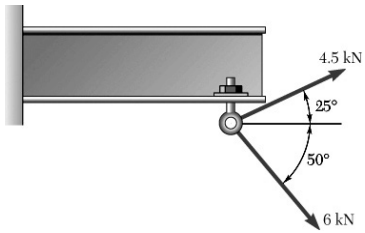


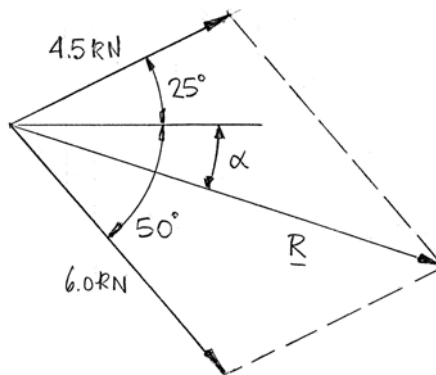
### PROBLEM 2.1



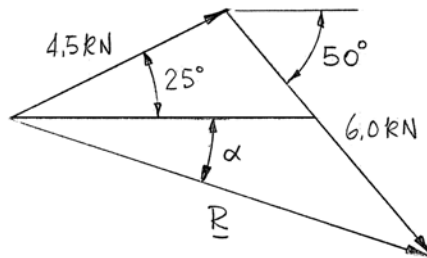
Two forces are applied to an eye bolt fastened to a beam. Determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.

### SOLUTION

(a)



(b)

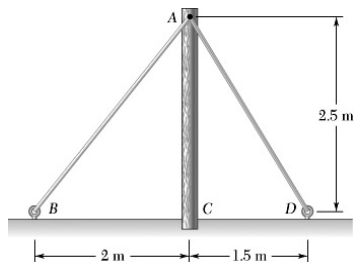


We measure:

$$R = 8.4 \text{ kN}$$

$$\alpha = 19^\circ$$

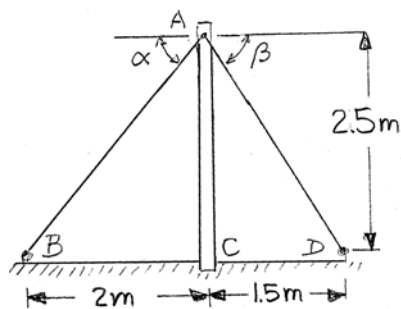
$$\mathbf{R} = 8.4 \text{ kN} \searrow 19^\circ \blacktriangleleft$$



## PROBLEM 2.2

The cable stays  $AB$  and  $AD$  help support pole  $AC$ . Knowing that the tension is 500 N in  $AB$  and 160 N in  $AD$ , determine graphically the magnitude and direction of the resultant of the forces exerted by the stays at  $A$  using (a) the parallelogram law, (b) the triangle rule.

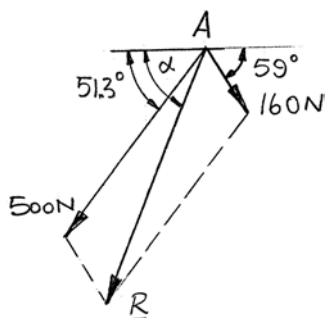
## SOLUTION



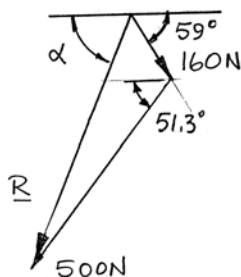
$$\alpha = 51.3^\circ, \beta = 59^\circ$$

We measure:

(a)



(b)

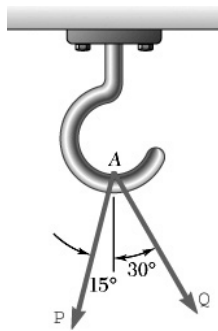


We measure:

$$R = 575 \text{ N}, \alpha = 67^\circ$$

$$\mathbf{R} = 575 \text{ N} \nearrow 67^\circ \blacktriangleleft$$

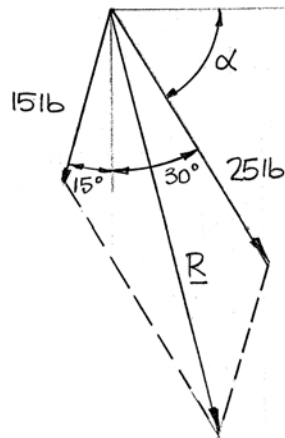
### PROBLEM 2.3



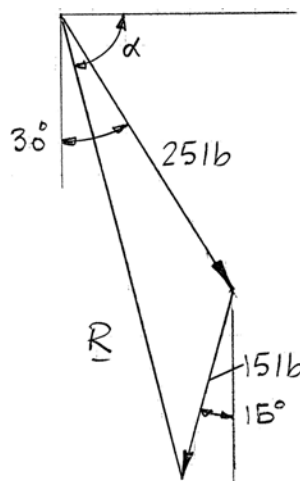
Two forces **P** and **Q** are applied as shown at point **A** of a hook support. Knowing that  $P = 15 \text{ lb}$  and  $Q = 25 \text{ lb}$ , determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.

### SOLUTION

(a)



(b)

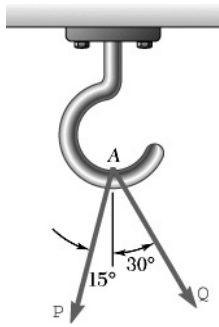


We measure:

$$R = 37 \text{ lb}, \alpha = 76^\circ$$

$$\mathbf{R} = 37 \text{ lb} \searrow 76^\circ \blacktriangleleft$$

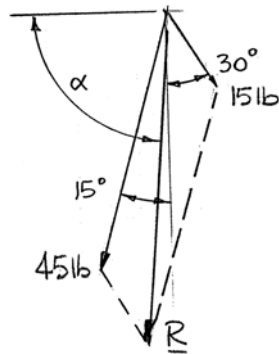
### PROBLEM 2.4



Two forces **P** and **Q** are applied as shown at point **A** of a hook support. Knowing that  $P = 45 \text{ lb}$  and  $Q = 15 \text{ lb}$ , determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.

