

Classify each of the structures shown as completely, partially, or improperly constrained; if completely constrained, further classify it as determinate or indeterminate. (All members can act both in tension and in compression.)

#### **SOLUTION**

Structure (a):

Non-simple truss with r = 4, m = 16, n = 10

so m + r = 20 = 2n, but must examine further.

**FBD Sections:** 

FBD I:  $\Sigma M_A = 0 \Rightarrow T_1$ 

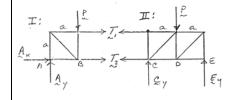
II: 
$$\Sigma F_x = 0 \implies T_2$$

I: 
$$\Sigma F_x = 0 \implies A_x$$

I: 
$$\Sigma F_{y} = 0 \implies A_{y}$$

II: 
$$\Sigma M_E = 0 \implies C_y$$

II: 
$$\Sigma F_{v} = 0 \implies E_{v}$$



Since each section is a simple truss with reactions determined,

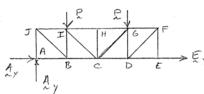
structure is completely constrained and determinate.

Non-simple truss with r = 3, m = 16, n = 10

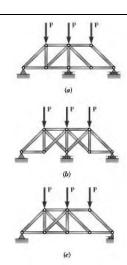
**Structure (b):** 

so m + r = 19 < 2n = 20 : structure is partially constrained

**Structure (c):** 



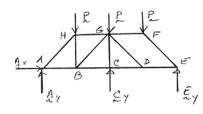
Simple truss with r = 3, m = 17, n = 10m + r = 20 = 2n, but the horizontal reaction forces  $A_x$  and  $E_x$  are collinear and no equilibrium equation will resolve them, so the structure is improperly constrained and indeterminate



Classify each of the structures shown as completely, partially, or improperly constrained; if completely constrained, further classify it as determinate or indeterminate. (All members can act both in tension and in compression.)

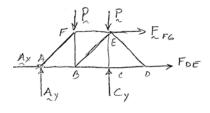
#### **SOLUTION**

#### Structure (a):



Non-simple truss with r = 4, m = 12, n = 8 so r + m = 16 = 2n, check for determinacy:

One can solve joint F for forces in EF, FG and then solve joint E for  $\mathbf{E}_{v}$  and force in DE.

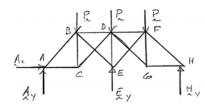


This leaves a simple truss ABCDGH with

$$r = 3$$
,  $m = 9$ ,  $n = 6$  so  $r + m = 12 = 2n$ 

Structure is completely constrained and determinate

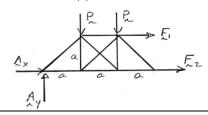
### **Structure (b):**



Simple truss (start with ABC and add joints alphabetically to complete truss) with r = 4, m = 13, n = 8

so 
$$r + m = 17 > 2n = 16$$
 Constrained but indeterminate

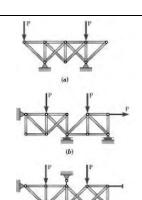
#### **Structure (c):**



Non-simple truss with r = 3, m = 13, n = 8 so r + m = 16 = 2n. To further examine, follow procedure in part (a) above to get truss at left. Since  $\mathbf{F}_1 \neq 0$  (from solution of joint F),

 $\Sigma M_A = aF_1$   $\neq 0$  and there is no equilibrium.

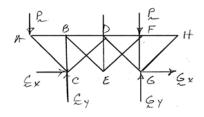
Structure is improperly constrained ◀



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### **SOLUTION**

#### Structure (a):

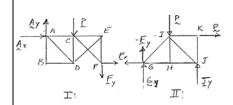


Simple truss (start with ABC and add joints alphabetical to complete truss), with

$$r = 4$$
,  $m = 13$ ,  $n = 8$  so  $r + m = 17 > 2n = 16$ 

Structure is completely constrained but indeterminate. ◀

## **Structure (b):**



From FBD II: 
$$\Sigma M_G = 0 \implies J_v$$

$$\Sigma F_x = 0 \implies F_x$$

FBD I: 
$$\Sigma M_A = 0 \implies F_v$$

$$\Sigma F_{\rm v} = 0 \implies A_{\rm v}$$

$$\Sigma F_x = 0 \implies A_x$$

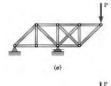
FBD II: 
$$\Sigma F_y = 0 \implies G_y$$

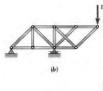
Thus have two simple trusses with all reactions known,

so structure is completely constrained and determinate.

