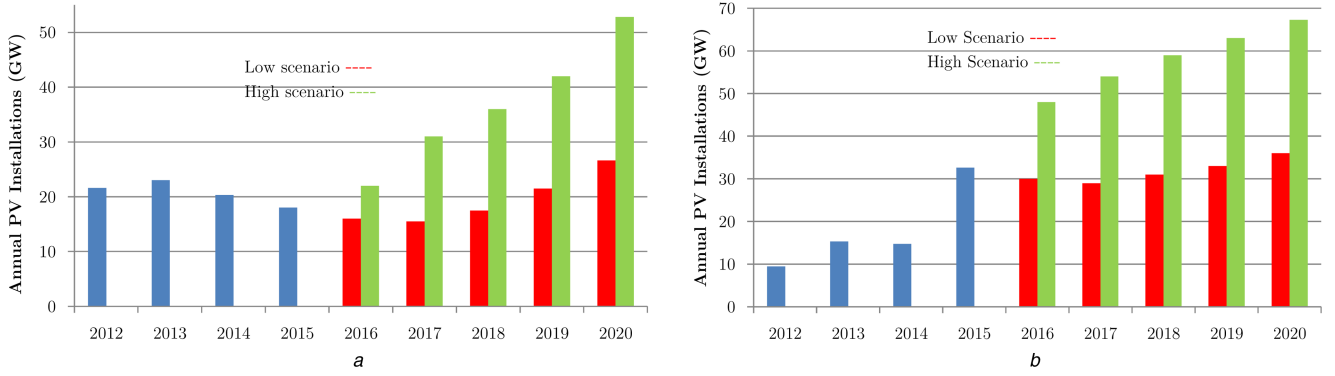


Fig. 2 Global annual historical rooftop and utility-scale PV installations, and the minimum and the maximum forecast values for future PV installations, according to [3–5]
(a) Rooftop PV installations, (b) Utility-scale PV installations

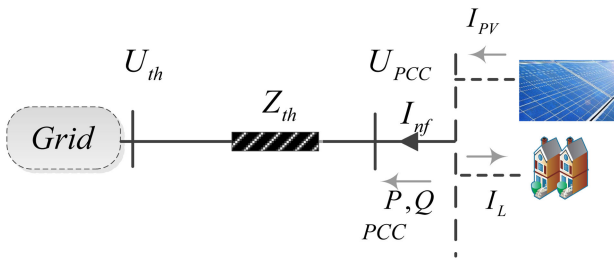


Fig. 3 Thevenin equivalent of a typical PV system connected to an LV grid

The annual historical rooftop and utility-scale PV installations from 2012 to 2015, as well as the minimum and maximum forecast values for future PV installations from 2016 to 2020, are shown in Fig. 2 [3–5].

Despite the economic and environmental advantages associated with these PVs, their potential impact on LV grids has yet to be thoroughly investigated, particularly as the locations of these units cannot be controlled by distribution system operators (DSOs) and their output power is stochastic and non-dispatchable. In addition, PV installation is usually non-uniform across distribution systems [6]. Low residential PV penetration can be considered as an ancillary service to improve the grid voltage quality and to decrease the power loss. However, a higher PV penetration may cause difficulties in the control and operation of LV grids. Among the challenges associated with high PV penetration are: overloading of the grid components such as LV transformers and cables [7, 8]; active and reactive power flow fluctuations [9–13]; the network protection malfunction [14]; and voltage unbalance [15–19]. However, overvoltage is the main challenge in many LV grids with PV, and is one of the main limiting factors in increasing PV penetration in LV grids. Overvoltage caused by PV systems happens when the power flow path is reversed from customers to the LV transformers. In residential feeders, in which the load consumption is relatively small during high PV generation periods, the potential for overvoltage is greater, and a lower share of PV systems may cause reverse power flow and an unacceptable voltage rise in the grid. Although various methods including the application of active medium-voltage (MV)/LV transformers [20–26], active power curtailment [27–32], reactive power absorption by PV inverters [20, 33–46], demand response (DR) [47–51], and the application of electrical energy storage systems (EESSs) [16, 50, 52–71] are proposed to overcome this challenge in recent years, there is a lack of research paper providing a detailed review of the methods and solutions proposed to facilitate higher PV penetration in LV grids, considering a comprehensive analysis of advantages and disadvantages of them.

The objective of this paper is to provide a detailed and in-depth review of methods proposed to prevent overvoltage in LV grids with PV, and to discuss the effectiveness, advantages, and disadvantages of these methods. To evaluate the voltage rise in LV grids with PV, a simple two-bus system is modelled in Section 2 and the voltage rise caused by PV and the potential solutions for

overvoltage prevention are discussed using a mathematical framework. In Section 3, the proposed overvoltage prevention methods: namely, reinforcement of the current grids, application of active MV/LV transformers, active power curtailment, reactive power absorption by PV inverters, DR, application of EESSs, and electric vehicle (EV) application are discussed. Selecting the most effective voltage control methods is also discussed in this section. In Section 4, using the voltage sensitivity analysis, the effects of local PV generation on an entire LV grid are studied, and the advantages and disadvantages of using localised, distributed, and centralised coordinated control methods are examined using a simplified three-bus system. Finally, the conclusion is provided in Section 5.

