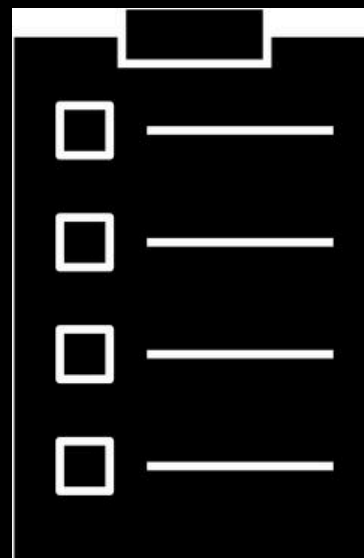


List



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Today's Plan



Recap

List ADT

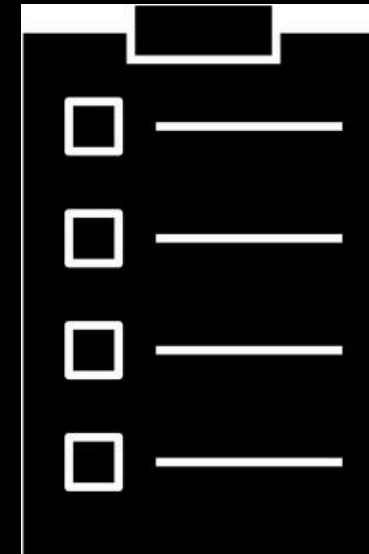
Recap

- Copy operations
 - Deep vs Shallow copy
 - Copy Constructor
 - invoked with `MyClass two = one;`
 - Assignment operator
 - invoked with `two = one;`
- Copy can be expensive and unnecessary when temporary
- Move operations
 - `std::move()` casts object as rvalue
 - If **rhs** can be cast as rvalue (don't care what happens to it next), move operations are more efficient.
 - Move constructor
 - invoked with `MyClass lvalue = rvalue;`
 - Move assignment operator
 - invoked with `lvalue = rvalue;`

List ADT

What makes a list?

E.g. Play**List**?

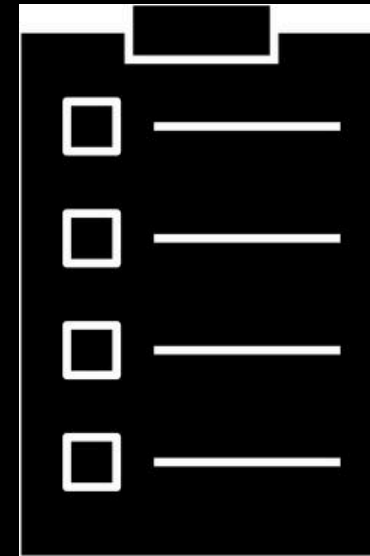


Duplicates allowed or not is not a defining factor

List ADT

What makes a list?

E.g. Play**List**?



Duplicates allowed or not is not a defining factor

ORDER!!!

Note

We will not consider Copy and Move operations in our ADTs going forward

A modern implementation should include them

The ideas are the same, so in lecture we don't need to reconsider them each time

Your textbook does not include them (not C++ 11-20 updated)

```
#ifndef LIST_H_
#define LIST_H_
```

Defines the ADT

```
template<class T>
class List
{
```

```
public:
```

```
List(); // constructor
List(const List<T>& a_list); // copy constructor
~List(); // destructor
// assume copy and move operations
bool isEmpty() const;
size_t getLength() const;
```

Used to represent the size of objects. Can think of it as unsigned int, but it is platform dependent.

```
//retains list order, position is 0 to n-1, if position > n-1 it inserts at end
bool insert(size_t position, const T& new_element);
bool remove(size_t position); //retains list order
T getItem(size_t position) const;
void clear();
```

```
private:
```

```
//implementation details here
```

Must choose implementation

```
}; // end List
```

```
#include "List.cpp"
#endif // LIST_H_
```

Implementation

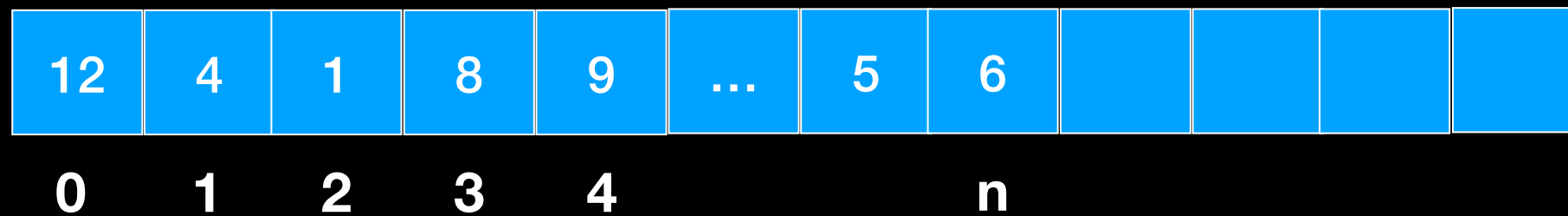
Array?

Linked Chain?

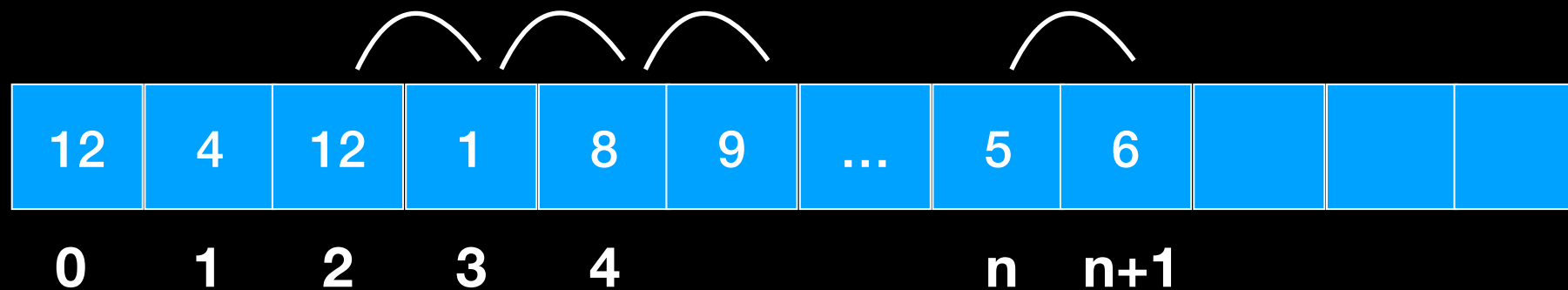
Must preserve order
No swapping tricks



Array

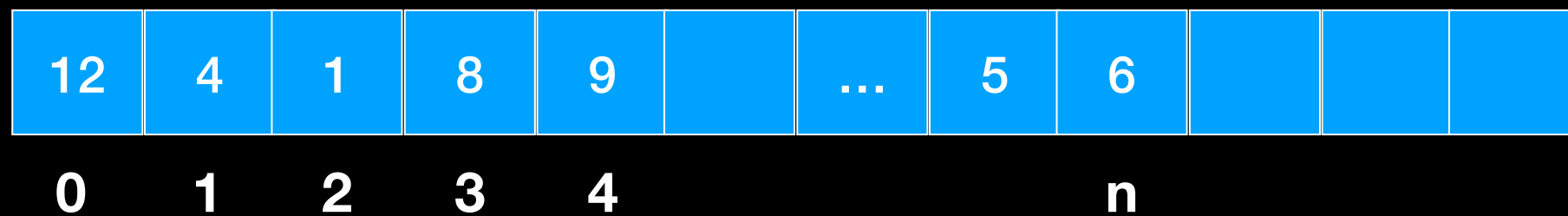


`insert(2, 12)`



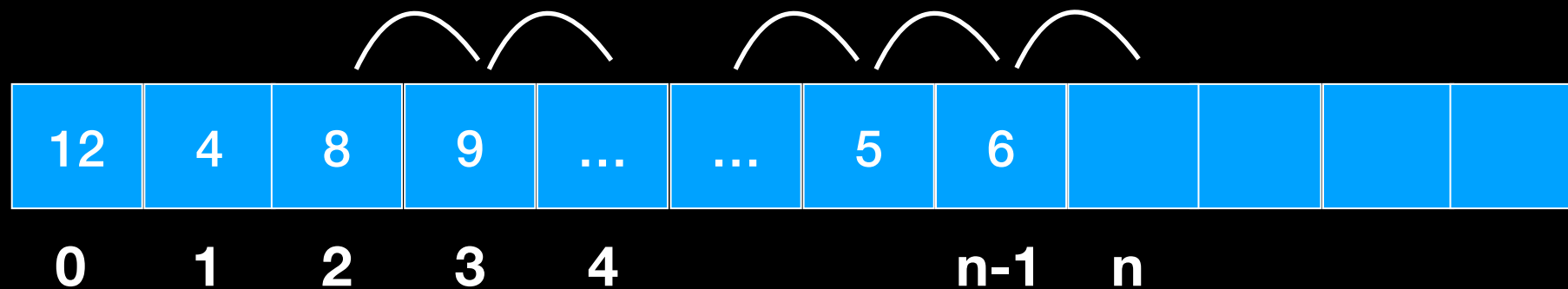
Must shift $n - (\text{position} + 1)$ elements

Array



`remove(2)`

similarly



Must shift **n-position** elements

Array Analysis

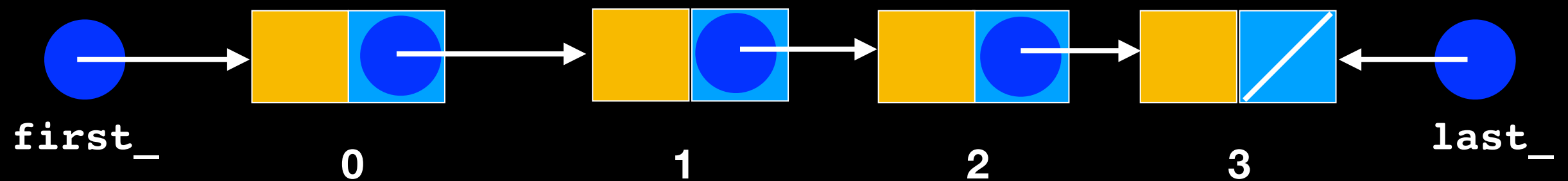
With Array both insert and remove are $O(n)$

Number of operations depends on size of List

Can we do better?

What makes a list?

