### **Economics of Human Capital**

Static model of educational choice

Philipp Eisenhauer

## Housekeeping

#### Lecture plan

- Static model of educational choices
- OpenSourceEconomics
- grmpy
- Estimating Marginal Returns to Education (Carneiro, Heckman, & Vytlacil, 2011)

#### **Course program**

- economics of human capital
- econometrics of human capital
- research seminar



### Introduction

#### Figure: Motivation

American Economic Review NN (Newbor 2011) - 2754-2781

#### Estimating Marginal Returns to Education®

By Pedro Carneiro, James J. Heckman, and Edward J. Vytlace.

Estimating marginal returns to policies is a central task of economic cost-benefit analysis. A comparison between marginal benefits and anagital costs determines the optimal size of a social programs. For example, to evaluate the optimality of a policy that promotes expansion in college attendance, analysis need to estimate the return to college for the marginal student and compare it to the marginal cost of the

This is a relatively simple task (i) if the effect of the policy is the same for everycue (conditional on observed variables) or (ii) if the effect of the policy series across individuals given observed variables to upstess either do not know their idiosyncrais returns to the policy, or if they issue them, they do not act on them. In those cases, individuals do not choose their schooling based on their realized idiosyncatic individual returns, and thus the marginal and average or, post returns to schooling arch be sure.<sup>38</sup>

Under these conditions, the mean marginal return to college can be estimated using conventional methods applied to the following Minorr equation:

$$Y = \alpha + \beta S + \varepsilon$$
,

where Y is the log wage, S is a dummy variable indicating college attendance,  $\beta$  is the return to schooling (which may vary sarring genoms), and  $\epsilon$  is a residual. The standard problem of selection bias (S correlated with  $\epsilon$ ) may be present, but this problem can be solved by a variety of conventional methods (instrumental variables (IV), regression discontinuity, and elsection models).

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See Hockman and Vythad (2007b).

Carneiro & al. (2011)

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May 2003

REVIEW Vol. 44, No. 2

2001 LAWRENCE R. KLEIN LECTURE
ESTIMATING DISTRIBUTIONS OF TREATMENT EFFECTS
WITH AN APPLICATION TO THE RETURNS TO SCHOOLING
AND MEASUREMENT OF THE EFFECTS OF UNCERTAINTY
DAY COLLEGE CHOICES.

By  $\;$  Pedbo Carneiro, Karsten T. Hansen, and James J. Heckman I

Department of Economics, University of Chicago; Kellogg School of Management, Northwestern University; Department of Economics, University of Chicago and The American Bar Foundation

This article uses factor models to identify and estimate the distributions of content factorial. We carised LEARLE, frameworks to a format tentance efforts extent, carbon factorial pass account for unabserved conditioning variables. Using them models, we can identify all palests and place transmiss of the League models, we can identify all palests and place transmiss of the league that the league of the league transmiss of the league transmissor of the league transmiss of the league transmiss of the leagu

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Carneiro & al. (2003)

## J. Heckman (2008) defines three policy evaluation tasks:

- Evaluating the impact of historical interventions on outcomes including their impact in terms of wellbeing of the treated and the society at large.
- Forecasting the impact of historical interventions implemented in one environment in other environments, including their impact in terms of well-being.
- Forecasting the impacts of interventions never historically experienced to various environments, including their impact on well-being.

#### **Econometrics of policy evaluation**

- ▶ is important
- is complicated
- is multifaceted

#### **Numerous applications**

- labor economics
- development economics
- industrial economics
- health economics

#### **Numerous effects**

- conventional average effects
- policy-relevant average effects
- marginal effects
- distributional effects
- effects on distributions

#### **Numerous estimation strategies**

- instrumental variables
- (quasi-)experimental methods
- matching

## Model

#### **Generalized Roy model**

#### **Potential Outcomes**

$$Y_1 = \mu_1(X) + U_1$$
  $C = \mu_C(Z) + U_C$ 

$$Y_0 = \mu_0(X) + U_0$$

#### Observed Outcomes

$$Y = DY_1 + (1 - D)Y_0$$
  $S = Y_1 - Y_0 - C$ 

#### Choice

Cost

$$S=Y_1-Y_0-C$$

$$D=\mathsf{I}[S>0]$$

## Individual Heterogeneity

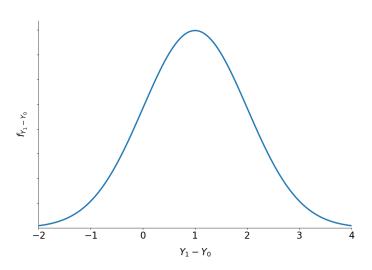
#### Individual-specific Benefit of Treatment

$$Y_1 - Y_0 = (\mu_1(X) - \mu_0(X)) + (U_1 - U_0)$$

#### **Sources of Heterogeneity**

- Difference in observables
- Difference in unobservables
  - Uncertainty
  - Private information

Figure: Distribution of benefits



#### **Observed outcome**

$$Y_i = Y_{0i} + D_i(Y_{1i} - Y_{0i}) = \begin{cases} Y_{1i} & \text{if } D_i = 1 \\ Y_{0i} & \text{if } D_i = 0 \end{cases}$$

#### **Econometric problems**

- ► **Evaluation problem**, we only observe an individual in either the treated or untreated state.
- ➤ **Selection problem**, individuals that select into treatment differ from those that do not.

