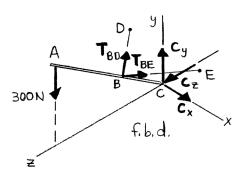


The 3-m flagpole AC forms an angle of  $30^{\circ}$  with the z axis. It is held by a ball-and-socket joint at C and by two thin braces BD and BE. Knowing that the distance BC is 0.9 m, determine the tension in each brace and the reaction at C.

#### **SOLUTION**



 $T_{BE}$  can be found from  $\Sigma M$  about line CE

From f.b.d. of flagpole

$$\Sigma M_{CE} = 0$$
:  $\lambda_{CE} \cdot (\mathbf{r}_{B/C} \times \mathbf{T}_{BD}) + \lambda_{CE} \cdot (\mathbf{r}_{A/C} \times \mathbf{F}_{A}) = 0$ 

$$\lambda_{CE} = \frac{(0.9 \text{ m})\mathbf{i} + (0.9 \text{ m})\mathbf{j}}{\sqrt{(0.9)^2 + (0.9)^2 \text{ m}}} = \frac{1}{\sqrt{2}}(\mathbf{i} + \mathbf{j})$$

$$\mathbf{r}_{B/C} = \left[ (0.9 \text{ m}) \sin 30^{\circ} \right] \mathbf{j} + \left[ (0.9 \text{ m}) \cos 30^{\circ} \right] \mathbf{k}$$
$$= (0.45 \text{ m}) \mathbf{j} + (0.77942 \text{ m}) \mathbf{k}$$

$$\mathbf{T}_{BD} = \lambda_{BD} T_{BD} = \left\{ \frac{-(0.9 \text{ m})\mathbf{i} + [0.9 \text{ m} - (0.9 \text{ m})\sin 30^{\circ}]\mathbf{j} - [(0.9 \text{ m})\cos 30^{\circ}]\mathbf{k}}{\sqrt{(0.9)^{2} + (0.45)^{2} + (0.77942)^{2}} \text{ m}} \right\} T_{BD}$$

$$= \left[ -(0.9 \text{ m})\mathbf{i} + (0.45 \text{ m})\mathbf{j} - (0.77942 \text{ m})\mathbf{k} \right] \frac{T_{BD}}{\sqrt{1.62}}$$

$$= (-0.70711\mathbf{i} + 0.35355\mathbf{j} - 0.61237\mathbf{k}) T_{BD}$$

$$\mathbf{r}_{A/C} = (3 \text{ m})\sin 30^{\circ}\mathbf{j} + (3 \text{ m})\cos 30^{\circ}\mathbf{k} = (1.5 \text{ m})\mathbf{j} + (2.5981 \text{ m})\mathbf{k}$$

$$\mathbf{F}_A = -\big(300 \text{ N}\big)\mathbf{j}$$

$$\begin{vmatrix} 1 & 1 & 0 \\ 0 & 0.45 & 0.77942 \\ -0.70711 & 0.35355 & -0.61237 \end{vmatrix} \left( \frac{T_{BD}}{\sqrt{2}} \right) + \begin{vmatrix} 1 & 1 & 0 \\ 0 & 1.5 & 2.5981 \\ 0 & -300 & 0 \end{vmatrix} \left( \frac{1}{\sqrt{2}} \right) = 0$$

