

# Returns to Education

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I heavily draw on the material presented in:

- ▶ Heckman, J. J., Lochner, L. J., and Todd, P. E. (2006a). Earnings functions, rates of return and treatment effects: The mincer equation and beyond. In Hanushek, E. A. and Welch, F., editors, *Handbook of the Economics of Education*, volume 1, pages 307–458. North-Holland Publishing Company

We will look at two papers that explore reduced-form estimations of the returns to education .

- ▶ Carneiro, P. and Heckman, J. J. (2002). The evidence on credit constraints in post-secondary schooling. *The Economic Journal*, 112(482):705–734
- ▶ Bhuller, M., Mogstad, M., and Salvanes, K. G. (2017). Life cycle earnings, education premiums and internal rates of return. *Journal of Labor Economics*, 35(4):993–1030

We will look at two papers that explore structural estimations of the returns to education .

- ▶ Cunha, F., Heckman, J. J., and Navarro, S. (2005). Separating uncertainty from heterogeneity in life cycle earnings. *Oxford Economic Papers*, 57(2):191–261
- ▶ Eisenhauer, P., Heckman, J. J., and Mosso, S. (2015). Estimation of dynamic discrete choice models by maximum likelihood and the simulated method of moments. *International Economic Review*, 56(2):331–357

Why are returns to education important?

- ▶ help explain wage inequality
- ▶ judge relative profitability of investment in education?
- ▶ ...

## Mincer Equation

$$Y(s, x) = \alpha + \rho_s s + \beta_0 x + \beta_1 x^2 + \epsilon$$

### Conceptual Frameworks

- ▶ compensating differences model
- ▶ accounting-identity model

## *Compensating Differences Model*

$$V(s) = Y(s) \int_s^T e^{-rt} dt = \frac{Y(s)}{r} (e^{-rs} - e^{-rT})$$



Equalizing present value of earnings across schooling levels:

$$\ln Y(s) = \ln Y(0) + rs + \ln \left( \frac{1 - e^{-rs}}{1 - e^{-r(T-s)}} \right)$$

$\Rightarrow \rho_s$  equals the market interest rate

## Model Features:

- ▶ identical abilities and opportunities
- ▶ no credit constraints
- ▶ perfect certainty
- ▶ no direct cost of schooling
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## *Accounting-Identity Model*

$$P_t \equiv P_{t-1}(1 + k_{t-1}\rho_{t-1}) \equiv \prod_{j=0}^{t-1} (1 + \rho_j k_j) P_0$$

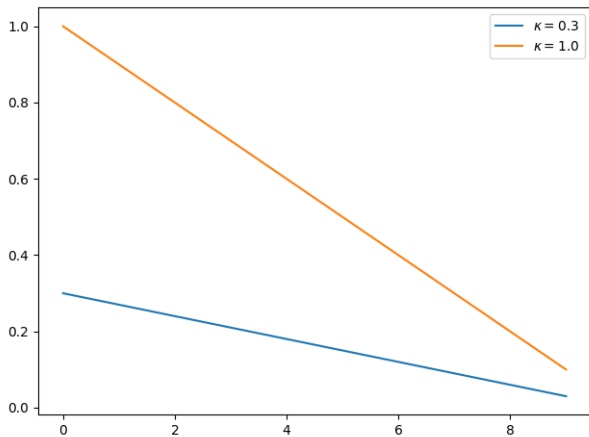
$$\ln P_t \equiv \ln P_0 + s \ln(1 + \rho_s) + \sum_{j=2}^{t-1} \ln(1 + \rho_0 k_j)$$

$$\approx \ln P_0 + s\rho_s + \rho_0 \sum_{j=s}^{t-1} k_j$$

Assuming linearly declining rate of post-school investment:

$$k_{s+x} = \kappa \left(1 - \frac{x}{T}\right), \text{ where } x = t - s$$

Figure: Post-School Investment



$$\ln P_{x+s} \approx \ln P_0 + s\rho_s + \left(\rho_0\kappa + \frac{\rho_0\kappa}{2T}\right)x - \frac{\rho_0\kappa}{2T}x^2$$