Order is implied

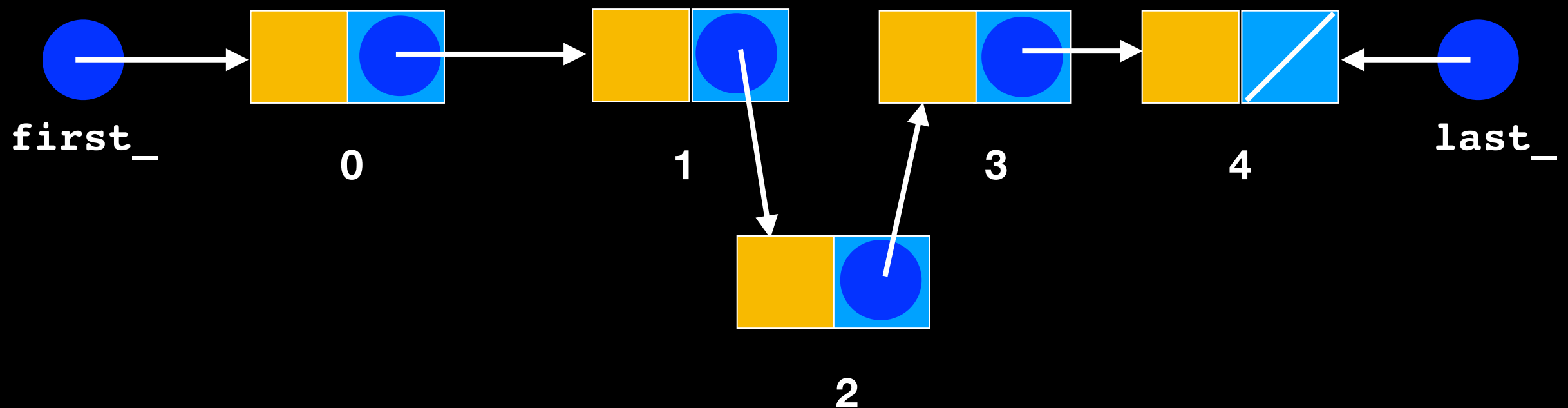


What makes a list?

Order is implied

Insertion and removal from middle retains order

No shifting necessary

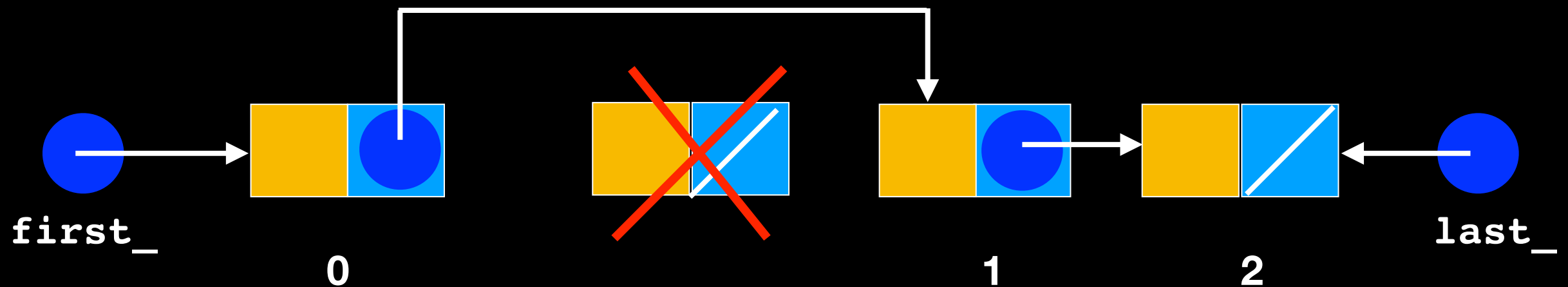


What makes a list?

Order is implied

Insertion and **removal** from middle retains order

No shifting necessary



What's the catch?

What's the catch?

No random access

As opposed to arrays or vectors with direct indexing

$O(n)$: each insertion and removal must traverse
`position+1` nodes

Here too, number of operations depends on size of
List



$O(1)$ Constant



$O(n)$ depends on # of items



	Arrays	Linked List
Random/direct access		
Retain order with Insert and remove At the back		
Retain order with insert and remove at front		
Retain order with insert and remove In the middle		



O(1) Constant



O(n) depends on # of items





	Arrays	Linked List
Random/direct access		
Retain order with Insert and remove At the back		
Retain order with insert and remove at front		
Retain order with insert and remove In the middle		



O(1) Constant



O(n) depends on # of items







	Arrays	Linked List
Random/direct access		
Retain order with Insert and remove At the back		
Retain order with insert and remove at front		
Retain order with insert and remove In the middle		



O(1) Constant



O(n) depends on # of items

	Arrays	Linked List
Random/direct access		
Retain order with Insert and remove At the back		
Retain order with insert and remove at front		
Retain order with insert and remove In the middle		



$O(1)$ Constant



$O(n)$ depends on # of items

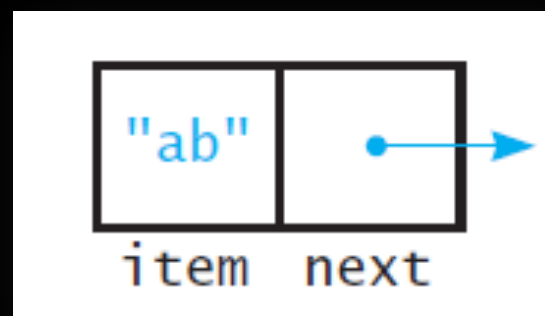
No shifting but incurs cost of finding the node to remove (call to getPointerTo)

	Arrays	Linked List
Random/direct access		
Retain order with Insert and remove At the back		
Retain order with insert and remove at front		
Retain order with insert and remove In the middle		



Singly-Linked List

Use the same node as the LinkedList



```

#ifndef LIST_H_
#define LIST_H_

#include "Node.hpp"

template<class T>
class List
{
public:
    List(); // constructor
    List(const List<T>& a_list); // copy constructor
    ~List(); // destructor
    bool isEmpty() const;
    size_t getLength() const;

    //retains list order, position is 0 to n-1, if position > n-1 it inserts at end
    bool insert(size_t position, const T& new_element);
    bool remove(size_t position); //retains list order
    T getItem(size_t position) const;
    void clear();

private:
    Node<T>* first_; // Pointer to first node
    Node<T>* last_; // Pointer to last node
    size_t item_count_; // number of items in the list

    Node<T>* getPointerTo(size_t position) const;

}; // end List

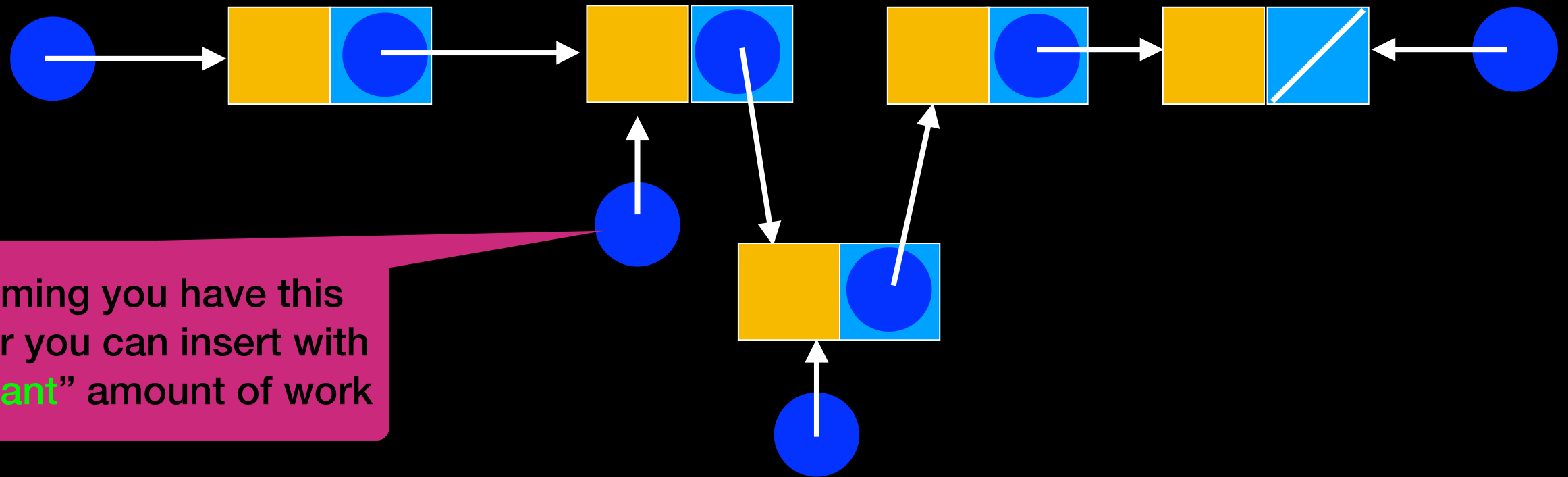
#include "List.cpp"
#endif // LIST_H_

```

Additional pointer to last node.

INSERT

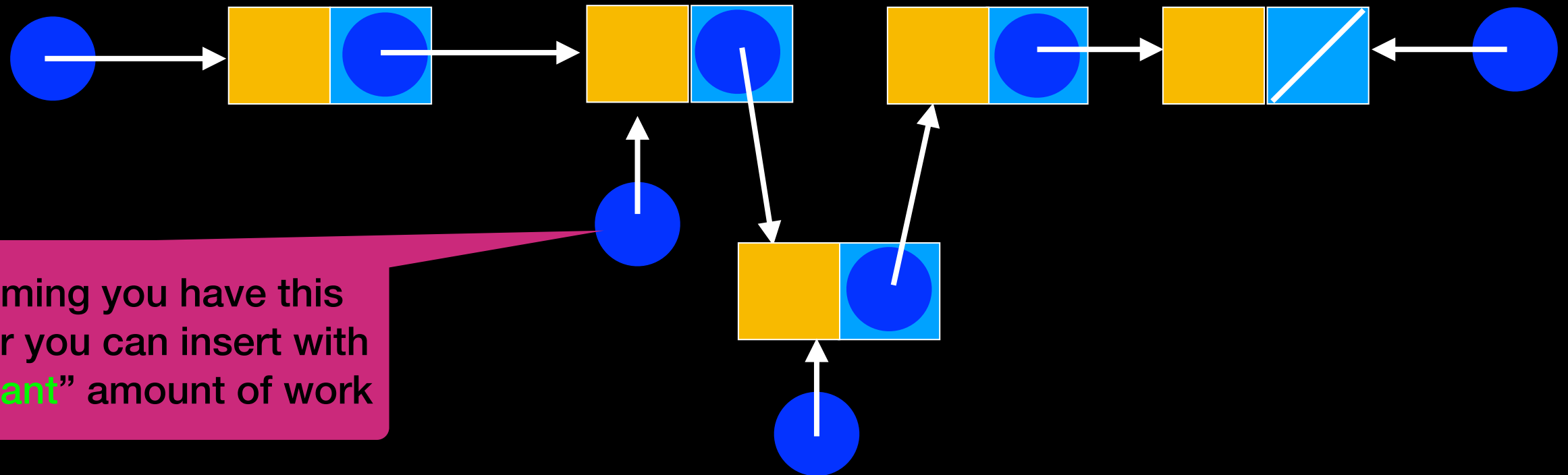
```
void insert(size_t position, T new_element);
```