# **PROBLEM 4.112 CONTINUED**

or 
$$-1.10227T_{BD} + 779.43 = 0$$

$$T_{BD} = 707.12 \text{ N}$$

$$7.12 \text{ N}$$
 or  $T_{BD} = 707 \text{ N}$  ◀

Based on symmetry with yz-plane,

$$T_{BE} = T_{BD} = 707.12 \text{ N}$$

or 
$$T_{BE} = 707 \text{ N} \blacktriangleleft$$

The reaction forces at C are found from  $\Sigma \mathbf{F} = 0$ 

$$\Sigma F_x = 0$$
:  $-(T_{BD})_x + (T_{BE})_x + C_x = 0$  or  $C_x = 0$ 

$$\Sigma F_y = 0$$
:  $(T_{BD})_y + (T_{BE})_y + C_y - 300 \text{ N} = 0$ 

$$C_y = 300 \text{ N} - 2(0.35355)(707.12 \text{ N})$$

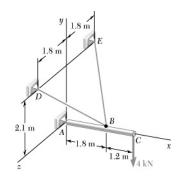
$$C_y = -200.00 \text{ N}$$

$$\Sigma F_z = 0$$
:  $C_z - (T_{BD})_z - (T_{BE})_z = 0$ 

$$C_z = 2(0.61237)(707.12 \text{ N})$$

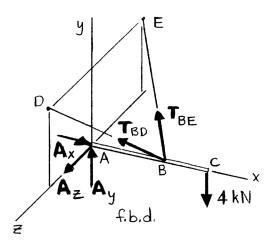
$$C_z = 866.04 \text{ N}$$

or  $C = -(200 \text{ N})\mathbf{j} + (866 \text{ N})\mathbf{k} \blacktriangleleft$ 



A 3-m boom is acted upon by the 4-kN force shown. Determine the tension in each cable and the reaction at the ball-and-socket joint at *A*.

# **SOLUTION**



From f.b.d. of boom

$$\Sigma M_{AE} = 0$$
:  $\lambda_{AE} \cdot (\mathbf{r}_{B/A} \times \mathbf{T}_{BD}) + \lambda_{AE} \cdot (\mathbf{r}_{C/A} \times \mathbf{F}_{C}) = 0$ 

$$\lambda_{AE} = \frac{(2.1 \text{ m})\mathbf{j} - (1.8 \text{ m})\mathbf{k}}{\sqrt{(2.1)^2 + (1.8)^2} \text{ m}}$$
$$= 0.27451\mathbf{j} - 0.23529\mathbf{k}$$

$$\mathbf{r}_{B/A} = (1.8 \text{ m})\mathbf{i}$$

$$\mathbf{T}_{BD} = \lambda_{BD} T_{BD} = \frac{(-1.8 \text{ m})\mathbf{i} + (2.1 \text{ m})\mathbf{j} + (1.8 \text{ m})\mathbf{k}}{\sqrt{(1.8)^2 + (2.1)^2 + (1.8)^2}} T_{BD}$$
$$= (-0.54545\mathbf{i} + 0.63636\mathbf{j} + 0.54545\mathbf{k}) T_{BD}$$