### SOLUTION

(a)



(b)

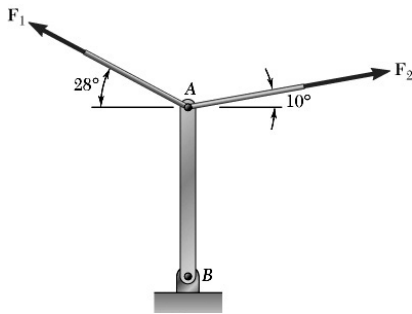


We measure:

$$R = 61.5 \text{ lb}, \alpha = 86.5^\circ$$

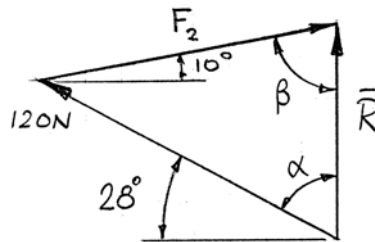
$$\mathbf{R} = 61.5 \text{ lb} \nearrow 86.5^\circ \nwarrow$$

### PROBLEM 2.5



Two control rods are attached at A to lever AB. Using trigonometry and knowing that the force in the left-hand rod is  $F_1 = 120 \text{ N}$ , determine (a) the required force  $F_2$  in the right-hand rod if the resultant  $\mathbf{R}$  of the forces exerted by the rods on the lever is to be vertical, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION



Graphically, by the triangle law

We measure:

$$F_2 \cong 108 \text{ N}$$

$$R \cong 77 \text{ N}$$

By trigonometry: Law of Sines

$$\frac{F_2}{\sin \alpha} = \frac{R}{\sin 38^\circ} = \frac{120}{\sin \beta}$$

$$\alpha = 90^\circ - 28^\circ = 62^\circ, \beta = 180^\circ - 62^\circ - 38^\circ = 80^\circ$$

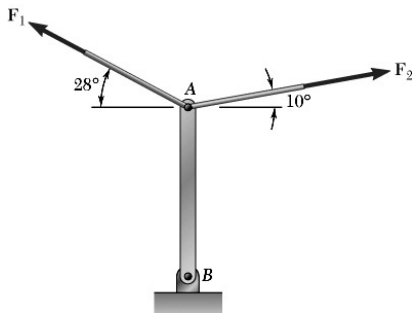
Then:

$$\frac{F_2}{\sin 62^\circ} = \frac{R}{\sin 38^\circ} = \frac{120 \text{ N}}{\sin 80^\circ}$$

$$\text{or (a) } F_2 = 107.6 \text{ N} \blacktriangleleft$$

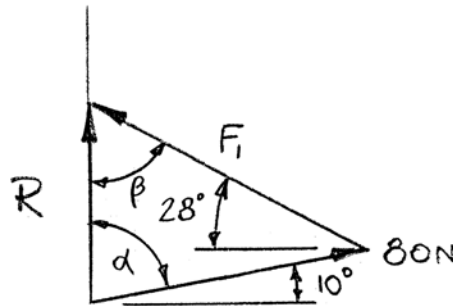
$$(b) \quad R = 75.0 \text{ N} \blacktriangleleft$$

### PROBLEM 2.6



Two control rods are attached at A to lever AB. Using trigonometry and knowing that the force in the right-hand rod is  $F_2 = 80 \text{ N}$ , determine (a) the required force  $F_1$  in the left-hand rod if the resultant  $\mathbf{R}$  of the forces exerted by the rods on the lever is to be vertical, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION



Using the Law of Sines

$$\frac{F_1}{\sin \alpha} = \frac{R}{\sin 38^\circ} = \frac{80}{\sin \beta}$$

$$\alpha = 90^\circ - 10^\circ = 80^\circ, \beta = 180^\circ - 80^\circ - 38^\circ = 62^\circ$$

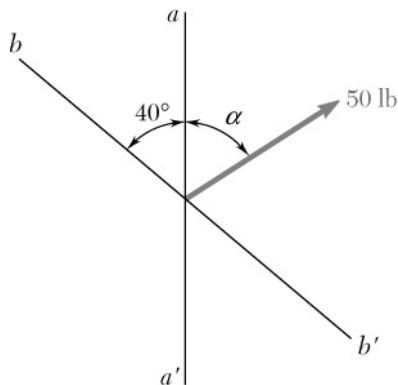
Then:

$$\frac{F_1}{\sin 80^\circ} = \frac{R}{\sin 38^\circ} = \frac{80 \text{ N}}{\sin 62^\circ}$$

$$\text{or (a) } F_1 = 89.2 \text{ N} \blacktriangleleft$$

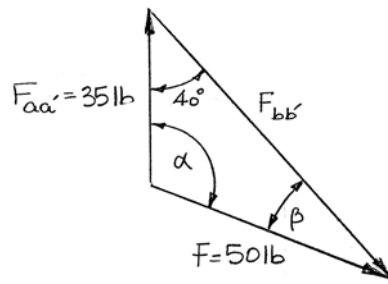
$$(b) R = 55.8 \text{ N} \blacktriangleleft$$

### PROBLEM 2.7



The 50-lb force is to be resolved into components along lines  $a-a'$  and  $b-b'$ . (a) Using trigonometry, determine the angle  $\alpha$  knowing that the component along  $a-a'$  is 35 lb. (b) What is the corresponding value of the component along  $b-b'$ ?

