

C Programming Basic – week 14

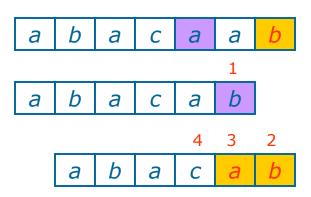
String Pattern Matching

Lecturers:

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Topics of this week

- String pattern matching algorithms
 - Naive algorithm
 - Knuth-Morris-Pratt algorithm
 - Boyer-Moore algorithm
- Exercises



String matching problem

- Let P be a string of size m
 - A substring P[i .. j] of P is the subsequence of P consisting of the characters with ranks between i and j
 - A prefix of P is a substring of the type P[0 .. i]
 - A suffix of P is a substring of the type P[i ..m 1]
- Given strings T (text) and P (pattern), the pattern matching problem consists of finding a substring of T equal to P
- Applications:
 - Text editors, Search engines, Biological research

Brute Force Matching

- The brute-force pattern matching algorithm compares the pattern P with the text T for each possible shift of P relative to T, until either
 - a match is found, or
 - all placements of the pattern have been tried
- Brute-force pattern matching runs in time O(nm)
- Example of worst case:
 - -\T = aaa ... ah
 - -P = aaah
 - may occur in images and DNA sequences
 - unlikely in English text

Algorithm

Algorithm BruteForceMatch(T, P)

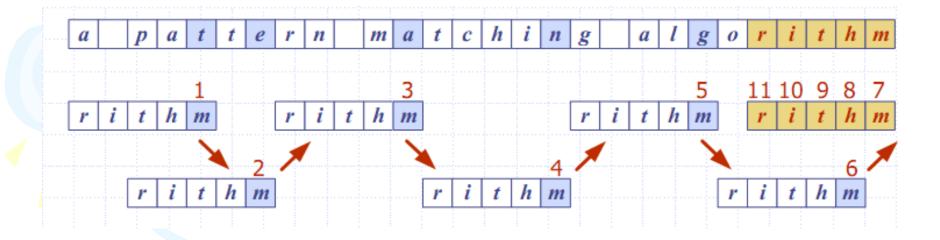
```
// Input text T of size n and pattern P of size m
// Output starting index of a substring of T equal to P or
if no such substring exists
  for i \leftarrow 0 to n - m {
      test shift i of the pattern
  j ← 0
  while j < m \land T[i + j] = P[j]
      j ← j + 1
  if j = m
      return i {match at i}
  else
  break while loop {mismatch}
return -1 {no match anywhere}
```

Exercise 13.1

- Make a random string that has about 2000 characters consisting of a set of characters..
- For example:
 - set of characters: abcdef
 - string: abcadacaeeeffaadbfacddedcedfbeccae...
- Write the program that searches the pattern, for example "aadbf", from the string.
- Note: use Simple searching string Algorithm

Boyer-Moore Heuristics

- The Boyer-Moore's pattern matching algorithm is based on two heuristics
- Looking-glass heuristic: Compare P with a subsequence of T
- moving backwards
- Character-jump heuristic: When a mismatch occurs at T[i] = c
 - If P contains c, shift P to align the last occurrence of c in P with T[i]
 - Else, shift P to align P[0] with T[i + 1]



Last-Occurrence Function

- Boyer-Moore's algorithm preprocesses the pattern P and the alphabet Σ to build the last-occurrence function L mapping Σ to integers, where L(c) is defined as
 - the largest index i such that P[i] = c or
 - − −1 if no such index exists
- Example:

$$-\Sigma = \{a, b, c, d\}$$

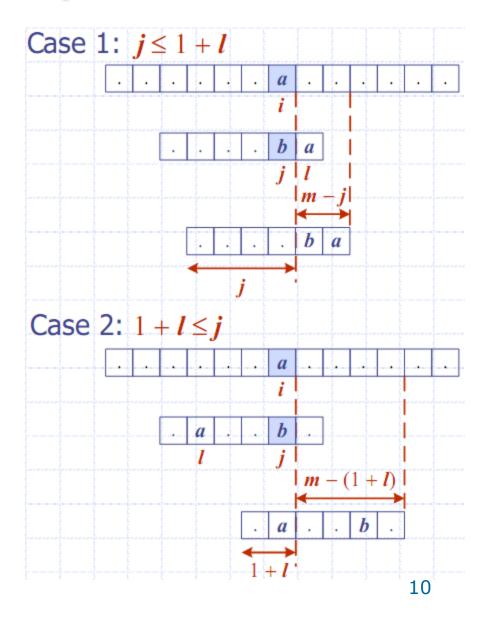
- P = abacab

С	а	b	С	d
L(C)	4	5	3	-1

- The last-occurrence function can be represented by an array indexed by the numeric codes of the characters
- The last-occurrence function can be computed in time O(m + s), where m is the size of P and s is the size of Σ

Algorithm Boyer Moore

```
Algorithm BoyerMooreMatch (T, P, \Sigma)
    L \leftarrow lastOccurenceFunction(P, \Sigma)
    i \leftarrow m - 1
   j \leftarrow m-1
    repeat
    if T[i] = P[j]
           if j = 0
           return i { match at i }
           else
           i \leftarrow i - 1
          j \leftarrow j - 1
    else
    { character-jump }
           l \leftarrow L/T/i
           i \leftarrow i + m - min(j, l + l)
          j \leftarrow m - 1
    until i > n - 1
    return -1 \{ no match \}
```

