

Sometimes, a the dependent variable y cannot easily written explicitly as a function of x . Therefore it is important that we can still find out the derivative of the variable y with respect to x . To do this, we use the chain rule.

Example 1. *Find the slope of the tangent line of the graph*

$$x^2 + y^2 = 1$$

Solution. *We take the derivative of the equation with respect to x for both sides, we have*

$$\begin{aligned}\frac{d}{dx}(x^2 + y^2) &= \frac{d}{dx}0 \\ 2x + 2yy' &= 0 \\ y' &= -\frac{x}{y}\end{aligned}$$

The reason why the derivative of the second term is $2yy'$ is because we assume that y is a function of x , therefore y^2 is a composite function which the "outer function" is square and the "inner function" is $y(x)$.