### SOLUTION



Using the triangle rule and the Law of Sines

$$(a) \quad \frac{\sin \beta}{35 \text{ lb}} = \frac{\sin 40^\circ}{50 \text{ lb}}$$

$$\sin \beta = 0.44995$$

$$\beta = 26.74^\circ$$

Then:

$$\alpha + \beta + 40^\circ = 180^\circ$$

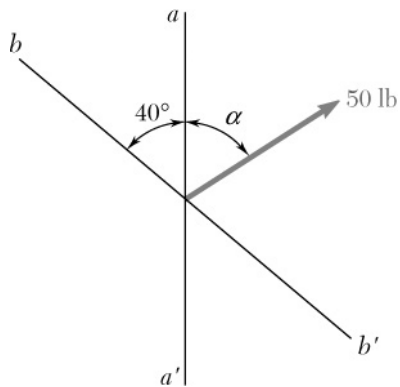
$$\alpha = 113.3^\circ \blacktriangleleft$$

(b) Using the Law of Sines:

$$\frac{F_{bb'}}{\sin \alpha} = \frac{50 \text{ lb}}{\sin 40^\circ}$$

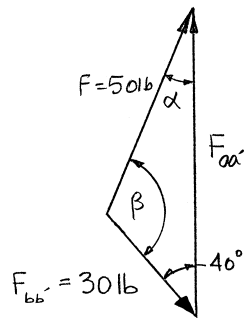
$$F_{bb'} = 71.5 \text{ lb} \blacktriangleleft$$

### PROBLEM 2.8



The 50-lb force is to be resolved into components along lines  $a-a'$  and  $b-b'$ . (a) Using trigonometry, determine the angle  $\alpha$  knowing that the component along  $b-b'$  is 30 lb. (b) What is the corresponding value of the component along  $a-a'$ ?

### SOLUTION



Using the triangle rule and the Law of Sines

$$(a) \quad \frac{\sin \alpha}{30 \text{ lb}} = \frac{\sin 40^\circ}{50 \text{ lb}}$$

$$\sin \alpha = 0.3857$$

$$\alpha = 22.7^\circ \blacktriangleleft$$

$$(b) \quad \alpha + \beta + 40^\circ = 180^\circ$$

$$\beta = 117.31^\circ$$

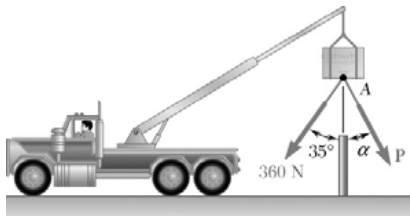
$$\frac{F_{aa'}}{\sin \beta} = \frac{50 \text{ lb}}{\sin 40^\circ}$$

$$F_{aa'} = 50 \text{ lb} \left( \frac{\sin \beta}{\sin 40^\circ} \right)$$

$$F_{aa'} = 69.1 \text{ lb} \blacktriangleleft$$

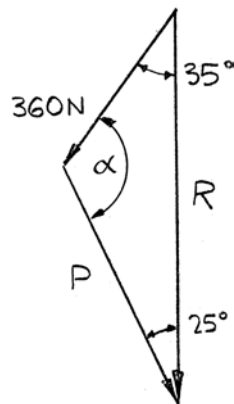


### PROBLEM 2.9



To steady a sign as it is being lowered, two cables are attached to the sign at A. Using trigonometry and knowing that  $\alpha = 25^\circ$ , determine (a) the required magnitude of the force  $\mathbf{P}$  if the resultant  $\mathbf{R}$  of the two forces applied at A is to be vertical, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION



Using the triangle rule and the Law of Sines

Have:

$$\begin{aligned}\alpha &= 180^\circ - (35^\circ + 25^\circ) \\ &= 120^\circ\end{aligned}$$

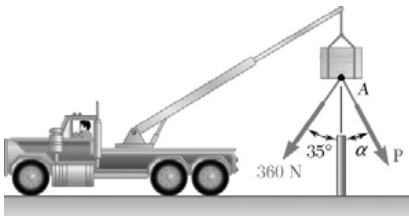
Then:

$$\frac{P}{\sin 35^\circ} = \frac{R}{\sin 120^\circ} = \frac{360 \text{ N}}{\sin 25^\circ}$$

$$\text{or } (a) \ P = 489 \text{ N} \blacktriangleleft$$

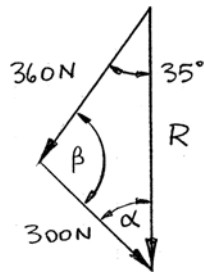
$$(b) \ R = 738 \text{ N} \blacktriangleleft$$

### PROBLEM 2.10



To steady a sign as it is being lowered, two cables are attached to the sign at A. Using trigonometry and knowing that the magnitude of  $\mathbf{P}$  is 300 N, determine (a) the required angle  $\alpha$  if the resultant  $\mathbf{R}$  of the two forces applied at A is to be vertical, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION



Using the triangle rule and the Law of Sines

(a) Have: 
$$\frac{360 \text{ N}}{\sin \alpha} = \frac{300 \text{ N}}{\sin 35^\circ}$$
$$\sin \alpha = 0.68829$$

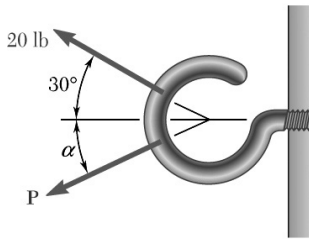
$$\alpha = 43.5^\circ \blacktriangleleft$$

