

# Longest Common Subsequence

1) Make  $c[i][0] = 0$  and  $c[0][j] = 0$

2) if  $x_i = y_j$  then

$$c[i, j] = c[i-1, j-1] + 1 \quad \& \text{ "}\nwarrow\text{"}$$

3) else if  $c[i-1, j] > c[i, j-1]$  then

$$c[i, j] = c[i-1, j] \quad \& \text{ "}\uparrow\text{"}$$

4) else  $c[i, j] = c[i, j-1]$  & "←"

Example :-

$S_1 = \text{abbacdcba}$

$S_2 = \text{bcdbbcaaa}$

		0	1	2	3	4	5	6	7	8
		$Y_j$	b	c	d	b	b	c	a	a
0	$X_i$	0	0	0	0	0	0	0	0	0
1	a	0	0↑	0↑	0↑	0↑	0↑	0↑	1↖	1↖
2	b	0								
3	b	0								
4	a	0								
5	c	0								
6	d	0								
7	c	0								
8	b	0								
9	a	0								

$$\begin{aligned}
 c[1,1] &= c[i-1,j] \\
 &= c[0,1] \\
 &= 0 \text{ "↑"}
 \end{aligned}$$

$$\begin{aligned}
 c[1,2] &= c[i-1,j] \\
 &= c[0,2] \\
 &= 0 \text{ "↑"}
 \end{aligned}$$

$$\begin{aligned}
 c[1,3] &= c[i-1,j] \\
 &= c[0,3] \\
 &= 0 \text{ "↑"}
 \end{aligned}$$

$$\begin{aligned}
 c[1,4] &= c[i-1,j] \\
 &= c[0,4] \\
 &= 0 \text{ "↑"}
 \end{aligned}$$

$$\begin{aligned} c[1,5] &= c[i-1, j] \\ &= c[0,4] \\ &= 0 \text{ "↑"} \end{aligned}$$

$$\begin{aligned} c[1,6] &= c[i-1, j] \\ &= c[0,5] \\ &= 0 \text{ "↑"} \end{aligned}$$

$$\begin{aligned} c[1,7] &= c[i-1, j-1] + 1 \\ &= c[0,6] + 1 \\ &= 0 + 1 \\ &= 1 \text{ "↖"} \end{aligned}$$

$$\begin{aligned} c[1,8] &= c[i-1, j-1] + 1 \\ &= c[0,7] + 1 \\ &= 0 + 1 \\ &= 1 \text{ "↖"} \end{aligned}$$

$$\begin{aligned} c[2,1] &= c[i-1, j-1] + 1 \\ &= c[1,0] + 1 \\ &= 0 + 1 \\ &= 1 \text{ "↖"} \end{aligned}$$

$$\begin{aligned} c[2,2] &= c[i, j-1] \\ &= c[2,1] \\ &= 1 \text{ "←"} \end{aligned}$$



Yj      b      c      d      b      b      c      a      a

0	Xi	0	0	0	0	0	0	0	0
1	a	0	0↑	0↑	0↑	0↑	0↑	↖1	↖1
2	b	0	↖1	1←	1←	↖1	↖1	1←	1↑
3	b	0	↖1	1↑	1↑	↖2	↖2	2←	1←
4	a	0	1↑	1↑	1↑	2↑	2↑	2↑	↖3
5	c	0	1↑	↖2	2←	2↑	2↑	↖3	3↑
6	d	0	1↑	2↑	↖3	3←	3←	3↑	3↑
7	c	0	1↑	↖2	3↑	3↑	3↑	↖4	4←
8	b	0	↖1	2↑	3↑	↖4	↖4	4↑	4↑
9	a	0	1↑	2↑	3↑	4↑	4↑	4↑	↖5



0	$X_i$	0	0	0	0	0	0	0	0
1	a	0	$0 \uparrow$	$0 \uparrow$	$0 \uparrow$	$0 \uparrow$	$0 \uparrow$	$\nwarrow 1$	$\nwarrow 1$
2	b	0	$\nwarrow 1$	$1 \leftarrow$	$1 \leftarrow$	$\nwarrow 1$	$\nwarrow 1$	$1 \uparrow$	$1 \uparrow$
3	b	0	$\nwarrow 1$	$1 \uparrow$	$1 \uparrow$	$\nwarrow 2$	$\nwarrow 2$	$2 \leftarrow$	$1 \leftarrow$
4	a	0	$1 \uparrow$	$1 \uparrow$	$1 \uparrow$	$2 \uparrow$	$2 \uparrow$	$2 \uparrow$	$\nwarrow 3$
5	c	0	$1 \uparrow$	$\nwarrow 2$	$2 \leftarrow$	$2 \uparrow$	$2 \uparrow$	$\nwarrow 3$	$3 \uparrow$
6	d	0	$1 \uparrow$	$2 \uparrow$	$\nwarrow 3$	$3 \leftarrow$	$3 \leftarrow$	$3 \uparrow$	$3 \uparrow$
7	c	0	$1 \uparrow$	$\nwarrow 2$	$3 \uparrow$	$3 \uparrow$	$3 \uparrow$	$\nwarrow 4$	$4 \leftarrow$
8	b	0	$\nwarrow 1$	$2 \uparrow$	$3 \uparrow$	$\nwarrow 4$	$\nwarrow 4$	$4 \uparrow$	$4 \uparrow$
9	a	0	$1 \uparrow$	$2 \uparrow$	$3 \uparrow$	$4 \uparrow$	$4 \uparrow$	$4 \uparrow$	$\nwarrow 5$

b

c

d

c

a