Assuming you have this pointer you can insert with “constant” amount of work

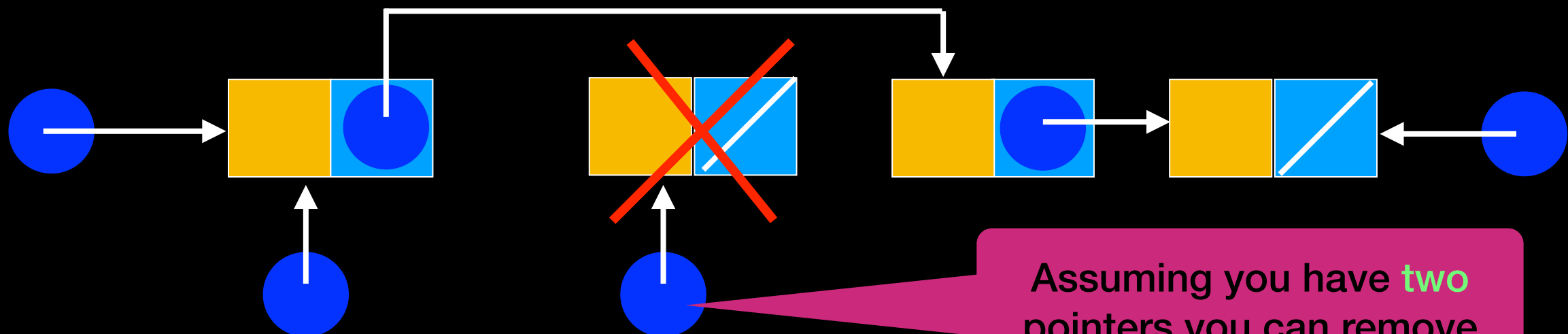
INSERT

```
void insert(size_t position, T new_element);
```



REMOVE

```
void remove(size_t position);
```

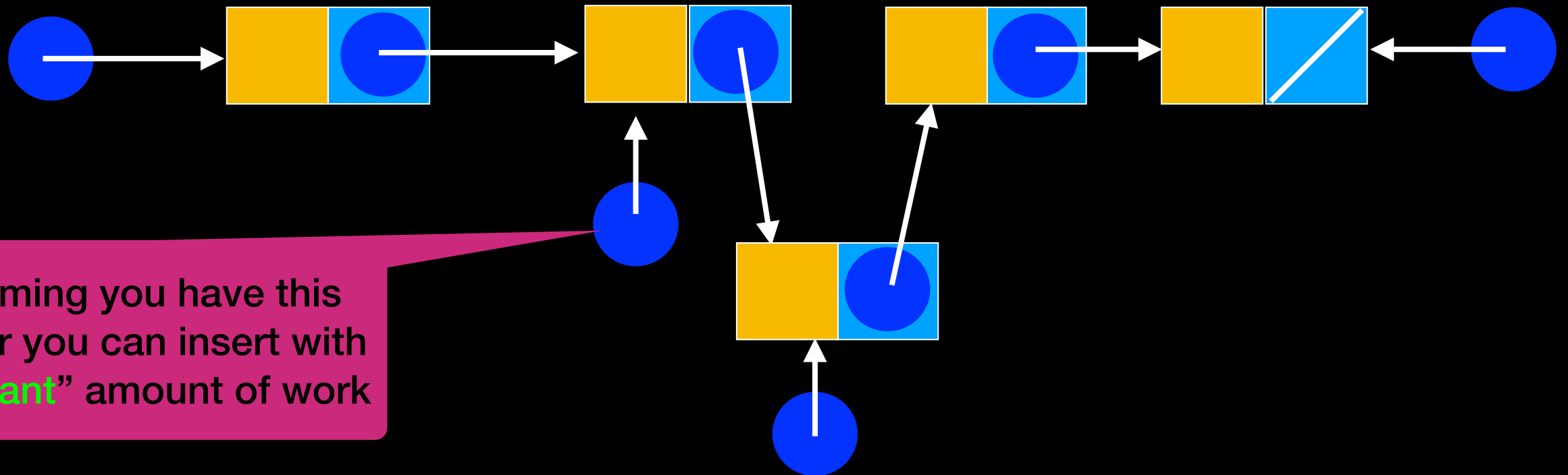


Caveat

Find the pointer to the node before inserting/
removing —> traversal: $O(n)$ - *depends on number of
elements in list*

INSERT

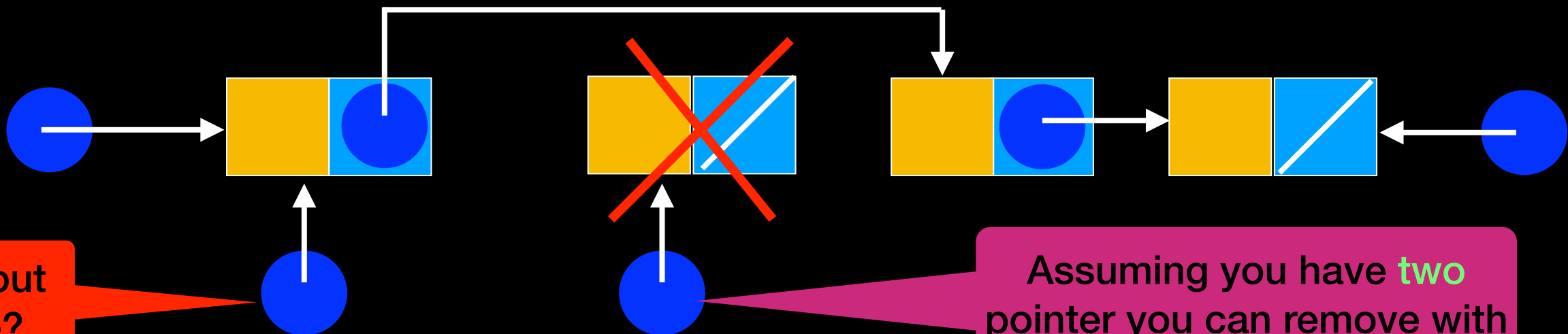
```
void insert(size_t position, T new_element);
```



Assuming you have this pointer you can insert with “constant” amount of work

REMOVE

```
void remove(size_t position);
```



What about this one?

Assuming you have **two** pointer you can remove with “**constant**” amount of work

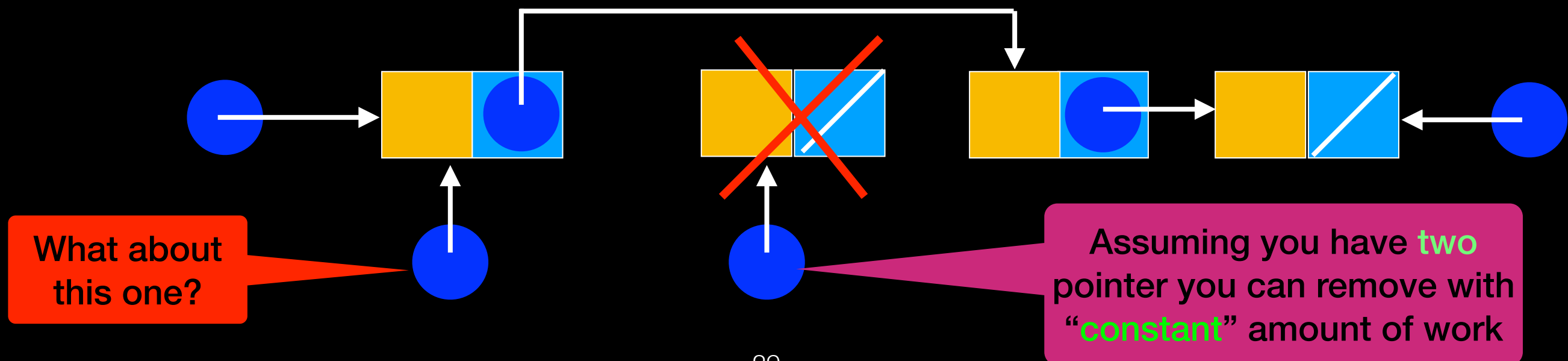
Lecture Activity

Design

Propose a solution to this problem:

In English write a few sentences describing the changes you would make to the Linked-Chain implementation of the List ADT to remove any node in the chain

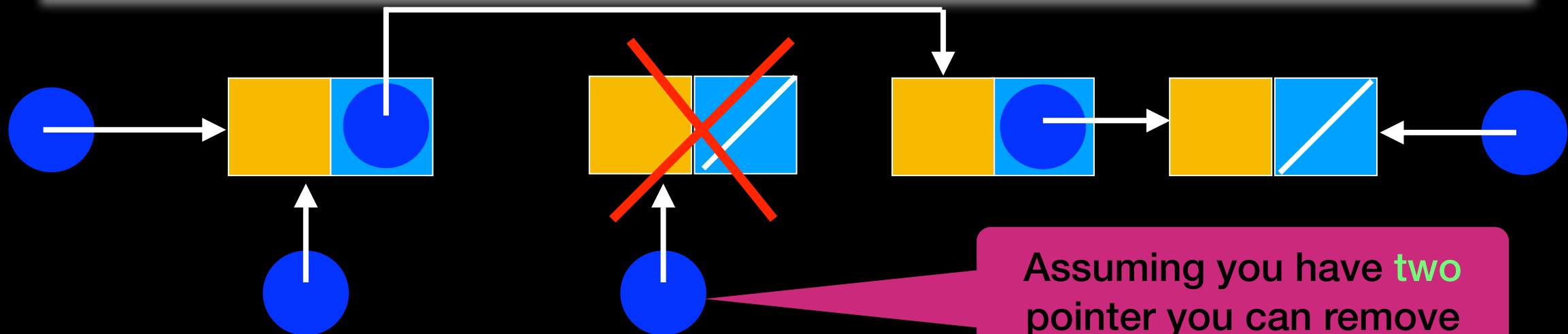
REMOVE `void remove(size_t position);`



One possible solution:
Remove makes **two calls** to `getPointerTo`,
One with `position` and another with
`position-1`

