Economics
of Human
Capital

Philipp Eisenhauer

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### **Economics of Human Capital**

Static model of educational choice

Philipp Eisenhauer

## Introduction

#### Figure: Motivation

#### Estimating Marginal Returns to Education

By Pedro Carnedio, James J. Heckman, and Edward J. Vytlacii.

Estimating marginal returns to policies is a central task of economic cost-benefit analysis. A comparison between marginal benefits and marginal costs determines the optimal size of a social program. For example, to evaluate the optimality of a policy that promotes expansion in college attendance, analysts need to estimate the return to college for the marginal student and compare it to the marginal cost of the

This is a relatively simple task (i) if the effect of the policy is the same for everyone (conditional on observed variables) or (ii) if the effect of the policy varies across individuals given observed variables but agents either do not know their idiosyncratic returns to the policy, or if they know them, they do not act on them. In these cases, individuals do not choose their schooling based on their mulized idiosyncratic individual returns, and thus the marginal and average ex post returns to schooling

Under these conditions, the mean marriral return to college can be estimated using conventional methods applied to the following Miner equation:

 $Y = \alpha + \beta S + \epsilon$ 

where Y is the log wage, S is a dummy variable indicating college attendance,  $\beta$  is the return to schooling (which may vary among persons), and  $\varepsilon$  is a residual. The standard problem of selection bias (S correlated with  $\epsilon$ ) may be present, but this problem can be solved by a variety of conventional methods (instrumental variables (IV) recression discontinuity, and selection models).

\*Caracire: Department of Economics, University College Lendon, Gover Steat, Lendon WCIE 68T, United Engliss, Institute for Fried Blades and Center for Microdial Methods and Practice (e-mid) possessivilent and (highest Propulations of Brownices, University of College, 11.28 E. 29th Steat, College, 10.28 Sec. 2014).
Sec. 2014. American Rev Foundation, Group Institute, and University College Dables (e-mid: jub thinkingsock), Vylands Department of Brownics and Center Securities, 100. authors and not necessarily those of these funders.

† To view additional materials, with the article page at his polywors assumed neglection, playblain 10: 3255/has 101.6.2954.

\*See Heckman and Vythacil (2007b).

Carneiro & al. (2011)

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2001 LAWRENCE R. KLEIN LECTURE WITH AN APPLICATION TO THE RETURNS TO SCHOOLING AND MEASUREMENT OF THE EFFECTS OF UNCERTAINTY

ON COLLEGE CHOICE. By PEDRO CARNEIRO, KARSTEN T. HANSEN, AND JAMES J. HECKMAN<sup>2</sup>

Department of Economics, University of Chicago; Kellogg School of Management, Northwestern University: Department University of Chicago and The American Ber Foundation

This article uses factor models to identify and estimate the distributions of counterfactuals. We extend LISREL frameworks to a denumic treatment effect setting, extending matching to account for unobserved conditioning variable

<sup>1</sup> Pravious venions of this paper were given at the Midwest Econometrics Goosp, Chicago, October 2000, Washington University St. Louis, May, 2001, the Needle Econometric Meetings, May, 2000 and workshops at Chicago. August. 2002 and Stanford, Insurary, 2005. A simple venion of this paper in conference in Monkholm Sortelan, Challers IRIC. We are guidful is all northinoparticipants for eigen-ciality flants Mark Doggan, Carolin Allemania, and Malhael Kanen for comments on the first of sith of this paper. We have breafted from discussions with Ricardo Barron, Richard Diandell, Francisco Darm, Plavio Casha, Mark Doggan, Lars Hannes, Steven Levill, Blac LL, Luig Holderin, and Sergio Urean on subsequent daths. We single out Rabshold Princery and Edward Visiolal for expectable the behalf comments. We are grateful to Flavio Cunha and Salvador Navarro for exceptional research assistance and hard work. This research is supported by NSF 97-09-073, SES-0099595, and NICHD-5RO1-HD54956. Culbenkian, Please address overspondence to: James I. Heckman, Department of Economics, Univer-sity of Chicago, 1126 E. 59th Space, Chicago, El. 6667, USA, Tell +773 702 6654; Fac: +773 702 6690.

