# **Economics of Human Capital**

Static model of educational choice

Philipp Eisenhauer

# Introduction

#### Figure: Motivation

American Economic Review NN (October 2011): 2754-2781

#### Estimating Marginal Returns to Education®

By Pedro Carneiro, James J. Heckman, and Edward J. Vytlace.

Estimating marginal returns to policies is a central task of economic cost-benefit analysis. A comparison between marginal benefits and marginal costs determines the optimal size of a social programs. For example, to evaluate the optimality of a policy that promotes expansion in college attendance, analysts need to estimate the return to college for the marginal sudest and connece it to the marginal cost of the

This is a relatively simple task (i) if the effect of the policy is the same for every new (conditional on observed variables) or (ii) if the effect of the policy varies across individuals given observed variables but agents either do not acro their idiosyscratic resums to the policy, or if they know them, they do not acro them the cases, individuals do not choose their shoothery based on their realized idiosystematic across the contract of the contract of

Under these conditions, the mean marginal return to college can be estimated using conventional methods applied to the following Minorr equation:

$$Y = \alpha + \beta S + \varepsilon$$
,

where Y is the log wage, S is a dummy variable indicating college attendance,  $\beta$  is the return to schooling (which may vary among persons), and  $\varepsilon$  is a residual. The standard problem of selection bits at S correlated with  $\varepsilon$  any log person, but this problem can be solved by a variety of conventional methods (instrumental variables (IV), regression discontinuity, and election models).

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See Hockman and Vythaci (2007b).

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Carneiro & al. (2011)

INTERNATIONAL

ECONOMIC REVIEW

May 2003 Vol. 44, No. 2

2011 LAWRENCE R. KLEIN LECTURE

\* Manageriet received October 2000 period January 2003

ESTIMATING DISTRIBUTIONS OF TREATMENT EFFECTS WITH AN APPLICATION TO THE RETURNS TO SCHOOLING AND MEASUREMENT OF THE EFFECTS OF UNCERTAINTY ON COLLEGE CHOICE\*

Department of Economics, University of Chicago; Kellogg School of Management, Northwestern University; Department of Economics, University of Chicago and The American Bar Foundation

This action uses factor models to identify and estimate the distributions of content factorial. We carised LEEACL Intersection to of granular transmiss content factorial and strategy as second or mosh-rowly conditioning vehicles. Using these models, we can identify all palests and place transmiss critical vehicles and the particular and particular and particular and particular and particular and particular particul

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Gulberkins, Please address correspondence to James I. Heckman, Department of Economics, Univ. sky of Chicago, 1256 E. 59th Street, Chicago, E. 6667, USA, Tul: +777 712-6654. Fac: +779 712-665.

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Carneiro & al. (2003)

# Heckman (2008) defines three policy evaluation tasks:

- Evaluating the impact of historical interventions on outcomes including their impact in terms of wellbeing of the treated and the society at large.
- Forecasting the impact of historical interventions implemented in one environment in other environments, including their impact in terms of well-being.
- Forecasting the impacts of interventions never historically experienced to various environments, including their impact on well-being.

# **Econometrics of policy evaluation**

- ▶ is important
- is complicated
- is multifaceted

# **Numerous applications**

- labor economics
- development economics
- industrial economics
- health economics

#### **Numerous effects**

- conventional average effects
- policy-relevant average effects
- marginal effects
- distributional effects
- effects on distributions

# **Numerous estimation strategies**

- instrumental variables
- (quasi-)experimental methods
- matching

# Model

# **Generalized Roy model**

#### **Potential Outcomes**

$$Y_1 = \mu_1(X) + U_1$$

$$Y = DY_1 + (1 - D)Y_0$$

$$Y_0 = \mu_0(X) + U_0$$

### Choice

$$D = I[\mu_D(X, Z) - V > 0]$$

# Individual Heterogeneity

## Individual-specific Benefit of Treatment

$$Y_1 - Y_0 = (\mu_1(X) - \mu_0(X)) + (U_1 - U_0)$$

# **Sources of Heterogeneity**

- Difference in observables
- Difference in unobservables
  - Uncertainty
  - Private information

Figure: Distribution of benefits



## **Econometric problems**

- ► **Evaluation problem**, we only observe an individual in either the treated or untreated state.
- ➤ **Selection problem**, individuals that select into treatment differ from those that do not.

