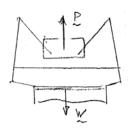


The drum lifter shown is used to lift a steel drum. Knowing that the mass of the drum and its contents is 240 kg, determine the forces exerted at *F* and *H* on member *DFH*.

SOLUTION

FBD System:



$$\dagger \Sigma F_{y} = 0;$$

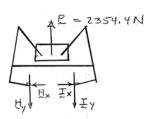
$$P - W = 0$$

$$P = W$$

$$= (240 \text{ kg})(9.81 \text{ m/s}^2)$$

$$P = 2354.4 \text{ N}$$

FBD machine:



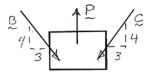
Symmetry:
$$H_x = I_x$$

$$H_y = I_y$$

$$\uparrow \Sigma F_y = 0: P - 2H_y = 0$$

$$H_y = \frac{P}{2} = 1177.2 \text{ N}$$

FBD ABC:



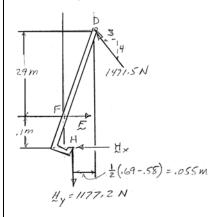
Symmetry:
$$C = B$$

$$\Sigma F_{y} = 0: P - 2\frac{4}{5}B = 0$$

$$B = \frac{5}{8}P = 1471.5 \text{ N}$$

PROBLEM 6.137 CONTINUED

FBD DFH:

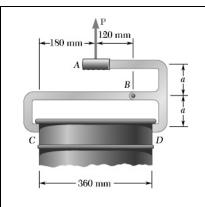


$$\sum M_H = 0: -(0.1 \text{ m}) F + (0.39 \text{ m}) \left(\frac{3}{5}1471.5 \text{ N}\right)$$

$$-(0.055 \text{ m}) \left(\frac{4}{5}1471.5 \text{ N}\right) = 0$$

$$F = 3973.05 \text{ N} \qquad \mathbf{F} = 3.97 \text{ kN} \longrightarrow \blacktriangleleft$$

 $H = 3.31 \text{ kN} 20.9^{\circ}$



A small barrel having a mass of 72 kg is lifted by a pair of tongs as shown. Knowing that a = 100 mm, determine the forces exerted at B and D on tong ABD.

SOLUTION

Notes: From FBD whole, by inspection,

FBB ABD:

$$P = W = mg = (72 \text{ kg})(9.81 \text{ m/s}^2)$$

$$P = 706.32 \text{ N}$$

BC is a two-force member: $B_x = 3B_y$

$$\sum M_D = 0: (0.1 \text{ m}) B_x + (0.06 \text{ m}) B_y - (0.18 \text{ m}) P = 0$$

$$3B_{\rm v} + 0.6B_{\rm v} = 1.8P$$

$$B_y = \frac{P}{2} = 353.16 \text{ N}$$

$$B_x = \frac{3P}{2} = 1059.48 \text{ N}$$

and **B** = 1.117 kN \nearrow 18.43°

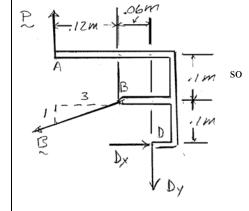
$$\longrightarrow \Sigma F_x = 0: -B_x + D_x = 0$$

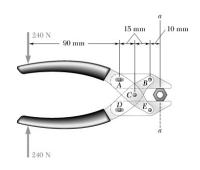
$$D_x = \frac{3P}{2} = 1059.48 \text{ N}$$

$$\uparrow \Sigma F_y = 0: P - B_y - D_y = 0$$

$$D_y = P - \frac{P}{2} = 353.16 \text{ N}$$

so **D** = 1.117 kN $\sqrt{}$ 18.43°

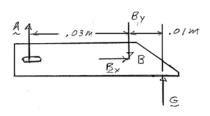




Determine the magnitude of the ripping forces exerted along line aa on the nut when two 240-N forces are applied to the handles as shown. Assume that pins A and D slide freely in slots cut in the jaws.