REMOVE

```
void remove(size_t position);  
Node<T>* getPointerTo(size_t position);
```



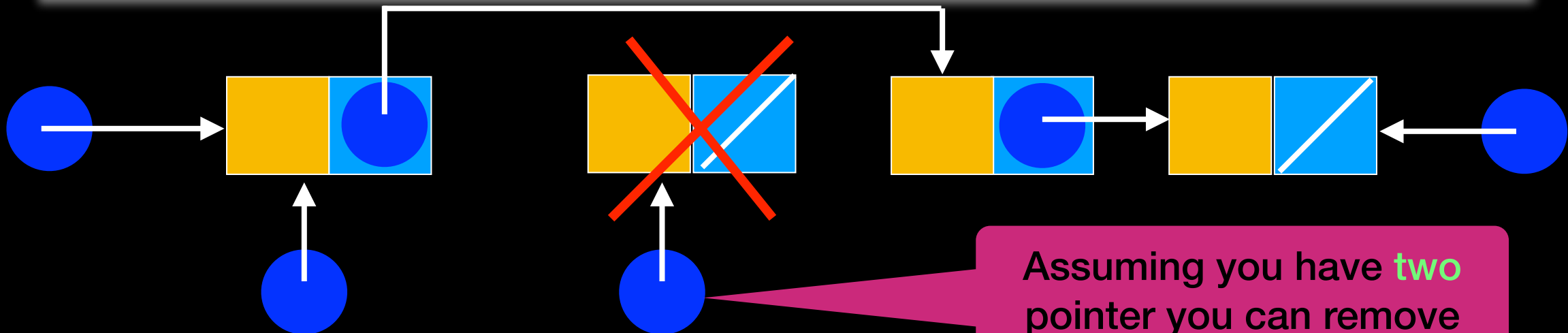
Assuming you have **two**
pointer you can remove
with “**constant**” amount of

Another possible solution:
Remove sets

```
position-1 = position->getNext();
```

REMOVE

```
void remove(size_t position);  
Node<T>* getPointerTo(size_t position);
```



Assuming you have **two** pointer you can remove with “**constant**” amount of

Another Approach

Doubly Linked List

New node with `previous_` and `next_` pointers




```
#ifndef NODE_H_
#define NODE_H_
```

```
template<class T>
class Node
{
```

```
public:
```

```
    Node();
    Node(const T& an_item);
    Node(const T& an_item, Node<T>* next_node_ptr);
    void setItem(const T& an_item);
    void setNext(Node<T>* next_node_ptr);
    void setPrevious(Node<T>* prev_node_ptr);
```

```
    T getItem() const;
    Node<T>* getNext() const;
    Node<T>* getPrevious() const;
```

```
private:
```

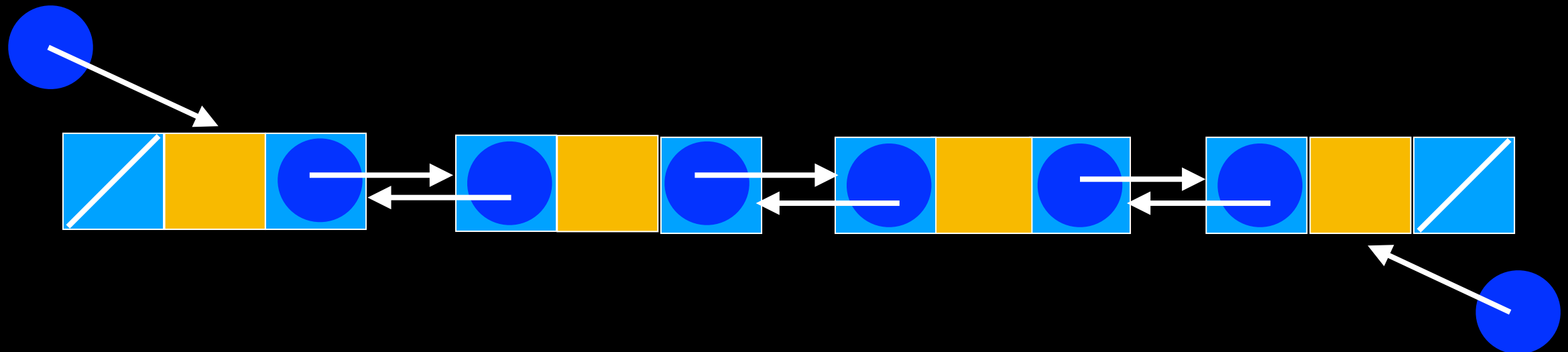
```
    T item_; // A data item
    Node<T>* next; // Pointer to next node
    Node<T>* previous_; // Pointer to previous node
```

```
}; // end Node
```

```
#include "Node.cpp"
#endif // NODE_H_
```



Doubly Linked List



```

#ifndef LIST_H_
#define LIST_H_

#include "Node.hpp"

template<class T>
class List
{
public:
    List(); // constructor
    List(const List<T>& a_list); // copy constructor
    ~List(); // destructor
    bool isEmpty() const;
    size_t getLength() const;
    //retains list order, position is 0 to n-1, if position > n-1 it inserts at end
    bool insert(size_t position, const T& new_element); //retains list order
    bool remove(size_t position); //retains list order
    T getItem(size_t position) const;
    void clear();

private:
    Node<T>* first_; // Pointer to first node
    Node<T>* last_; // Pointer to last node
    size_t item_count_; // number of items in the list

    Node<T>* getPointerTo(size_t position) const;
}; // end List

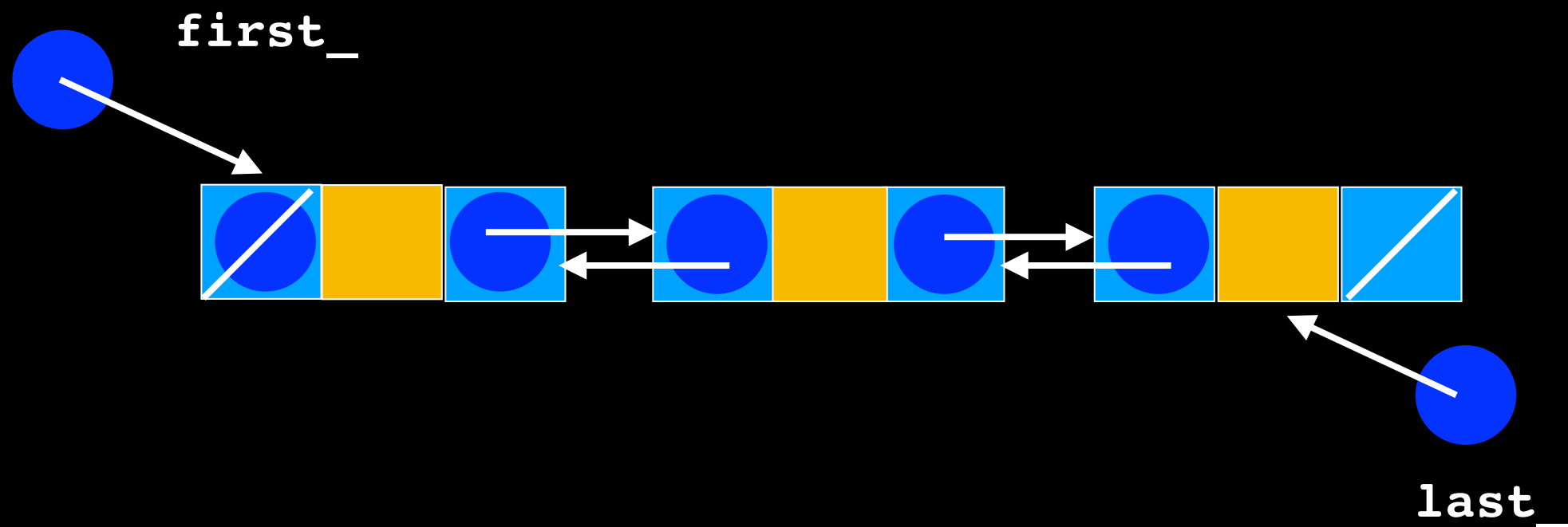
#include "List.cpp"
#endif // LIST_H_

```

Same interface as
Singly-Linked list but
uses different node

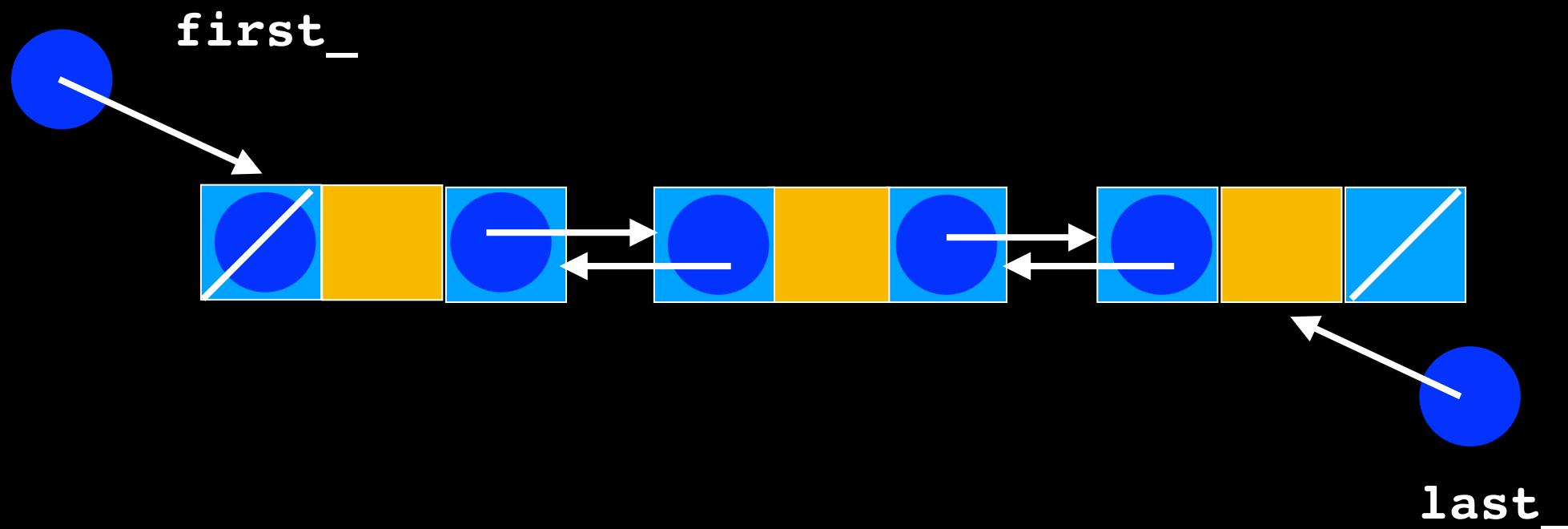
List::insert

What are the different cases that should be considered?