$$\mathbf{r}_{C/A} = (3.0 \text{ m})\mathbf{i}$$

$$\mathbf{F}_C = -(4 \text{ kN})\mathbf{j}$$

# **PROBLEM 4.113 CONTINUED**

$$(-0.149731 - 0.149729)1.8T_{BD} + 2.82348 = 0$$

$$T_{BD} = 5.2381 \text{ kN}$$

or 
$$T_{BD} = 5.24 \text{ kN} \blacktriangleleft$$

$$T_{BE} = T_{BD} = 5.2381 \,\mathrm{kN}$$

or 
$$T_{BE} = 5.24 \text{ kN} \blacktriangleleft$$

$$\Sigma F_z = 0$$
:  $A_z + (T_{BD})_z - (T_{BE})_z = 0$   $A_z = 0$ 

$$\Sigma F_y = 0$$
:  $A_y + (T_{BD})_y + (T_{BD})_y - 4 \text{ kN} = 0$ 

$$A_y + 2(0.63636)(5.2381 \text{ kN}) - 4 \text{ kN} = 0$$

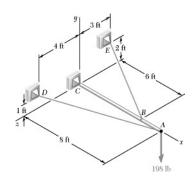
$$A_y = -2.6666 \text{ kN}$$

$$\Sigma F_x = 0: \quad A_x - (T_{BD})_x - (T_{BE})_x = 0$$

$$A_x - 2(0.54545)(5.2381 \,\mathrm{kN}) = 0$$

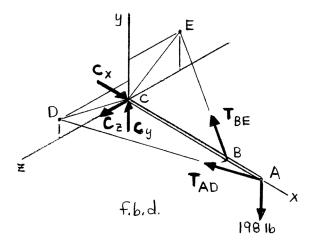
$$\therefore A_x = 5.7142 \text{ kN}$$

and 
$$\mathbf{A} = (5.71 \,\mathrm{N})\mathbf{i} - (2.67 \,\mathrm{N})\mathbf{j} \blacktriangleleft$$



An 8-ft-long boom is held by a ball-and-socket joint at C and by two cables AD and BE. Determine the tension in each cable and the reaction at C.

# **SOLUTION**



From f.b.d. of boom

$$\Sigma M_{CE} = 0$$
:  $\lambda_{CE} \cdot (\mathbf{r}_{A/C} \times \mathbf{T}_{AD}) + \lambda_{CE} \cdot (\mathbf{r}_{A/C} \times \mathbf{F}_{A}) = 0$ 

$$\lambda_{CE} = \frac{(2 \text{ ft})\mathbf{j} - (3 \text{ ft})\mathbf{k}}{\sqrt{(2)^2 + (3)^2} \text{ ft}} = \frac{1}{\sqrt{13}} (2\mathbf{j} - 3\mathbf{k})$$

$$\mathbf{r}_{A/C} = (8 \text{ ft})\mathbf{i}$$

$$\mathbf{T}_{AD} = \boldsymbol{\lambda}_{AD} T_{AD} = \frac{-\left(8 \text{ ft}\right)\mathbf{i} + \left(1 \text{ ft}\right)\mathbf{j} + \left(4 \text{ ft}\right)\mathbf{k}}{\sqrt{\left(8\right)^2 + \left(1\right)^2 + \left(4\right)^2}} T_{AD}$$
$$= \left(\frac{1}{9}\right) T_{AD} \left(-8\mathbf{i} + \mathbf{j} + 4\mathbf{k}\right)$$

$$\mathbf{F}_A = -(198 \text{ lb})\mathbf{j}$$

$$\begin{vmatrix} 0 & 2 & -3 \\ 8 & 0 & 0 \\ -8 & 1 & 4 \end{vmatrix} \left( \frac{T_{AD}}{9\sqrt{13}} \right) + \begin{vmatrix} 0 & 2 & -3 \\ 8 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \left( \frac{198}{\sqrt{13}} \right) = 0$$

#### **PROBLEM 4.114 CONTINUED**

$$(-64 - 24)\frac{T_{AD}}{9\sqrt{13}} + (24)\frac{198}{\sqrt{13}} = 0$$
  
$$\therefore T_{AD} = 486.00 \text{ lb}$$

or  $T_{AD} = 486 \text{ lb} \blacktriangleleft$ 

$$\Sigma M_{CD} = 0$$
:  $\lambda_{CD} \cdot (\mathbf{r}_{B/C} \times \mathbf{T}_{BE}) + \lambda_{CD} \cdot (\mathbf{r}_{A/C} \times \mathbf{F}_{A})$ 

where

$$\lambda_{CD} = \frac{\left(1 \text{ ft}\right)\mathbf{j} + \left(4 \text{ ft}\right)\mathbf{k}}{\sqrt{17} \text{ ft}} = \frac{1}{\sqrt{17}} \left(1\mathbf{j} + 4\mathbf{k}\right)$$

$$\mathbf{r}_{B/C} = (6 \text{ ft})\mathbf{i}$$

$$\mathbf{T}_{BE} = \lambda_{BE} T_{BE} = \frac{-(6 \text{ ft})\mathbf{i} + (2 \text{ ft})\mathbf{j} - (3 \text{ ft})\mathbf{k}}{\sqrt{(6)^2 + (2)^2 + (3)^2} \text{ ft}} T_{BE} = \left(\frac{1}{7}\right) T_{BE} \left(-6\mathbf{i} + 2\mathbf{j} - 3\mathbf{k}\right)$$