Carneiro & al. (2003)

## Heckman (2008) defines three policy evaluation tasks:

- Evaluating the impact of historical interventions on outcomes including their impact in terms of wellbeing of the treated and the society at large.
- Forecasting the impact of historical interventions implemented in one environment in other environments, including their impact in terms of well-being.
- Forecasting the impacts of interventions never historically experienced to various environments, including their impact on well-being.

#### **Econometrics of policy evaluation**

- ▶ is important
- ▶ is complicated
- is multifaceted

#### **Numerous applications**

- ▶ labor economics
- development economics
- industrial economics
- health economics

#### **Numerous effects**

- conventional average effects
- policy-relevant average effects
- marginal effects
- distributional effects
- effects on distributions

#### **Numerous estimation strategies**

- instrumental variables
- ► (quasi-)experimental methods
- matching

## Model

#### **Generalized Roy model**

$$Y_1 = \mu_1(X) + U_1$$

$$Y = DY_1 + (1 - D)Y_0$$

$$Y_0 = \mu_0(X) + U_0$$

#### Choice

$$D = I[S > 0]$$

$$S = \mu_D(X, Z) - V$$

- ▶ *S* is the overall surplus from treatment participation
- V captures the individual's unobservable dislike of treatment

## Individual Heterogeneity

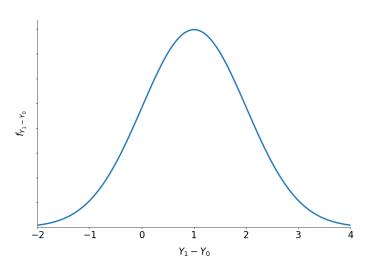
#### Individual-specific benefit of treatment

$$Y_1 - Y_0 = (\mu_1(X) - \mu_0(X)) + (U_1 - U_0)$$

#### **Sources of Heterogeneity**

- Difference in observables
- Difference in unobservables
  - Uncertainty
  - Private information

#### Figure: Distribution of benefits



#### **Econometric problems**

- ► **Evaluation problem**, we only observe an individual in either the treated or untreated state.
- ➤ **Selection problem**, individuals that select into treatment differ from those that do not.

#### **Essential Heterogeneity**

**Definition:** Individuals select their treatment status based on gains unobservable by the econometrician. More formally,

$$Y_1 - Y_0 \not\perp \!\!\!\perp D \mid X = x.$$

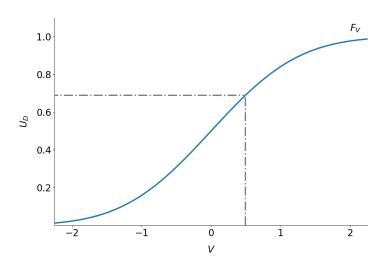
⇒ consequences for the choice of the estimation strategy

## **Objects of interest**

#### **Useful Notation**

$$P(X, Z) = \Pr(D = 1 \mid X, Z) = F_V(\mu_D(X, Z))$$
  
 $U_D = F_V(V)$ 

#### Figure: First-stage unobservable



#### Figure: Support

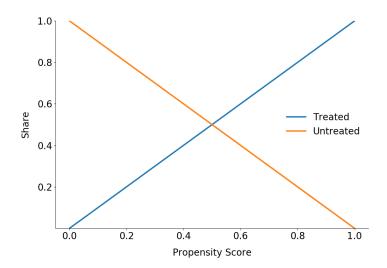
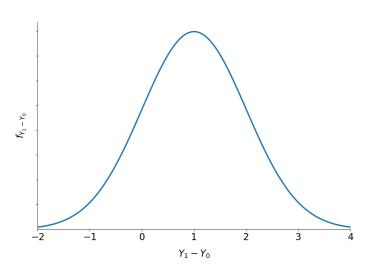
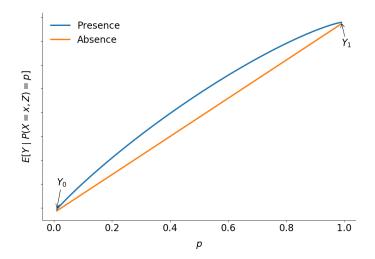


