

## Case-study 4

Q) Finding a number in an array  
 $A = [3, 6, 1, 33, 8, 5, 11, 23, 0]$

$B = [0, 1, 3, 5, 6, 8, 11, 23, 33, 88]$

Solution:

$A = [3, 6, 1, 33, 8, 5, 11, 23, 0]$

A is unsorted

let  $x = 23$   $\therefore N$  is number of elements in list/array

if  $(x < A[0] \text{ or } x > A[N-1])$

print  $\rightarrow$  X is not present in the list

for  $i = 0 \rightarrow (N-1)$

if  $(A[i] == x)$

print  $\rightarrow$  X is present

return;

else

print  $\rightarrow$  X is not present

return;

Best case:

Best case is when X is present at the index 0.

$\Omega(\cdot) = 1$

**Worst case:**

Worst case is when we have to check till the last index of array i.e.  $N-1$

$$O(\cdot) = N$$

**Solution:**

$B = [0, 1, 3, 5, 8, 11, 23, 33, 88]$

if  $(X < B[0] \text{ or } X > B[N-1])$

print  $\rightarrow$  X is not present

for  $(i=0; i < N; i++)$

if  $(B[i] == X)$

print  $\rightarrow$  X is present return;

else if  $(B[i] > X)$

print  $\rightarrow$  X is not present  
return;

In this case, the loop will stop when  $B[i]$  is greater than X, because the list is sorted, and no need to check when  $B[i] > X$ .



**Best case:**

Best case is when we have to find the  $x$  at zero index

$$R(-) = 1$$

**Worst case:**

Worst case is when we have to find the  $x$  till the last index

$$[O](-) = N$$

**Solution :**

$B = [0, 1, 3, 5, 6, 8, 11, 23, 33, 88]$   
Sorted list

Using Binary Search:  $N \rightarrow \frac{N}{2} \rightarrow \frac{N}{4} \rightarrow \frac{N}{8} \dots$

Let  $X = 10$

$B = [0, 1, 3, 5, 6, 8, 11, 23, 33, 88]$

$mid = 6$

$B_1 = [0, 1, 3, 5, 6]$

$B_2 = [8, 11, 23, 33, 88]$

$$X > \text{mid}$$

$$10 > 6$$

remove  $B_1$  as  $X$  is greater than the all elements in  $B_1$ .

$$B_2 = [8, 11, 23, 33, 88]$$

$$\text{mid} = 23$$

$$B_3 = [8, 11, 23]$$

$$B_4 = [33, 88]$$

$$X < \text{mid}$$

$$10 < 23$$

remove  $B_4$  as  $X$  is lesser than all elements in  $B_4$ .

$$B_3 = [8, 11, 23]$$

$$\text{mid} = 11$$

$$B_5 = [8]$$

$$B_6 = [11, 23]$$

$$10 < 11$$

$$X < \text{mid}$$

remove  $B_6$ .

$$B_5 = [8]$$

$X$  is not present in the list