$$\therefore \begin{vmatrix} 0 & 1 & 4 \\ 6 & 0 & 0 \\ -6 & 2 & -3 \end{vmatrix} \frac{T_{BE}}{7\sqrt{17}} + \begin{vmatrix} 0 & 1 & 4 \\ 8 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \frac{198}{\sqrt{17}} = 0$$

$$(18+48)\frac{T_{BE}}{7} + (-32)198 = 0$$

$$T_{BE} = 672.00 \text{ lb}$$

or  $T_{BE} = 672 \text{ lb} \blacktriangleleft$ 

$$\Sigma F_x = 0$$
:  $C_x - (T_{AD})_x - (T_{BE})_x = 0$   
 $C_x - (\frac{8}{9})486 - (\frac{6}{7})672 = 0$ 

$$\therefore C_x = 1008 \text{ lb}$$

$$\Sigma F_y = 0$$
:  $C_y + (T_{AD})_y + (T_{BE})_y - 198 \text{ lb} = 0$ 

$$C_y + \left(\frac{1}{9}\right) 486 + \left(\frac{2}{7}\right) 672 - 198 \text{ lb} = 0$$

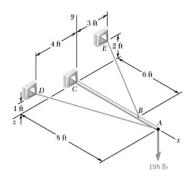
$$C_v = -48.0 \text{ lb}$$

$$\Sigma F_z = 0$$
:  $C_z + (T_{AD})_z - (T_{BE})_z = 0$ 

$$C_z + \left(\frac{4}{9}\right) 486 - \left(\frac{3}{7}\right) (672) = 0$$

:. 
$$C_z = 72.0 \text{ lb}$$

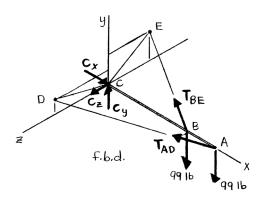
or 
$$\mathbf{C} = (1008 \text{ lb})\mathbf{i} - (48.0 \text{ lb})\mathbf{j} + (72.0 \text{ lb})\mathbf{k} \blacktriangleleft$$



Solve Problem 4.114 assuming that the given 198-lb load is replaced with two 99-lb loads applied at *A* and *B*.

**P4.114** An 8-ft-long boom is held by a ball-and-socket joint at C and by two cables AD and BE. Determine the tension in each cable and the reaction at C.

# **SOLUTION**



From f.b.d. of boom

$$\Sigma M_{CE} = 0: \quad \boldsymbol{\lambda}_{CE} \cdot \left( \mathbf{r}_{A/C} \times \mathbf{T}_{AD} \right) + \boldsymbol{\lambda}_{CE} \cdot \left( \mathbf{r}_{A/C} \times \mathbf{F}_{A} \right) + \boldsymbol{\lambda}_{CE} \cdot \left( \mathbf{r}_{B/C} \times \mathbf{F}_{B} \right) = 0$$

$$\lambda_{CE} = \frac{(2 \text{ ft})\mathbf{j} - (3 \text{ ft})\mathbf{k}}{\sqrt{(2)^2 + (3)^2} \text{ ft}} = \frac{1}{\sqrt{13}} (2\mathbf{j} - 3\mathbf{k})$$

$$\mathbf{r}_{A/C} = (8 \text{ ft})\mathbf{i}$$

$$\mathbf{r}_{B/C} = (6 \text{ ft})\mathbf{i}$$

$$\mathbf{T}_{AD} = \boldsymbol{\lambda}_{AD} T_{AD} = \frac{-\left(8 \text{ ft}\right)\mathbf{i} + \left(1 \text{ ft}\right)\mathbf{j} + \left(4 \text{ ft}\right)\mathbf{k}}{\sqrt{\left(8\right)^2 + \left(1\right)^2 + \left(4\right)^2}} T_{AD}$$
$$= \left(\frac{1}{9}\right) T_{AD} \left(-8\mathbf{i} + \mathbf{j} + 4\mathbf{k}\right)$$