# Structure (c): Structure has r = 4, m = 13, n = 9

so 
$$r + m = 17 < 2n = 18$$
, structure is partially constrained





Classify each of the structures shown as completely, partially, or improperly constrained; if completely constrained, further classify it as determinate or indeterminate. (All members can act both in tension and in compression.)

### **SOLUTION**

Structure (a):

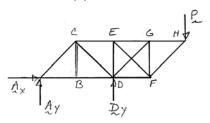
Rigid truss with r = 3, m = 14, n = 8

so

$$r + m = 17 > 2n = 16$$

so completely constrained but indeterminate

**Structure (b):** 



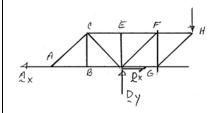
Simple truss (start with ABC and add joints alphabetically), with

$$r = 3, m = 13, n = 8$$

$$r + m = 16 = 2n$$

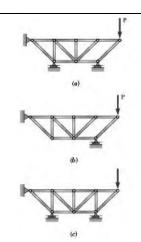
so completely constrained and determinate

**Structure (c):** 



Simple truss with r = 3, m = 13, n = 8 so r + m = 16 = 2n, but horizontal reactions  $(A_x \text{ and } D_x)$  are collinear so cannot be resolved by any equilibrium equation.

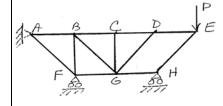
∴ structure is improperly constrained ◀



Classify each of the structures shown as completely, partially, or improperly constrained; if completely constrained, further classify it as determinate or indeterminate. (All members can act both in tension and in compression.)

### **SOLUTION**

### Structure (a):

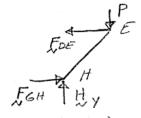


No. of members m = 12

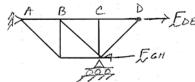
No. of joints n = 8 m + r = 16 = 2n

No. of react. comps. r = 4 unks = eqns

#### FBD of EH:



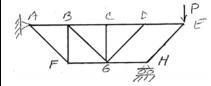
$$\Sigma M_H = 0 \rightarrow F_{DE}; \ \Sigma F_x = 0 \rightarrow F_{GH}; \ \Sigma F_y = 0 \rightarrow H_y$$



Then *ABCDGF* is a simple truss and all forces can be determined.

This example is completely constrained and determinate. ◀

## **Structure (b):**



No. of members m = 12

No. of joints n = 8 m + r = 15 < 2n = 16

No. of react. comps. r = 3 unks < eqns

partially constrained ◀

Note: Quadrilateral DEHG can collapse with joint D moving downward: in (a) the roller at F prevents this action.

# **PROBLEM 6.75 CONTINUED**

**Structure (c):** 

No. of members m = 13

No. of joints

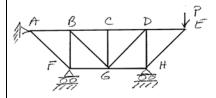
n = 8

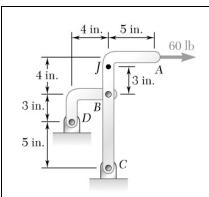
m + r = 17 > 2n = 16

No. of react. comps. r = 4

unks > eqns

completely constrained but indeterminate ◀



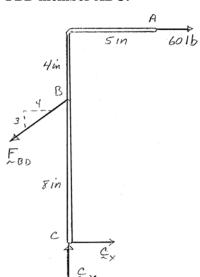


For the frame and loading shown, determine the force acting on member ABC(a) at B, (b) at C.

# **SOLUTION**

FBD member ABC:

Note: BD is a two-force member so  $\mathbf{F}_{BD}$  is through D.



(a) 
$$(\Sigma M_C = 0: (8 \text{ in.}) \left(\frac{4}{5}F_{BD}\right) - (12 \text{ in.})(60 \text{ lb}) = 0$$

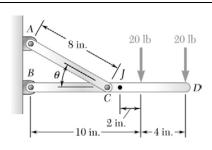
(b) 
$$\longrightarrow \Sigma F_x = 0$$
: 60 lb +  $C_x - \frac{4}{5} (112.5 \text{ lb}) = 0$ 

$$C_x = 30 \text{ lb}$$

$$\uparrow \Sigma F_y = 0: C_y - \frac{3}{5} (112.5 \text{ lb}) = 0$$

$$C_y = 67.5 \text{ lb}$$

so **C** = 73.9 lb  $\angle$ 66.0° ◀



Determine the force in member AC and the reaction at B when (a)  $\theta = 30^{\circ}$ , (b)  $\theta = 60^{\circ}$ .