(b) 
$$\beta = 180 - (35^\circ + 43.5^\circ)$$
$$= 101.5^\circ$$

Then: 
$$\frac{R}{\sin 101.5^\circ} = \frac{300 \text{ N}}{\sin 35^\circ}$$

$$\text{or } R = 513 \text{ N} \blacktriangleleft$$

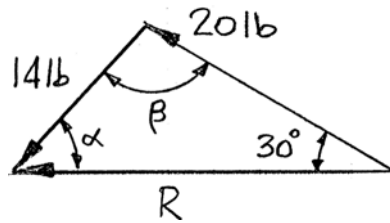
### PROBLEM 2.11



Two forces are applied as shown to a hook support. Using trigonometry and knowing that the magnitude of  $\mathbf{P}$  is 14 lb, determine (a) the required angle  $\alpha$  if the resultant  $\mathbf{R}$  of the two forces applied to the support is to be horizontal, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION

Using the triangle rule and the Law of Sines



(a) Have:

$$\frac{20 \text{ lb}}{\sin \alpha} = \frac{14 \text{ lb}}{\sin 30^\circ}$$

$$\sin \alpha = 0.71428$$

$$\alpha = 45.6^\circ \blacktriangleleft$$

(b)

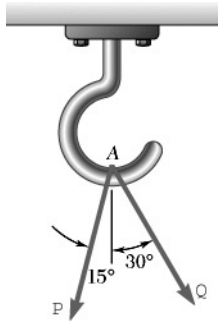
$$\begin{aligned} \beta &= 180^\circ - (30^\circ + 45.6^\circ) \\ &= 104.4^\circ \end{aligned}$$

Then:

$$\frac{R}{\sin 104.4^\circ} = \frac{14 \text{ lb}}{\sin 30^\circ}$$

$$R = 27.1 \text{ lb} \blacktriangleleft$$

### PROBLEM 2.12

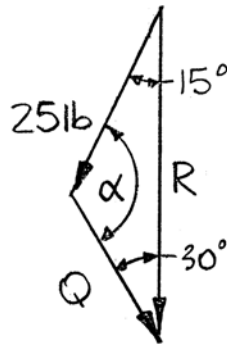


For the hook support of Problem 2.3, using trigonometry and knowing that the magnitude of **P** is 25 lb, determine (a) the required magnitude of the force **Q** if the resultant **R** of the two forces applied at A is to be vertical, (b) the corresponding magnitude of **R**.

**Problem 2.3:** Two forces **P** and **Q** are applied as shown at point A of a hook support. Knowing that  $P = 15$  lb and  $Q = 25$  lb, determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.

### SOLUTION

Using the triangle rule and the Law of Sines



(a) Have:

$$\frac{Q}{\sin 15^\circ} = \frac{25 \text{ lb}}{\sin 30^\circ}$$

$$Q = 12.94 \text{ lb} \blacktriangleleft$$

(b)

$$\begin{aligned}\beta &= 180^\circ - (15^\circ + 30^\circ) \\ &= 135^\circ\end{aligned}$$

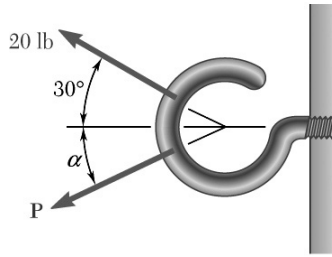
Thus:

$$\frac{R}{\sin 135^\circ} = \frac{25 \text{ lb}}{\sin 30^\circ}$$

$$R = 25 \text{ lb} \left( \frac{\sin 135^\circ}{\sin 30^\circ} \right) = 35.36 \text{ lb}$$

$$R = 35.4 \text{ lb} \blacktriangleleft$$

### PROBLEM 2.13

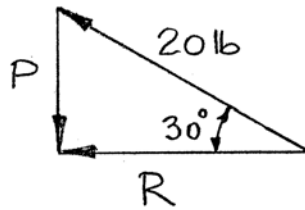


For the hook support of Problem 2.11, determine, using trigonometry, (a) the magnitude and direction of the smallest force **P** for which the resultant **R** of the two forces applied to the support is horizontal, (b) the corresponding magnitude of **R**.

**Problem 2.11:** Two forces are applied as shown to a hook support. Using trigonometry and knowing that the magnitude of **P** is 14 lb, determine (a) the required angle  $\alpha$  if the resultant **R** of the two forces applied to the support is to be horizontal, (b) the corresponding magnitude of **R**.

### SOLUTION

(a) The smallest force **P** will be perpendicular to **R**, that is, vertical



$$P = (20 \text{ lb}) \sin 30^\circ$$

$$= 10 \text{ lb}$$

$$\mathbf{P} = 10 \text{ lb} \downarrow \blacktriangleleft$$

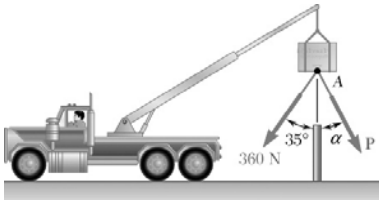
(b)

$$R = (20 \text{ lb}) \cos 30^\circ$$

$$= 17.32 \text{ lb}$$

$$\mathbf{R} = 17.32 \text{ lb} \blacktriangleleft$$

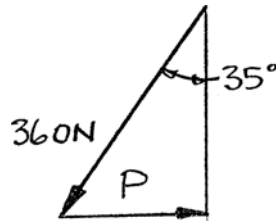
### PROBLEM 2.14



As shown in Figure P2.9, two cables are attached to a sign at  $A$  to steady the sign as it is being lowered. Using trigonometry, determine (a) the magnitude and direction of the smallest force  $\mathbf{P}$  for which the resultant  $\mathbf{R}$  of the two forces applied at  $A$  is vertical, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION

We observe that force  $\mathbf{P}$  is minimum when  $\alpha$  is  $90^\circ$ , that is,  $\mathbf{P}$  is horizontal



Then:

