Economics of Human Capital

Returns to schooling

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Introduction

I heavily draw on the material presented in:

► Heckman, J. J., Lochner, L. J., & Todd, P. E. (2006). Earnings functions, rates of return and treatment effects: The Mincer equation and beyond. In E. A. Hanushek & F. Welch (Eds.), *Handbook of the economics of education* (1st ed., Vol. 1, pp. 307–458). Amsterdam, Netherlands: North-Holland Publishing Company.

Importance of returns

- explain wage inequality within countries
- explain growth differentials across countries
- assess schooling investment on individual level
- evaluate public policies to foster educational attainment

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Return concepts

- Mincer returns
- internal rate of return
- true rate of return

Mathematical models

Lecture

All models are designed to shed light on the process of schooling decisions.

- Compensating differences
- Accounting-identity
- Option value

Economic models facilitate experiential learning.

- What question are they designed to address?
- What are the underlying economic mechanisms?
- How robust are the conclusions?
- What is missing?
- **>** . . .

Figure: Modeling process

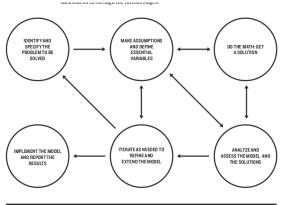


FIGURE 1.2: THE MATH MODELING PROCESS

Mincer returns

Mincer Equation

$$\ln Y(s,x) = \alpha + \rho_s s + \beta_0 x + \beta_1 x^2 + \epsilon$$

 \Rightarrow How to interpret the *Mincer Coefficient* ρ_s ?

Conceptual Frameworks

- compensating differences
- accounting-identity

Compensating Differences Model

Let Y(s) represent the annual earnings of an individual with s years of education, assumed to be constant over his lifetime. Let r be an externally determined interest rate and T the length of working life, assumed not to depend on s. The present value of earnings associated with schooling level s is

$$V(s) = Y(s) \int_{s}^{T} e^{-rt} dt = \frac{Y(s)}{r} (e^{-rs} - e^{-rT}).$$

Figure: Earnings

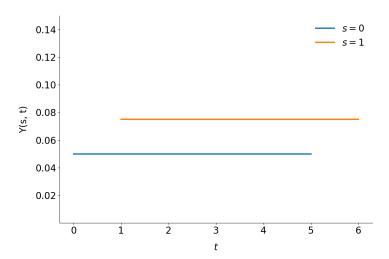
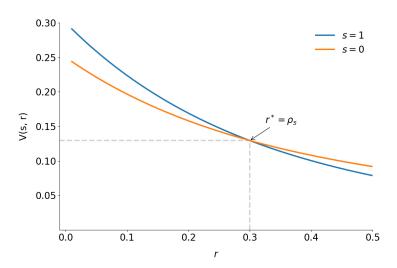


Figure: Value



Equilibrium across heterogeneous schooling levels requires that individuals be indifferent between schooling choices, with allocations being driven by demand conditions. Equating earnings streams across schooling levels and taking logs yields

$$\ln Y(s) = \ln Y(0) + rs + \ln \left(\frac{1-e^{-rs}}{1-e^{-r(T-s)}}\right).$$

 $\Rightarrow \rho_s$ equals the market interest rate and the internal rate of return to schooling by construction.

Model features

- identical abilities and opportunities
- no credit constraints
- perfect certainty
- no direct cost of schooling
- no nonpecuniary benefits of school and work

Accounting-Identity Model

Model ingredients

 P_t potential earnings at t $C_t = k_t P_t$ investment cost of training at t ρ_t average return to investment at t

$$P_t \equiv P_{t-1}(1 + k_{t-1}\rho_{t-1}) \equiv \prod_{j=0}^{t-1} (1 + \rho_j k_j) P_0$$

Formal schooling is defined as years spent in full-time investment $(k_t=1)$, which is assumed to take place at the beginning of life and to yield a rate of return ρ_s that is constant across all years of schooling.

