Economics
of Human
Capital

Philipp Eisenhauer

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### **Economics of Human Capital**

Static model of educational choice

Philipp Eisenhauer

## Introduction

#### Figure: Motivation

American Research Review XX (October 2011): 2754-2781

#### Estimating Marginal Returns to Education®

By Pedro Carnedo, James J. Heckman, and Edward J. Vytlace.

Estimating marginal returns to policies is a central task of economic cost-benefit analysis. A comparison between marginal brentits and marginal costs determines the optimal site of a social programs. For example, to evaluate the optimality of a policy that promotes expansion in college attendance, analysis need to estimate the tentum to college of the marginal suders and occurace in to the marginal cost of the college.

This is a relatively simple task (i) if the effect of the peloy is the some for everyence (conditional or theoreted variables) or (ii) if the effect of the peloy wints across individuals given observed variables but agents either do not know their ideopcerals returns to the peloy; or if they know them, they do not act on them. In those cases, individuals do not choose their schooling based on their railized disloyration individual returns, and thus the marginal and average or post returns to schooling are the same?

Under these conditions, the mean marginal return to college can be estimated using conventional methods applied to the following Miner equation:

 $Y = \alpha + \beta S + \varepsilon$ ,

where Y is the log wage, S is a dummy variable indicating college attendance,  $\beta$  is the return to schooling (which may vary among persons), and e is a residual. The standard problem of selection bits as (S correlated with e) may be present, but this problem can be solved by a variety of conventional methods (instrumental variables IVV) repression discontinuity, and absence in models.

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authors and not necessarily those of these handers.

† To view additional materials, visit the article page at http://www.naseub.org/addition.ph/blain 10.1255/has 101.6.2754.

\*See Heckman and Vydacl (2007b).

Carneiro & al. (2011)

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ECONOMIC REVIEW

May 2003 Vol. 44, No. 2

2001 LAWRENCE R. KLEIN LECTURE
ESTIMATING DISTRIBUTIONS OF TREATMENT EFFECTS
WITH AN APPLICATION TO THE RETURNS TO SCHOOLING
AND MEASTREMENT OF THE EFFECTS OF UNCERTAINTY

ON COLLEGE CHOICE\*

By PEDRO CASNESSO, KARSTEN T. HANSEN, AND JAMES J. HECKMAN\*

Department of Economics, University of Chicago, Kellogg School of Management, Northwestern University; Department of Economics, University of Chicago and The American Bar Foundation

This makes must factor models to dentify and estimates the distributions of constructional. We extend LEMEL frameworks to a dynamic transmiss efficiency constructional. We extend LEMEL frameworks to desire the construction of the construction of

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Carneiro & al. (2003)

## Heckman (2008) defines three policy evaluation tasks:

- Evaluating the impact of historical interventions on outcomes including their impact in terms of wellbeing of the treated and the society at large.
- ➤ Forecasting the impact of historical interventions implemented in one environment in other environments, including their impact in terms of well-being.
- Forecasting the impacts of interventions never historically experienced to various environments, including their impact on well-being.

#### **Econometrics of policy evaluation**

- ▶ is important
- ▶ is complicated
- is multifaceted

#### **Numerous applications**

- ► labor economics
- development economics
- industrial economics
- health economics

#### **Numerous effects**

- conventional average effects
- policy-relevant average effects
- marginal effects
- distributional effects
- effects on distributions

#### **Numerous estimation strategies**

- instrumental variables
- ► (quasi-)experimental methods
- matching

### Model

#### **Generalized Roy model**

$$Y_1 = \mu_1(X) + U_1$$

$$Y = DY_1 + (1 - D)Y_0$$

$$Y_0 = \mu_0(X) + U_0$$

#### Choice

$$D = I[S > 0]$$

$$S = \mu_D(X, Z) - V$$

- ▶ *S* is the overall surplus from treatment participation
- V captures the individual's unobservable dislike of treatment

## Individual Heterogeneity

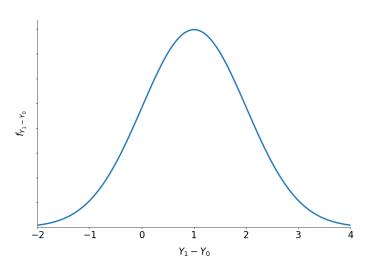
#### Individual-specific benefit of treatment

$$Y_1 - Y_0 = (\mu_1(X) - \mu_0(X)) + (U_1 - U_0)$$

#### **Sources of Heterogeneity**

- Difference in observables
- Difference in unobservables
  - Uncertainty
  - Private information

#### Figure: Distribution of benefits



#### **Econometric problems**

- ► **Evaluation problem**, we only observe an individual in either the treated or untreated state.
- ► **Selection problem**, individuals that select into treatment differ from those that do not.

