

Definition 1. Compound propositions are made of primitive propositions.

Definition 2. Logic connectives and their symbols are

negation	not	\neg
conjunction	and	\wedge
disjunction	or	\vee
exclusive OR	either...or...	\oplus
implication	if...then...	\rightarrow
equivalent	if and only if	\leftrightarrow

p	$\neg p$	p	q	$p \wedge q$	p	q	$p \vee q$
1	0	1	0	0	1	0	1
0	1	1	1	1	1	1	1
1	0	0	0	0	0	0	0
		0	1	0	0	1	1

p	q	$q \oplus q$	p	q	$p \rightarrow q$	p	q	$p \leftrightarrow q$
1	0	1	1	0	0	1	0	0
1	1	0	1	1	1	1	1	1
0	0	0	0	0	1	0	0	0
0	1	1	0	1	1	0	1	0

Definition 3. Two statements are logically equivalent to each other if they have the same truth table.

Theorem 1. Law of substitution: If two statements are logically equivalent, one can substitute the other.

Definition 4. Logic substitution rules

Commutative	$p \wedge q \Leftrightarrow q \wedge p$	$p \vee q \Leftrightarrow q \vee p$
Associative	$(p \wedge q) \wedge r \Leftrightarrow q \wedge (p \wedge r)$	$(p \vee q) \vee r \Leftrightarrow q \vee (p \vee r)$
Distributive	$p \wedge (q \vee r) \Leftrightarrow (p \wedge q) \vee (p \wedge r)$	$p \vee (q \wedge r) \Leftrightarrow (p \vee q) \wedge (p \vee r)$
Identity	$p \wedge T \Leftrightarrow p$	$p \vee F \Leftrightarrow p$
Negation	$p \vee \neg p \Leftrightarrow T$	$p \wedge \neg p \Leftrightarrow F$
Double Negation	$\neg(\neg p) \Leftrightarrow p$	
Idempotent	$p \wedge p \Leftrightarrow p$	$p \vee p \Leftrightarrow p$
Universal Bound	$p \vee T \Leftrightarrow T$	$p \wedge F \Leftrightarrow F$
De Morgan's	$\neg(p \wedge q) \Leftrightarrow (\neg p) \vee (\neg q)$	$\neg(p \vee q) \Leftrightarrow (\neg p) \wedge (\neg q)$
Absorption	$p \vee (p \wedge q) \Leftrightarrow p$	$p \wedge (p \vee q) \Leftrightarrow p$
Conditional	$(p \rightarrow q) \Leftrightarrow (\neg p \vee q)$	$\neg(p \rightarrow q) \Leftrightarrow (p \wedge \neg q)$