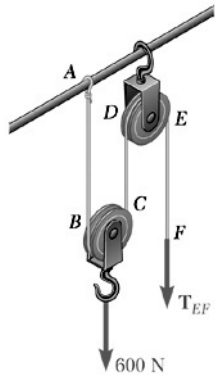


### PROBLEM 8.81

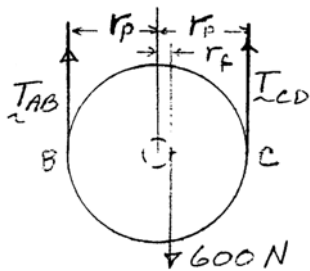


The block and tackle shown are used to raise a 600-N load. Each of the 60-mm-diameter pulleys rotates on a 10-mm-diameter axle. Knowing that the coefficient of kinetic friction is 0.20, determine the tension in each portion of the rope as the load is slowly raised.

### SOLUTION

Pulley FBD's:

Left:



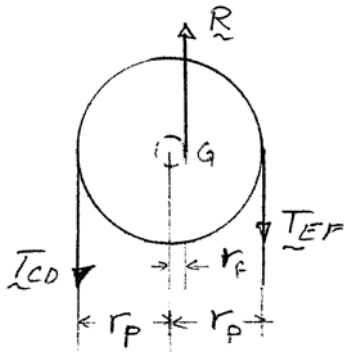
$$r_p = 30 \text{ mm}$$

$$\begin{aligned} r_f &= r_{\text{axle}} \sin \phi_k = r_{\text{axle}} \sin (\tan^{-1} \mu_k)^* \\ &= (5 \text{ mm}) \sin (\tan^{-1} 0.2) \\ &= 0.98058 \text{ mm} \end{aligned}$$

Left:

$$\left( \sum M_C = 0: (r_p - r_f)(600 \text{ lb}) - 2r_p T_{AB} = 0 \right.$$

Right:



or

$$T_{AB} = \frac{30 \text{ mm} - 0.98058 \text{ mm}}{2(30 \text{ mm})}(600 \text{ N}) = 290.19 \text{ N}$$

$$T_{AB} = 290 \text{ N} \blacktriangleleft$$

$$\uparrow \sum F_y = 0: 290.19 \text{ N} - 600 \text{ N} + T_{CD} = 0$$

or

$$T_{CD} = 309.81 \text{ N}$$

$$T_{CD} = 310 \text{ N} \blacktriangleleft$$

Right:

$$\left( \sum M_G = 0: (r_p + r_f)T_{CD} - (r_p - r_f)T_{EF} = 0 \right.$$

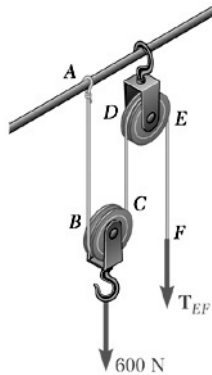
or

$$T_{EF} = \frac{30 \text{ mm} + 0.98058 \text{ mm}}{30 \text{ mm} - 0.98058 \text{ mm}}(309.81 \text{ N}) = 330.75 \text{ N}$$

$$T_{EF} = 331 \text{ N} \blacktriangleleft$$

\* See note before Problem 8.75.

### PROBLEM 8.82

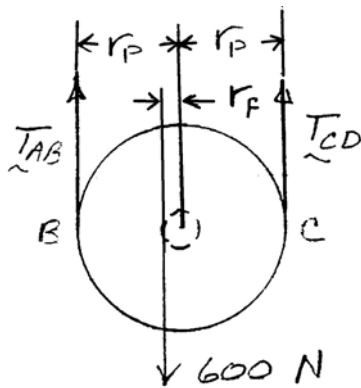


The block and tackle shown are used to lower a 600-N load. Each of the 60-mm-diameter pulleys rotates on a 10-mm-diameter axle. Knowing that the coefficient of kinetic friction is 0.20, determine the tension in each portion of the rope as the load is slowly lowered.