#### **Essential Heterogeneity**

**Definition:** Individuals select their treatment status based on gains unobservable by the econometrician. More formally,

$$Y_1 - Y_0 \not\perp\!\!\!\perp D | X = x.$$

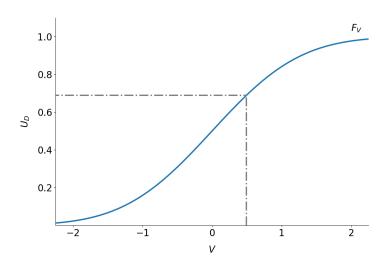
⇒ consequences for the choice of the estimation strategy

## **Objects of interest**

#### **Useful Notation**

$$P(X, Z) = \Pr(D = 1 \mid X, Z) = F_V(\mu_D(X, Z))$$
  
 $U_D = F_V(V)$ 

#### Figure: First-stage unobservable



#### Figure: Support

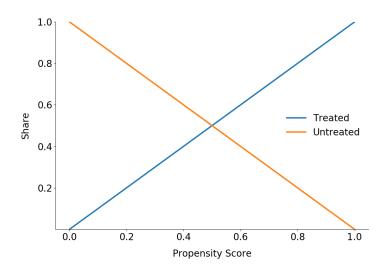


Figure: Distribution of benefits

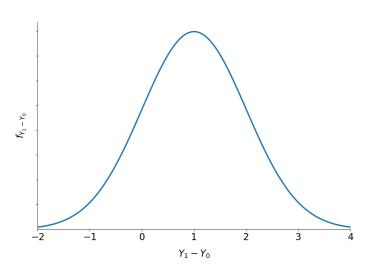
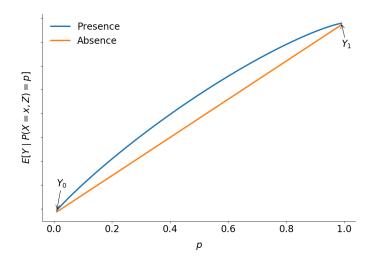


Figure: Conditional expectation and essential heterogeneity



# Conventional Average Treatment Effects

#### **Conventional Average Treatment Effects**

$$B^{ATE} = E[Y_1 - Y_0]$$
  
 $B^{TT} = E[Y_1 - Y_0 \mid D = 1]$   
 $B^{TUT} = E[Y_1 - Y_0 \mid D = 0]$ 

⇒ correspond to *extreme* policy alternatives

#### **Selection Problem**

$$E[Y \mid D = 1] - E[Y \mid D = 0] = \underbrace{E[Y_1 - Y_0 \mid D = 1]}_{B^{TT}} + \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection bias}}$$

$$\begin{split} E[Y \mid D = 1] - E[Y \mid D = 0] &= \underbrace{E[Y_1 - Y_0]}_{B^{ATE}} \\ &+ \underbrace{E[Y_1 - Y_0 \mid D = 1] - E[Y_1 - Y_0]}_{\text{Sorting on gains}} \\ &+ \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Sorting on levels}} \end{split}$$

- bias depends on the parameter of interest
- selection bias as sorting on levels

Figure: Distribution of effects with essential heterogeneity

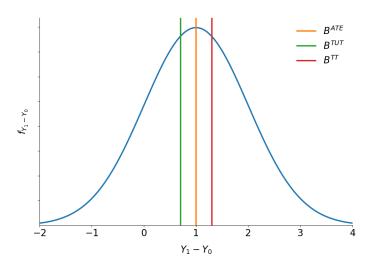
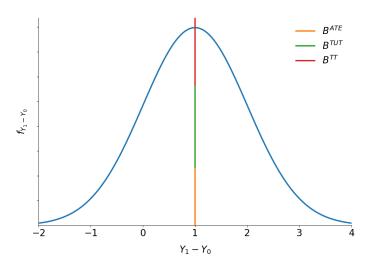


Figure: Distribution of effects without essential heterogeneity



## Policy-Relevant Average Treatment Effects

#### **Observed Outcomes**

$$Y_B = D_B Y_1 + (1 - D_B) Y_0$$
  
 $Y_A = D_A Y_1 + (1 - D_A) Y_0$ 

#### **Effect of Policy**

$$B^{PRTE} = \frac{1}{E[D_A] - E[D_B]} (E[Y_A] - E[Y_B])$$

## Marginal Benefit of Treatment

#### **Marginal Benefit of Treatment**

$$B^{MTE}(x, u_D) = E[Y_1 - Y_0 \mid X = x, U_D = u_D]$$

**Intuition:** Mean gross return to treatment for persons at quantile  $u_D$  of the first-stage unobservable V or a willingness to pay for individuals at the margin of indifference.