$$\mathbf{F}_A = -(99 \text{ lb})\mathbf{j}$$

$$\mathbf{F}_B = -(99 \text{ lb})\mathbf{j}$$

$$\begin{vmatrix} 0 & 2 & -3 \\ 8 & 0 & 0 \\ -8 & 1 & 4 \end{vmatrix} \frac{T_{AD}}{9\sqrt{13}} + \begin{vmatrix} 0 & 2 & -3 \\ 8 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \frac{99}{\sqrt{13}} + \begin{vmatrix} 0 & 2 & -3 \\ 6 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \frac{99}{\sqrt{13}} = 0$$

#### **PROBLEM 4.115 CONTINUED**

$$(-64 - 24)\frac{T_{AD}}{9\sqrt{13}} + (24 + 18)\frac{99}{\sqrt{13}} = 0$$
$$T_{AD} = 425.25 \text{ lb}$$

or

or  $T_{AD} = 425 \text{ lb} \blacktriangleleft$ 

$$\Sigma M_{CD} = 0$$
:  $\lambda_{CD} \cdot (\mathbf{r}_{B/C} \times \mathbf{T}_{BE}) + \lambda_{CD} \cdot (\mathbf{r}_{A/C} \times \mathbf{F}_{A}) + \lambda_{CD} \cdot (\mathbf{r}_{B/C} \times \mathbf{F}_{B}) = 0$ 

where

$$\lambda_{CD} = \frac{\left(1 \text{ ft}\right)\mathbf{j} + \left(4 \text{ ft}\right)\mathbf{k}}{\sqrt{17}} = \frac{1}{\sqrt{17}} \left(\mathbf{j} + 4\mathbf{k}\right)$$

$$\mathbf{r}_{B/C} = (6 \text{ ft})\mathbf{i}$$

$$\mathbf{r}_{A/C} = (8 \text{ ft})\mathbf{j}$$

$$\mathbf{T}_{BE} = \lambda_{BE} T_{BE} = \frac{-(6 \text{ ft})\mathbf{i} + (2 \text{ ft})\mathbf{j} - (3 \text{ ft})\mathbf{k}}{\sqrt{(6)^2 + (2)^2 + (3)^2}} T_{BE} = \frac{T_{BE}}{7} (-6\mathbf{i} + 2\mathbf{j} - 3\mathbf{k})$$

$$\begin{vmatrix} 0 & 1 & 4 \\ 6 & 0 & 0 \\ -6 & 2 & -3 \end{vmatrix} \left( \frac{T_{BE}}{7\sqrt{17}} \right) + \begin{vmatrix} 0 & 1 & 4 \\ 8 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \left( \frac{99}{\sqrt{17}} \right) + \begin{vmatrix} 0 & 1 & 4 \\ 6 & 0 & 0 \\ 0 & -1 & 0 \end{vmatrix} \left( \frac{99}{\sqrt{17}} \right) = 0$$

$$(18+48)\left(\frac{T_{BE}}{7\sqrt{17}}\right) + (-32-24)\left(\frac{99}{\sqrt{17}}\right) = 0$$