Figure: Distribution of benefits



#### Figure: Conditional expectation and essential heterogeneity



# Conventional Average Treatment Effects

#### **Conventional Average Treatment Effects**

$$B^{ATE} = E[Y_1 - Y_0]$$
  
 $B^{TT} = E[Y_1 - Y_0 \mid D = 1]$   
 $B^{TUT} = E[Y_1 - Y_0 \mid D = 0]$ 

⇒ correspond to *extreme* policy alternatives

#### **Selection Problem**

$$E[Y \mid D = 1] - E[Y \mid D = 0] = \underbrace{E[Y_1 - Y_0 \mid D = 1]}_{B^{TT}} + \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection bias}}$$

$$\begin{split} E[Y \mid D=1] - E[Y \mid D=0] &= \underbrace{E[Y_1 - Y_0]}_{B^{ATE}} \\ &+ \underbrace{E[Y_1 - Y_0 \mid D=1] - E[Y_1 - Y_0]}_{\text{Sorting on gains}} \\ &+ \underbrace{E[Y_0 \mid D=1] - E[Y_0 \mid D=0]}_{\text{Sorting on levels}} \end{split}$$

- bias depends on the parameter of interest
- selection bias as sorting on levels

Figure: Distribution of effects with essential heterogeneity

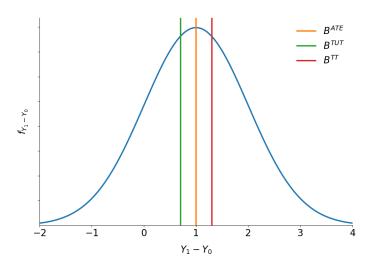
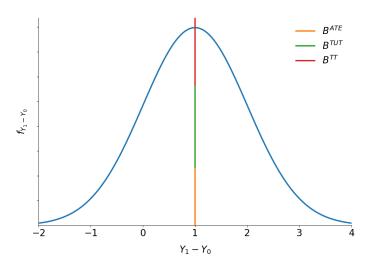


Figure: Distribution of effects without essential heterogeneity



## Policy-Relevant Average Treatment Effects

#### **Observed Outcomes**

$$Y_B = D_B Y_1 + (1 - D_B) Y_0$$
  
 $Y_A = D_A Y_1 + (1 - D_A) Y_0$ 

#### **Effect of Policy**

$$B^{PRTE} = \frac{1}{E[D_A] - E[D_B]} (E[Y_A] - E[Y_B])$$

## Marginal Benefit of Treatment

#### **Marginal Benefit of Treatment**

$$B^{MTE}(x, u_D) = E[Y_1 - Y_0 \mid X = x, U_D = u_D]$$

**Intuition:** Mean gross return to treatment for persons at quantile  $u_D$  of the first-stage unobservable V or a willingness to pay for individuals at the margin of indifference.