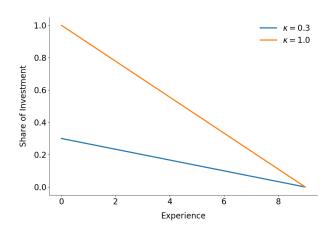
$$\ln P_{t} \equiv \ln P_{0} + s \ln (1 + \rho_{s}) + \sum_{j=s}^{t-1} \ln (1 + \rho_{0} k_{j})$$

$$\approx \ln P_{0} + s \rho_{s} + \rho_{0} \sum_{j=s}^{t-1} k_{j}$$

Mincer (1974) assumes a linearly declining rate of postschool investment:

$$k_{s+x} = \kappa (1 - x/T)$$
, where $x = t - s$

Figure: Post-School Investment



The derivations draws on the following results for arithmetic series.

$$\sum_{i=0}^{n} i = \sum_{i=1}^{n} i = \frac{n(n+1)}{2}$$

$$\ln P_{X+S} \approx \ln P_0 + S\rho_S + \underbrace{\left(\rho_0 \kappa + \frac{\rho_0 \kappa}{2T}\right) x - \frac{\rho_0 \kappa}{2T} x^2}_{(1)}$$

You can derive (1) using the previous results.

Accounting for the difference in potential and observed earnings:

$$\ln Y(s, x) \approx \ln P_{x+s} - \kappa (1 - x/T)$$

$$= [\ln P_0 - \kappa] + \rho_s s + \left(\rho_0 \kappa + \frac{\rho_0 \kappa}{2T} + \frac{\kappa}{T}\right) x - \frac{\rho_0 \kappa}{2T} x^2$$

 $\Rightarrow \rho_s$ is the average earnings increase with schooling

Standard Mincer Equation

$$\ln Y(s,x) = \alpha + \rho_s s + \beta_0 x + \beta_1 x^2,$$

where

$$\alpha = \ln P_0 - \kappa$$

$$\beta_0 = \left(\rho_0 \kappa + \frac{\rho_0 \kappa}{2T} + \frac{\kappa}{T}\right)$$

$$\beta_1 = -\frac{\rho_0 \kappa}{2T}$$

What about heterogeneous returns?

Random Coefficient Version

$$\ln Y(s_i,x_i) = \alpha_i + \rho_{si}s_i + \beta_{0i}x_i + \beta_{1i}x_i^2$$

and let

$$ar{lpha} = \mathsf{E}[lpha_i] \qquad ar{eta}_\mathsf{S} = \mathsf{E}[eta_{\mathit{S}i}] \ ar{eta}_\mathsf{0} = \mathsf{E}[eta_{0i}] \qquad ar{eta}_\mathsf{1} = \mathsf{E}[eta_{1i}]$$

Dropping individual subscripts ...

$$\ln Y(s,x) = \bar{\alpha} + \bar{\rho}_s s + \bar{\beta}_0 x + \bar{\beta}_1 x^2 + \underbrace{\left[(\alpha - \bar{\alpha}) + (\rho_s - \bar{\rho}_s) s + (\beta_0 - \bar{\beta}_0) x + (\beta_1 - \bar{\beta}_1) x^2 \right]}_{\epsilon}$$

⇒ If the schooling decision is determined by individual returns, then we are back in the case of a correlated random coefficient model (Heckman, Urzua, & Vytlacil, 2006).

Table 2: Estimated Coefficients from Mincer Log Earnings Regression for Men

| | | Whites | | Blacks | |
|------|--------------------|-------------|------------|-------------|-----------|
| | | Coefficient | Std. Error | Coefficient | Std. Erro |
| 1940 | Intercept | 4.4771 | 0.0096 | 4.6711 | 0.0298 |
| | Education | 0.1250 | 0.0007 | 0.0871 | 0.0022 |
| | Experience | 0.0904 | 0.0005 | 0.0646 | 0.0018 |
| | Experience-Squared | -0.0013 | 0.0000 | -0.0009 | 0.0000 |
| 1950 | Intercept | 5.3120 | 0.0132 | 5.0716 | 0.0409 |
| | Education | 0.1058 | 0.0009 | 0.0998 | 0.0030 |
| | Experience | 0.1074 | 0.0006 | 0.0933 | 0.0023 |
| | Experience-Squared | -0.0017 | 0.0000 | -0.0014 | 0.0000 |
| 1960 | Intercept | 5.6478 | 0.0066 | 5.4107 | 0.0220 |
| | Education | 0.1152 | 0.0005 | 0.1034 | 0.0016 |
| | Experience | 0.1156 | 0.0003 | 0.1035 | 0.0011 |
| | Experience-Squared | -0.0018 | 0.0000 | -0.0016 | 0.0000 |
| 1970 | Intercept | 5.9113 | 0.0045 | 5.8938 | 0.0155 |
| | Education | 0.1179 | 0.0003 | 0.1100 | 0.0012 |
| | Experience | 0.1323 | 0.0002 | 0.1074 | 0.0007 |
| | Experience-Squared | -0.0022 | 0.0000 | -0.0016 | 0.0000 |
| 1980 | Intercept | 6.8913 | 0.0030 | 6.4448 | 0.0120 |
| | Education | 0.1023 | 0.0002 | 0.1176 | 0.0009 |
| | Experience | 0.1255 | 0.0001 | 0.1075 | 0.0005 |
| | Experience-Squared | -0.0022 | 0.0000 | -0.0016 | 0.0000 |
| 1990 | Intercept | 6.8912 | 0.0034 | 6.3474 | 0.0144 |
| | Education | 0.1292 | 0.0002 | 0.1524 | 0.0011 |
| | Experience | 0.1301 | 0.0001 | 0.1109 | 0.0006 |
| | Experience-Squared | -0.0023 | 0.0000 | -0.0017 | 0.0000 |