Lecture Activity

Write **Pseudocode** to insert a node at $\text{position} > 0$ and $\text{position} < n-1$ in a doubly-linked list (assume position follows classic indexing from 0 to $\text{item_count} - 1$)



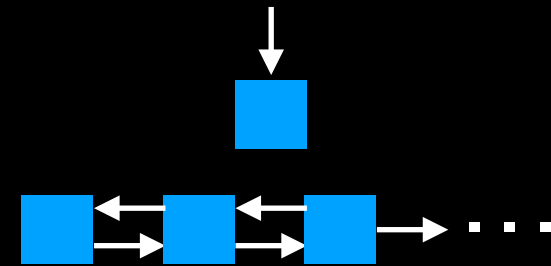
Pseudocode

Instantiate new node

Obtain pointer

Connect new node to chain

Reconnect the relevant nodes



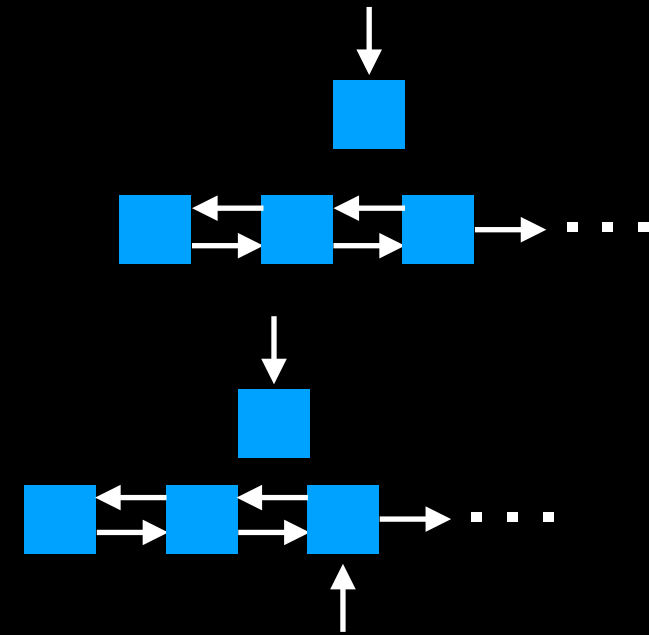
Pseudocode

Instantiate new node

Obtain pointer

Connect new node to chain

Reconnect the relevant nodes

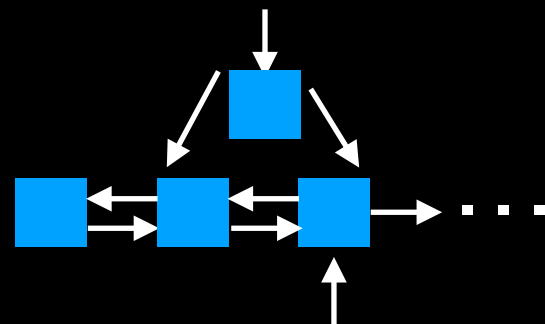


Pseudocode

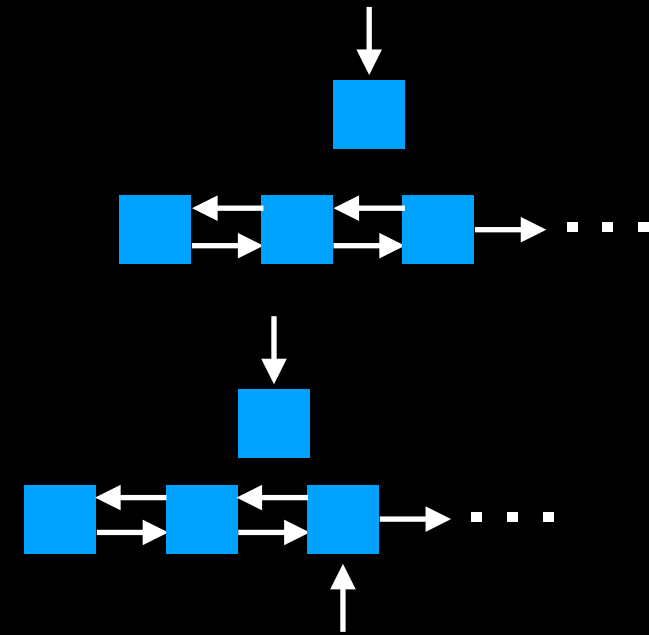
Instantiate new node

Obtain pointer

Connect new node to chain



Reconnect the relevant nodes



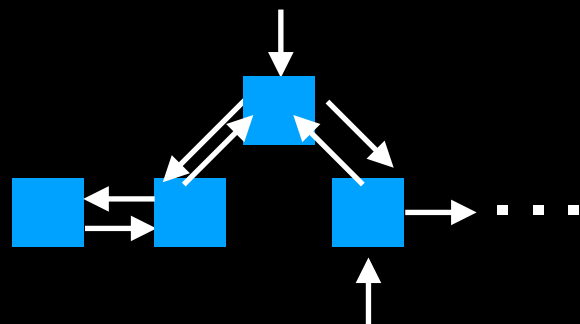
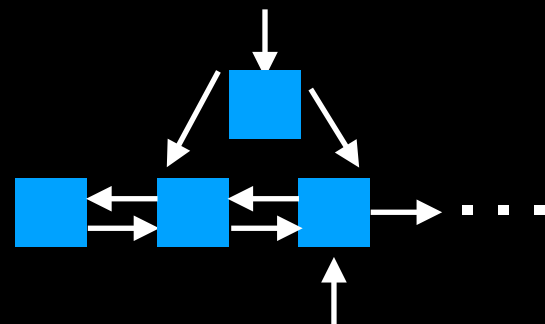
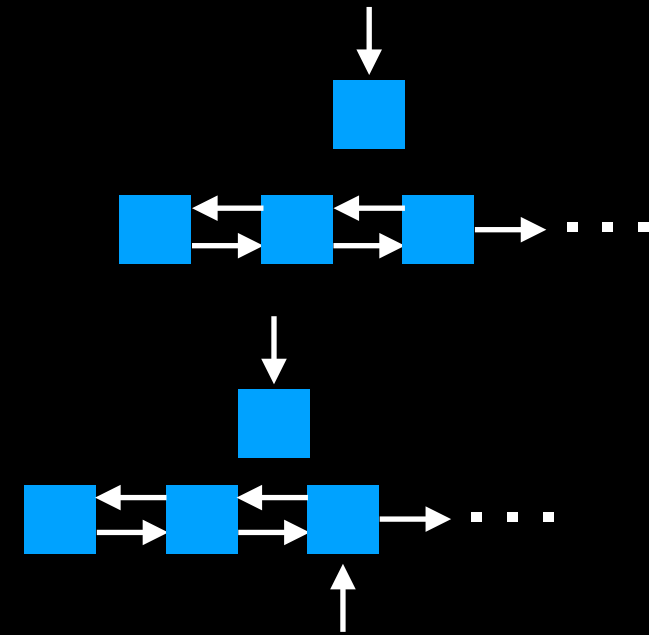
Pseudocode

Instantiate new node

Obtain pointer

Connect new node to chain

Reconnect the relevant nodes



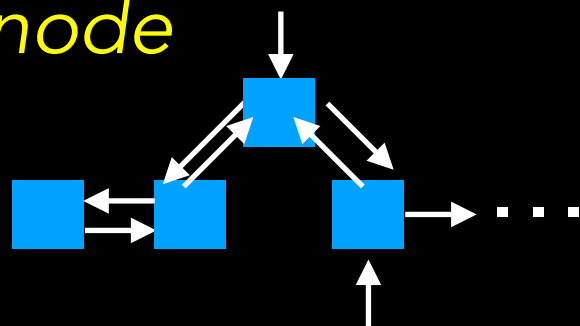
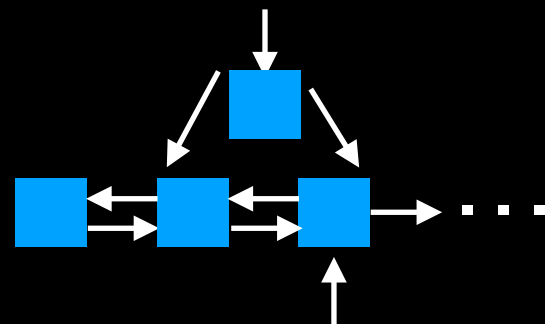
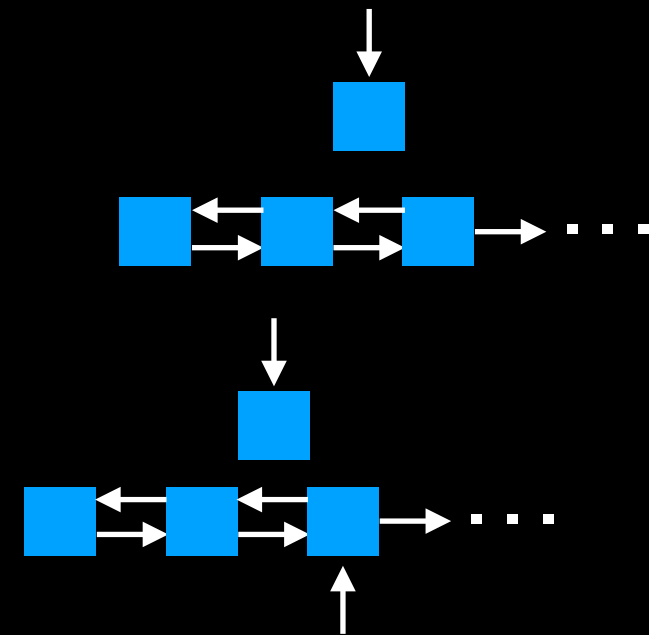
Pseudocode

Instantiate new node to be inserted and set its value

Obtain pointer to node currently at position

Connect new node to chain by pointing *its next pointer* to the node currently at *position* and *its previous pointer* to the node at *position->previous*

Reconnect the relevant nodes in the chain by pointing *position->previous->next* to the *new node* and *position->previous* to the *new node*



Order Matters!