### SOLUTION

**Pulley FBDs:**

Left:



$$r_p = 30 \text{ mm}$$

$$\begin{aligned} r_f &= r_{\text{axle}} \sin \phi_k = r_{\text{axle}} \sin (\tan^{-1} \mu_k)^* \\ &= (5 \text{ mm}) \sin (\tan^{-1} 0.2) \\ &= 0.98058 \text{ mm} \end{aligned}$$

$$\sum M_C = 0: (r_p + r_f)(600 \text{ N}) - 2r_p T_{AB} = 0$$

or

$$T_{AB} = \frac{30 \text{ mm} + 0.98058 \text{ mm}}{2(30 \text{ mm})}(600 \text{ N}) = 309.81 \text{ N}$$

$$T_{AB} = 310 \text{ N} \blacktriangleleft$$

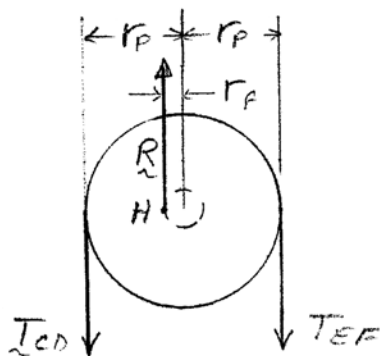
$$\sum F_y = 0: T_{AB} - 600 \text{ N} + T_{CD} = 0$$

or

$$T_{CD} = 600 \text{ N} - 309.81 \text{ N} = 290.19 \text{ N}$$

$$T_{CD} = 290 \text{ N} \blacktriangleleft$$

Right:



$$\sum M_H = 0: (r_p - r_f)T_{CD} - (r_p + r_f)T_{EF} = 0$$

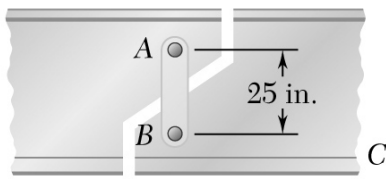
or

$$T_{EF} = \frac{30 \text{ mm} - 0.98058 \text{ mm}}{30 \text{ mm} + 0.98058 \text{ mm}}(290.19 \text{ N})$$

$$T_{EF} = 272 \text{ N} \blacktriangleleft$$

\* See note before Problem 8.75.

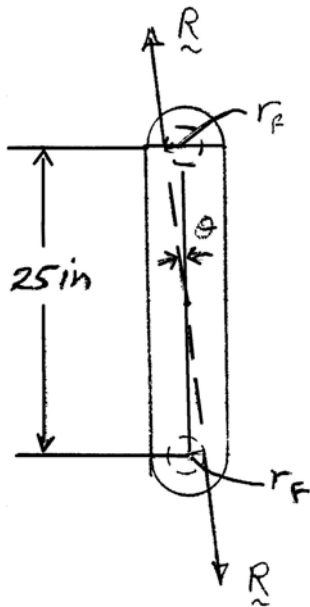
### PROBLEM 8.83



The link arrangement shown is frequently used in highway bridge construction to allow for expansion due to changes in temperature. At each of the 3-in.-diameter pins  $A$  and  $B$  the coefficient of static friction is 0.20. Knowing that the vertical component of the force exerted by  $BC$  on the link is 50 kips, determine (a) the horizontal force which should be exerted on beam  $BC$  to just move the link, (b) the angle that the resulting force exerted by beam  $BC$  on the link will form with the vertical.

### SOLUTION

FBD link AB:



Note that  $AB$  is a two force member. For impending motion, the pin forces are tangent to the friction circles.

$$\theta = \sin^{-1} \frac{r_f}{25 \text{ in.}}$$

where

$$r_f = r_p \sin \phi_s = r_p \sin (\tan^{-1} \mu_s)^*$$

$$= (1.5 \text{ in.}) \sin (\tan^{-1} 0.2) = 0.29417 \text{ in.}$$

Then

$$\theta = \sin^{-1} \frac{0.29417 \text{ in.}}{12.5 \text{ in.}} = 1.3485^\circ$$

(b)  $\theta = 1.349^\circ \blacktriangleleft$

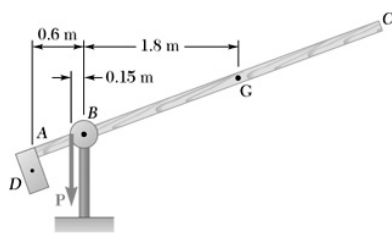
$$R_{\text{vert}} = R \cos \theta \quad R_{\text{horiz}} = R \sin \theta$$

$$R_{\text{horiz}} = R_{\text{vert}} \tan \theta = (50 \text{ kips}) \tan 1.3485^\circ = 1.177 \text{ kips}$$

(a)  $R_{\text{horiz}} = 1.177 \text{ kips} \blacktriangleleft$

\* See note before Problem 8.75.

