

# **BCNF Normalization - examples**

# Functional dependencies

## Example 1

- ❑ Database schema
  - *inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)
- ❑ Functional dependencies (domain knowledge)
  - $ID \rightarrow name$ ,
  - $ID \rightarrow salary$ ,
  - $ID \rightarrow dept\_name$
  - $dept\_name \rightarrow building$
  - $dept\_name \rightarrow budget$
- ❑ Derived dependencies
  - $ID \rightarrow building$
  - $ID \rightarrow budget$

| <i>ID</i> | <i>name</i> | <i>salary</i> | <i>dept_name</i> | <i>building</i> | <i>budget</i> |
|-----------|-------------|---------------|------------------|-----------------|---------------|
| 22222     | Einstein    | 95000         | Physics          | Watson          | 70000         |
| 12121     | Wu          | 90000         | Finance          | Painter         | 120000        |
| 32343     | El Said     | 60000         | History          | Painter         | 50000         |
| 45565     | Katz        | 75000         | Comp. Sci.       | Taylor          | 100000        |
| 98345     | Kim         | 80000         | Elec. Eng.       | Taylor          | 85000         |
| 76766     | Crick       | 72000         | Biology          | Watson          | 90000         |
| 10101     | Srinivasan  | 65000         | Comp. Sci.       | Taylor          | 100000        |
| 58583     | Califieri   | 62000         | History          | Painter         | 50000         |
| 83821     | Brandt      | 92000         | Comp. Sci.       | Taylor          | 100000        |
| 15151     | Mozart      | 40000         | Music            | Packard         | 80000         |
| 33456     | Gold        | 87000         | Physics          | Watson          | 70000         |
| 76543     | Singh       | 80000         | Finance          | Painter         | 120000        |

# Functional dependencies

## Example 1

- ❑ Database schema
  - *inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)
- ❑ All functional dependencies (domain knowledge)
  - $ID \rightarrow name$ ,
  - $ID \rightarrow salary$ ,
  - $ID \rightarrow dept\_name$
  - $dept\_name \rightarrow building$
  - $dept\_name \rightarrow budget$
  - $ID \rightarrow building$
  - $ID \rightarrow budget$
- ❑ We see that
  - *ID* is a superkey
  - *dept\_name* is NOT a superkey
- ❑ Can be “rewritten” (is covered by)
  - $ID \rightarrow name, salary, dept\_name, building, budget$
  - $dept\_name \rightarrow building, budget$

# Functional dependencies

## Example 1

- ❑ Database schema
  - *inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)
- ❑ functional dependencies to take into consideration
  - *ID* → *name*, *salary*, *dept\_name*, *building*, *budget*
  - *dept\_name* → *building*, *budget*
- ❑ We see that
  - *ID* is a superkey
  - *dept\_name* is NOT a superkey
- ❑ thus
  - *dept\_name* → *building*, *budget*
  - violates BCNF

# BCNF Decomposition Algorithm

Example 1

Database schema

*inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)

→ *result* := {*R*<sub>1</sub>} = {*inst\_dept*};  
*done* := false;  
compute *F*<sup>+</sup>;  
**while** (**not** *done*) **do**  
  **if** (there is a schema *R*<sub>*i*</sub> in *result* that is not in BCNF)  
  **then begin**  
    let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
    holds on *R*<sub>*i*</sub> such that  $\alpha \rightarrow R_i$  is not in *F*<sup>+</sup>,  
    and  $\alpha \cap \beta = \emptyset$ ;  
    *result* := (*result* − *R*<sub>*i*</sub>) ∪ (*R*<sub>*i*</sub> −  $\beta$ ) ∪ ( $\alpha, \beta$ );  
  **end**  
  **else** *done* := **true**;

- *dept\_name* → *building, budget*
- violates BCNF in *inst\_dept*

# BCNF Decomposition Algorithm

Example 1

Database schema

*inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)

- *dept\_name* → *building*, *budget*
- violates BCNF in *inst\_dept*

let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
and  $\alpha \cap \beta = \emptyset$ ;  
 $result := (result - R_i) \cup (R_i - \beta) \cup (\alpha, \beta)$ ;

for “ $\alpha \rightarrow \beta$ ” = “*dept\_name* → *building*, *budget*”

Means **we need to decompose into**

*R1*(*dept\_name*, *building*, *budget*)

*inst\_dept1*(*ID*, *name*, *salary*, *dept\_name*)