More Pseudocode

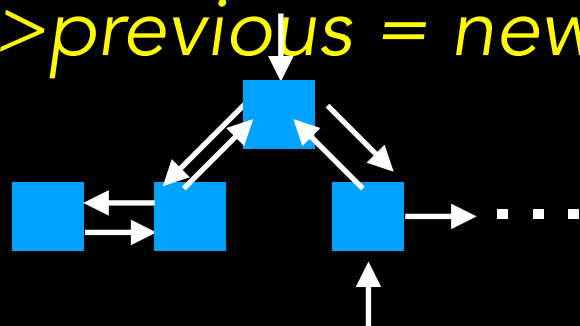
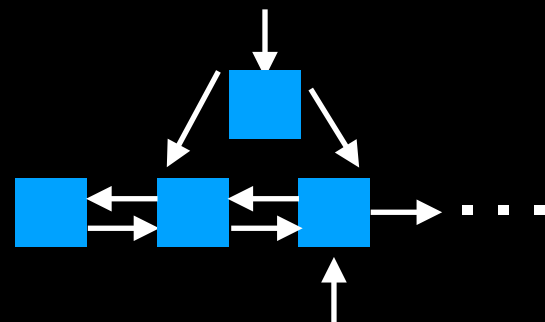
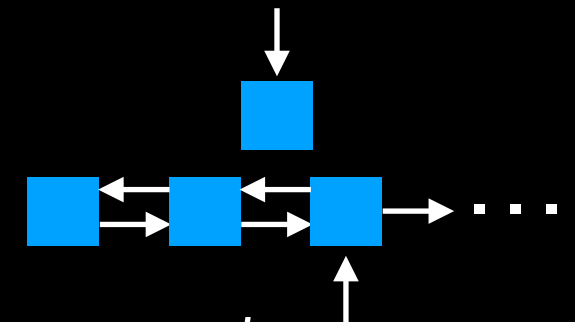
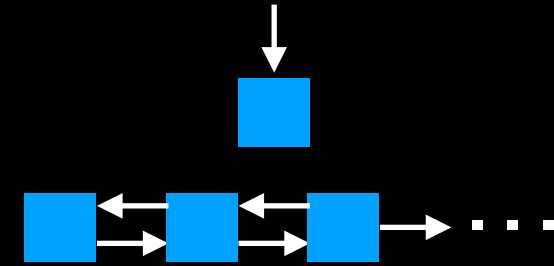
Instantiate new node $\text{new_ptr} = \text{new Node}()$ and $\text{new_ptr} \rightarrow \text{setItem}()$

Obtain pointer $\text{position_ptr} = \text{getPointerTo}(\text{position})$

Connect new node to chain $\text{new_ptr} \rightarrow \text{next} = \text{position_ptr}$ and
 $\text{new_ptr} \rightarrow \text{previous} = \text{temp} \rightarrow \text{previous}$

Reconnect the relevant nodes

$\text{position_ptr} \rightarrow \text{previous} \rightarrow \text{next} = \text{new_ptr}$ and
 $\text{position} \rightarrow \text{previous} = \text{new_ptr}$



List::insert

```
template<class T>
bool List<T>::insert(size_t position, const T& new_element)
{
    // Create a new node containing the new entry and get a pointer to position
    Node<T>* new_node_ptr = new Node<T>(new_element);
    Node<T>* pos_ptr = getPointerTo(position);  $O(n)$ 

    // Attach new node to chain

    2 else if (pos_ptr == first_)
    {
        // Insert new node at beginning of list
        new_node_ptr->setNext(first_);
        new_node_ptr->setPrevious(nullptr);
        first_>setPrevious(new_node_ptr);
        first_ = new_node_ptr;
    }

    3 else if (pos_ptr == nullptr)
    {
        //insert at end of list
        new_node_ptr->setNext(nullptr);
        new_node_ptr->setPrevious(last_);
        last_>setNext(new_node_ptr);
        last_ = new_node_ptr;
    }

    4 else
    {
        // Insert new node before node to which position points
        new_node_ptr->setNext(pos_ptr);
        new_node_ptr->setPrevious(pos_ptr->getPrevious());
        pos_ptr->getPrevious()->setNext(new_node_ptr);
        pos_ptr->setPrevious(new_node_ptr);
    } // end if

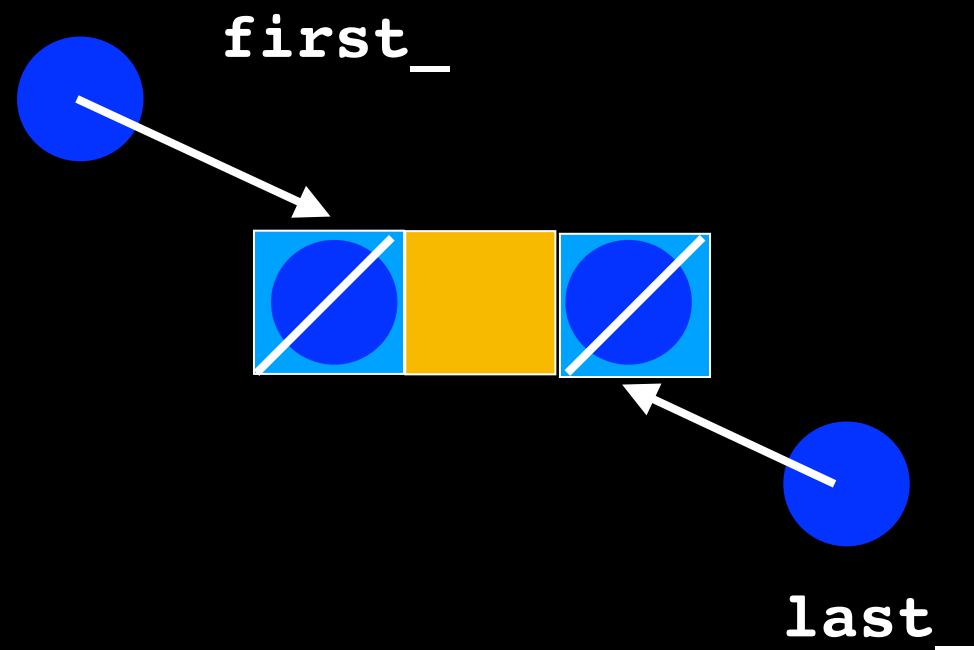
    item_count++; // Increase count of entries
    return true;
} // end insert
```

```
1 if (first_ == nullptr)
{
    // Insert first node
    new_node_ptr->setNext(nullptr);
    new_node_ptr->setPrevious(nullptr);
    first_ = new_node_ptr;
    last_ = new_node_ptr;
}
```