#### Figure: Margin of indifference

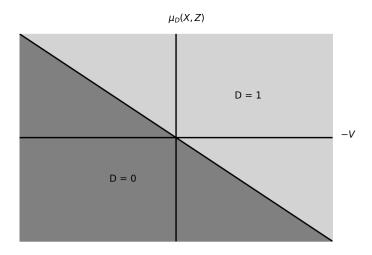
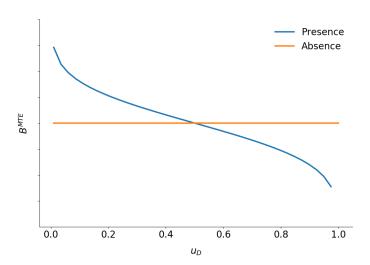


Figure:  $B^{MTE}$  and essential heterogeneity



Effects of treatment as weighted averages Parameter  $\Delta_j$ , can be written as a weighted average of the  $B^{MTE}(x, u_D)$ .

$$\Delta_j(x) = \int_0^1 B^{MTE}(x, u_D) \omega^j(x, u_D) du_D,$$

where the weights  $\omega^{j}(x,u_{D})$  are specific to parameter j and integrate to one.

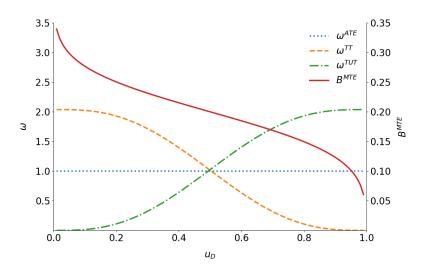
### Weights

$$\omega^{ATE}(x, u_D) = 1$$

$$\omega^{TT}(x, u_D) = \frac{1 - F_{P|X=X}(u_D)}{E[P \mid X = x]}$$

$$\omega^{TUT}(x, u_D) = \frac{F_{P|X=X}(u_D)}{E[1 - P \mid X = x]}$$

Figure: Effects of treatment as weighted averages



## Local Average Treatment Effect

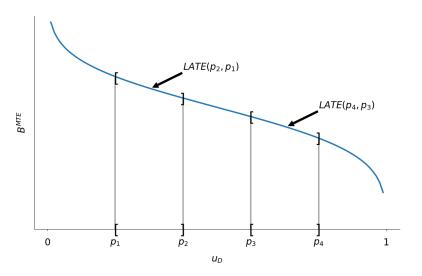
### **Local Average Treatment Effect**

- ► Local Average Treatment Effect: Average effect for those induced to change treatment because of a change in the instrument.
  - ⇒ instrument-dependent parameter
- ▶ Marginal Treatment Effect: Average effect for those individuals with a given unobserved desire to receive treatment.
  - ⇒ deep economic parameter

$$B^{LATE} = \frac{E[Y \mid Z = z] - E[Y \mid Z = z']}{P(z) - P(z')}$$

$$B^{LATE}(x, u_D, u_{D'}) = \frac{1}{u_D - u_{D'}} \int_{u_D}^{u_{D'}} B^{MTE}(x, u) du,$$

### Figure: Local average treatment effect



## Distributions of Effects

#### **Distributions of Effects**

- marginal distribution of benefits
- joint distribution of potential outcomes
- joint distribution of benefits and surplus

### Figure: Distribution of benefits

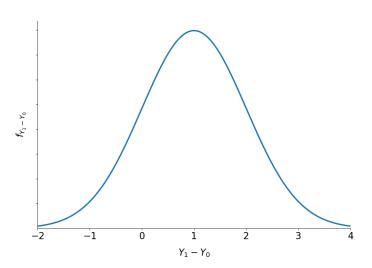


Figure: Distribution of potential outcomes

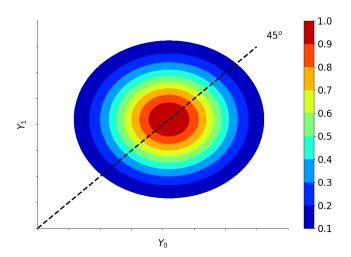
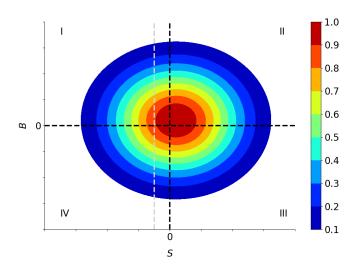


Figure: Distribution of benefits and surplus



## **Conclusion**

# **Appendix**

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