Notes: Data taken from 1940-90 Decennial Censuses. See Appendix B for data description.

We can analyze this model in a Jupyter Noteboook. Visit

http://bit.ly/2kAtcyg

for the implementation.

Implications

Log-earnings profiles are parallel across schooling levels.

$$\frac{\partial \ln Y(s,x)}{\partial s \partial x} = 0$$

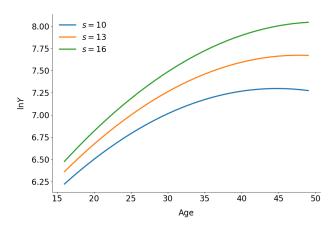
Log-earnings age profiles diverge with age across schooling levels.

$$\frac{\partial \ln Y(s,x)}{\partial s \partial t} = \frac{\rho_0 \kappa}{T} > 0$$

Figure: Experience profiles



Figure: Age profiles



► The variance of earnings over the life cycle has a U-shaped pattern.

Derivation for minimizing variance

$$\ln Y(s, x) = \ln P_{s+x} + \ln (1 - k_{s+x})$$

$$\approx \ln P_s + \rho_0 \sum_{j=0}^{x-1} k_{s+j} - k_{s+x}$$

Further, using the assumption of linearly declining investment yields

$$\ln Y(s,x) \approx \ln P_s + \kappa \left(\rho_0 \sum_{j=0}^{x-1} (1-j/T) - (1-x/T) \right)$$

Assuming only initial earnings potential P_s and investment levels κ vary in the population, the variance of log earnings is given by

$$\begin{aligned} \text{var}(\ln Y(s,x)) &= \text{var}(\ln P_s) \\ &+ \left(\rho_0 \sum_{j=0}^{x-1} (1-j/T) - (1-x/T)\right)^2 \text{var}(\kappa) \\ &+ 2 \left(\rho_0 \sum_{j=0}^{x-1} (1-j/T) - (1-x/T)\right) \text{cov}(\ln P_s,k). \end{aligned}$$

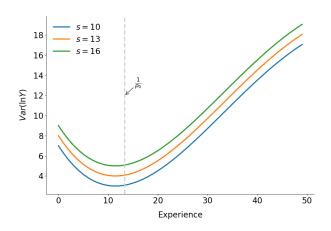
If κ and $\ln P_s$ are uncorrelated, then earnings are minimized (and equal to $Var(\ln P_s)$) when

$$\rho_0 \sum_{j=0}^{x-1} (1-j/T) = 1-x/T, or$$

$$\rho_0\left(x-\frac{x(x-1)}{2T}\right)=(1-x/T).$$

Clearly, $\lim_{T\to\infty} x^* = \frac{1}{\rho_0}$, so the variance minimizing age is $\frac{1}{\rho_0}$ when the work-life is long.