2 Voltage rise caused by PV systems and potential solutions

To have a better understanding of different methods for overvoltage prevention in LV grids, a simplified two-bus system is presented and the methods for mitigating the overvoltage are discussed here. Consider a PV system connected to an LV grid as shown in Fig. 3. Z_{th} and U_{th} are the Thevenin impedance and the Thevenin voltage, respectively, I_{PV} is the PV feed-in current, U_{PCC} is the voltage at the PV point of connection (PCC), and I_L is the load consumption. The net feed-in current can be calculated by

$$I_{nf} = I_{PV} - I_L = \left(\frac{S_{nf}}{U_{PCC}} \right)^* \quad (1)$$

where S_{nf} is the net apparent power injected into the grid. By neglecting the power loss across the Thevenin impedance, the I_{nf} can be rewritten as

$$I_{nf} = \left(\frac{P - jQ}{U_{th}} \right) \quad (2)$$

The voltage at PCC can be calculated as

$$U_{PCC} = U_{th} + Z_{th} \times I_{nf} \quad (3)$$

Suppose that $Z_{th} = R_{th} + jX_{th}$. Thus

$$U_{PCC} = \left(U_{th} + \frac{P \times R_{th} + Q \times X_{th}}{U_{th}} + j \frac{P \times X_{th} - Q \times R_{th}}{U_{th}} \right) \quad (4)$$

$$= U_{Re} + jU_{Im}$$

where U_{Re} and U_{Im} are the real and imaginary parts of the U_{PCC} , respectively. The magnitude of U_{PCC} can be calculated as in the following:

$$U_{PCC} = \sqrt{U_{Re}^2 + U_{Im}^2} \quad (5)$$

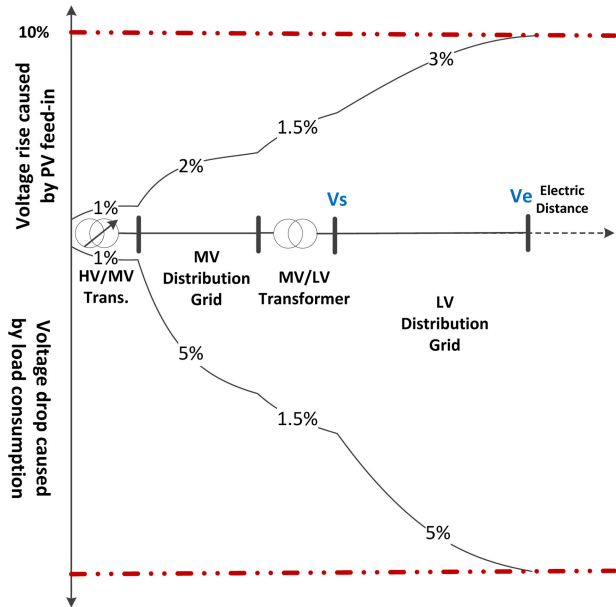


Fig. 4 Typical design consideration for distribution systems

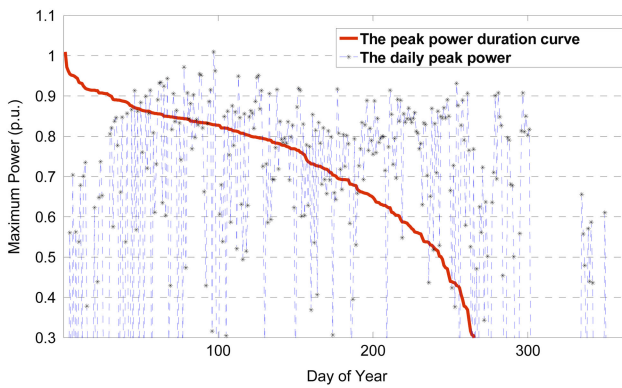


Fig. 5 Daily peak power and the peak PDCs

For most connection points in distribution systems, the $U_{Re}^2 \gg U_{Im}^2$ [20]; therefore, the approximate voltage magnitude at PCC can be simplified as follows:

$$U_{PCC} \approx U_{th} + \frac{P \times R_{th} + Q \times X_{th}}{U_{th}} \quad (6)$$

The voltage increase at PCC can be calculated as

$$(\Delta U \times U_{th}) \approx (P \times R_{th} + Q \times X_{th}) \quad (7)$$

According to the standards applied to LV grids, the voltage at the connection point has to be limited to a specific amount. Suppose that the maximum voltage increase is limited to ΔU_{max} ; therefore, the maximum active power that can be injected into the grid without overvoltage is as follows:

$$P_{max} = \left(\frac{\Delta U_{max} \times U_{th} - Q \times X_{th}}{R_{th}} \right) \quad (8)$$

If the active power increases to more than P_{max} defined in (8), the PCC voltage exceeds the allowed boundary. According to (8), three main factors determine the P_{max} : $\Delta U_{max} \times U_{th}$, $Q \times X_{th}$, and R_{th} . To decrease the R_{th} , the lines have to be replaced by stronger lines or new lines have to be constructed to reinforce the grid. The reactive power absorption by PV inverters can also increase the P_{max} . In addition to these methods, if the power generated by PV inverter is

consumed locally and is not injected to the grid, the permissible PV installation can increase.