#### **Essential Heterogeneity**

**Definition:** Individuals select their treatment status based on gains unobservable by the econometrician. More formally,

$$Y_1 - Y_0 \not\perp\!\!\!\perp D | X = x.$$

⇒ consequences for the choice of the estimation strategy

## **Objects of interest**

#### **Useful Notation**

$$P(X, Z) = Pr(D = 1 | X, Z) = F_V(\mu_D(X, Z))$$
  
 $U_D = F_V(V)$ 

#### Figure: First-stage unobservable

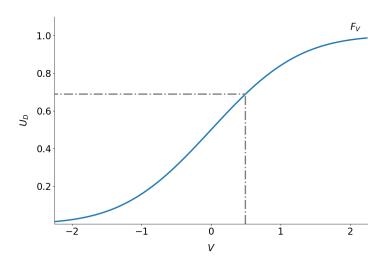


Figure: Support

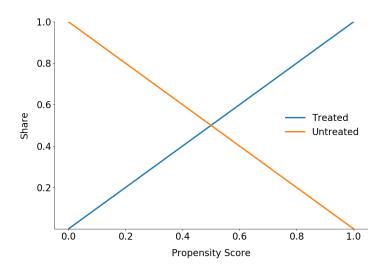
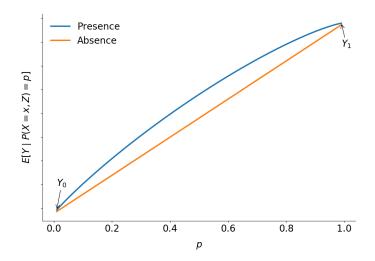


Figure: Distribution of benefits



Figure: Conditional expectation and essential heterogeneity



# Conventional Average Treatment Effects

#### **Conventional Average Treatment Effects**

$$B^{ATE} = E[Y_1 - Y_0]$$
  
 $B^{TT} = E[Y_1 - Y_0 \mid D = 1]$   
 $B^{TUT} = E[Y_1 - Y_0 \mid D = 0]$ 

⇒ correspond to *extreme* policy alternatives

#### **Selection Problem**

$$\begin{split} E[Y \mid D = 1] - E[Y \mid D = 0] &= \underbrace{E[Y_1 - Y_0]}_{B^{ATE}} \\ &+ \underbrace{E[Y_1 - Y_0 \mid D = 1] - E[Y_1 - Y_0]}_{\text{Sorting Gain}} \\ &+ \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection Bias}} \end{split}$$

$$E[Y \mid D = 1] - E[Y \mid D = 0] = \underbrace{E[Y_1 - Y_0 \mid D = 1]}_{B^{TT}} + \underbrace{E[Y_0 \mid D = 1] - E[Y_0 \mid D = 0]}_{\text{Selection Bias}}$$

⇒ the bias depends on the parameter of interest

Figure: Distribution of effects with essential heterogeneity

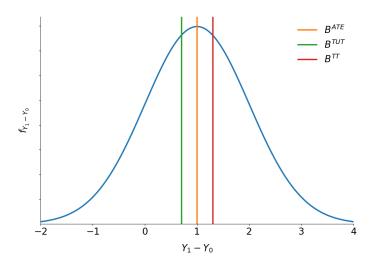
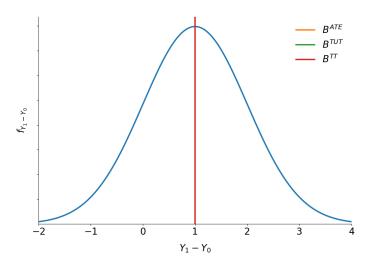


Figure: Distribution of effects without essential heterogeneity



# Policy-Relevant Average Treatment Effects

#### **Observed Outcomes**

$$Y_B = D_B Y_1 + (1 - D_B) Y_0$$
  
 $Y_A = D_A Y_1 + (1 - D_A) Y_0$ 

#### **Effect of Policy**

$$B^{PRTE} = \frac{1}{E[D_A] - E[D_B]} (E[Y_A] - E[Y_B])$$

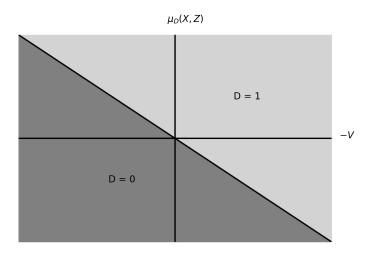
## Marginal Effect of Treatment

#### **Marginal Benefit of Treatment**

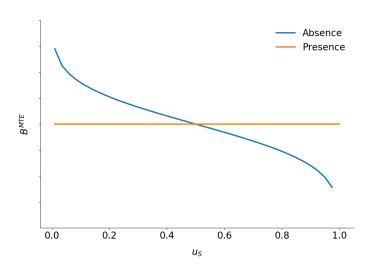
$$B^{MTE}(x, u_D) = E[Y_1 - Y_0 \mid X = x, U_D = u_D]$$

**Intuition:** Mean gross return to treatment for persons at quantile  $u_D$  of the first-stage unobservable V or a willingness to pay for individuals at the margin of indifference.