## **Essential Heterogeneity**

**Definition:** Individuals select their treatment status based on gains unobservable by the econometrician. More formally,

$$Y_1 - Y_0 \not\perp \!\!\!\perp D \mid X = x.$$

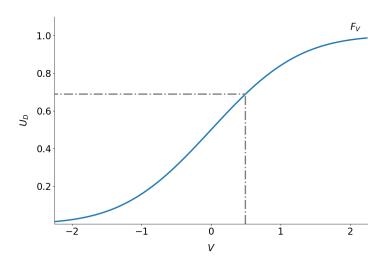
⇒ consequences for the choice of the estimation strategy

# **Objects of interest**

### **Useful Notation**

$$P(X, Z) = Pr(D = 1 | X, Z) = F_V(\mu_D(X, Z))$$
  
 $U_D = F_V(V)$ 

# Figure: First-stage unobservable



## Figure: Support

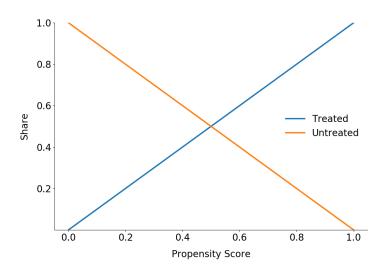


Figure: Distribution of benefits

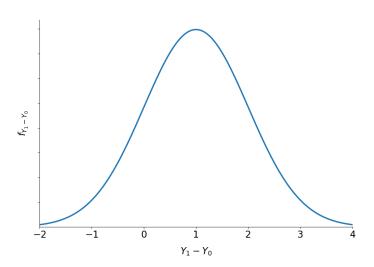
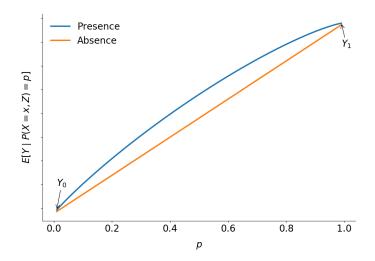


Figure: Conditional expectation and essential heterogeneity



# Conventional Average Treatment Effects

# **Conventional Average Treatment Effects**

$$B^{ATE} = E[Y_1 - Y_0]$$
  
 $B^{TT} = E[Y_1 - Y_0 \mid D = 1]$   
 $B^{TUT} = E[Y_1 - Y_0 \mid D = 0]$ 

⇒ correspond to *extreme* policy alternatives

#### **Selection Problem**

$$\begin{split} E[Y \mid D = 1] - E[Y \mid D = 0] &= \underbrace{E[Y_1 - Y_0]}_{B^{ATE}} \\ &+ \underbrace{E[Y_1 - Y_0 \mid D = 1] - E[Y_1 - Y_0]}_{\text{Sorting Gain}} \\ &+ \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection Bias}} \end{split}$$

$$E[Y \mid D = 1] - E[Y \mid D = 0] = \underbrace{E[Y_1 - Y_0 \mid D = 1]}_{B^{TT}} + \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection Bias}}$$

⇒ the bias depends on the parameter of interest

Figure: Distribution of effects with essential heterogeneity

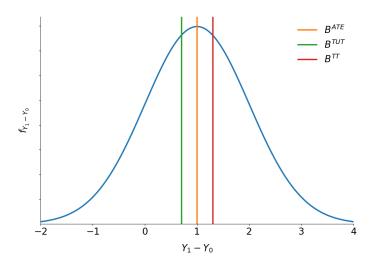
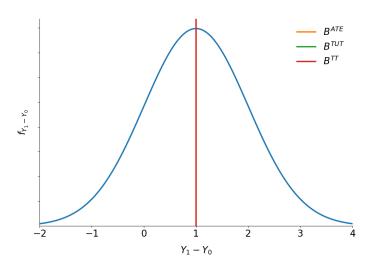