4 $O(1)$ cases

Always insert

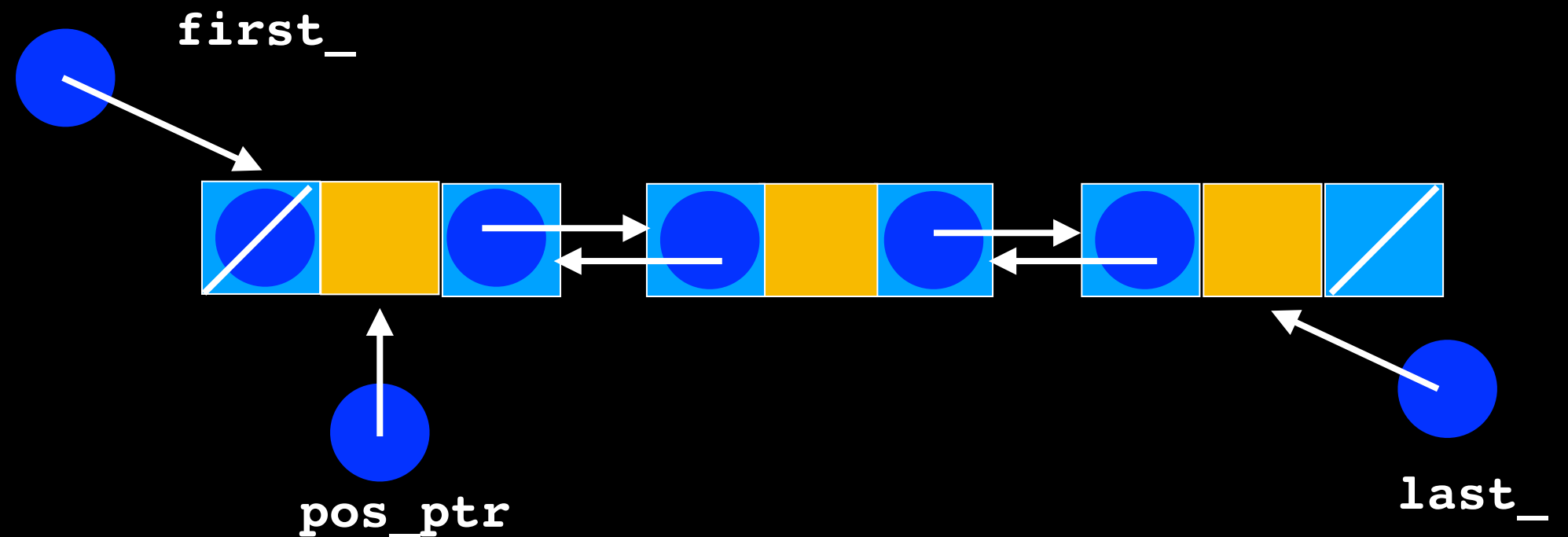
```
1  if (first_ == nullptr)
    {
        // Insert first node
        new_node_ptr->setNext(nullptr);
        new_node_ptr->setPrevious(nullptr);
        first_ = new_node_ptr;
        last_ = new_node_ptr;
    }
```



```

2 else if (pos_ptr == first_)
{
    // Insert new node at beginning of chain
    new_node_ptr->setNext(first_);
    new_node_ptr->setPrevious(nullptr);
    first_->setPrevious(new_node_ptr);
    first_ = new_node_ptr;
}

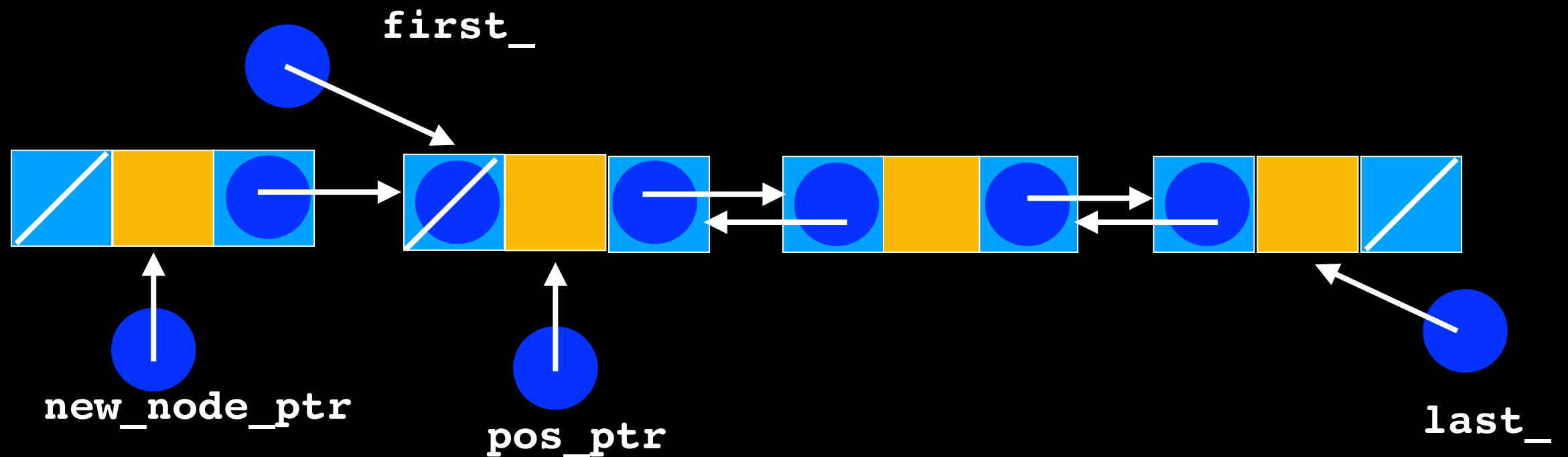
```



```

2 else if (pos_ptr == first_)
{
    // Insert new node at beginning of chain
    new_node_ptr->setNext(first_);
    new_node_ptr->setPrevious(nullptr);
    first_>setPrevious(new_node_ptr);
    first_ = new_node_ptr;
}

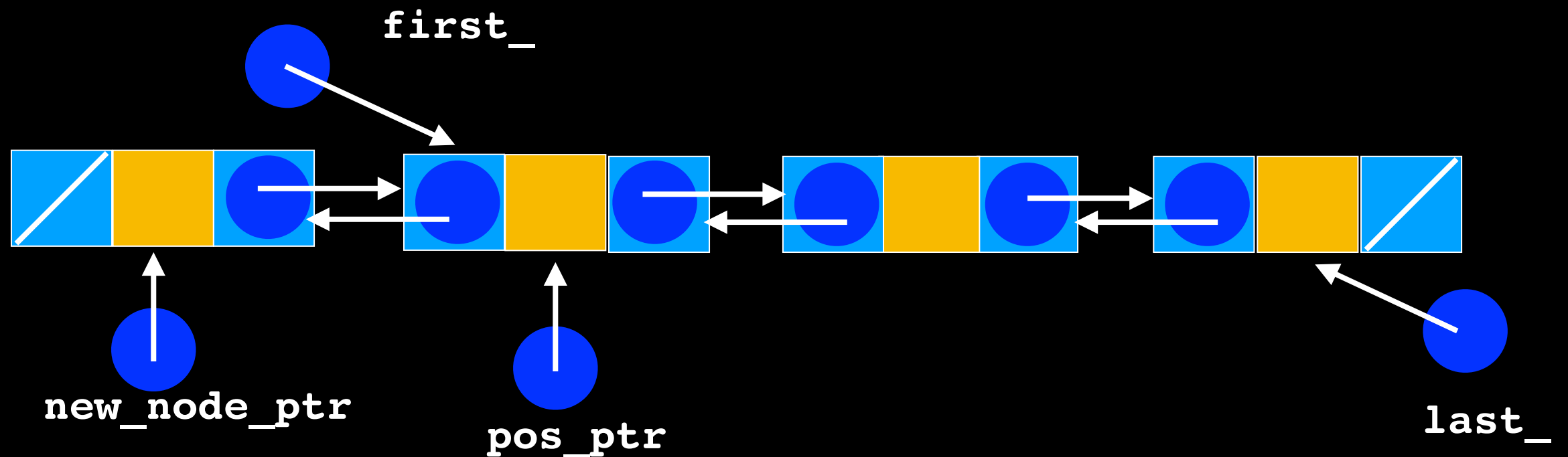
```



```

2 else if (pos_ptr == first_)
{
    // Insert new node at beginning of chain
    new_node_ptr->setNext(first_);
    new_node_ptr->setPrevious(nullptr);
    first_>setPrevious(new_node_ptr);
    first_ = new_node_ptr;
}

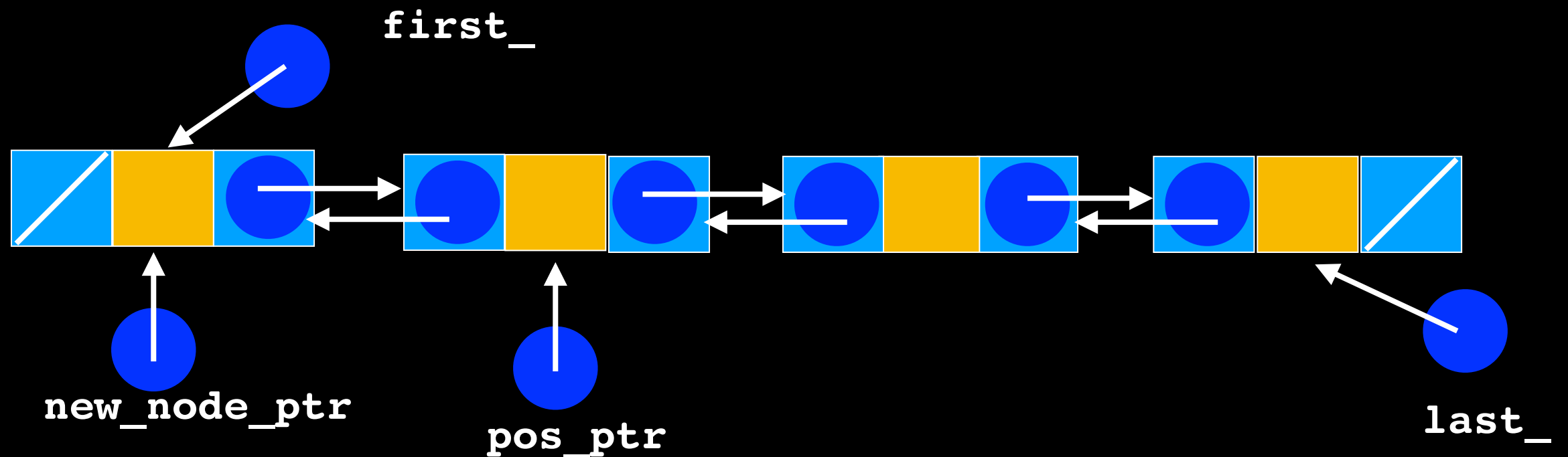
```




```

2 else if (pos_ptr == first_)
{
    // Insert new node at beginning of chain
    new_node_ptr->setNext(first_);
    new_node_ptr->setPrevious(nullptr);
    first_>setPrevious(new_node_ptr);
    first_ = new_node_ptr;