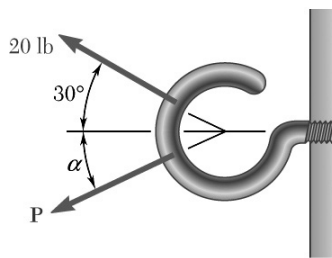
$$(a) P = (360 \text{ N}) \sin 35^\circ$$

$$\text{or } \mathbf{P} = 206 \text{ N} \rightarrow \blacktriangleleft$$

And:

$$(b) R = (360 \text{ N}) \cos 35^\circ$$

$$\text{or } \mathbf{R} = 295 \text{ N} \blacktriangleleft$$



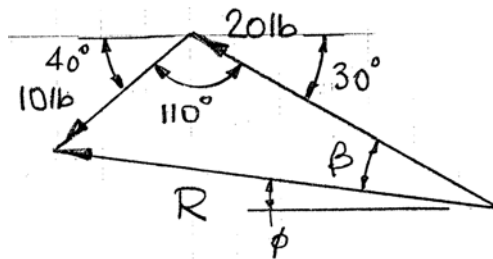
### PROBLEM 2.15

For the hook support of Problem 2.11, determine, using trigonometry, the magnitude and direction of the resultant of the two forces applied to the support knowing that  $P = 10$  lb and  $\alpha = 40^\circ$ .

**Problem 2.11:** Two forces are applied as shown to a hook support. Using trigonometry and knowing that the magnitude of  $\mathbf{P}$  is 14 lb, determine (a) the required angle  $\alpha$  if the resultant  $\mathbf{R}$  of the two forces applied to the support is to be horizontal, (b) the corresponding magnitude of  $\mathbf{R}$ .

### SOLUTION

Using the force triangle and the Law of Cosines



$$\begin{aligned}
 R^2 &= (10 \text{ lb})^2 + (20 \text{ lb})^2 - 2(10 \text{ lb})(20 \text{ lb})\cos 110^\circ \\
 &= [100 + 400 - 400(-0.342)]\text{lb}^2 \\
 &= 636.8 \text{ lb}^2 \\
 R &= 25.23 \text{ lb}
 \end{aligned}$$

Using now the Law of Sines

$$\begin{aligned}
 \frac{10 \text{ lb}}{\sin \beta} &= \frac{25.23 \text{ lb}}{\sin 110^\circ} \\
 \sin \beta &= \left( \frac{10 \text{ lb}}{25.23 \text{ lb}} \right) \sin 110^\circ \\
 &= 0.3724
 \end{aligned}$$

So:  $\beta = 21.87^\circ$

Angle of inclination of  $R$ ,  $\phi$  is then such that:

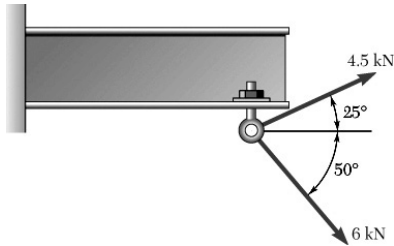
$$\begin{aligned}
 \phi + \beta &= 30^\circ \\
 \phi &= 8.13^\circ
 \end{aligned}$$

Hence:

$$\mathbf{R} = 25.2 \text{ lb} \searrow 8.13^\circ \blacktriangleleft$$

### PROBLEM 2.16

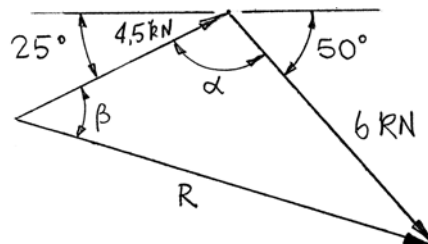
Solve Problem 2.1 using trigonometry



**Problem 2.1:** Two forces are applied to an eye bolt fastened to a beam. Determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.

### SOLUTION

Using the force triangle, the Law of Cosines and the Law of Sines



We have:

$$\begin{aligned}\alpha &= 180^\circ - (50^\circ + 25^\circ) \\ &= 105^\circ\end{aligned}$$

Then:

$$\begin{aligned}R^2 &= (4.5 \text{ kN})^2 + (6 \text{ kN})^2 - 2(4.5 \text{ kN})(6 \text{ kN})\cos 105^\circ \\ &= 70.226 \text{ kN}^2\end{aligned}$$

or

$$R = 8.3801 \text{ kN}$$

Now:

$$\frac{8.3801 \text{ kN}}{\sin 105^\circ} = \frac{6 \text{ kN}}{\sin \beta}$$

$$\sin \beta = \left( \frac{6 \text{ kN}}{8.3801 \text{ kN}} \right) \sin 105^\circ$$

$$= 0.6916$$

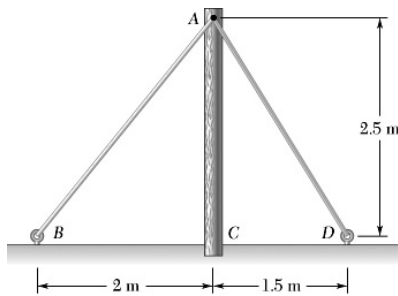
$$\beta = 43.756^\circ$$

$$\mathbf{R} = 8.38 \text{ kN} \quad \nearrow 18.76^\circ \blacktriangleleft$$



## PROBLEM 2.17

Solve Problem 2.2 using trigonometry



**Problem 2.2:** The cable stays  $AB$  and  $AD$  help support pole  $AC$ . Knowing that the tension is 500 N in  $AB$  and 160 N in  $AD$ , determine graphically the magnitude and direction of the resultant of the forces exerted by the stays at  $A$  using (a) the parallelogram law, (b) the triangle rule.