 $T_{RE} = 588.00 \text{ lb}$ 

or

or  $T_{BE} = 588 \text{ lb} \blacktriangleleft$ 

$$\Sigma F_x = 0$$
:  $C_x - (T_{AD})_x - (T_{BE})_x = 0$   
 $C_x - \left(\frac{8}{9}\right) 425.25 - \left(\frac{6}{7}\right) 588.00 = 0$ 

$$\therefore$$
  $C_x = 882 \text{ lb}$ 

$$\Sigma F_y = 0$$
:  $C_y + (T_{AD})_y + (T_{BE})_y - 99 - 99 = 0$ 

$$C_y + \left(\frac{1}{9}\right) 425.25 + \left(\frac{2}{7}\right) 588.00 - 198 = 0$$

$$C_y = -17.25 \text{ lb}$$

$$\Sigma F_z = 0$$
:  $C_z + (T_{AD})_z - (T_{BE})_z = 0$ 

$$C_z + \left(\frac{4}{9}\right) 425.25 - \left(\frac{3}{7}\right) 588.00 = 0$$

:. 
$$C_z = 63.0 \text{ lb}$$

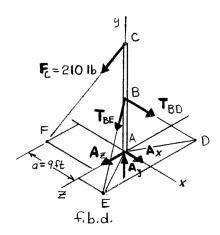
or  $C = (882 \text{ lb})\mathbf{i} - (17.25 \text{ lb})\mathbf{j} + (63.0 \text{ lb})\mathbf{k} \blacktriangleleft$ 

# 9 ft 210 lb 8 9 ft 4.5 ft 2 ft 4.5 ft x

# **PROBLEM 4.116**

The 18-ft pole ABC is acted upon by a 210-lb force as shown. The pole is held by a ball-and-socket joint at A and by two cables BD and BE. For a=9 ft, determine the tension in each cable and the reaction at A.

#### **SOLUTION**



From f.b.d. of pole *ABC* 

$$\Sigma M_{AE} = 0$$
:  $\lambda_{AE} \cdot (\mathbf{r}_{B/A} \times \mathbf{T}_{BD}) + \lambda_{AE} \cdot (\mathbf{r}_{C/A} \times \mathbf{F}_{C}) = 0$ 

$$\lambda_{AE} = \frac{(4.5 \text{ ft})\mathbf{i} + (9 \text{ ft})\mathbf{k}}{\sqrt{(4.5)^2 + (9)^2} \text{ ft}} = \frac{1}{\sqrt{101.25}} (4.5\mathbf{i} + 9\mathbf{k})$$

$$\mathbf{r}_{B/A} = (9 \text{ ft})\mathbf{j}$$

$$\mathbf{r}_{C/A} = (18 \text{ ft})\mathbf{j}$$

$$\mathbf{T}_{BD} = \lambda_{BD} T_{BD} = \frac{(4.5 \text{ ft})\mathbf{i} - (9 \text{ ft})\mathbf{j} - (9 \text{ ft})\mathbf{k}}{\sqrt{(4.5)^2 + (9)^2 + (9)^2} \text{ ft}} T_{BD}$$
$$= \left(\frac{T_{BD}}{13.5}\right) (4.5\mathbf{i} - 9\mathbf{j} - 9\mathbf{k})$$

$$\mathbf{F}_{C} = \lambda_{CF} (210 \text{ lb}) = \frac{-9\mathbf{i} - 18\mathbf{j} + 6\mathbf{k}}{\sqrt{(9)^{2} + (18)^{2} + (6)^{2}}} (210 \text{ lb}) = 10 \text{ lb}(-9\mathbf{i} - 18\mathbf{j} + 6\mathbf{k})$$

$$\begin{vmatrix} 4.5 & 0 & 9 \\ 0 & 9 & 0 \\ 4.5 & -9 & -9 \end{vmatrix} \left( \frac{T_{BD}}{13.5\sqrt{101.25}} \right) + \begin{vmatrix} 4.5 & 0 & 9 \\ 0 & 18 & 0 \\ -9 & -18 & 6 \end{vmatrix} \left( \frac{10 \text{ lb}}{\sqrt{101.25}} \right) = 0$$