### **SOLUTION**

**FBD** member BCD:

Note: AC is two-force member so  $\mathbf{F}_{AC}$  is through A.

$$\widehat{BC} = (8 \text{ in.})\cos\theta$$

$$\left(\Sigma M_B = 0: (8 \text{ in.})\cos\theta \left(F_{AC} \sin\theta\right) - (10 \text{ in.})(20 \text{ lb})\right)$$

$$-(14 \text{ in.})(20 \text{ lb}) = 0$$

$$F_{AC} = \frac{60 \text{ lb}}{\sin \theta \cos \theta}$$

$$\rightarrow \Sigma F_x = 0$$
:  $B_x - F_{AC} \cos \theta = 0$   $B_x = \frac{60 \text{ lb}}{\sin \theta}$ 

$$\Sigma F_y = 0$$
:  $B_y + F_{AC} \sin \theta - 20 \text{ lb} - 20 \text{ lb} = 0$ 

$$B_{y} = 40 lb - \frac{60 lb}{\cos \theta}$$

(a) 
$$\theta = 30^{\circ}$$

$$F_{AC} = 138.56 \text{ lb}$$

$$F_{AC} = 138.6 \text{ lb T} \blacktriangleleft$$

$$B_x = 120.0 \text{ lb}$$
  $B_y = -29.28 \text{ lb}$ 

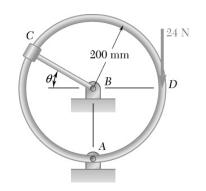
$$B$$
 = 123.5 lb  $\sqrt{13.71}$ ° ◀

(b) 
$$\theta = 60^{\circ}$$

$$F_{AC} = 138.56 \text{ lb}$$

$$F_{AC} = 138.6 \text{ lb T} \blacktriangleleft$$

$$B_x = 69.28 \text{ lb}$$
  $B_y = -80 \text{ lb}$ 



(b)

A circular ring of radius 200 mm is pinned at A and is supported by rod BC, which is fitted with a collar at C that can be moved along the ring. For the position when  $\theta = 35^{\circ}$ , determine (a) the force in rod BC, (b) the reaction at A.

# **SOLUTION**

FBD ring:

(a) 
$$\theta = 35^{\circ}$$
 (  $\Sigma M_A = 0$ : (0.2 m) $F_{BC} \cos 35^{\circ} - (0.2 \text{ m})(24 \text{ N}) = 0$ 

$$F_{BC} = \frac{24 \text{ N}}{\cos 35^{\circ}} = 29.298 \text{ N}$$

C EBC D D D A Ax

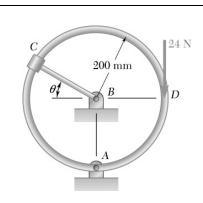
$$A_x = 24 \text{ N}$$

$$\sum F_y = 0$$
:  $A_y + \frac{24 \text{ N}}{\cos 35^\circ} \sin 35^\circ - 24 \text{ N} = 0$ 

$$A_y = 7.195 \text{ N}$$

so  $A = 25.1 \text{ N} \angle 16.69^{\circ} \blacktriangleleft$ 

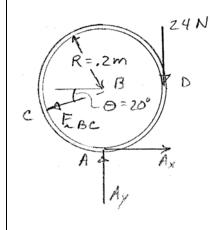
 $F_{BC} = 29.3 \, \text{N C} \blacktriangleleft$ 



Solve Prob. 6.78 when  $\theta = -20^{\circ}$ .

# **SOLUTION**

FBD ring:



(a) 
$$\theta = 20^{\circ} (\Sigma M_A = 0: (0.2 \text{ m})(F_{BC} \cos 20^{\circ}) - (0.2 \text{ m})(24 \text{ N}) = 0$$

$$F_{BC} = \frac{24 \text{ N}}{\cos 20^{\circ}} = 25.54 \text{ N}$$

 $F_{BC} = 25.5 \text{ N C} \blacktriangleleft$ 

$$A_{y} = 32.735 \text{ lb}$$

$$(\Sigma M_B = 0: (0.2 \text{ m}) A_x - (0.2 \text{ m}) (24 \text{ N}) = 0$$

$$A_x = 24 \text{ N}$$

so  $A = 40.6 \text{ N} \angle 53.8^{\circ} \blacktriangleleft$