## SOLUTION

From the geometry of the problem:

$$\alpha = \tan^{-1} \frac{2}{2.5} = 38.66^\circ$$

$$\beta = \tan^{-1} \frac{1.5}{2.5} = 30.96^\circ$$

Now:  $\theta = 180^\circ - (38.66^\circ + 30.96^\circ) = 110.38^\circ$

And, using the Law of Cosines:

$$\begin{aligned} R^2 &= (500 \text{ N})^2 + (160 \text{ N})^2 - 2(500 \text{ N})(160 \text{ N})\cos 110.38^\circ \\ &= 331319 \text{ N}^2 \end{aligned}$$

$$R = 575.6 \text{ N}$$

Using the Law of Sines:

$$\frac{160 \text{ N}}{\sin \gamma} = \frac{575.6 \text{ N}}{\sin 110.38^\circ}$$

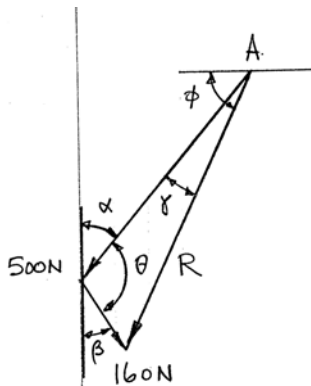
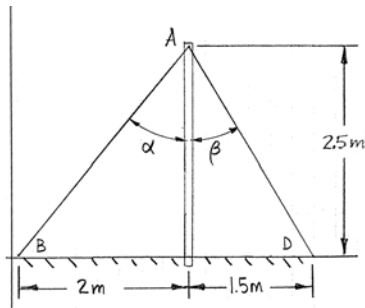
$$\sin \gamma = \left( \frac{160 \text{ N}}{575.6 \text{ N}} \right) \sin 110.38^\circ$$

$$= 0.2606$$

$$\gamma = 15.1^\circ$$

$$\phi = (90^\circ - \alpha) + \gamma = 66.44^\circ$$

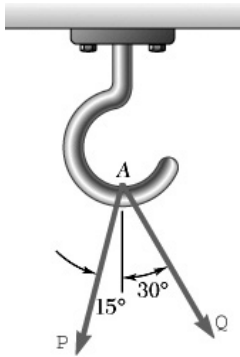
$$\mathbf{R} = 576 \text{ N } \nearrow 66.4^\circ \blacktriangleleft$$



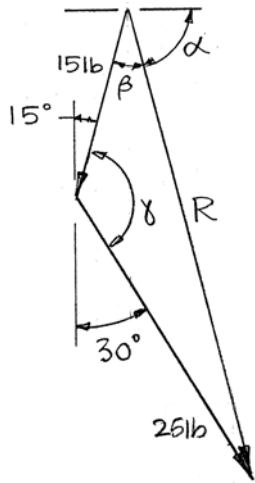
### PROBLEM 2.18

Solve Problem 2.3 using trigonometry

**Problem 2.3:** Two forces **P** and **Q** are applied as shown at point A of a hook support. Knowing that  $P = 15 \text{ lb}$  and  $Q = 25 \text{ lb}$ , determine graphically the magnitude and direction of their resultant using (a) the parallelogram law, (b) the triangle rule.



### SOLUTION



Using the force triangle and the Laws of Cosines and Sines

We have:

$$\begin{aligned}\gamma &= 180^\circ - (15^\circ + 30^\circ) \\ &= 135^\circ\end{aligned}$$

$$\begin{aligned}\text{Then: } R^2 &= (15 \text{ lb})^2 + (25 \text{ lb})^2 - 2(15 \text{ lb})(25 \text{ lb})\cos 135^\circ \\ &= 1380.3 \text{ lb}^2\end{aligned}$$

or

$$R = 37.15 \text{ lb}$$

and

$$\frac{25 \text{ lb}}{\sin \beta} = \frac{37.15 \text{ lb}}{\sin 135^\circ}$$

$$\sin \beta = \left( \frac{25 \text{ lb}}{37.15 \text{ lb}} \right) \sin 135^\circ$$

$$= 0.4758$$

$$\beta = 28.41^\circ$$

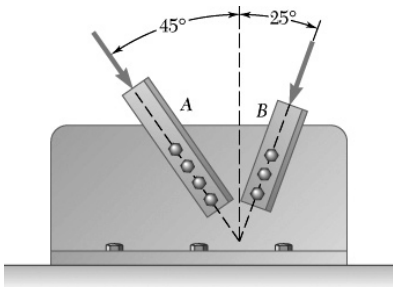
Then:

$$\alpha + \beta + 75^\circ = 180^\circ$$

$$\alpha = 76.59^\circ$$

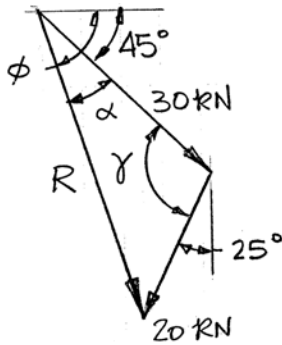
$$\mathbf{R} = 37.2 \text{ lb} \swarrow 76.6^\circ \blacktriangleleft$$

### PROBLEM 2.19



Two structural members *A* and *B* are bolted to a bracket as shown. Knowing that both members are in compression and that the force is 30 kN in member *A* and 20 kN in member *B*, determine, using trigonometry, the magnitude and direction of the resultant of the forces applied to the bracket by members *A* and *B*.