SOLUTION

FBD jaw AB:



$$\longrightarrow \Sigma F_x = 0$$
: $B_x = 0$

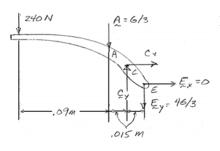
$$(\Sigma M_B = 0: (0.01 \text{ m})G - (0.03 \text{ m})A = 0$$

$$A = \frac{G}{3}$$

$$\uparrow \Sigma F_y = 0 : A + G - B_y = 0$$

$$B_y = A + G = \frac{4G}{3}$$

FBD handle ACE:

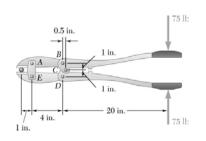


By symmetry and FBD jaw DE: $D = A = \frac{G}{3}$, $E_x = B_x = 0$,

$$E_y = B_y = \frac{4G}{3}$$

$$(\Sigma M_C = 0: (0.105 \text{ m})(240 \text{ N}) + (0.015 \text{ m})\frac{G}{3} - (0.015 \text{ m})\frac{4G}{3} = 0$$

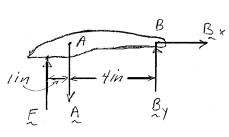
G = 1680 N



In using the bolt cutter shown, a worker applies two 75-lb forces to the handles. Determine the magnitude of the forces exerted by the cutter on the bolt.

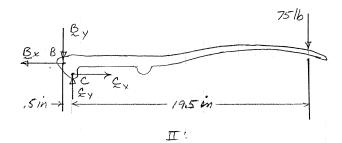
SOLUTION

FBD Cutter AB:



FBD I: $\longrightarrow \Sigma F_x = 0$: $B_x = 0$

FBD handle BC:



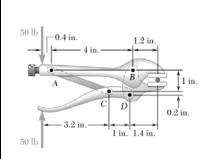
FBD II:
$$\sum M_C = 0$$
: $(0.5 \text{ in.}) B_y - (19.5 \text{ in.}) 75 \text{ lb} = 0$

$$B_y = 2925 \text{ lb}$$

Then

FBD I:
$$(\Sigma M_A = 0: (4 \text{ in.})B_y - (1 \text{ in.})F = 0$$
 $F = 4B_y$

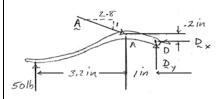
$$F = 11700 \text{ lb} = 11.70 \text{ kips} \blacktriangleleft$$



Determine the magnitude of the gripping forces produced when two 50-lb forces are applied as shown.

SOLUTION

FBD handle CD:

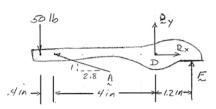


$$\sum M_D = 0: -(4.2 \text{ in.})(50 \text{ lb}) - (0.2 \text{ in.})\frac{2.8}{\sqrt{8.84}}A$$

$$+ \left(1 \text{ in.}\right) \left(\frac{1}{\sqrt{8.84}}A\right) = 0$$

$$A = 477.27\sqrt{8.84}$$
 lb

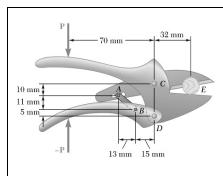
FBD handle AD:



$$\left(\sum \Delta M_D = 0: (4.4 \text{ in.})(50 \text{ lb}) - (4 \text{ in.}) \frac{1}{\sqrt{8.84}} (477.27 \sqrt{8.84} \text{ lb})\right)$$

$$+(1.2 \text{ in.})F = 0$$

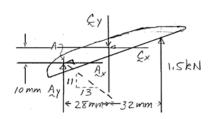
 $F = 1.408 \text{ kips} \blacktriangleleft$



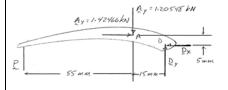
The compound-lever pruning shears shown can be adjusted by placing pin *A* at various ratchet positions on blade *ACE*. Knowing that 1.5-kN vertical forces are required to complete the pruning of a small branch, determine the magnitude *P* of the forces that must be applied to the handles when the shears are adjusted as shown.

SOLUTION

FBD cutter AC:



FBD handle AD:



$$\sum M_C = 0$$
: (32 mm)1.5 KN - (28 mm) A_y - (10 mm) A_x = 0

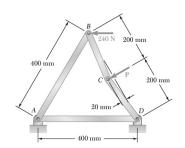
$$10A_x + 28\left(\frac{11}{13}A_x\right) = 48 \text{ kN}$$

$$A_x = 1.42466 \text{ kN}$$

$$A_{\rm v} = 1.20548 \text{ kN}$$

$$\sum M_D = 0$$
: $(15 \text{ mm})(1.20548 \text{ kN}) - (5 \text{ mm})(1.42466 \text{ kN})$
 $-(70 \text{ mm})P = 0$

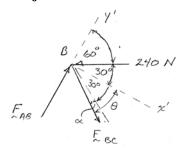
$$P = 0.1566 \text{ kN} = 156.6 \text{ N} \blacktriangleleft$$



Determine the force \mathbf{P} which must be applied to the toggle BCD To maintain equilibrium in the position shown.