#### Figure: Margin of indifference

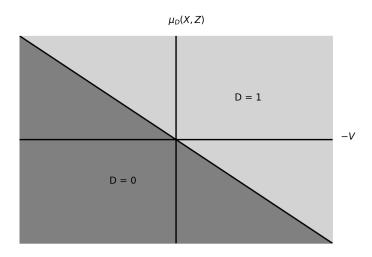


Figure:  $B^{MTE}$  and essential heterogeneity

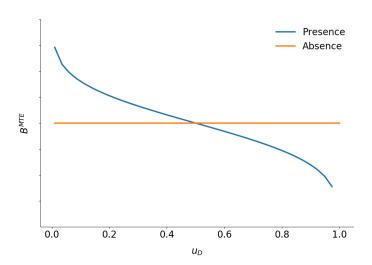
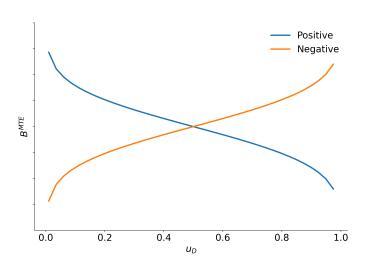


Figure: Selection scenarios



Effects of treatment as weighted averages Parameter  $\Delta_j$ , can be written as a weighted average of the  $B^{MTE}(x, u_D)$ .

$$\Delta_j(x) = \int_0^1 B^{MTE}(x, u_D) \omega^j(x, u_D) du_D,$$

where the weights  $\omega^{j}(x,u_{D})$  are specific to parameter j and integrate to one.

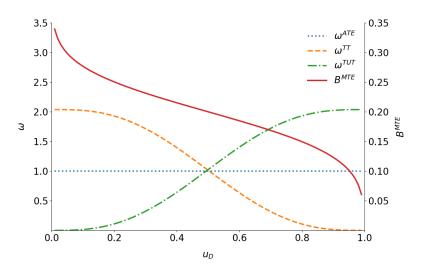
### Weights

$$\omega^{ATE}(x, u_D) = 1$$

$$\omega^{TT}(x, u_D) = \frac{1 - F_{P|X=X}(u_D)}{E[P \mid X = x]}$$

$$\omega^{TUT}(x, u_D) = \frac{F_{P|X=X}(u_D)}{E[1 - P \mid X = x]}$$

Figure: Effects of treatment as weighted averages



# Local Average Treatment Effect

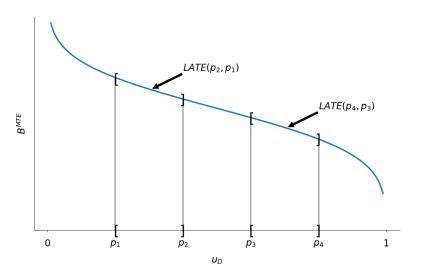
### **Local Average Treatment Effect**

- ► Local Average Treatment Effect: Average effect for those induced to change treatment because of a change in the instrument.
  - ⇒ instrument-dependent parameter
- ▶ Marginal Treatment Effect: Average effect for those individuals with a given unobserved desire to receive treatment.
  - ⇒ deep economic parameter

$$B^{LATE} = \frac{E[Y \mid Z = z] - E[Y \mid Z = z']}{P(z) - P(z')}$$

$$B^{LATE}(x, u_D, u_{D'}) = \frac{1}{u_D - u_{D'}} \int_{u_D}^{u_{D'}} B^{MTE}(x, u) du,$$

Figure: Local average treatment effect



## Distributions of Effects

#### **Distributions of Effects**

- marginal distribution of benefits
- joint distribution of potential outcomes
- joint distribution of benefits and surplus

## Figure: Distribution of benefits

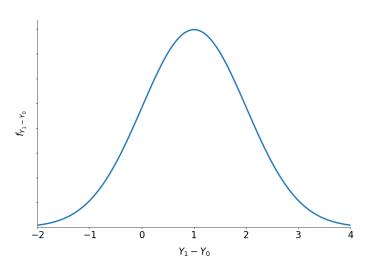


Figure: Distribution of potential outcomes

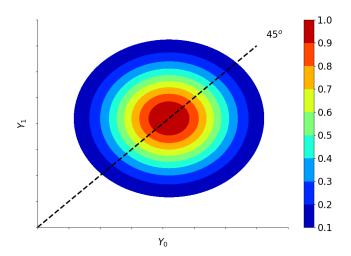
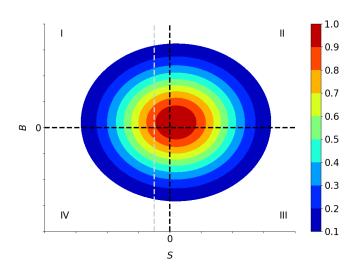


Figure: Distribution of benefits and surplus



# **Conclusion**

# **Appendix**

## References

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- Heckman, J. J. (2008). Schools, skills, and synapses. *Economic Inquiry*, 46, 289–324.