As analysed later in this paper, the majority of the proposed methods for overvoltage prevention focus on decreasing the voltage rise along LV feeders. According to (6), the PCC voltage also depends on the voltage on the LV side of MV/LV transformer. In many LV distribution grids, the voltage variations on the MV side cannot be mitigated, as the tap positions of MV/LV transformers are fixed. Considering these voltage variations in MV distribution systems, ΔU_{max} is usually limited to $<5\%$ to ensure acceptable voltage at the PCC. To illustrate further, a typical design consideration for distribution systems in Germany is depicted in Fig. 4 [26, 72]. As can be seen, to have an acceptable voltage quality at the customer points of connection, the maximum voltage increase in LV grids is limited to 3%, which can potentially limit the maximum PV installation in the grid. Using active MV/LV transformers, a higher voltage increase along the feeder is acceptable. Therefore, the ΔU_{max} can be increased considerably, which results in more possible PV installations.

3 Overvoltage prevention methods applied to LV grids

As discussed before, according to the standards applied to LV grids the maximum voltage at the connection point has to be limited to a specific amount. Limiting the PV installation in LV grids is one of the methods that maybe used by DSOs to prevent overvoltage in the grid. In this approach, using the grid data such as impedances of lines, grid configuration, and number of customers, the maximum possible PV installation in the grid without overvoltage occurrence is estimated. It is also possible to determine a maximum PV installation per customer. In [50], a method is proposed based on the voltage sensitivity analysis to determine the maximum active power that each customer can inject into the grid without overvoltage occurrence. The Monte Carlo analysis can be used to consider the probabilistic nature of PV location and size in maximum PV penetration determination [73]. Although simplified methods can be used to estimate the maximum voltage across LV feeders, the grid data is still required [74].

One of the main problems associated with limiting the PV installation is that the maximum possible PV installation differs considerably for each grid and extending the calculated values of one grid or the average of some LV grids to all grids is not a reliable solution. Therefore, each grid has to be studied individually and the relevant data such as the grid structure and types of conductors have to be established. In many LV grids, these data are not readily accessible. In addition, even in an individual grid and according to the location of PV systems, different maximum PV penetrations maybe achieved [75].

Limiting the PV installation in the grid is not an optimal solution because PV generation is variable during the day and the maximum daily PV generation is not fixed during the year. The measured maximum PV generation for a PV panel located at the Technical University of Denmark is shown in Fig. 5. As can be seen, the nominal peak generation of a PV unit only happens during a limited number of days during the year. Therefore, considering this maximum value and determining the PV penetration based on it may considerably limit the possible PV installation in the grid. As a result, overvoltage prevention methods need to be applied to LV grids to increase the PV hosting capacity.

Different methods are proposed to increase the permissible active power feed-in in the grid, and they are classified in Fig. 6. Some of these methods are provided by customers, and some of them need to be applied by DSOs. These methods are explained as follows.

3.1 Grid reinforcement

Grid reinforcement is the conventional solution to overcome the challenges associated with increasing the residential load consumption. This increase may cause an unacceptable voltage drop across the distribution feeder during high-load consumption periods. Grid reinforcement is suggested as a solution to improve