#### **PROBLEM 4.116 CONTINUED**

$$\frac{\left(-364.5 - 364.5\right)}{13.5\sqrt{101.25}}T_{BD} + \frac{\left(486 + 1458\right)}{\sqrt{101.25}}(10 \text{ lb}) = 0$$

 $T_{RD} = 360.00 \text{ lb}$ 

and

or  $T_{BD} = 360 \text{ lb} \blacktriangleleft$ 

$$\Sigma M_{AD} = 0$$
:  $\lambda_{AD} \cdot (\mathbf{r}_{B/A} \times \mathbf{T}_{BE}) + \lambda_{AD} \cdot (\mathbf{r}_{C/A} \times \mathbf{F}_{C}) = 0$ 

where

$$\lambda_{AD} = \frac{(4.5 \text{ ft})\mathbf{i} - (9 \text{ ft})\mathbf{k}}{\sqrt{(4.5)^2 + (9)^2} \text{ ft}} = \frac{1}{\sqrt{101.25}} (4.5\mathbf{i} - 9\mathbf{k})$$

$$\mathbf{r}_{B/A} = (9 \text{ ft})\mathbf{j}$$

$$\mathbf{r}_{C/A} = (18 \text{ ft})\mathbf{j}$$

$$\mathbf{T}_{BE} = \lambda_{BE} T_{BE} = \frac{(4.5 \text{ ft})\mathbf{i} - (9 \text{ ft})\mathbf{j} + (9 \text{ ft})\mathbf{k}}{\sqrt{(4.5)^2 + (9)^2 + (9)^2}} T_{BE} = \frac{T_{BE}}{13.5} (4.5\mathbf{i} - 9\mathbf{j} + 9\mathbf{k})$$

$$\begin{vmatrix} 4.5 & 0 & -9 \\ 0 & 9 & 0 \\ 4.5 & -9 & 9 \end{vmatrix} \left( \frac{T_{BE}}{13.5\sqrt{101.25}} \right) + \begin{vmatrix} 4.5 & 0 & -9 \\ 0 & 18 & 0 \\ -9 & -18 & 6 \end{vmatrix} \left( \frac{10 \text{ lb}}{\sqrt{101.25}} \right) = 0$$

$$\frac{\left(364.5 + 364.5\right)}{13.5\sqrt{101.25}}T_{BE} + \frac{\left(486 - 1458\right)10 \text{ lb}}{\sqrt{101.25}} = 0$$

 $T_{BE} = 180.0 \text{ lb}$ 

or

or  $T_{BE} = 180.0 \text{ lb} \blacktriangleleft$ 

or 
$$T_{BE} = 100.0 \text{ to}$$

$$\Sigma F_x = 0: \quad A_x + (T_{BD})_x + (T_{BE})_x - (F_C)_x = 0$$

$$A_x + \left(\frac{4.5}{13.5}\right)360 + \left(\frac{4.5}{13.5}\right)180 - \left(\frac{9}{21}\right)210 = 0$$

$$A_x = -90.0 \text{ lb}$$

$$\Sigma F_{v} = 0$$
:  $A_{v} - (T_{BD})_{v} - (T_{BE})_{v} - (F_{C})_{v} = 0$ 

$$A_y - \left(\frac{9}{13.5}\right)360 - \left(\frac{9}{13.5}\right)180 - \left(\frac{18}{21}\right)210 = 0$$

$$\therefore A_v = 540 \text{ lb}$$

$$\Sigma F_z = 0$$
:  $A_z - (T_{BD})_z + (T_{BE})_z + (F_C)_z = 0$ 

$$A_z - \left(\frac{9}{13.5}\right)360 + \left(\frac{9}{13.5}\right)180 + \left(\frac{6}{21}\right)210 = 0$$

$$A_7 = 60.0 \text{ lb}$$

or 
$$\mathbf{A} = -(90.0 \text{ lb})\mathbf{i} + (540 \text{ lb})\mathbf{j} + (60.0 \text{ lb})\mathbf{k} \blacktriangleleft$$