# BCNF Decomposition Algorithm

Example 1

Database schema

*inst\_dept*(*ID*, *name*, *salary*, *dept\_name*, *building*, *budget*)

- *dept\_name* → *building*, *budget*
- violates BCNF in *inst\_dept*

let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
and  $\alpha \cap \beta = \emptyset$ ;  
 $result := (result - R_i) \cup (R_i - \beta) \cup (\alpha, \beta)$ ;

for “ $\alpha \rightarrow \beta$ ” = “*dept\_name* → *building*, *budget*”

A normalised schema with **better relation schema names**:

*dept*(*dept\_name*, *building*, *budget*)

*inst*(*ID*, *name*, *salary*, *dept\_name*)

# Resulting database after BCNF-normalisation

## Example 1

*inst\_dept*

| <i>ID</i> | <i>name</i> | <i>salary</i> | <i>dept_name</i> | <i>building</i> | <i>budget</i> |
|-----------|-------------|---------------|------------------|-----------------|---------------|
| 22222     | Einstein    | 95000         | Physics          | Watson          | 70000         |
| 12121     | Wu          | 90000         | Finance          | Painter         | 120000        |
| 32343     | El Said     | 60000         | History          | Painter         | 50000         |
| 45565     | Katz        | 75000         | Comp. Sci.       | Taylor          | 100000        |
| 98345     | Kim         | 80000         | Elec. Eng.       | Taylor          | 85000         |
| 76766     | Crick       | 72000         | Biology          | Watson          | 90000         |
| 10101     | Srinivasan  | 65000         | Comp. Sci.       | Taylor          | 100000        |
| 58583     | Califieri   | 62000         | History          | Painter         | 50000         |
| 83821     | Brandt      | 92000         | Comp. Sci.       | Taylor          | 100000        |
| 15151     | Mozart      | 40000         | Music            | Packard         | 80000         |
| 33456     | Gold        | 87000         | Physics          | Watson          | 70000         |
| 76543     | Singh       | 80000         | Finance          | Painter         | 120000        |

| <i>ID</i> | <i>name</i> | <i>dept_name</i> | <i>salary</i> |
|-----------|-------------|------------------|---------------|
| 10101     | Srinivasan  | Comp. Sci.       | 65000         |
| 12121     | Wu          | Finance          | 90000         |
| 15151     | Mozart      | Music            | 40000         |
| 22222     | Einstein    | Physics          | 95000         |
| 32343     | El Said     | History          | 60000         |
| 33456     | Gold        | Physics          | 87000         |
| 45565     | Katz        | Comp. Sci.       | 75000         |
| 58583     | Califieri   | History          | 62000         |
| 76543     | Singh       | Finance          | 80000         |
| 76766     | Crick       | Biology          | 72000         |
| 83821     | Brandt      | Comp. Sci.       | 92000         |
| 98345     | Kim         | Elec. Eng.       | 80000         |

*inst*

*dept*

| <i>dept_name</i> | <i>building</i> | <i>budget</i> |
|------------------|-----------------|---------------|
| Biology          | Watson          | 90000         |
| Comp. Sci.       | Taylor          | 100000        |
| Elec. Eng.       | Taylor          | 85000         |
| Finance          | Painter         | 120000        |
| History          | Painter         | 50000         |
| Music            | Packard         | 80000         |
| Physics          | Watson          | 70000         |



# Functional dependencies

## Example 2

- ❑ Database schema
  - *class (course\_id, title, dept\_name, credits, sec\_id, semester, year, building, room\_number, capacity, time slot id)*
- ❑ functional dependencies to take into consideration
  - *course\_id* → *title, dept\_name, credits*
  - *building, room\_number* → *capacity*
  - *course\_id, sec\_id, semester, year* → *building, room\_number, time slot\_id*
- ❑ We see that
  - *course\_id, sec\_id, semester, year* is a superkey
  - *course\_id* is NOT a superkey
- ❑ thus
  - *course\_id* → *title, dept\_name, credits*
  - violates BCNF

# BCNF Decomposition

Example 2

Database schema

*class* (*course\_id*, *title*, *dept\_name*, *credits*, *sec\_id*, *semester*, *year*,  
*building*, *room\_number*, *capacity*, *time slot id*)