Accounting for the difference in potential and observed earnings:

$$\begin{aligned}\ln Y(s, x) &= \ln P_{x+s} - \kappa \left(1 - \frac{x}{T}\right) \\ &= [\ln P_0 - \kappa] + \rho_s s + \left(\rho_0\kappa + \frac{\rho_0\kappa}{2T} + \frac{\kappa}{T}\right)x - \frac{\rho_0\kappa}{2T}x^2\end{aligned}$$

$\Rightarrow \rho_s$  is the average earnings increase with schooling



## Standard Mincer Equation

$$\ln Y(s, x) = \alpha + \rho_s s + \beta_0 x + \beta_1 x^2,$$

where

$$\alpha = \ln P_0 - \kappa$$

$$\beta_0 = \left( \rho_0 \kappa + \frac{\rho_0 \kappa}{2T} + \frac{\kappa}{T} \right)$$

$$\beta_1 = \frac{\rho_0 \kappa}{2T}$$

## Random Coefficient Version

$$\ln Y(s_i, x_i) = \alpha_i + \rho_{si}s_i + \beta_{0i}x_i + \beta_{1i}x_i^2$$

and let

$$\begin{aligned}\bar{\alpha} &= E[\alpha_i] & \bar{\rho}_s &= E[\rho_{si}] \\ \bar{\beta}_0 &= E[\beta_{0i}] & \bar{\beta}_1 &= E[\beta_{1i}]\end{aligned}$$

Dropping individual subscripts ...

$$\ln Y(s, x) = \bar{\alpha} + \bar{\rho}_s s + \bar{\beta}_0 x + \bar{\beta}_1 x^2 \\ + \underbrace{[(\alpha - \bar{\alpha}) + (\rho_s - \bar{\rho}_s)s + (\beta_0 - \bar{\beta}_0)x + (\beta_1 - \bar{\beta}_1)x^2]}_{\epsilon}$$

⇒ If the schooling decision is determined by individual returns, then we are back in the case of a correlated random coefficient model (Heckman et al., 2006b).

Table 2: Estimated Coefficients from Mincer Log Earnings Regression for Men

		Whites		Blacks	
		Coefficient	Std. Error	Coefficient	Std. Error
1940	Intercept	4.4771	0.0096	4.6711	0.0298
	Education	0.1250	0.0007	0.0871	0.0022
	Experience	0.0904	0.0005	0.0646	0.0018
	Experience-Squared	-0.0013	0.0000	-0.0009	0.0000
1950	Intercept	5.3120	0.0132	5.0716	0.0409
	Education	0.1058	0.0009	0.0998	0.0030
	Experience	0.1074	0.0006	0.0933	0.0023
	Experience-Squared	-0.0017	0.0000	-0.0014	0.0000
1960	Intercept	5.6478	0.0066	5.4107	0.0220
	Education	0.1152	0.0005	0.1034	0.0016
	Experience	0.1156	0.0003	0.1035	0.0011
	Experience-Squared	-0.0018	0.0000	-0.0016	0.0000
1970	Intercept	5.9113	0.0045	5.8938	0.0155
	Education	0.1179	0.0003	0.1100	0.0012
	Experience	0.1323	0.0002	0.1074	0.0007
	Experience-Squared	-0.0022	0.0000	-0.0016	0.0000
1980	Intercept	6.8913	0.0030	6.4448	0.0120
	Education	0.1023	0.0002	0.1176	0.0009
	Experience	0.1255	0.0001	0.1075	0.0005
	Experience-Squared	-0.0022	0.0000	-0.0016	0.0000
1990	Intercept	6.8912	0.0034	6.3474	0.0144
	Education	0.1292	0.0002	0.1524	0.0011
	Experience	0.1301	0.0001	0.1109	0.0006
	Experience-Squared	-0.0023	0.0000	-0.0017	0.0000

Notes: Data taken from 1940-90 Decennial Censuses. See Appendix B for data description.

## *Implications*

- ▶ Log-earnings profiles are parallel across schooling levels.

$$\frac{\partial \ln Y(s, x)}{\partial s \partial x} = 0$$

- ▶ Log-earnings age profiles diverge with age across schooling levels.

$$\frac{\partial \ln Y(s, x)}{\partial s \partial t} = \frac{\rho_0 \kappa}{T} > 0$$

- ▶ The variance of earnings over the life cycle has a U-shaped pattern.