### PROBLEM 8.84

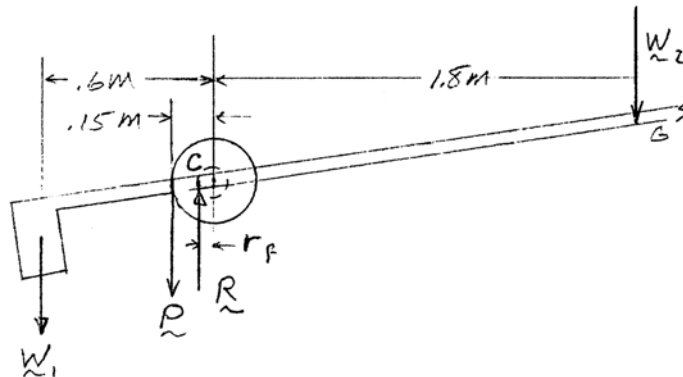


A gate assembly consisting of a 24-kg gate  $ABC$  and a 66-kg counterweight  $D$  is attached to a 24-mm-diameter shaft  $B$  which fits loosely in a fixed bearing. Knowing that the coefficient of static friction is 0.20 between the shaft and the bearing, determine the magnitude of the force  $P$  for which counterclockwise rotation of the gate is impending.

BEER • JOHNSTON Fig. P8-84 and P8-86  
Vector Mechanics for Engineers: Statics & Dynamics, 7e  
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### SOLUTION

FBD gate:



$$W_1 = 66 \text{ kg}(9.81 \text{ m/s}^2) = 647.46 \text{ N}$$

$$W_2 = 24 \text{ kg}(9.81 \text{ m/s}^2) = 235.44 \text{ N}$$

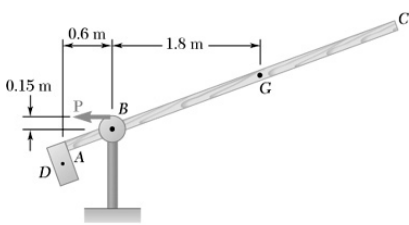
$$\begin{aligned} r_f &= r_s \sin \phi_s = r_s \sin(\tan^{-1} \mu_s) \\ &= (0.012 \text{ m}) \sin(\tan^{-1} 0.2) = 0.0023534 \text{ m} \end{aligned}$$

$$\sum M_C = 0: (0.6 \text{ m} - r_f)W_1 + (0.15 \text{ m} - r_f)P - (1.8 \text{ m} + r_f)W_2 = 0$$

$$\begin{aligned} P &= \frac{(1.80235 \text{ m})(235.44 \text{ N}) - (0.59765 \text{ m})(647.46 \text{ N})}{(0.14765 \text{ m})} \\ &= 253.2 \text{ N} \end{aligned}$$

$$P = 253 \text{ N} \blacktriangleleft$$

### PROBLEM 8.85



A gate assembly consisting of a 24-kg gate  $ABC$  and a 66-kg counterweight  $D$  is attached to a 24-mm-diameter shaft  $B$  which fits loosely in a fixed bearing. Knowing that the coefficient of static friction is 0.20 between the shaft and the bearing, determine the magnitude of the force  $P$  for which counterclockwise rotation of the gate is impending.

BEER • JOHNSTON Fig. P8-85 and P8-87  
Vector Mechanics for Engineers: Statics & Dynamics, 7e  
100% of size Fine Line Illustrations (516) 501-0400

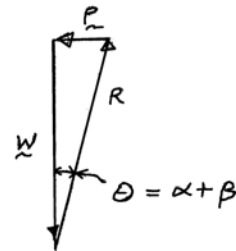
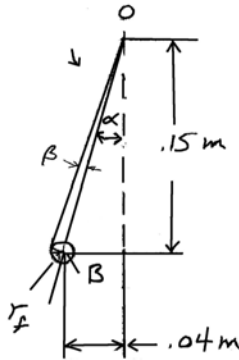
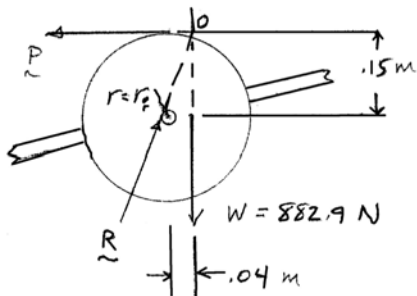
### SOLUTION