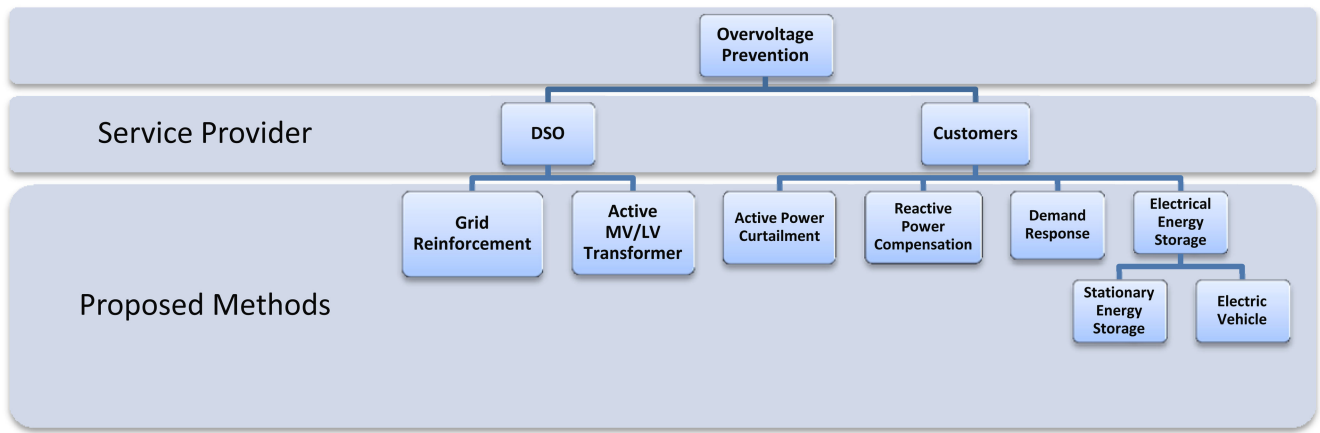


Fig. 6 Classification of the proposed overvoltage prevention methods that can be applied to LV grids

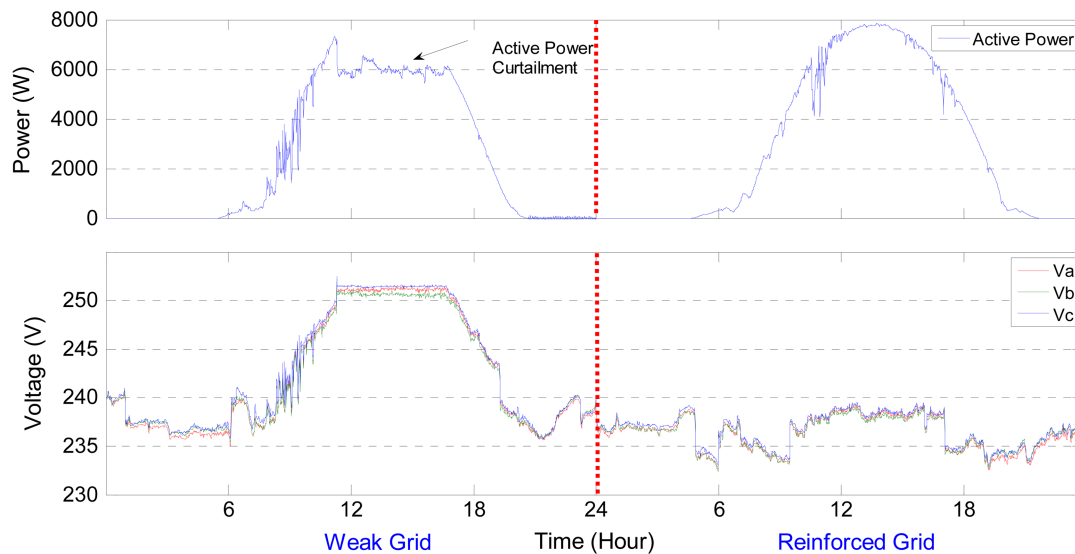


Fig. 7 Comparison between the PV integration in a weak grid and the reinforced grid

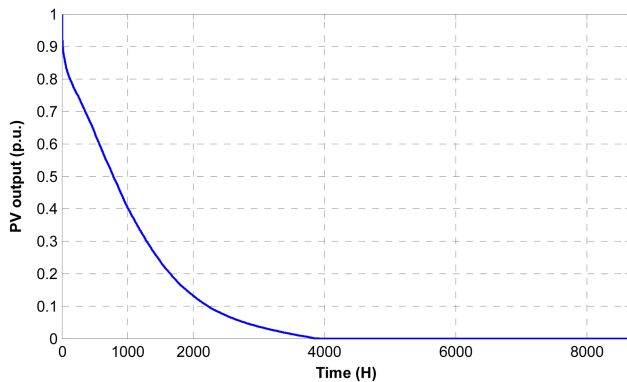


Fig. 8 YPDC of a PV system based on real data

the voltage profiles of customers in the condition of high EV penetration. In a similar way, grid reinforcement seems one of the most effective methods for solving the overvoltage issue in high PV generation conditions [76]. On the basis of (8), decreasing resistances of the lines in an LV grid, either by replacing the previous lines with new lines with higher cross-section or adding new lines in parallel with the previous lines, can effectively decrease the voltage rise in the PV points of connections. Although decreasing the feeder impedance by replacing the MV/LV transformers is also possible, this is not as efficient as reinforcement of the lines. In some radial LV grids, changing the structure to ring grids can improve the PV hosting capacity of those grids. However, the effects on the protection system and power flow directions should be thoroughly investigated. A comparison

between the PV integration in a weak grid and the reinforced grid is shown in Fig. 7 according to the real measurements. As can be seen, in the reinforced grid the voltage fluctuation caused by PV system is small, while active power generated by PV is curtailed in the weak grid during high PV generation period.