Figure: Distribution of effects without essential heterogeneity



# Policy-Relevant Average Treatment Effects

#### **Observed Outcomes**

$$Y_B = D_B Y_1 + (1 - D_B) Y_0$$
  
 $Y_A = D_A Y_1 + (1 - D_A) Y_0$ 

## **Effect of Policy**

$$B^{PRTE} = \frac{1}{E[D_A] - E[D_B]} (E[Y_A] - E[Y_B])$$

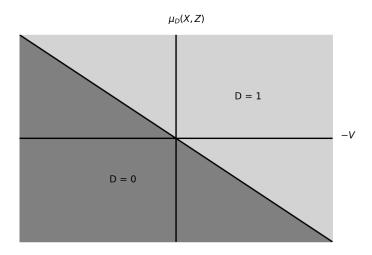
# Marginal Effect of Treatment

## **Marginal Benefit of Treatment**

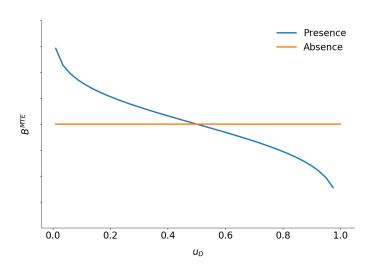
$$B^{MTE}(x, u_D) = E[Y_1 - Y_0 \mid X = x, U_D = u_D]$$

**Intuition:** Mean gross return to treatment for persons at quantile  $u_D$  of the first-stage unobservable V or a willingness to pay for individuals at the margin of indifference.

# Figure: Margin of indifference



# Figure: $B^{MTE}$ and essential heterogeneity



Effects of treatment as weighted averages Parameter  $\Delta_j$ , can be written as a weighted average of the  $B^{MTE}(x, u_D)$ .

$$\Delta_j(x) = \int_0^1 B^{MTE}(x, u_D) \omega^j(x, u_D) du_D,$$

where the weights  $\omega^{j}(x,u_{D})$  are specific to parameter j and integrate to one.

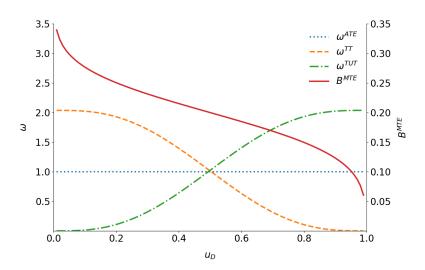
## Weights

$$\omega^{ATE}(x, u_D) = 1$$

$$\omega^{TT}(x, u_D) = \frac{1 - F_{P|X=X}(u_D)}{E[P \mid X = x]}$$

$$\omega^{TUT}(x, u_D) = \frac{F_{P|X=X}(u_D)}{E[1 - P \mid X = x]}$$

Figure: Effects of treatment as weighted averages



# Local Average Treatment Effect

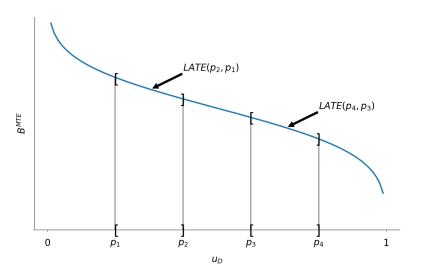
### **Local Average Treatment Effect**

- Local Average Treatment Effect: Average effect for those induced to change treatment because of a change in the instrument.
  - ⇒ instrument-dependent parameter
- Marginal Treatment Effect: Average effect for those individuals with a given unobserved desire to receive treatment.
  - ⇒ deep economic parameter

$$B^{LATE} = \frac{E[Y \mid Z = z] - E[Y \mid Z = z']}{P(z) - P(z')}$$

$$B^{LATE}(x, u_D, u_{D'}) = \frac{1}{u_D - u_{D'}} \int_{u_D}^{u_{D'}} B^{MTE}(x, u) du,$$

### Figure: Local average treatment effect



## Distributions of Effects

#### **Distributions of Effects**

- marginal distribution of benefits
- joint distribution of potential outcomes
- joint distribution of benefits and surplus

## Figure: Distribution of benefits



Figure: Distribution of potential outcomes

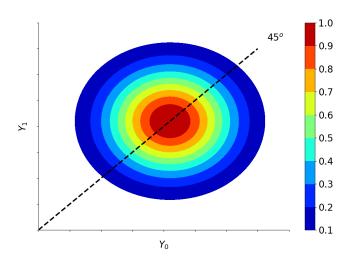
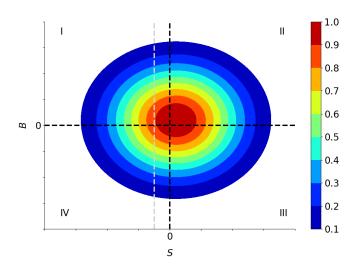


Figure: Distribution of benefits and surplus



## **Conclusion**

# **Appendix**

# References

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