It is convenient to replace the  $(66 \text{ kg})g$  and  $(24 \text{ kg})g$  weights with a single combined weight of

$(90 \text{ kg})(9.81 \text{ m/s}^2) = 882.9 \text{ N}$ , located at a distance  $x = \frac{(1.8 \text{ m})(24 \text{ kg}) - (0.6 \text{ m})(24 \text{ kg})}{90 \text{ kg}} = 0.04 \text{ m}$  to the right of  $B$ .

$$r_f = r_s \sin \phi_s = r_s \sin(\tan^{-1} \mu_s)^* = (0.012 \text{ m}) \sin(\tan^{-1} 0.2) \\ = 0.0023534 \text{ m}$$

**FBD pulley + gate:**



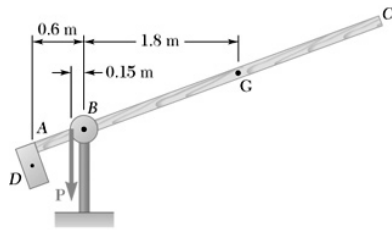
$$\alpha = \tan^{-1} \frac{0.04 \text{ m}}{0.15 \text{ m}} = 14.931^\circ \quad OB = \frac{0.15}{\cos \alpha} = 0.15524 \text{ m}$$

$$\beta = \sin^{-1} \frac{r_f}{OB} = \sin^{-1} \frac{0.0023534 \text{ m}}{0.15524 \text{ m}} = 0.8686^\circ \quad \text{then} \quad \theta = \alpha + \beta = 15.800^\circ$$

$$P = W \tan \theta = 248.9 \text{ N}$$

$$P = 250 \text{ N} \blacktriangleleft$$

\* See note before Problem 8.75.



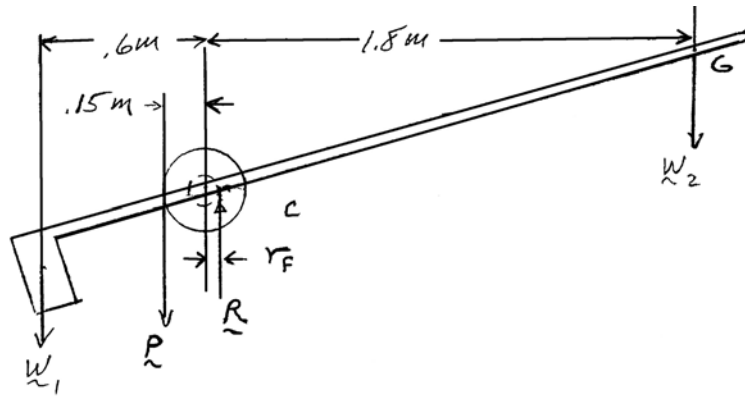
### PROBLEM 8.86

A gate assembly consisting of a 24-kg gate  $ABC$  and a 66-kg counterweight  $D$  is attached to a 24-mm-diameter shaft  $B$  which fits loosely in a fixed bearing. Knowing that the coefficient of static friction is 0.20 between the shaft and the bearing, determine the magnitude of the force  $P$  for which clockwise rotation of the gate is impending.

BEER • JOHNSTON Fig. P8-84 and P8-86  
Vector Mechanics for Engineers: Statics & Dynamics, 7e  
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### SOLUTION

FBD gate:



$$W_1 = 66 \text{ kg} (9.81 \text{ m/s}^2) = 647.46 \text{ N}$$

$$W_2 = 24 \text{ kg} (9.81 \text{ m/s}^2) = 235.44 \text{ N}$$

$$\begin{aligned} r_f &= r_s \sin \phi_s = r_s \sin (\tan^{-1} \mu_s)^* \\ &= (0.012 \text{ m}) \sin (\tan^{-1} 0.2) = 0.0023534 \text{ m} \end{aligned}$$

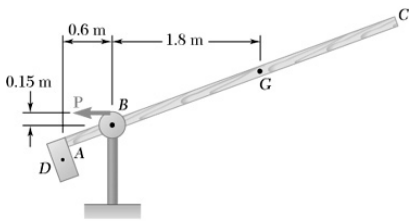
$$\sum M_C = 0: (0.6 \text{ m} + r_f) W_1 + (0.15 \text{ m} + r_f) P - (1.8 \text{ m} - r_f) W_2 = 0$$

$$\begin{aligned} P &= \frac{(1.79765 \text{ m})(235.44 \text{ N}) - (0.60235 \text{ m})(647.46 \text{ N})}{0.15235 \text{ m}} \\ &= 218.19 \text{ N} \end{aligned}$$

$$P = 218 \text{ N} \blacktriangleleft$$

\* See note before Problem 8.75.

