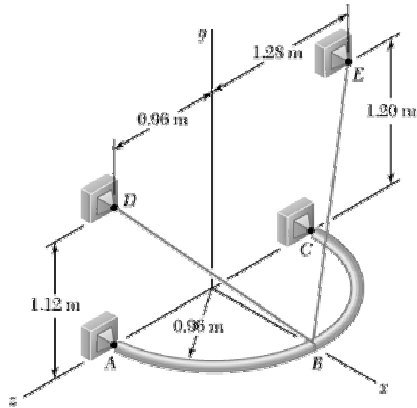


PROBLEM 2.97

For the semicircular ring of Problem 2.91, determine the magnitude and direction of the resultant of the forces exerted by the cables at B knowing that the tensions in cables BD and BE are 220 N and 250 N, respectively.



SOLUTION

For the solutions to Problems 2.91 and 2.92, we have

$$\mathbf{T}_{BD} = -(120 \text{ N})\mathbf{i} + (140 \text{ N})\mathbf{j} + (120 \text{ N})\mathbf{k}$$

$$\mathbf{T}_{BE} = -(120 \text{ N})\mathbf{i} + (150 \text{ N})\mathbf{j} - (160 \text{ N})\mathbf{k}$$

Then:

$$\begin{aligned}\mathbf{R}_B &= \mathbf{T}_{BD} + \mathbf{T}_{BE} \\ &= -(240 \text{ N})\mathbf{i} + (290 \text{ N})\mathbf{j} - (40 \text{ N})\mathbf{k}\end{aligned}$$

and

$$R = 378.55 \text{ N}$$

$$R_B = 379 \text{ N} \blacktriangleleft$$

$$\cos \theta_x = -\frac{240}{378.55} = -0.6340$$

$$\theta_x = 129.3^\circ \blacktriangleleft$$

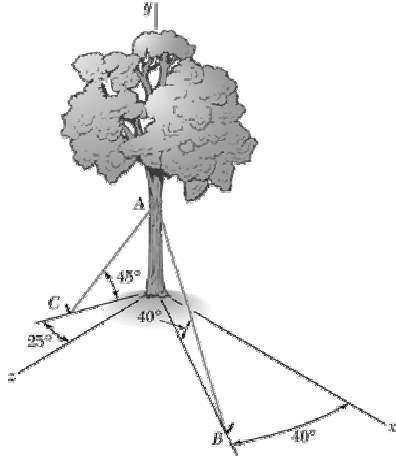
$$\cos \theta_y = \frac{290}{378.55} = 0.7661$$

$$\theta_y = 40.0^\circ \blacktriangleleft$$

$$\cos \theta_z = -\frac{40}{378.55} = -0.1057$$

$$\theta_z = 96.1^\circ \blacktriangleleft$$

PROBLEM 2.98



To stabilize a tree partially uprooted in a storm, cables AB and AC are attached to the upper trunk of the tree and then are fastened to steel rods anchored in the ground. Knowing that the tension in AB is 920 lb and that the resultant of the forces exerted at A by cables AB and AC lies in the yz plane, determine (a) the tension in AC , (b) the magnitude and direction of the resultant of the two forces.

SOLUTION

Have

$$\mathbf{T}_{AB} = (920 \text{ lb})(\sin 50^\circ \cos 40^\circ \mathbf{i} - \cos 50^\circ \mathbf{j} + \sin 50^\circ \sin 40^\circ \mathbf{j})$$

$$\mathbf{T}_{AC} = T_{AC}(-\cos 45^\circ \sin 25^\circ \mathbf{i} - \sin 45^\circ \mathbf{j} + \cos 45^\circ \cos 25^\circ \mathbf{j})$$

(a)

$$\mathbf{R}_A = \mathbf{T}_{AB} + \mathbf{T}_{AC}$$

$$(R_A)_x = 0$$

$$\therefore (R_A)_x = \Sigma F_x = 0: (920 \text{ lb})\sin 50^\circ \cos 40^\circ - T_{AC} \cos 45^\circ \sin 25^\circ = 0$$

or

$$T_{AC} = 1806.60 \text{ lb}$$

$$T_{AC} = 1807 \text{ lb} \blacktriangleleft$$

(b)

$$(R_A)_y = \Sigma F_y: -(920 \text{ lb})\cos 50^\circ - (1806.60 \text{ lb})\sin 45^\circ$$

$$(R_A)_y = -1868.82 \text{ lb}$$

$$(R_A)_z = \Sigma F_z: (920 \text{ lb})\sin 50^\circ \sin 40^\circ + (1806.60 \text{ lb})\cos 45^\circ \cos 25^\circ$$

$$(R_A)_z = 1610.78 \text{ lb}$$

$$\therefore \mathbf{R}_A = -(1868.82 \text{ lb})\mathbf{j} + (1610.78 \text{ lb})\mathbf{k}$$