The main drawback of grid reinforcement is the high cost associated with this method. This cost differs according to the grid structure, short circuit capacity of the grid, length of feeders, and types of conductors used in the grid. Therefore, the associated cost is difficult to estimate in a whole grid. In addition, though the overvoltage occurs more often with increasing PV penetration, in many cases the overvoltage happens during only a few hours of the day. As the capacity factor of PV panels, which is the ratio of yearly energy generated by PV to its theoretical output if operated at its kilowatt peak power over a year [50] is small, grid reinforcement cannot be considered as a cost-efficient solution to mitigate the overvoltage caused by PV systems. To clarify, the yearly power duration curve (YPDC) of a PV panel located at the Technical University of Denmark is shown in Fig. 8. The YPDC is extracted by arranging the 10 min average PV output power in descending order during a year. As can be seen, the PV generates power higher than 50% in <10% of a year.

3.2 Application of active transformers

Application of active transformers is another effective solution that seems more attractive than conductors' reinforcement in some grids. These active transformers can be transformers with on-load tap-changers (OLTCs) or solid-state and full power-electronic-based transformers. Technically, it has a high potential for increasing the PV hosting capacity of LV grids [23], though the

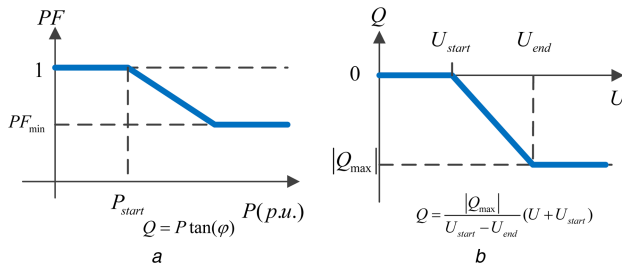


Fig. 11 Schematics of local reactive power absorption methods
(a) $PF(P)$, (b) $Q(U)$

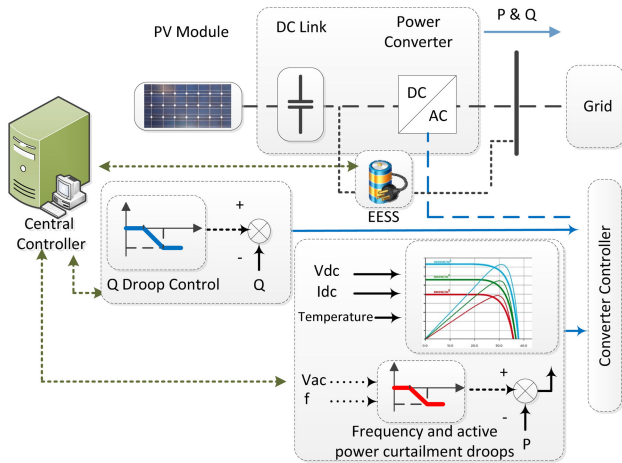


Fig. 12 Overview of a PV system with EESS

The localised methods are usually applied to the inverter controllers using the droop control method. Two main droop control methods for reactive power management of PV inverters are the power factor as a function of injected active power [$PF(P)$], and the reactive power as a function of voltage in the PV connection point [$Q(U)$] [20, 33–36]. In the $Q(U)$ method, the voltage at the PV connection point is considered as a reference for the droop control and the PV inverter absorbs the reactive power only when the terminal voltage is higher than a specific value. The main drawback of this method is that in high PV penetration conditions, the inverters located near the LV transformer do not participate in reactive power management effectively [33]. In the $PF(P)$ method, the reactive power is a function of the generated active power and the droop characteristics can be set, so that during low PV generation hours, no reactive power is absorbed by the PV inverter. The schematics of these methods are shown in Fig. 11. In general, the effectiveness of the reactive power absorption method greatly depends on the grid structure and the R/X ratio of the grid, rather the method applied for the reactive power control. According to Bletterie *et al.* [37], the reactive power absorption can compensate the voltage increase caused by PVs by up to 25 and 60% for feeders with cables and overhead lines, respectively. For many typical MV/LV transformers, by applying the $PF(P)$ method and considering the power factor of 0.9 at the terminal of transformers, the voltage can usually be decreased by more than 1%. Although the allowed voltage increase at the LV grid depends on the grid design concept, it is usually <5%; therefore, the PV hosting capacity can be increased by more than 20% by applying reactive power absorption.

The reactive power absorption by the PV inverter increases the power loss and congestion of distribution lines. To decrease the reactive power loss caused by reactive power absorption, the parameters of the droops should be set according to the PV penetration, or certain PV inverters should be selected for the reactive power absorption [29]. It is also suggested to select some PV inverters at the beginning of each LV feeder to provide reactive power consumed by PV inverters located at the end of feeder, to decrease the power loss across MV distribution systems [38]. Certain methods are also proposed to decrease this power loss and the majority of them are based on central control or distributed

methods that require communication among the PV inverters [39–46]. Although the communication-based methods are usually more efficient, the cost associated with them is usually high [81]. In addition, according to a recent study, the application of communication-based reactive power compensation methods for LV grid loss minimisation may have a marginal effect on the loss reduction and is not an economic solution [23].