### PROBLEM 8.87



A gate assembly consisting of a 24-kg gate  $ABC$  and a 66-kg counterweight  $D$  is attached to a 24-mm-diameter shaft  $B$  which fits loosely in a fixed bearing. Knowing that the coefficient of static friction is 0.20 between the shaft and the bearing, determine the magnitude of the force  $P$  for which clockwise rotation of the gate is impending.

BEER • JOHNSTON Fig. P8-85 and P8-87  
Vector Mechanics for Engineers: Statics & Dynamics, 7e  
100% of size Fine Line Illustrations (516) 501-0400

### SOLUTION

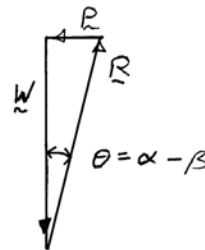
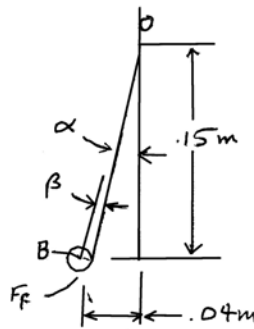
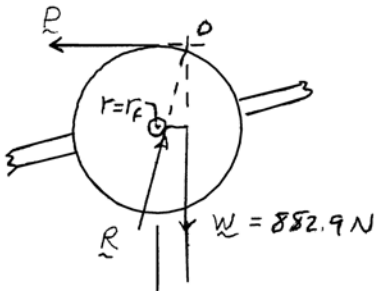
It is convenient to replace the  $(66 \text{ kg})g$  and  $(24 \text{ kg})g$  weights with a single weight of

$(90 \text{ kg})(9.81 \text{ N/kg}) = 882.9 \text{ N}$ , located at a distance  $x = \frac{(1.8 \text{ m})(24 \text{ kg}) - (0.15 \text{ m})(66 \text{ kg})}{90 \text{ kg}} = 0.04 \text{ m}$  to the right of  $B$ .

**FBD pulley + gate:**

$$r_f = r_s \sin \phi_s = r_s \sin(\tan^{-1} \mu_s)^* = (0.012 \text{ m}) \sin(\tan^{-1} 0.2)$$

$$r_f = 0.0023534 \text{ m}$$



$$\alpha = \tan^{-1} \frac{0.04 \text{ m}}{0.15 \text{ m}} = 14.931^\circ \quad OB = \frac{0.15 \text{ m}}{\cos \alpha} = 0.15524 \text{ m}$$

$$\beta = \sin^{-1} \frac{r_f}{OB} = \sin^{-1} \frac{0.0023534 \text{ m}}{0.15524 \text{ m}} = 0.8686^\circ \quad \text{then} \quad \theta = \alpha - \beta = 14.062^\circ$$

$$P = W \tan \theta = 221.1 \text{ N}$$

$$P = 221 \text{ N} \blacktriangleleft$$

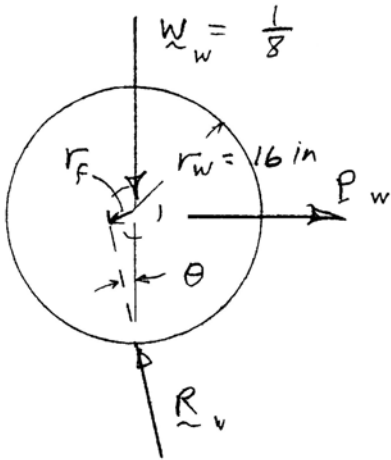
\* See note before Problem 8.75.

### PROBLEM 8.88

A loaded railroad car has a weight of 35 tons and is supported by eight 32-in.-diameter wheels with 5-in.-diameter axles. Knowing that the coefficients of friction are  $\mu_s = 0.020$  and  $\mu_k = 0.015$ , determine the horizontal force required (a) for impending motion of the car, (b) to keep the car moving at a constant speed. Neglect rolling resistance between the wheels and the track.