Figure: Variance profiles



Empirical Evidence

Figure 1a: Experience-Earnings Profiles, 1940-1960





Table 1: Tests of Parallelism in Log Earnings Experience Profiles for Men

| | | Estimated Difference Between College and High | | | | | | | | |
|--------|------------|---|---------|-----------|------------|------------|------------|--|--|--|
| | Experience | Schoo | l Log E | arnings a | t Differen | t Experier | nce Levels | | | |
| Sample | Level | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | | | |
| Whites | 10 | 0.54 | 0.30 | 0.46 | 0.41 | 0.37 | 0.59 | | | |
| | 20 | 0.40 | 0.40 | 0.43 | 0.49 | 0.45 | 0.54 | | | |
| | 30 | 0.54 | 0.27 | 0.46 | 0.48 | 0.43 | 0.52 | | | |
| | 40 | 0.58 | 0.21 | 0.50 | 0.45 | 0.27 | 0.30 | | | |
| | p-value | 0.32 | 0.70 | < 0.001 | < 0.001 | < 0.001 | < 0.001 | | | |
| Blacks | 10 | 0.20 | 0.58 | 0.48 | 0.38 | 0.70 | 0.77 | | | |
| | 20 | 0.38 | 0.05 | 0.25 | 0.22 | 0.48 | 0.69 | | | |
| | 30 | -0.11 | 0.24 | 0.08 | 0.33 | 0.36 | 0.53 | | | |
| | 40 | -0.20 | 0.00 | 0.73 | 0.26 | 0.22 | -0.04 | | | |
| | p-value | 0.46 | 0.55 | 0.58 | 0.91 | < 0.001 | < 0.001 | | | |

Notes: Data taken from 1940-90 Decennial Censuses without adjustment for inflation. Because there are very few blacks in the 1940 and 1950 samples with college degrees, especially at higher experience levels, the test results for blacks in those years refer to a test of the difference between earnings for high school graduates and persons with 8 years of education. See Appendix B for data description. See Appendix C for the formulae used for the test statistics.

Figure 2: Age-Earnings Profiles, 1940,1960,1980

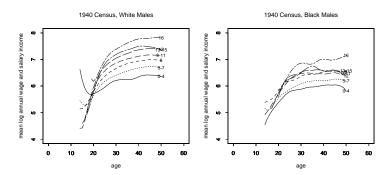




Figure 3: Experience-Variance Log Earnings





In the end, (Heckman, Lochner, & Todd, 2006) conclude:

In common usage, the coefficient on schooling in a regression of log earnings on years of schooling is often called a rate of return. In fact, it is a price of schooling from a hedonic market wage equation. It is a growth rate of market earnings with years of schooling and not an internal rate of return measure, except under stringent conditions which we specify, test and reject in this chapter.

Table 2 Estimated coefficients from Mincer log earnings regression for men

| | Whites | | Blacks | | | |
|----------------|-------------|------------|-------------|------------|--|--|
| | Coefficient | Std. Error | Coefficient | Std. Error | | |
| cept | 4.4771 | 0.0096 | 4.6711 | 0.0298 | | |
| ation | 0.1250 | 0.0007 | 0.0871 | 0.0022 | | |
| rience | 0.0904 | 0.0005 | 0.0646 | 0.0018 | | |
| rience-squared | -0.0013 | 0.0000 | -0.0009 | 0.0000 | | |

| 1940 | Intercept | 4.4771 | 0.0096 | 4.6711 | 0.0298 |
|------|--------------------|---------|--------|---------|--------|
| 1510 | Education | 0.1250 | 0.0007 | 0.0871 | 0.0022 |
| | Experience | 0.0904 | 0.0005 | 0.0646 | 0.0018 |
| | Experience-squared | -0.0013 | 0.0000 | -0.0009 | 0.0000 |
| 1950 | Intercept | 5.3120 | 0.0132 | 5.0716 | 0.0409 |
| | Education | 0.1058 | 0.0009 | 0.0998 | 0.0030 |
| | Experience | 0.1074 | 0.0006 | 0.0933 | 0.0023 |
| | Experience-squared | -0.0017 | 0.0000 | -0.0014 | 0.0000 |

Internal rate of returns

Income Maximization under Perfect Certainty

- s schooling level
- x experience level
- Y(s,x) wage income
 - T(s) last age of earnings
 - v tuition and psychic cost of schooling
 - au proportional tax rate
 - r before-tax interest rate

Present Discounted Value of Lifetime Earnings

$$V(s) = \int_0^{T(s)-s} (1-\tau)e^{-(1-\tau)r(x+s)}Y(s,x)dx$$
$$-\int_0^s ve^{-(1-\tau)rz}dz$$

First-Order Condition

$$[T'(s)-1]e^{-(1-\tau)r(T(s)-s)}Y(s,T(s)-s)$$

$$-(1-\tau)r\int_{0}^{T(s)-s}e^{-(1-\tau)rx}Y(s,x)dx$$

$$+\int_{0}^{T(s)-s}e^{-(1-\tau)rx}\frac{\partial Y(s,x)}{\partial s}dx$$

$$-\frac{v}{1-\tau}=0$$

Rearranging and defining $\tilde{r} = (1 - \tau)r$...