Then:

$$R_A = 2467.2 \text{ lb}$$

$$R_A = 2.47 \text{ kips} \blacktriangleleft$$

PROBLEM 2.98 CONTINUED

and

$$\cos \theta_x = \frac{0}{2467.2} = 0$$

$$\theta_x = 90.0^\circ \blacktriangleleft$$

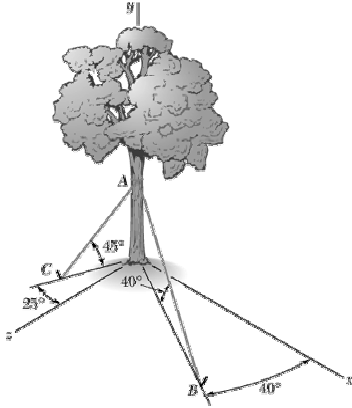
$$\cos \theta_y = \frac{-1868.82}{2467.2} = -0.7560$$

$$\theta_y = 139.2^\circ \blacktriangleleft$$

$$\cos \theta_z = \frac{1610.78}{2467.2} = 0.65288$$

$$\theta_z = 49.2^\circ \blacktriangleleft$$

PROBLEM 2.99



To stabilize a tree partially uprooted in a storm, cables AB and AC are attached to the upper trunk of the tree and then are fastened to steel rods anchored in the ground. Knowing that the tension in AC is 850 lb and that the resultant of the forces exerted at A by cables AB and AC lies in the yz plane, determine (a) the tension in AB , (b) the magnitude and direction of the resultant of the two forces.

SOLUTION

Have

$$\mathbf{T}_{AB} = T_{AB}(\sin 50^\circ \cos 40^\circ \mathbf{i} - \cos 50^\circ \mathbf{j} + \sin 50^\circ \sin 40^\circ \mathbf{j})$$

$$\mathbf{T}_{AC} = (850 \text{ lb})(-\cos 45^\circ \sin 25^\circ \mathbf{i} - \sin 45^\circ \mathbf{j} + \cos 45^\circ \cos 25^\circ \mathbf{j})$$

(a)

$$(R_A)_x = 0$$

$$\therefore (R_A)_x = \Sigma F_x = 0: T_{AB} \sin 50^\circ \cos 40^\circ - (850 \text{ lb}) \cos 45^\circ \sin 25^\circ = 0$$

$$T_{AB} = 432.86 \text{ lb}$$

$$T_{AB} = 433 \text{ lb} \blacktriangleleft$$

(b)

$$(R_A)_y = \Sigma F_y: -(432.86 \text{ lb}) \cos 50^\circ - (850 \text{ lb}) \sin 45^\circ$$

$$(R_A)_y = -879.28 \text{ lb}$$

$$(R_A)_z = \Sigma F_z: (432.86 \text{ lb}) \sin 50^\circ \sin 40^\circ + (850 \text{ lb}) \cos 45^\circ \cos 25^\circ$$

$$(R_A)_z = 757.87 \text{ lb}$$

$$\therefore \mathbf{R}_A = -(879.28 \text{ lb})\mathbf{j} + (757.87 \text{ lb})\mathbf{k}$$

$$R_A = 1160.82 \text{ lb}$$

$$R_A = 1.161 \text{ kips} \blacktriangleleft$$

$$\cos \theta_x = \frac{0}{1160.82} = 0$$

$$\theta_x = 90.0^\circ \blacktriangleleft$$

$$\cos \theta_y = \frac{-879.28}{1160.82} = -0.75746$$

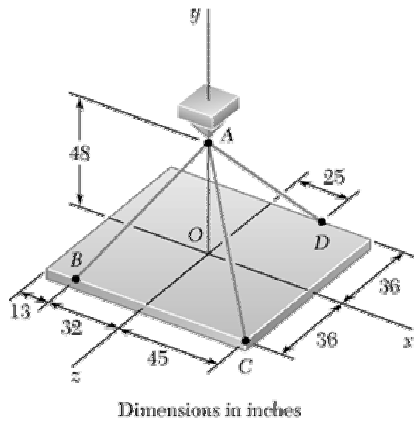
$$\theta_y = 139.2^\circ \blacktriangleleft$$