## Figure: Margin of indifference



## Figure: $B^{MTE}$ and essential heterogeneity



Effects of treatment as weighted averages Parameter  $\Delta_j$ , can be written as a weighted average of the  $B^{MTE}(x, u_D)$ .

$$\Delta_j(x) = \int_0^1 B^{MTE}(x, u_D) \omega^j(x, u_D) du_D,$$

where the weights  $\omega^{j}(x,u_{D})$  are specific to parameter j and integrate to one.

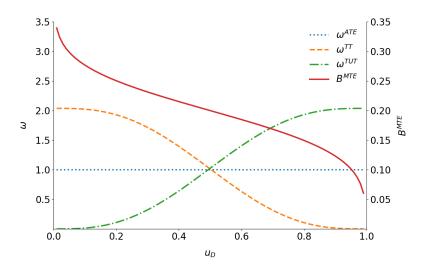
### Weights

$$\omega^{ATE}(x, u_D) = 1$$

$$\omega^{TT}(x, u_D) = \frac{1 - F_{P|X=X}(u_D)}{E[P \mid X = X]}$$

$$\omega^{TUT}(x, u_D) = \frac{F_{P|X=X}(u_D)}{E[1 - P \mid X = X]}$$

Figure: Effects of treatment as weighted averages



# Local Average Treatment Effect

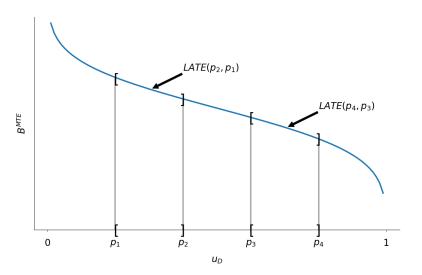
### **Local Average Treatment Effect**

- Local Average Treatment Effect: Average effect for those induced to change treatment because of a change in the instrument.
  - ⇒ instrument-dependent parameter
- Marginal Treatment Effect: Average effect for those individuals with a given unobserved desire to receive treatment.
  - ⇒ deep economic parameter

$$B^{LATE} = \frac{E[Y \mid Z = z] - E[Y \mid Z = z']}{P(z) - P(z')}$$

$$B^{LATE}(x, u_D, u_{D'}) = \frac{1}{u_D - u_{D'}} \int_{u_D}^{u_{D'}} B^{MTE}(x, u) du,$$

Figure: Local average treatment effect



# Distributions of Effects

#### **Distributions of Effects**

- marginal distribution of benefits
- joint distribution of potential outcomes
- joint distribution of benefits and surplus

## Figure: Distribution of benefits



Figure: Distribution of potential outcomes

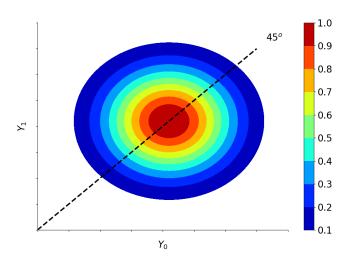
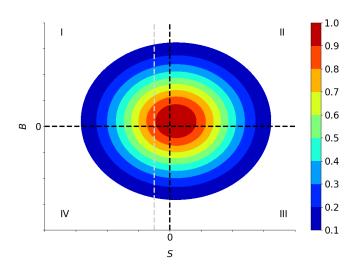


Figure: Distribution of benefits and surplus



# **Conclusion**

# **Appendix**

# References

- Carneiro, P., Hansen, K. T., & Heckman, J. J. (2003). Estimating distributions of treatment effects with an application to the returns to schooling and measurement of the effects of uncertainty on college choice. *International Economic Review*, 44(2), 361–422.
- Carneiro, P., Heckman, J. J., & Vytlacil, E. J. (2011). Estimating marginal returns to education. *American Economic Review*, 101(6), 2754–2781.
- Heckman, J. (2008). Schools, skills, and synapses. *Economic Inquiry*, 46, 289–324.

- Heckman, J. J., & Vytlacil, E. J. (2007a). Econometric evaluation of social programs, part I: Causal effects, structural models and econometric policy evaluation. In J. J. Heckman & E. E. Leamer (Eds.), Handbook of econometrics (Vol. 6B, pp. 4779–4874). Amsterdam, Netherlands: Elsevier Science.
- Heckman, J. J., & Vytlacil, E. J. (2007b). Econometric evaluation of social programs, part II: Using the marginal treatment effect to organize alternative economic estimators to evaluate social programs and to forecast their effects in new environments. In J. J. Heckman & E. E. Leamer (Eds.), Handbook of econometrics (Vol. 6B, pp. 4875–5144). Amsterdam, Netherlands: Elsevier Science.