$$\tilde{r} = \frac{[T'(s) - 1]e^{-\tilde{r}(T(s) - s)}Y(s, T(s) - s)}{\int_0^{T(s) - s} e^{-\tilde{r}x}Y(s, x)dx}$$
(1)

$$+\frac{\int_0^{T(s)-s} e^{-\tilde{r}x} \left[\frac{\partial Y(s,x)}{\partial s}\right] dx}{\int_0^{T(s)-s} e^{-\tilde{r}x} Y(s,x) dx}$$
 (2)

$$-\frac{\frac{v}{1-\tau}}{\int_0^{T(s)-s} e^{-\tilde{r}x} Y(s,x) dx}$$
 (3)

Interpretation

- ▶ (1) ... the change in the present value of earnings due to a change in working-life with additional schooling
- (2) ... weighted average effect of schooling on log earnings by experience
- ▶ (3) ... tuition and psychic costs

All components are expressed as a fraction of the present value of earnings measured at age s

Getting back to Mincer

no tuition and psychic costs of schooling

$$\Rightarrow v = 0$$

no loss of working life from schooling

$$\Rightarrow T'(s) = 1$$

 multiplicative separability between schooling and experience component of earnings

$$\Rightarrow$$
 $Y(s, x) = \mu(s)\psi(x)$

$$\tilde{r} = \frac{\mu'(s)}{\mu(s)} \quad \forall \quad s$$

Thus, wage growth must be log linear in schooling and $\mu(s)=\mu(0)e^{\rho_s s}$ and $\tilde{r}=\rho_s$.

(Heckman, Lochner, & Todd, 2006) thus establish ...

After allowing for taxes, tuition, variable length of working life, and a flexible relationship between earnings, schooling and experience, the coefficient on years of schooling in a log earnings regression need no longer equal the internal rate of return.

Structural Approach for the IRR

The internal rate of return for schooling level s_1 versus s_2 , $r(s_1, s_2)$ solves ...

$$\int_{0}^{T(s_{1})-s_{1}} (1-\tau)e^{-r(x+s_{1})}Y(s_{1},x)dx - \int_{0}^{s_{1}} ve^{-rz}dz$$

$$= \int_{0}^{T(s_{2})-s_{2}} (1-\tau)e^{-r(x+s_{2})}Y(s_{2},x)dx - \int_{0}^{s_{2}} ve^{-rz}dz$$

Back to Mincer

no taxes and no direct or psychic costs of schooling

$$\Rightarrow$$
 $v = 0$ and $\tau = 0$

$$\int_0^{T(s_1)-s_1} e^{-r(x+s_1)} Y(s_1,x) dx = \int_0^{T(s_2)-s_2} e^{-r(x+s_2)} Y(s_2,x) dx$$

equal work-lives irrespective of years of schooling

$$\Rightarrow T = T(s_1) - s_1 = T(s_2) - s_2$$

$$\int_0^T e^{-r(x+s_1)} Y(s_1, x) dx = \int_0^T e^{-r(x+s_2)} Y(s_2, x) dx$$

parallelism in experience across schooling categories

$$\Rightarrow$$
 Y(s, x) = μ (s) ψ (x)

$$\int_0^T e^{-r(x+s_1)} \mu(s) \psi(x) dx = \int_0^T e^{-r(x+s_2)} \mu(s) \psi(x) dx$$

linearity of log earnings in schooling

$$\Rightarrow \mu(s) = \mu(0)e^{\rho_s s}$$

$$\int_0^T e^{-r(x+s_1)} \mu(0) e^{\rho_s s_1} \psi(x) dx = \int_0^T e^{-r(x+s_2)} \mu(0) e^{\rho_s s_2} \psi(x) dx$$

After some further rearranging ...