→ *result* := {*R*<sub>1</sub>} = {*class*};  
*done* := false;  
compute *F*<sup>+</sup>;  
**while** (**not** *done*) **do**  
  **if** (there is a schema *R<sub>i</sub>* in *result* that is not in BCNF)  
  **then begin**  
    let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
    holds on *R<sub>i</sub>* such that  $\alpha \rightarrow R_i$  is not in *F*<sup>+</sup>,  
    and  $\alpha \cap \beta = \emptyset$ ;  
    *result* := (*result* − *R<sub>i</sub>*) ∪ (*R<sub>i</sub>* −  $\beta$ ) ∪ ( $\alpha$ ,  $\beta$ );  
  **end**  
  **else** *done* := **true**;

- *course\_id* → *title*, *dept\_name*, *credits*
- violates BCNF in *class*

Algorithm from DSC fig 8.11

# BCNF Decomposition

Example 2

Database schema

*class* (*course\_id*, *title*, *dept\_name*, *credits*, *sec\_id*, *semester*, *year*,  
*building*, *room\_number*, *capacity*, *time slot id*)

- *course\_id*  $\rightarrow$  *title*, *dept\_name*, *credits*
- violates BCNF in *class*

let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
and  $\alpha \cap \beta = \emptyset$ ;  
*result* := (*result* -  $R_i$ )  $\cup$  ( $R_i - \beta$ )  $\cup$  ( $\alpha, \beta$ );

for “ $\alpha \rightarrow \beta$ ” = “*course\_id*  $\rightarrow$  *title*, *dept\_name*, *credits*”

Means we need to decompose *class* into

*course* (*course\_id*, *title*, *dept\_name*, *credits*)

*class1* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *capacity*, *time\_slot\_id*)

# BCNF Decomposition

Example 2

Database schema

*course* (*course\_id*, *title*, *dept\_name*, *credits*)

*class1* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *capacity*, *time\_slot\_id*)

*result* := {*R*<sub>1</sub>, *R*<sub>2</sub>} = {*course*, *class1*};

- *building, room\_number* → *capacity*
- violates BCNF in *class1*

*done* := false;

compute  $F^+$ ;

**while** (**not** *done*) **do**

**if** (there is a schema *R<sub>i</sub>* in *result* that is not in BCNF)

**then begin**

      let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
      holds on *R<sub>i</sub>* such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
      and  $\alpha \cap \beta = \emptyset$ ;

*result* := (*result* − *R<sub>i</sub>*) ∪ (*R<sub>i</sub>* −  $\beta$ ) ∪ ( $\alpha, \beta$ );

**end**

**else** *done* := **true**;

Algorithm from DSC fig 8.11

# BCNF Decomposition

## Example 2

Database schema

*course* (*course\_id*, *title*, *dept\_name*, *credits*)

*class1* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *capacity*, *time\_slot\_id*)

- *building, room\_number*  $\rightarrow$  *capacity*
- violates BCNF in *class1*

let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
and  $\alpha \cap \beta = \emptyset$ ;  
 $result := (result - R_i) \cup (R_i - \beta) \cup (\alpha, \beta)$ ;

for “ $\alpha \rightarrow \beta$ ” = “*building, room\_number*  $\rightarrow$  *capacity*”

Means we need to decompose *class1* into

*classroom* (*building*, *room\_number*, *capacity*)

*section* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *time\_slot\_id*)

# BCNF Decomposition

## Example 2

Database schema

*course* (*course\_id*, *title*, *dept\_name*, *credits*)

*classroom* (*building*, *room\_number*, *capacity*)

*section* (*course\_id*, *sec\_id*, *semester*, *year*, *building*, *room\_number*, *time\_slot\_id*)

*result* := { $R_1$ ,  $R_2$ ,  $R_3$ } = {*course*, *classroom*, *section*};

*done* := false;

compute  $F^+$ ;

- No dependency violates BCNF

**while** (**not** *done*) **do**

**if** (there is a schema  $R_i$  in *result* that is not in BCNF)

**then begin**

      let  $\alpha \rightarrow \beta$  be a nontrivial functional dependency that  
      holds on  $R_i$  such that  $\alpha \rightarrow R_i$  is not in  $F^+$ ,  
      and  $\alpha \cap \beta = \emptyset$ ;

*result* := (*result* -  $R_i$ )  $\cup$  ( $R_i - \beta$ )  $\cup$  ( $\alpha, \beta$ );

**end**

**else** *done* := **true**;

- So we are done

Algorithm from DSC fig 8.11