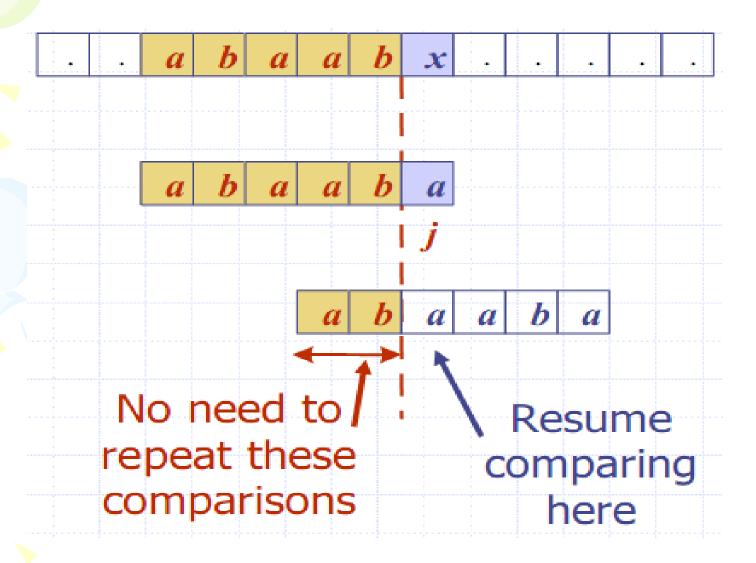


Exercise 13.2: Searching string by Boyer-Moore

- Make a random string that has about 2000 characters consisting of a set of characters.
- set of characters: abcdef
- string: abcadacaeeeffaadbfacddedcedfbeccae...
- Write the program that search the pattern, for example "aadbf", from the string.
- Note: use Boyer-Moore Algorithm

KMP string matching

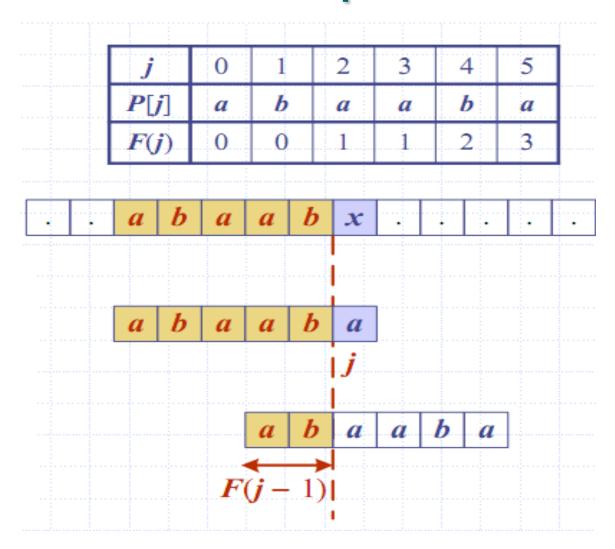
- Knuth-Morris-Pratt's algorithm compares the pattern to the text in left-to-right, but shifts the pattern more intelligently than the bruteforce algorithm.
- When a mismatch occurs, what is the most we can shift the pattern so as to avoid redundant comparisons?
- Answer: the largest prefix of P[0..j] that is a suffix of P[1..j]



KMP Failure Function

- Knuth-Morris-Pratt's algorithm preprocesses the pattern to find matches of prefixes of the pattern with the pattern itself
- The failure function F(j) is defined as the size of the largest prefix of P[0..j] that is also a suffix of P[1..j]
- Knuth-Morris-Pratt's algorithm modifies the brute-force algorithm so that if a mismatch occurs at P[j] ≠ T[i] we set

$$j \leftarrow F(j-1)$$



```
Algorithm failureFunction(P)
   F[0] ← 0
   i \leftarrow 1
  j \leftarrow 0
   while i < m
        if P[i] = P[i]
        {we have matched j + 1 chars}
               F[i] \leftarrow i + 1
                i \leftarrow i + 1
               j \leftarrow j + 1
        else if j > 0 then
        {use failure function to shift P}
              j \leftarrow F [j-1]
        else
                F[i] \leftarrow 0 \{ no match \}
                i \leftarrow i + 1
```

Exercise 13.3

- Repeat the exercise 13.2 using the KMP algorithm.
- Calculate the number of comparisons.

The KMP algorithm

- The failure function can be represented by an array and can be computed in O(m) time
- At each iteration of the while-loop, either
 - i increases by one, or
 - the shift amount i j increases by at least one (observe that F(j 1) < j)
- Hence, there are no more than 2n iterations of the while-loop
- Thus, KMP's algorithm runs in optimal time O(m + n)

```
Algorithm KMPMatch(T, P)
   F \leftarrow failureFunction(P)
   i \leftarrow 0
   j \leftarrow 0
   while i < n
          if T[i] = P[j]
                    if j = m - 1
                               return i - j \{ match \}
                     else
                               i \leftarrow i + 1
                               j \leftarrow j + 1
          else
                    if j > 0
                              j \leftarrow F[j-1]
                     else
                               i \leftarrow i + 1
   return -1 { no match }
```

1 2 3 4 5 6 a b a c a b	
a b a c a b	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
8 9 10 11 12	
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	
_13	
j 0 1 2 3 4 5 a b a	$a \mid c \mid a \mid b$
P[i] a b a c a b 14 15	5 16 17 18 19
F(j) 0 0 1 0 1 2	$b \mid a \mid c \mid a \mid b$