SOLUTION

FBD joint B:



Note:

$$\theta = 30^{\circ} + \alpha$$

$$= 30^{\circ} + \tan^{-1} \frac{20}{200}$$

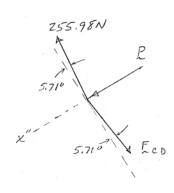
$$= 30^{\circ} + 5.711^{\circ}$$

$$= 35.711^{\circ}$$

$$\Sigma F_{x'} = 0: F_{BC} \cos 35.711^{\circ} - (240 \text{ N}) \cos 30^{\circ} = 0$$

$$F_{BC} = 255.98 \text{ N T}$$

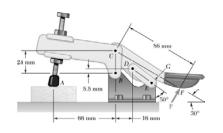
FBD joint C:



By symmetry: $F_{CD} = 255.98 \text{ N}$

$$\sum F_{x''} = 0$$
: $P - 2(255.98 \text{ N})\sin 5.711^\circ = 0$

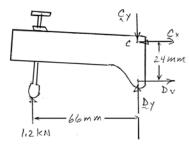
 $P = 50.9 \text{ N} 30.0^{\circ}$



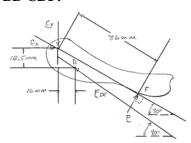
In the locked position shown, the toggle clamp exerts at A a vertical 1.2-kN force on the wooden block, and handle CF rests against the stop at G. Determine the force \mathbf{P} required to release the clamp. (*Hint:* To release the clamp, the forces of contact at G must be zero.)

SOLUTION

FBD BC:



FBD CDF:



$$\sum M_B = 0: (24 \text{ mm})C_x - (66 \text{ mm})(1.2 \text{ kN}) = 0$$

$$C_x = 3.3 \text{ kN}$$

$$EF_x = 0: D_x - C_x = 0 \qquad D_x = 3.3 \text{ kN}$$

$$\sum M_C = 0: (86 \text{ mm})P$$

$$-[18.5 mm - (16 mm) \tan 40^\circ](F_{DE} \cos 40^\circ) = 0$$

$$F_{DE} = 22.124 P$$

$$EF_x = 0: C_x - F_{DE} \cos 40^\circ + P \sin 30^\circ = 0$$

$$3.3 \text{ kN} - (22.124 P) \cos 40^\circ + P \sin 30^\circ = 0$$

 $P = 201 \text{ N} \angle 60^{\circ} \blacktriangleleft$

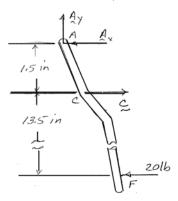


The garden shears shown consist of two blades and two handles. The two handles are connected by pin C and the two blades are connected by pin D. The left blade and the right handle are connected by pin A; the right blade and the left handle are connected by pin B. Determine the magnitude of the forces exerted on the small branch E when two 20-lb forces are applied to the handles as shown.

SOLUTION

Note: By symmetry the vertical components of pin forces ${\bf C}$ and ${\bf D}$ are zero.

FBD handle ACF: (not to scale)

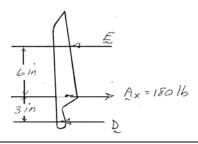


$$\uparrow \Sigma F_y = 0: A_y = 0$$

$$(\Sigma M_C = 0: (13.5 \text{ in.})(20 \text{ lb}) - (1.5 \text{ in.})A_x = 0 \qquad A_x = 180 \text{ lb}$$

$$\to \Sigma F_x = 0: C - A_x - 20 \text{ lb} = 0 \qquad C = (180 + 20) \text{ lb} = 200 \text{ lb}$$

FBD blade DE:



$$\sum M_D = 0$$
: $(9 \text{ in.})E - (3 \text{ in.})(180 \text{ lb}) = 0$
 $E = 60.0 \text{ lb} \blacktriangleleft$