Figure: Mincerian Experience Profiles

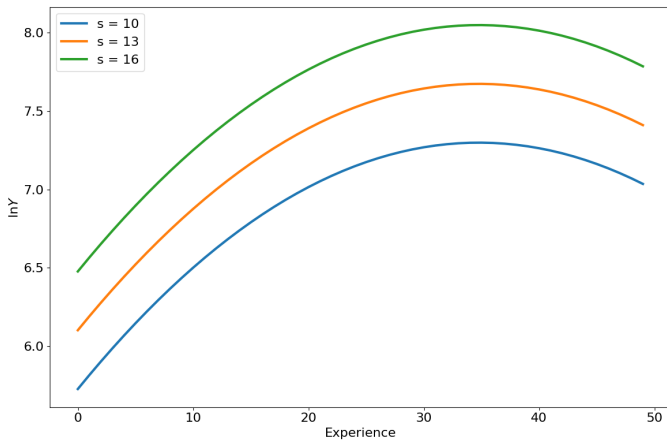
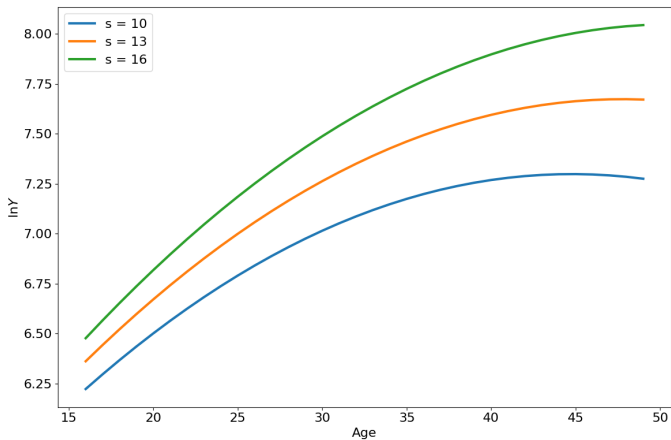


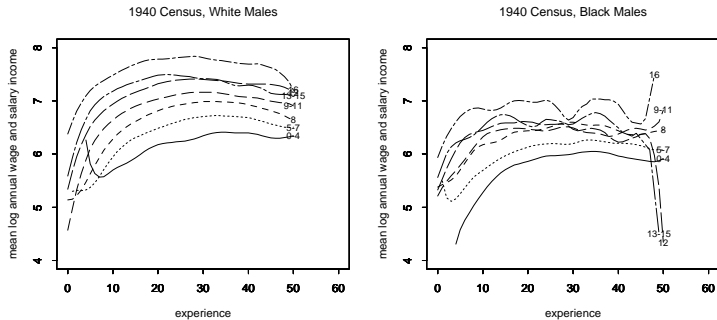
Figure: Mincerian Age Profiles



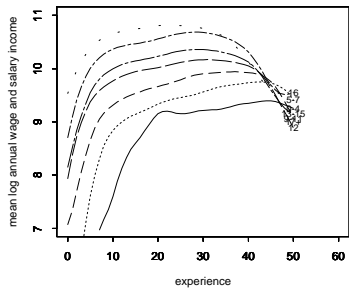


# *Empirical Evidence*

Figure 1a: Experience-Earnings Profiles, 1940-1960



1990 Census, White Males



1990 Census, Black Males

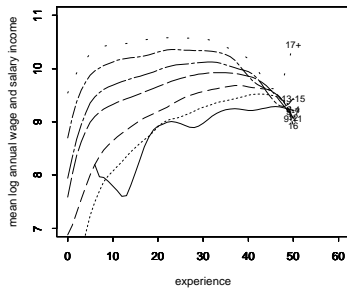
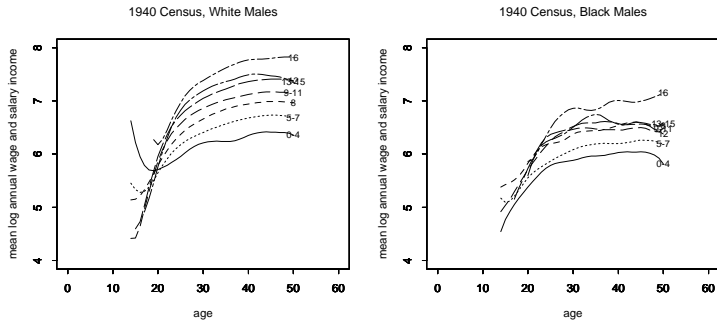