Regardless of the method applied to the inverter controller, the PV inverters need to be oversized to absorb the reactive power. The minimum power factor is usually considered as 0.9, which means that the inverter capacity has to be increased by around 11%. An alternative is that during high PV generation periods, a part of the active power is curtailed to prevent the overloading of the inverter. Considering a minimum power factor of 0.9 resulting in the maximum reactive power absorption of 48% of nominal inverter capacity, the active power has to be curtailed at around 88% to prevent the inverter overloading. This curtailment does not mean that around 12% of energy generated by PV system is lost. For the PV system of Fig. 8, this energy loss is <1%. For a power factor of minimum 0.95, the active power curtailment level is around 94%. It should be noted that for power factors of 0.95 and 0.9, when the PV generation is <94 and 88% of nominal inverter capacity, respectively, active power curtailment is not needed.

3.5 Demand response

There are some thermal storage units in the grid such as freezers, refrigerators, and off-peak heating systems, which can be managed and controlled to improve the local generation–consumption balance during high PV generation periods. These thermal storage units and other controllable loads in the grid can increase the PV hosting capacity of that grid. DR can be applied to the loads directly and a central server can generate the control signals. Moreover, loads can also be controlled indirectly using a bonus tariff incentive system [47]. Applying DR can reduce the energy that is transferred from and to LV grids and also decrease the reverse power flow and peak load power [48]. Increasing the local consumption decreases the net power injected into the grid by PV inverters; therefore, the total PV installation in the grid can be increased.

Although DR can shape the load consumption and decrease the power loss in the grid, it cannot be considered as a reliable method for grid voltage control as DR depends to a great extent on customers' consumption patterns, and some controllable domestic loads are not necessarily used on a daily basis [47, 49]. However, a combination of DR with active power curtailment can decrease the energy loss caused by curtailment [50]. In addition, it can also decrease the energy storage required for overvoltage prevention in the grid [51].

3.6 Application of EESSs

3.6.1 Stationary energy storage: In recent years, EESS have been proposed as a solution to overcome the challenges of renewable energy technologies. To prevent the overvoltage in high PV penetration conditions, EESS can be applied in order to store a part of the energy generated by PVs and limit the amount of active power injected into the grid by PV units. To this aim, the output power of PV is limited to a specific amount by storing the excess energy, and this stored energy can be used when load consumption or the price of electricity is high [51]. An overview of a PV system with EESS is depicted in Fig. 12. As can be seen, EESS can be connected into the DC bus of the PV inverter or be connected separately to the AC terminal. The active and reactive powers are controlled independently in PV inverters and can be controlled locally using fixed set points or droop-based methods. When the system is centrally controlled, the droops are replaced by some control signals generated by a central server.

Although battery technologies have developed in recent years, the main concern about the application of EESS is still the initial investment in the system, and a strategy to optimise the size of energy storage units in the distribution system is required. A cost–benefit analysis can be performed to determine the required investment. In addition, several other factors should be considered

including: the possibility of EESS for undervoltage prevention in high-load condition; the energy storage lifetime under different operation modes; the effect of energy storage utilisation on operation cost of transformer with OLTC and step voltage regulators; and the effects of EESS on reduction of peak power generation cost [52]. As both PV output and load consumption are stochastic, the uncertainties associated with them have to be modelled to determine the minimum EESS to be installed in LV grids. This procedure usually involves a computationally expensive time-series analysis. To model these uncertainties without the time-series study problems, PV generation and load consumption can be modelled using remaining power curves with different occurrence probabilities [50].

Although the EESS utilisation is an effective solution to prevent overvoltage, advanced methods are needed to control these units as efficiently as possible. Different static and dynamic control strategies can be applied to EESS to increase the self-consumption and prevent the overvoltage in the grid [53–60]. Compared with the static control methods, voltage-dependent dynamical charging methods have better performance; however, the benefits to the customers located at the critical voltage node maybe reduced and mechanisms are required to share the costs among all system owners [61]. To have equal investment in EESS from all customers and decrease the EESS size, variable droop-based methods can be implemented [62]. Efficient control of EESS can be performed to minimise the total distribution losses and control the grid voltage in high PV penetration conditions. To this aim, a decision technique is usually required to determine a power reference schedule for the control system of OLTC, controllable loads, and EESS [63, 64].

Coordinated use of EESS and other overvoltage prevention methods can increase the effectiveness of voltage control while reducing the need for EESS. Droop control of EESS and local reactive power control of PV inverters can provide efficient voltage control in the grid in high PV penetration conditions [62]. Coordination of EESSs and active and reactive powers of PV inverters through a combination of localised and distributed control methods can minimise the active power curtailment and prevent the overvoltage while reducing the energy storage need [65]. By using both localised and communication-based methods, the communication failure can only reduce the efficiency by increasing the active power curtailment and the power absorbed by energy storage units. It is worth mentioning that without reactive power compensation, the EESS capacity required for overvoltage prevention increases considerably [33].