$$e^{(\rho_s-r)s_1} = e^{(\rho_s-r)s_2}$$
$$\Rightarrow \rho_s = r$$

Empirical Evidence

Table 3a: Internal Rates of Return for White Men: Earnings Function Assumptions (Specifications Assume Work Lives of 47 Years)

| | Schooling Comparisons | | | | | |
|--------------------------------------|-----------------------|------|-------|-------|-------|-------|
| | 6-8 | 8-10 | 10-12 | 12-14 | 12-16 | 14-16 |
| 1940 | | | | | | |
| Mincer Specification | 13 | 13 | 13 | 13 | 13 | 13 |
| Relax Linearity in S | 16 | 14 | 15 | 10 | 15 | 21 |
| Relax Linearity in S & Quad. in Exp. | 16 | 14 | 17 | 10 | 15 | 20 |
| Relax Lin. in S & Parallelism | 12 | 14 | 24 | 11 | 18 | 26 |
| 1950 | | | | | | |
| Mincer Specification | 11 | 11 | 11 | 11 | 11 | 11 |
| Relax Linearity in S | 13 | 13 | 18 | 0 | 8 | 16 |
| Relax Linearity in S & Quad. in Exp. | 14 | 12 | 16 | 3 | 8 | 14 |
| Relax Linearity in S & Parallelism | 26 | 28 | 28 | 3 | 8 | 19 |
| 1960 | | | | | | |
| Mincer Specification | 12 | 12 | 12 | 12 | 12 | 12 |
| Relax Linearity in S | 9 | 7 | 22 | 6 | 13 | 21 |
| Relax Linearity in S & Quad. in Exp. | 10 | 9 | 17 | 8 | 12 | 17 |
| Relax Linearity in S & Parallelism | 23 | 29 | 33 | 7 | 13 | 25 |
| 1970 | | | | | | |
| Mincer Specification | 13 | 13 | 13 | 13 | 13 | 13 |
| Relax Linearity in S | 2 | 3 | 30 | 6 | 13 | 20 |
| Relax Linearity in S & Quad. in Exp. | 5 | 7 | 20 | 10 | 13 | 17 |
| Relax Linearity in S & Parallelism | 17 | 29 | 33 | 7 | 13 | 24 |
| 1980 | | | | | | |
| Mincer Specification | 11 | 11 | 11 | 11 | 11 | 11 |
| Relax Linearity in S | 3 | -11 | 36 | 5 | 11 | 18 |
| Relax Linearity in S & Quad. in Exp. | 4 | -4 | 28 | 6 | 11 | 16 |
| Relax Linearity in S & Parallelism | 16 | 66 | 45 | 5 | 11 | 21 |
| 1990 | | | | | | |
| Mincer Specification | 14 | 14 | 14 | 14 | 14 | 14 |
| Relax Linearity in S | -7 | -7 | 39 | 7 | 15 | 24 |
| Relax Linearity in S & Quad. in Exp. | -3 | -3 | 30 | 10 | 15 | 20 |

Table 3b: Internal Rates of Return for Black Men: Earnings Function Assumptions (Specifications Assume Work Lives of 47 Years)

| | | Schooling Comparisons | | | | |
|--------------------------------------|-----|-----------------------|-------|-------|-------|-----|
| | 6-8 | 8-10 | 10-12 | 12-14 | 12-16 | 14- |
| 1940 | | | | | | |
| Mincer Specification | 9 | 9 | 9 | 9 | 9 | 9 |
| Relax Linearity in S | 18 | 7 | 5 | 3 | 11 | 18 |
| Relax Linearity in S & Quad. in Exp. | 18 | 8 | 6 | 2 | 10 | 19 |
| Relax Linearity in S & Parallelism | 11 | 0 | 10 | 5 | 12 | 20 |
| 1950 | | | | | | |
| Mincer Specification | 10 | 10 | 10 | 10 | 10 | 10 |
| Relax Linearity in S | 16 | 14 | 18 | -2 | 4 | 9 |
| Relax Linearity in S & Quad. in Exp. | 16 | 14 | 18 | 0 | 3 | 6 |
| Relax Linearity in S & Parallelism | 35 | 15 | 48 | -3 | 6 | 34 |
| 1960 | | | | | | |
| Mincer Specification | 11 | 11 | 11 | 11 | 11 | 11 |
| Relax Linearity in S | 13 | 12 | 18 | 5 | 8 | 11 |
| Relax Linearity in S & Quad. in Exp. | 13 | 11 | 18 | 5 | 7 | 10 |
| Relax Linearity in S & Parallelism | 22 | 15 | 38 | 5 | 11 | 25 |
| 1970 | | | | | | |
| Mincer Specification | 12 | 12 | 12 | 12 | 12 | 12 |
| Relax Linearity in S | 5 | 11 | 30 | 7 | 10 | 14 |
| Relax Linearity in S & Quad. in Exp. | 6 | 11 | 24 | 10 | 11 | 12 |
| Relax Linearity in S & Parallelism | 15 | 27 | 44 | 9 | 14 | 23 |
| 1980 | | | | | | |
| Mincer Specification | 12 | 12 | 12 | 12 | 12 | 12 |
| Relax Linearity in S | -4 | 1 | 35 | 10 | 15 | 19 |
| Relax Linearity in S & Quad. in Exp. | -4 | 6 | 29 | 11 | 14 | 17 |
| Relax Linearity in S & Parallelism | 10 | 44 | 48 | 8 | 16 | 31 |
| 1990 | | | | | | |
| Mincer Specification | 16 | 16 | 16 | 16 | 16 | 16 |
| Relax Linearity in S | -5 | -5 | 41 | 15 | 20 | 25 |
| Relax Linearity in S & Quad. in Exp. | -3 | -3 | 35 | 17 | 19 | 22 |