### SOLUTION

FBD wheel:



$$W_w = \frac{1}{8} W_c = \frac{1}{8} (35 \text{ ton}) = \frac{1}{8} (70,000) \text{ lb}$$

$$r_f = r_a \sin \phi = r_a \sin (\tan^{-1} \mu)^*$$

$$\begin{aligned} \theta &= \sin^{-1} \frac{r_f}{r_w} = \sin^{-1} \left[ \frac{(2.5 \text{ in.}) \sin (\tan^{-1} \mu)}{16 \text{ in.}} \right] \\ &= \sin^{-1} [0.15625 \sin (\tan^{-1} \mu)] \end{aligned}$$

(a) For impending motion use  $\mu_s = 0.02$ : then  $\theta_s = 0.179014^\circ$

(b) For steady motion use  $\mu_k = 0.015$ : then  $\theta_k = 0.134272^\circ$

$$P_w = W_w \tan \theta \quad P_c = W_c \tan \theta = 8W_w \tan \theta$$

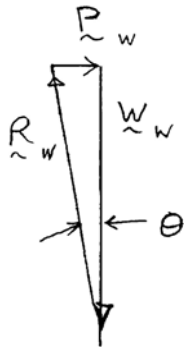
(a)  $P_c = (70,000 \text{ lb}) \tan (0.179014^\circ)$

$$P_c = 219 \text{ lb} \blacktriangleleft$$

(b)  $P_c = (70,000 \text{ lb}) \tan (0.134272^\circ)$

$$P_c = 164.0 \text{ lb} \blacktriangleleft$$

\* See note before Problem 8.75.



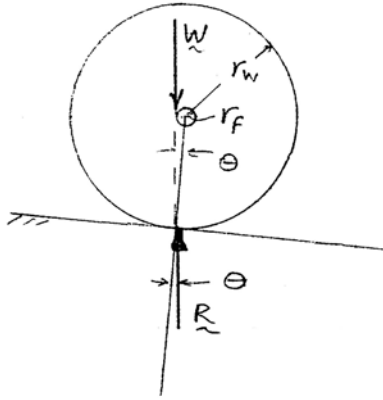


### PROBLEM 8.89

A scooter is designed to roll down a 2 percent slope at a constant speed. Assuming that the coefficient of kinetic friction between the 1-in.-diameter axles and the bearing is 0.10, determine the required diameter of the wheels. Neglect the rolling resistance between the wheels and the ground.

### SOLUTION

FBD wheel:



Note: The wheel is a two-force member in equilibrium, so **R** and **W** must be collinear and tangent to friction circle.

$$2\% \text{ slope} \Rightarrow \tan \theta = 0.02$$

Also 
$$\sin \theta = \frac{r_f}{r_w} \sin(\tan^{-1} 0.02) = 0.019996$$

But 
$$r_f = r_a \sin \phi_k = r_a \sin(\tan^{-1} \mu_k)^*$$

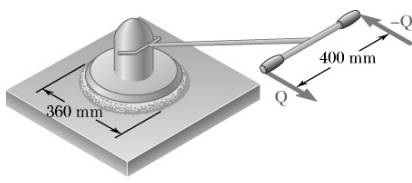
$$= (1 \text{ in.}) \sin(\tan^{-1} 0.1) = 0.099504 \text{ in.}$$

Then 
$$r_w = \frac{r_f}{\sin \theta} = \frac{0.099504}{0.019996} = 4.976 \text{ in.}$$

and 
$$d_w = 2r_w \qquad d_w = 9.95 \text{ in.} \blacktriangleleft$$

\* See note before Problem 8.75.

### PROBLEM 8.90



A 25-kg electric floor polisher is operated on a surface for which the coefficient of kinetic friction is 0.25. Assuming that the normal force per unit area between the disk and the floor is uniformly distributed, determine the magnitude  $Q$  of the horizontal forces required to prevent motion of the machine.

### SOLUTION

Couple exerted on handle

$$M_H = dQ = (0.4 \text{ m})Q$$

Couple exerted on floor

$$M_F = \frac{2}{3} \mu_k PR \quad (\text{Equation 8.9})$$

where

$$\mu_k = 0.25, \quad P = (25 \text{ kg})(9.81 \text{ m/s}^2) = 245.25 \text{ N}, \quad R = 0.18 \text{ m}$$

For equilibrium

$$M_H = M_F,$$

so

$$Q = \frac{\frac{2}{3}(0.25)(245.25 \text{ N})(0.18 \text{ m})}{0.4 \text{ m}}$$

$$Q = 18.39 \text{ N} \quad \blacktriangleleft$$