$$\cos \theta_z = \frac{757.87}{1160.82} = 0.65287$$

$$\theta_z = 49.2^\circ \blacktriangleleft$$

PROBLEM 2.100

For the plate of Problem 2.89, determine the tension in cables AB and AD knowing that the tension of cable AC is 27 lb and that the resultant of the forces exerted by the three cables at A must be vertical.



SOLUTION

With:

$$\overrightarrow{AC} = (45 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} + (36 \text{ in.})\mathbf{k}$$

$$AC = \sqrt{(45 \text{ in.})^2 + (-48 \text{ in.})^2 + (36 \text{ in.})^2} = 75 \text{ in.}$$

$$\mathbf{T}_{AC} = T_{AC}\boldsymbol{\lambda}_{AC} = T_{AC} \frac{\overrightarrow{AC}}{AC} = \frac{27 \text{ lb}}{75 \text{ in.}} [(45 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} + (36 \text{ in.})\mathbf{k}]$$

$$\mathbf{T}_{AC} = (16.2 \text{ lb})\mathbf{i} - (17.28 \text{ lb})\mathbf{j} + (12.96 \text{ lb})\mathbf{k}$$

and

$$\overrightarrow{AB} = (-32 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} + (36 \text{ in.})\mathbf{k}$$

$$AB = \sqrt{(-32 \text{ in.})^2 + (-48 \text{ in.})^2 + (36 \text{ in.})^2} = 68 \text{ in.}$$

$$\mathbf{T}_{AB} = T_{AB}\boldsymbol{\lambda}_{AB} = T_{AB} \frac{\overrightarrow{AB}}{AB} = \frac{T_{AB}}{68 \text{ in.}} [(-32 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} + (36 \text{ in.})\mathbf{k}]$$

$$\mathbf{T}_{AB} = T_{AB}(-0.4706\mathbf{i} - 0.7059\mathbf{j} + 0.5294\mathbf{k})$$

and

$$\overrightarrow{AD} = (25 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} - (36 \text{ in.})\mathbf{k}$$

$$AD = \sqrt{(25 \text{ in.})^2 + (-48 \text{ in.})^2 + (-36 \text{ in.})^2} = 65 \text{ in.}$$

$$\mathbf{T}_{AD} = T_{AD}\boldsymbol{\lambda}_{AD} = T_{AD} \frac{\overrightarrow{AD}}{AD} = \frac{T_{AD}}{65 \text{ in.}} [(25 \text{ in.})\mathbf{i} - (48 \text{ in.})\mathbf{j} - (36 \text{ in.})\mathbf{k}]$$

$$\mathbf{T}_{AD} = T_{AD}(0.3846\mathbf{i} - 0.7385\mathbf{j} - 0.5538\mathbf{k})$$

PROBLEM 2.100 CONTINUED

Now

$$\begin{aligned}\mathbf{R} &= \mathbf{T}_{AB} + \mathbf{T}_{AD} + \mathbf{T}_{AD} \\ &= T_{AB}(-0.4706\mathbf{i} - 0.7059\mathbf{j} + 0.5294\mathbf{k}) + [(16.2 \text{ lb})\mathbf{i} - (17.28 \text{ lb})\mathbf{j} + (12.96)\mathbf{k}] \\ &\quad + T_{AD}(0.3846\mathbf{i} - 0.7385\mathbf{j} - 0.5538\mathbf{k})\end{aligned}$$

Since R must be vertical, the \mathbf{i} and \mathbf{k} components of this sum must be zero.

Hence:

$$-0.4706T_{AB} + 0.3846T_{AD} + 16.2 \text{ lb} = 0 \quad (1)$$

$$0.5294T_{AB} - 0.5538T_{AD} + 12.96 \text{ lb} = 0 \quad (2)$$

Solving (1) and (2), we obtain:

$$T_{AB} = 244.79 \text{ lb}, \quad T_{AD} = 257.41 \text{ lb}$$

$$T_{AB} = 245 \text{ lb} \blacktriangleleft$$

$$T_{AD} = 257 \text{ lb} \blacktriangleleft$$