3.6.2 Electric vehicle: EV also can be considered as an EESS solution for overvoltage prevention. The EV charging stations can be used as voltage support facilities in LV grids with high PV penetration and coordination of EV charging facilities and PV units can potentially mitigate the voltage rise in the grid [16, 66–71]. Prioritising EV charging around peak generation hours can effectively decrease the required EESS and prevent the overvoltage during high PV generation hours [49]. In addition, in order to minimise the required EESS capacity, the charging stations have to be located farthest from the transformer [66]. The EV home charging also can decrease the voltage rise during high PV generation periods; however, according to the home-charging concept, the customers would tend to start charging their EVs when they reach home; therefore, the majority of EV charging occurs at the time when there are no or low PV generation [50].

3.7 Combination of voltage control methods

Selecting the most efficient methods highly depends on the grid structure and the grid regulatory specifications. Combination of active power curtailment and reactive power absorption [82–87], EESS and reactive power absorption [33, 62, 88], and transformer with OLTC and reactive power absorption [23, 89–91], can potentially provide more efficient voltage control. Economic evaluation cannot be performed without considering the grid structure, the future grid extension plans, the future development in renewable technologies, the current PV penetration in the grid, and possible future PV installations, the standards and grid codes

applied to the grids, and possibility of active power curtailment and its permissible level. As a result, a decision-making procedure is required to determine the most techno-economic solution for overvoltage prevention in each grid and the result associated with an individual LV grid cannot be generalised to other grids.

4 Discussion on coordination strategies for voltage control in high PV penetration conditions

Methods that are suitable for overvoltage prevention and increasing the LV grid PV hosting capacity can be applied using both localised and centralised control strategies. Centralised methods have better performance [92, 93]; however, voltage control using central control approaches requires high speed and fast computers and broadband networks, all of which imply substantial investment [94]. Local control strategies for voltage control act only according to local measurements and do not need broadband networks. However, they are not as effective as central control approaches due to a lack of broader information. To clarify, consider an N -bus power system with the following power flow equations at bus k :

$$\begin{cases} P_k = \sum_{n=1}^N V_k V_n Y_{kn} \cos(\theta_{kn} + \delta_n - \delta_k) \\ Q_k = - \sum_{n=1}^N V_k V_n Y_{kn} \sin(\theta_{kn} + \delta_n - \delta_k) \end{cases} \quad (9)$$

where P is the active power, Q is the reactive power, V is the magnitude of bus voltage phasor, δ is the angle of bus voltage phasor, Y is the magnitude of Y_{bus} , and θ is the angle of Y_{bus} . Expanding these two equations in a Taylor series for the initial estimate and neglecting all higher-order terms result in the following set of linear equations:

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \underbrace{\begin{bmatrix} \frac{\partial P}{\partial \delta} & \frac{\partial P}{\partial V} \\ \frac{\partial Q}{\partial \delta} & \frac{\partial Q}{\partial V} \end{bmatrix}}_{\text{Jacobian}} \begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix} \quad (10)$$

By solving the previous equation, the voltage sensitivity matrix can be extracted as follows:

$$\begin{bmatrix} \Delta \delta \\ \Delta V \end{bmatrix} = \begin{bmatrix} S_{\delta P} & S_{\delta Q} \\ S_{VP} & S_{VQ} \end{bmatrix} \begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} \quad (11)$$

where S_{VP} and S_{VQ} are the sensitivities of the bus voltage magnitudes to the active and reactive powers, respectively, and $S_{\delta P}$ and $S_{\delta Q}$ are the sensitivities of the bus voltage angles. The magnitude of the voltage at bus k can be calculated using the following linear equation:

$$V_k = V_s + \sum_{n=2}^N (S_{VP, k, n} P_n + S_{VQ, k, n} Q_n) \quad (12)$$

where V_s is the voltage at the connection point to the grid. On the basis of this equation, it can be found that the active and reactive powers generated or consumed at any location in an LV grid affect the whole grid. To clarify, suppose that the two-bus system of Fig. 3 is converted to a three-bus system with the following conditions: the PV generation is divided into P_2 and P_3 and the line impedance is divided into Z_2 and Z_3 , as shown in Fig. 13. Using (9)–(12), the voltage at bus 3 is then

$$V_3 = V_1 + \frac{R_2 P_2 + X_2 Q_2}{V_1} + \frac{(R_2 + R_3) P_3 + (X_2 + X_3) Q_3}{V_1} \quad (13)$$

On the basis of (13), the active power and the reactive power injected or consumed at bus 3 have more effect on V_3 than active

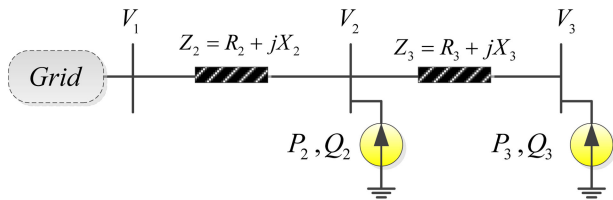


Fig. 13 Three-bus system with two PV installations

and reactive powers at bus 2; therefore, controlling the active and reactive powers at bus 3 is more effective than bus 2. This is a simplified three-bus radial grid, and for a real LV grid with complex configuration, suitable locations have to be found for the most efficient grid voltage control. To this aim, the grid data as well as the information of generation and consumption in different buses have to be known.