Table 4: Internal Rates of Return for White & Black Men: Accounting for Taxes and Tuition (General Non-Parametric Specification Assuming Work Lives of 47 Years)

| | | Schooling Comparisons | | | | | |
|-------|----------------------------------|-----------------------|---------|-------------|------------|---------|---------|
| | | Whites Blacks | | | | | |
| | | 12-14 | 12 - 16 | 14-16 | 12-14 | 12-16 | 14-16 |
| 1940 | No Taxes or Tuition | 11 | 18 | 26 | 5 | 12 | 20 |
| | Including Tuition Costs | 9 | 15 | 21 | 4 | 10 | 16 |
| | Including Tuition & Flat Taxes | 8 | 15 | 21 | 4 | 9 | 16 |
| | Including Tuition & Prog. Taxes | 8 | 15 | 21 | 4 | 10 | 16 |
| 1950 | No Taxes or Tuition | 3 | 8 | 19 | -3 | 6 | 34 |
| | Including Tuition Costs | 3 | 8 | 16 | -3 | 5 | 25 |
| | Including Tuition & Flat Taxes | 3 | 8 | 16 | -3 | 5 | 24 |
| | Including Tuition & Prog. Taxes | 3 | 7 | 15 | -3 | 5 | 21 |
| 1960 | No Taxes or Tuition | 7 | 13 | 25 | 5 | 11 | 25 |
| | Including Tuition Costs | 6 | 11 | 21 | 5 | 9 | 18 |
| | Including Tuition & Flat Taxes | 6 | 11 | 20 | 4 | 8 | 17 |
| | Including Tuition & Prog. Taxes | 6 | 10 | 19 | 4 | 8 | 15 |
| 1970 | No Taxes or Tuition | 7 | 13 | 24 | 9 | 14 | 23 |
| | Including Tuition Costs | 6 | 12 | 20 | 7 | 12 | 18 |
| | Including Tuition & Flat Taxes | 6 | 11 | 20 | 7 | 11 | 17 |
| | Including Tuition & Prog. Taxes | 5 | 10 | 18 | 7 | 10 | 16 |
| 1980 | No Taxes or Tuition | 5 | 11 | 21 | 8 | 16 | 31 |
| | Including Tuition Costs | 4 | 10 | 18 | 7 | 13 | 24 |
| | Including Tuition & Flat Taxes | 4 | 9 | 17 | 6 | 12 | 21 |
| | Including Tuition & Prog. Taxes | 4 | 8 | 15 | 6 | 11 | 20 |
| 1990 | No Taxes or Tuition | 10 | 16 | 26 | 18 | 25 | 35 |
| | Including Tuition Costs | 9 | 14 | 20 | 14 | 18 | 25 |
| | Including Tuition & Flat Taxes | 8 | 13 | 19 | 13 | 17 | 22 |
| | Including Tuition & Prog. Taxes | 8 | 12 | 18 | 13 | 17 | 22 |
| Notes | : Data taken from 1940-90 Decenn | ial Cens | uses. S | ee discussi | on in text | and App | endix B |

Notes: Data taken from 1940-90 Decennial Censuses. See discussion in text and Appendix F for a description of tuition and tax amounts.