### SOLUTION



Using the force triangle and the Laws of Cosines and Sines

We have:  $\gamma = 180^\circ - (45^\circ + 25^\circ) = 110^\circ$

$$\text{Then: } R^2 = (30 \text{ kN})^2 + (20 \text{ kN})^2 - 2(30 \text{ kN})(20 \text{ kN})\cos 110^\circ$$

$$= 1710.4 \text{ kN}^2$$

$$R = 41.357 \text{ kN}$$

and

$$\frac{20 \text{ kN}}{\sin \alpha} = \frac{41.357 \text{ kN}}{\sin 110^\circ}$$

$$\sin \alpha = \left( \frac{20 \text{ kN}}{41.357 \text{ kN}} \right) \sin 110^\circ$$

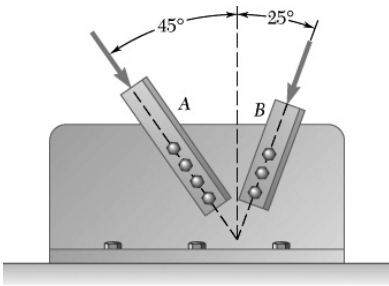
$$= 0.4544$$

$$\alpha = 27.028^\circ$$

$$\text{Hence: } \phi = \alpha + 45^\circ = 72.028^\circ$$

$$\mathbf{R} = 41.4 \text{ kN} \searrow 72.0^\circ \blacktriangleleft$$

### PROBLEM 2.20



Two structural members *A* and *B* are bolted to a bracket as shown. Knowing that both members are in compression and that the force is 20 kN in member *A* and 30 kN in member *B*, determine, using trigonometry, the magnitude and direction of the resultant of the forces applied to the bracket by members *A* and *B*.

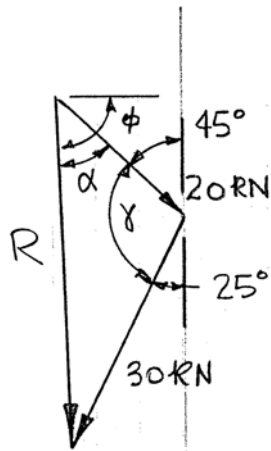
### SOLUTION

Using the force triangle and the Laws of Cosines and Sines

We have:  $\gamma = 180^\circ - (45^\circ + 25^\circ) = 110^\circ$

$$\begin{aligned} \text{Then: } R^2 &= (30 \text{ kN})^2 + (20 \text{ kN})^2 - 2(30 \text{ kN})(20 \text{ kN})\cos 110^\circ \\ &= 1710.4 \text{ kN}^2 \\ R &= 41.357 \text{ kN} \end{aligned}$$

and



$$\frac{30 \text{ kN}}{\sin \alpha} = \frac{41.357 \text{ kN}}{\sin 110^\circ}$$

$$\sin \alpha = \left( \frac{30 \text{ kN}}{41.357 \text{ kN}} \right) \sin 110^\circ$$

$$= 0.6816$$

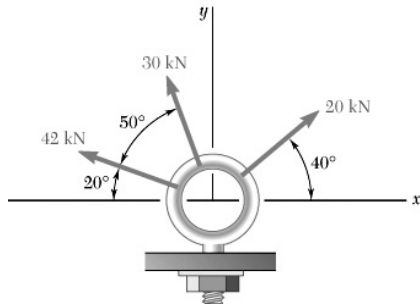
$$\alpha = 42.97^\circ$$

$$\text{Finally: } \phi = \alpha + 45^\circ = 87.97^\circ$$

$$\mathbf{R} = 41.4 \text{ kN} \searrow 88.0^\circ \blacktriangleleft$$

### PROBLEM 2.21

Determine the  $x$  and  $y$  components of each of the forces shown.



### SOLUTION

*20 kN Force:*

$$F_x = +(20 \text{ kN})\cos 40^\circ, \quad F_x = 15.32 \text{ kN} \blacktriangleleft$$

$$F_y = +(20 \text{ kN})\sin 40^\circ, \quad F_y = 12.86 \text{ kN} \blacktriangleleft$$

*30 kN Force:*

$$F_x = -(30 \text{ kN})\cos 70^\circ, \quad F_x = -10.26 \text{ kN} \blacktriangleleft$$

$$F_y = +(30 \text{ kN})\sin 70^\circ, \quad F_y = 28.2 \text{ kN} \blacktriangleleft$$

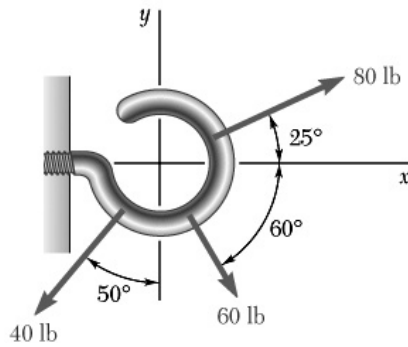
*42 kN Force:*

$$F_x = -(42 \text{ kN})\cos 20^\circ, \quad F_x = -39.5 \text{ kN} \blacktriangleleft$$

$$F_y = +(42 \text{ kN})\sin 20^\circ, \quad F_y = 14.36 \text{ kN} \blacktriangleleft$$

### PROBLEM 2.22

Determine the  $x$  and  $y$  components of each of the forces shown.



### SOLUTION

*40 lb Force:*

$$F_x = -(40 \text{ lb}) \sin 50^\circ, \quad F_x = -30.6 \text{ lb} \blacktriangleleft$$

$$F_y = -(40 \text{ lb}) \cos 50^\circ, \quad F_y = -25.7 \text{ lb} \blacktriangleleft$$

*60 lb Force:*

$$F_x = +(60 \text{ lb}) \cos 60^\circ, \quad F_x = 30.0 \text{ lb} \blacktriangleleft$$

$$F_y = -(60 \text{ lb}) \sin 60^\circ, \quad F_y = -52.0 \text{ lb} \blacktriangleleft$$

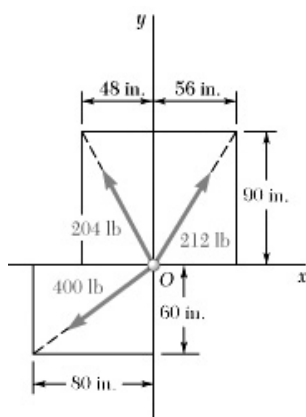
*80 lb Force:*

$$F_x = +(80 \text{ lb}) \cos 25^\circ, \quad F_x = 72.5 \text{ lb} \blacktriangleleft$$

$$F_y = +(80 \text{ lb}) \sin 25^\circ, \quad F_y = 33.8 \text{ lb} \blacktriangleleft$$

### PROBLEM 2.23

Determine the  $x$  and  $y$  components of each of the forces shown.