Local control strategies for voltage control are not as effective as central control approaches due to a lack of information about other buses. On the other hand, there are two main drawbacks associated with centralised control methods; first, the associated cost and second, the reliability of these methods. The reliability of centralised methods is less than localised methods due to the possibility of communication failure. To overcome this challenge, centralised and localised control methods can be combined to provide a robust method for overvoltage prevention [82]. On the other hand, the cost associated with the centralised methods is high and can limit implementation. Distributed control methods are another alternative and can be applied for voltage control. These methods usually require communication; however, broadband and fast communication are generally not required [94, 95]. In these methods, locally controlled units are coordinated through communication links and the communication failure can only reduce the efficiency. Although these methods do not lead to network-wide optimal behaviour [96], the costs associated with implementing distributed control methods are lower than for centrally controlled methods. The associated cost varies according to the grid structure and the control algorithm.

5 Conclusion

In this paper, a detailed and in-depth review of methods and strategies proposed to prevent overvoltage in LV grids with PV was provided including comments and thoughts on the methodologies referenced. The overvoltage caused by high PV penetration and the solutions for facilitating high share of PV systems were illustrated using the provided mathematical framework, and an evaluation of localised, distributed, and centralised voltage control methods was presented using the voltage sensitivity analysis. The effectiveness of overvoltage prevention methods, i.e. reinforcement of current grids, application of active transformers, active power curtailment, reactive power absorption by PV inverters, DR, and application of EESSs were discussed. According to the analyses, without knowledge of the grid data specifically the impedances of the grid conductors, efficient voltage control is difficult; therefore, the grid data has to be estimated as precisely as possible using relevant methods, if the relevant information is not available. In addition, selecting a proper method to increase the PV hosting capacity of an LV grid highly depends on the grid structure and the grid regulatory specifications. However, combination of different methods can provide the most efficient solutions for overvoltage prevention. The concluding remarks regarding the proposed methods are listed below:

- From the technical point of view, the grid reinforcement is highly effective for the overvoltage prevention; however, it is an expensive solution and the cost associated with the grid reinforcement highly depends on the grid structure, types of conductors, and the grid development plan.
- Active transformers are applicable to almost all LV grids and have a high potential for increasing the PV hosting capacity of LV grids. By efficient control of active transformers, the limiting factor of installing new PV systems will no longer be

overvoltage in the grid but rather the ratings of the grid components. Advanced local control methods for the efficient control of active transformers are needed, as the ICT infrastructures can increase the overall cost considerably and decrease the economic efficiency.

- Active power curtailment is probably an unavoidable solution in high PV-penetration conditions; without accepting a level of curtailment, reaching a high share of PV is quite expensive. Accepting a level of curtailment is specifically important for determining the size of electrical energy storage required for overvoltage prevention. The energy loss associated with active power curtailment depends on factors such as the orientation and inclination of PV panels, weather conditions, and the curtailment strategy. By applying advanced voltage-dependent curtailment strategies, this energy loss can be decreased.
- DR depends to a great extent on customers' domestic loads that may not be used on a daily basis, or loads of which their consumption is not considerable compared with the PV generation during peak generation periods. Shifting the EV charging to the peak-PV-generation hours by controlled EV charging can decrease the net power injected into the grid and prevent overvoltage during high PV-generation hours, when the penetration of EVs is increased.
- Reactive power absorption by PV inverters can also increase the PV hosting capacity of LV grids. The effectiveness of reactive power absorption depends to a large extent on the grid's characteristics; however, in most cases the PV hosting capacity can be increased by more than 20% by applying reactive power absorption. Therefore, when the PV penetration in the grid is high, the reactive power absorption can considerably decrease the risk of overvoltage and increase the overall efficiency of the grid by preventing the disconnection of PV inverters or active power curtailment. In general, localised droop methods applied to the new PV inverters can provide proper voltage support without need for ICT infrastructures, and centralised methods are not needed in many cases.
- Electrical energy storage application has a high potential for overcoming the challenges associated with PV systems, and, in addition to its application for overvoltage prevention, it can be used to prevent the overloading of the grid components and trade power in electricity markets. Localised methods for energy storage charging control are not effective solutions and can considerably increase the energy storage capacity that is required for overvoltage prevention; therefore, advanced control methods are needed to decrease the initial investment associated with the ICT infrastructures as well as provide more efficient energy storage management.

6 References

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