Figure 4a: Average College Tuition Paid (in 2000 dollars)



Figure 4b: Marginal Tax Rates (from Barro & Sahasakul, 1983, Mulligan & Marion, 2000)



Figure 5: IRR for High School Completion (White and Black Men)



Figure 6: IRR for College Completion (White and Black Men)

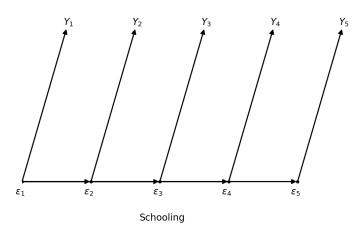


True rate of return

Suppose their is uncertainty about net earnings conditional on *s* and actual lifetime earnings for someone with *s* years of schooling are:

$$Y_s = \underbrace{\left[\sum_{x=0}^T (1+r)^{-1} Y(s,x)\right]}_{\widetilde{Y}_s} \epsilon_s$$

Figure: Model structure



The decision problem for a person with *s* years of schooling given the sequential revelation of information is to complete another year of schooling if

$$Y_s \leq \frac{E_s(V_{s+1})}{1+r}.$$

So the value of schooling level s, V_s , is

$$V_{s} = \max \left\{ Y_{s}, rac{E_{s}(V_{s+1})}{1+r}
ight\}$$

for $s \leq \bar{S}$. At the maximum schooling level, \bar{S} , after all information is revealed, we obtain $V_{\bar{S}} = Y_{\bar{S}} = \bar{Y}_{\bar{S}} \epsilon_{\bar{S}}$.

The endogenously determined probability of going on from school level s to s+1 is

$$p_{s+1,s} = \Pr\left(\epsilon_s \leq \frac{E_s(V_{s+1})}{(1+r)\bar{Y}_s}\right),$$

where $E_s(V_{s+1})$ may depend on ϵ_s because it enters the agent's information set.

Thus, the expected value of schooling level s as perceived at current schooling s-1 is:

$$E_{s-1}(V_s) = \underbrace{(1 - p_{s+1,s})\bar{Y}_s E_{s-1}\left(\epsilon \mid \epsilon \ge \frac{E_s(V_{s+1})}{(1+r)\bar{Y}_s}\right)}_{\text{direct return}} + \underbrace{p_{s+1,s}\left(\frac{E_{s-1}(V_{s+1})}{1+r}\right)}_{\text{option value}}.$$

Objects of interest

Option value

$$O_{s,s-1} = \mathsf{E}_{s-1} [V_s - Y_s]$$

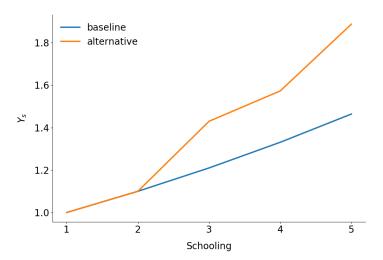
True rate of return

$$R_{s,s-1} = \frac{\mathsf{E}_{s-1} \left[V_s \right] - Y_{s-1}}{Y_{s-1}}$$

Model specification

$$\log(\epsilon_s) \sim \mathbb{N}(0, \sigma)$$
 $r = 0.1$ $Y_{s+1} = (1 + \rho_{s+1})Y_s$ $\sigma = 0.1$

Figure: Scenarios



We can analyze this model in a Jupyter Noteboook. Visit

http://bit.ly/2skwwli

for the implementation.

Figure: Option values and uncertainty

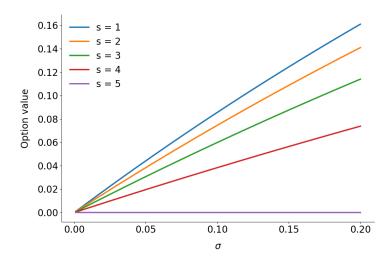


Figure: Option values and sheepskin effects

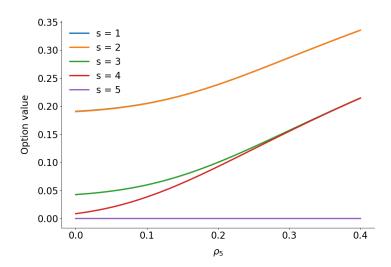
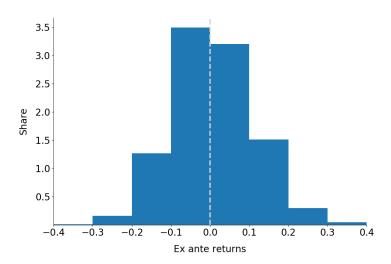


Figure: Returns



Conclusion

Appendix

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