Table 1: Tests of Parallelism in Log Earnings Experience Profiles for Men

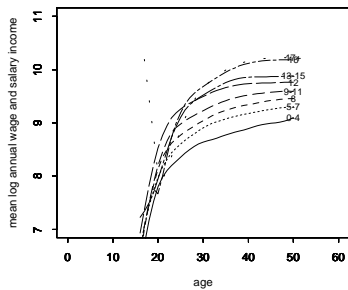
Sample	Experience Level	Estimated Difference Between College and High School Log Earnings at Different Experience Levels					
		1940	1950	1960	1970	1980	1990
Whites	10	0.54	0.30	0.46	0.41	0.37	0.59
	20	0.40	0.40	0.43	0.49	0.45	0.54
	30	0.54	0.27	0.46	0.48	0.43	0.52
	40	0.58	0.21	0.50	0.45	0.27	0.30
	p-value	0.32	0.70	<0.001	<0.001	<0.001	<0.001
Blacks	10	0.20	0.58	0.48	0.38	0.70	0.77
	20	0.38	0.05	0.25	0.22	0.48	0.69
	30	-0.11	0.24	0.08	0.33	0.36	0.53
	40	-0.20	0.00	0.73	0.26	0.22	-0.04
	p-value	0.46	0.55	0.58	0.91	<0.001	<0.001

Notes: Data taken from 1940-90 Decennial Censuses without adjustment for inflation. Because there are very few blacks in the 1940 and 1950 samples with college degrees, especially at higher experience levels, the test results for blacks in those years refer to a test of the difference between earnings for high school graduates and persons with 8 years of education. See Appendix B for data description. See Appendix C for the formulae used for the test statistics.

Figure 2: Age-Earnings Profiles, 1940,1960,1980



1980 Census, White Males



1980 Census, Black Males

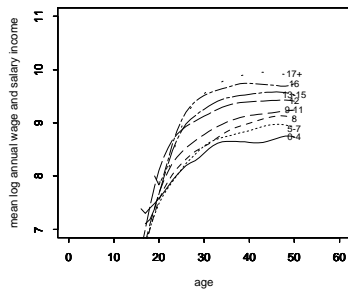
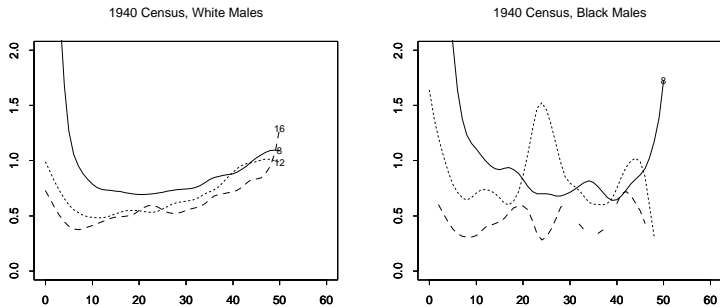
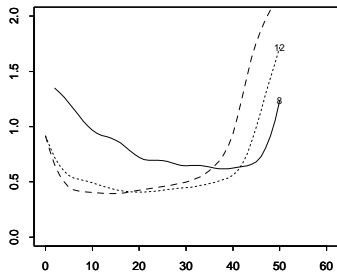


Figure 3: Experience-Variance Log Earnings

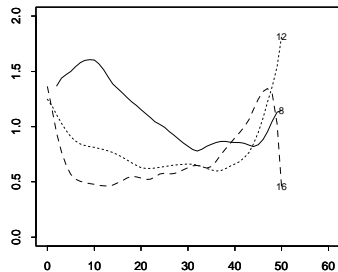


1980 Census, White Males

16



1980 Census, Black Males





# Appendix

## *References*

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