### SOLUTION

We compute the following distances:

$$OA = \sqrt{(48)^2 + (90)^2} = 102 \text{ in.}$$

$$OB = \sqrt{(56)^2 + (90)^2} = 106 \text{ in.}$$

$$OC = \sqrt{(80)^2 + (60)^2} = 100 \text{ in.}$$

Then:

*204 lb Force:*

$$F_x = -(102 \text{ lb}) \frac{48}{102}, \quad F_x = -48.0 \text{ lb} \blacktriangleleft$$

$$F_y = +(102 \text{ lb}) \frac{90}{102}, \quad F_y = 90.0 \text{ lb} \blacktriangleleft$$

*212 lb Force:*

$$F_x = +(212 \text{ lb}) \frac{56}{106}, \quad F_x = 112.0 \text{ lb} \blacktriangleleft$$

$$F_y = +(212 \text{ lb}) \frac{90}{106}, \quad F_y = 180.0 \text{ lb} \blacktriangleleft$$

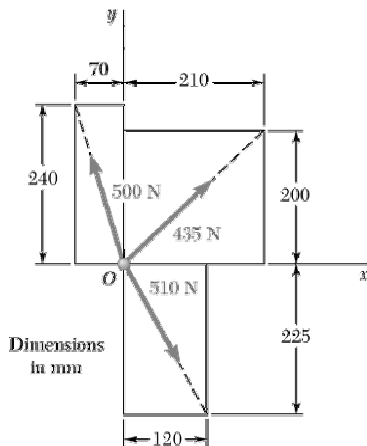
*400 lb Force:*

$$F_x = -(400 \text{ lb}) \frac{80}{100}, \quad F_x = -320 \text{ lb} \blacktriangleleft$$

$$F_y = -(400 \text{ lb}) \frac{60}{100}, \quad F_y = -240 \text{ lb} \blacktriangleleft$$

## PROBLEM 2.24

Determine the  $x$  and  $y$  components of each of the forces shown.



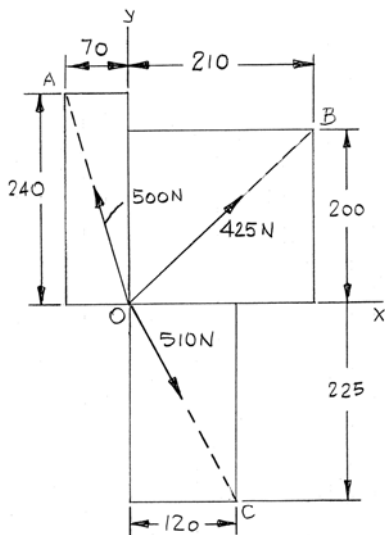
## SOLUTION

We compute the following distances:

$$OA = \sqrt{(70)^2 + (240)^2} = 250 \text{ mm}$$

$$OB = \sqrt{(210)^2 + (200)^2} = 290 \text{ mm}$$

$$OC = \sqrt{(120)^2 + (225)^2} = 255 \text{ mm}$$



500 N Force:

$$F_x = -500 \text{ N} \left( \frac{70}{250} \right) \quad F_x = -140.0 \text{ N} \blacktriangleleft$$

$$F_y = +500 \text{ N} \left( \frac{240}{250} \right) \quad F_y = 480 \text{ N} \blacktriangleleft$$

435 N Force:

$$F_x = +435 \text{ N} \left( \frac{210}{290} \right) \quad F_x = 315 \text{ N} \blacktriangleleft$$

$$F_y = +435 \text{ N} \left( \frac{200}{290} \right) \quad F_y = 300 \text{ N} \blacktriangleleft$$

510 N Force:

$$F_x = +510 \text{ N} \left( \frac{120}{255} \right) \quad F_x = 240 \text{ N} \blacktriangleleft$$

$$F_y = -510 \text{ N} \left( \frac{225}{255} \right) \quad F_y = -450 \text{ N} \blacktriangleleft$$

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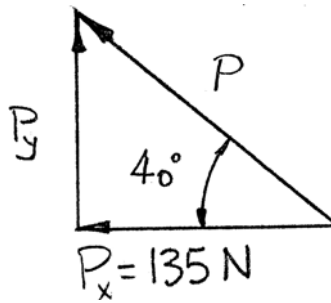


### PROBLEM 2.25



While emptying a wheelbarrow, a gardener exerts on each handle  $AB$  a force  $\mathbf{P}$  directed along line  $CD$ . Knowing that  $\mathbf{P}$  must have a 135-N horizontal component, determine (a) the magnitude of the force  $\mathbf{P}$ , (b) its vertical component.

### SOLUTION



(a)

$$P = \frac{P_x}{\cos 40^\circ}$$
$$= \frac{135 \text{ N}}{\cos 40^\circ}$$

or  $P = 176.2 \text{ N} \blacktriangleleft$

(b)

$$P_y = P_x \tan 40^\circ = P \sin 40^\circ$$
$$= (135 \text{ N}) \tan 40^\circ$$

or  $P_y = 113.3 \text{ N} \blacktriangleleft$