}

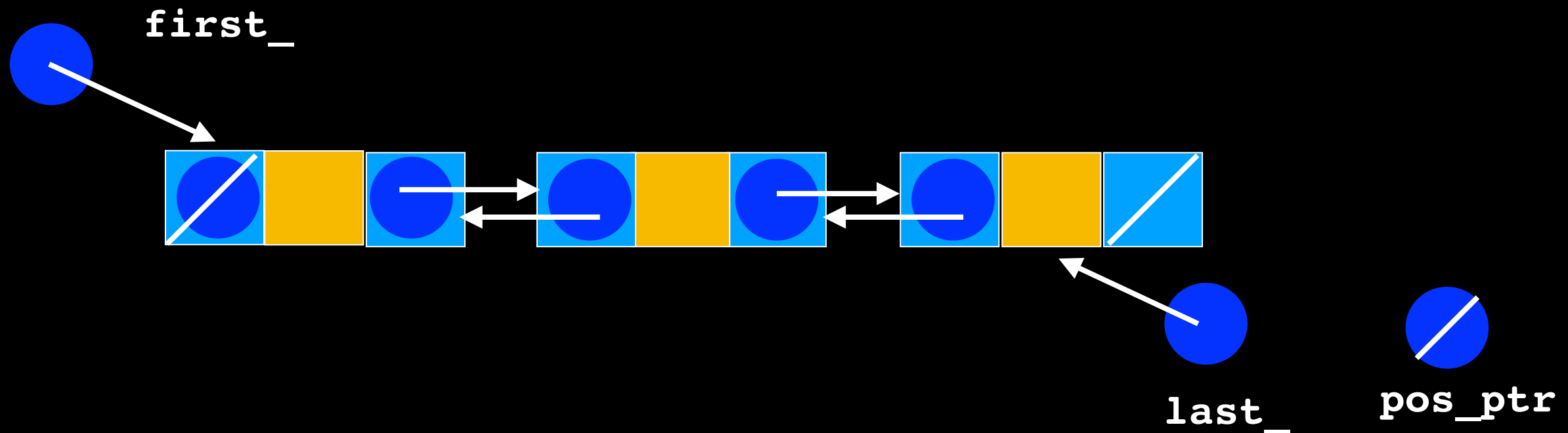
```



```

3  else if (pos_ptr == nullptr)
{
    //insert at end of list
    new_node_ptr->setNext(nullptr);
    new_node_ptr->setPrevious(last_);
    last_->setNext(new_node_ptr);
    last_ = new_node_ptr;
}

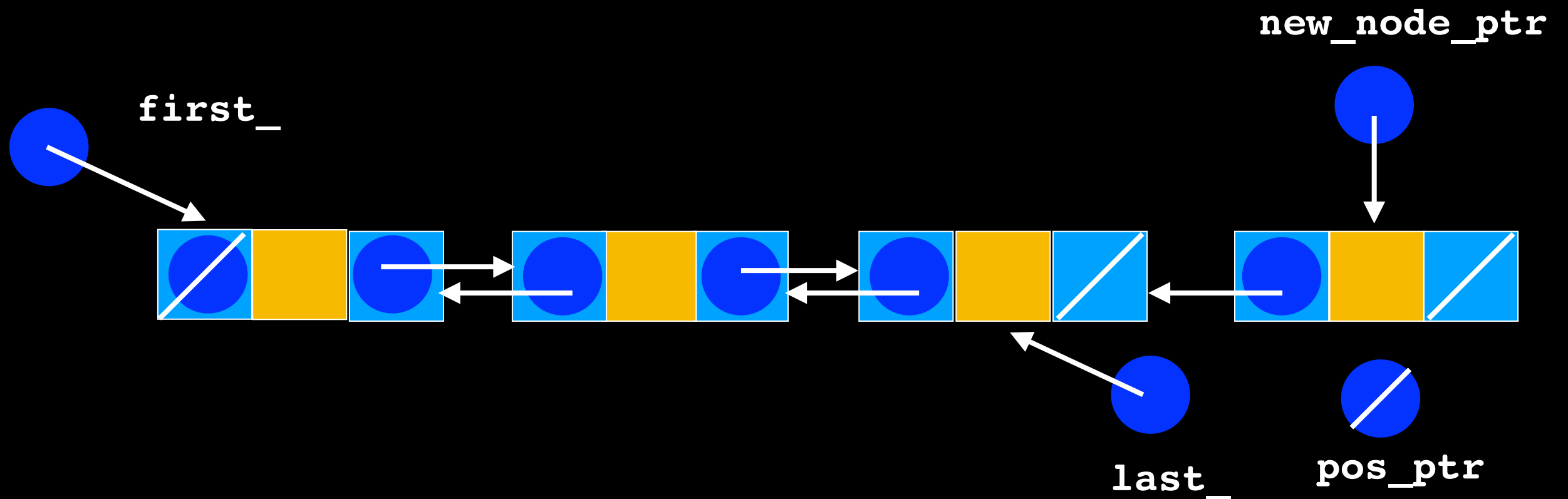
```



```

3  else if (pos_ptr == nullptr)
{
    //insert at end of list
    new_node_ptr->setNext(nullptr);
    new_node_ptr->setPrevious(last_);
    last_->setNext(new_node_ptr);
    last_ = new_node_ptr;
}

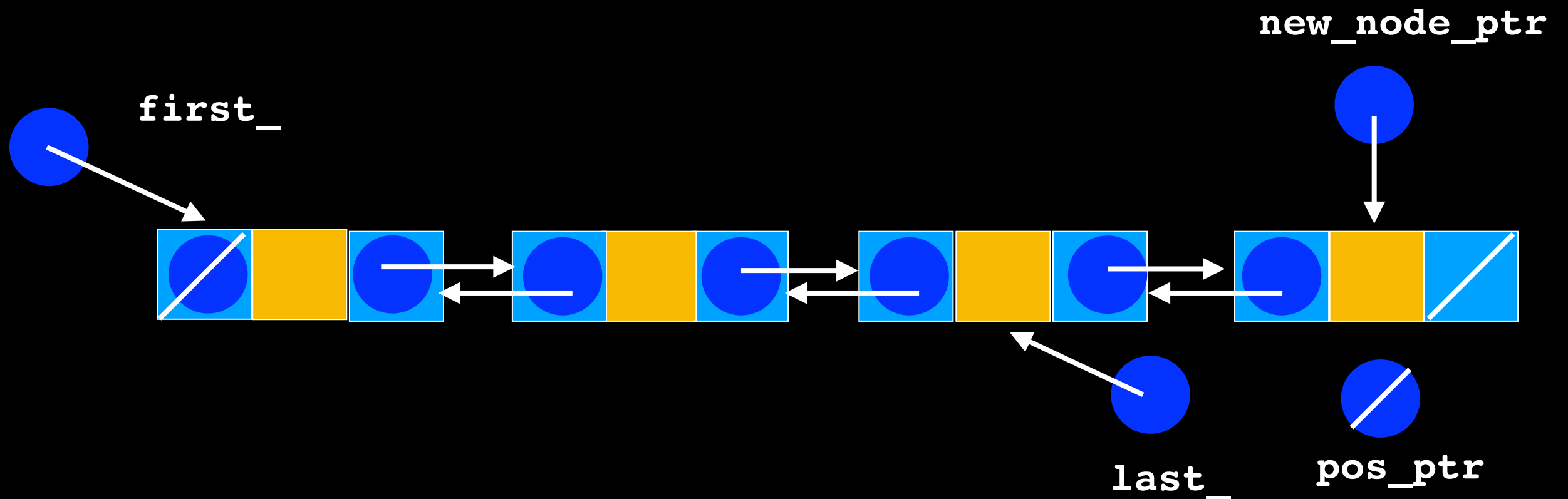
```



```

3  else if (pos_ptr == nullptr)
{
    //insert at end of list
    new_node_ptr->setNext(nullptr);
    new_node_ptr->setPrevious(last_);
    last_->setNext(new_node_ptr);
    last_ = new_node_ptr;
}

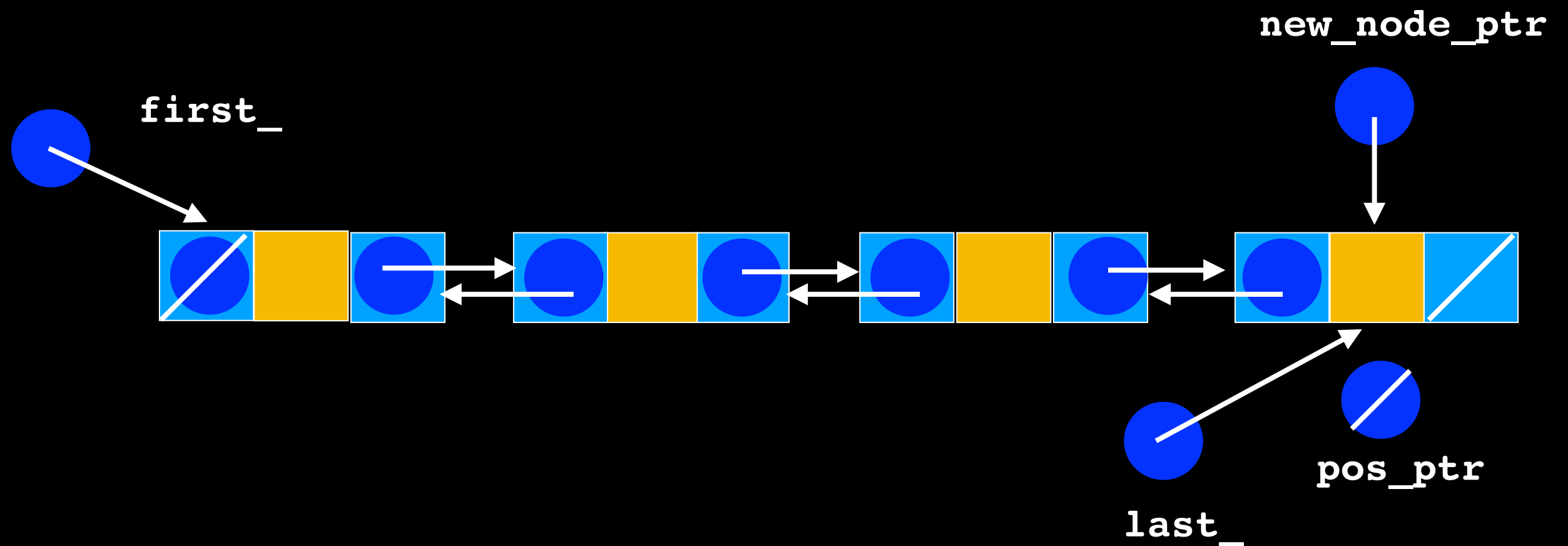
```



```

3  else if (pos_ptr == nullptr)
{
    //insert at end of list
    new_node_ptr->setNext(nullptr);
    new_node_ptr->setPrevious(last_);
    last_>setNext(new_node_ptr);
    last_ = new_node_ptr;
}

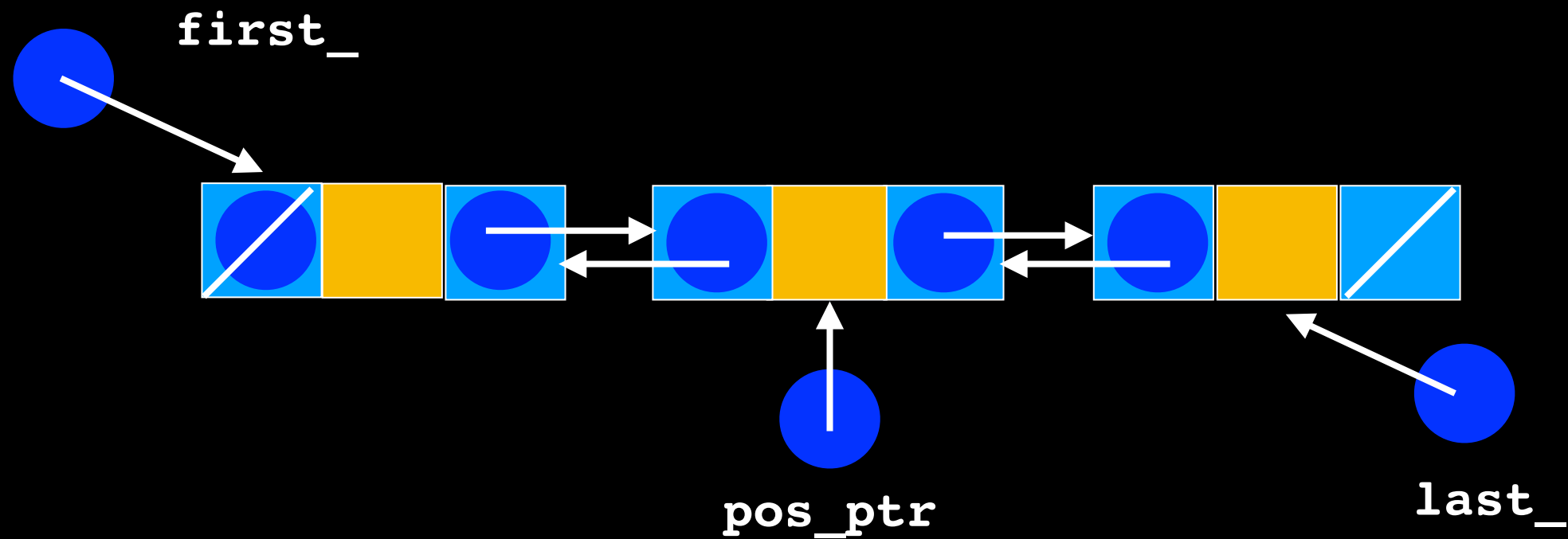
```



```

4 else
{
    // Insert new node before node to which position points
    new_node_ptr->setNext(pos_ptr);
    new_node_ptr->setPrevious(pos_ptr->getPrevious());
    pos_ptr->getPrevious()->setNext(new_node_ptr);
    pos_ptr->setPrevious(new_node_ptr);
} // end if

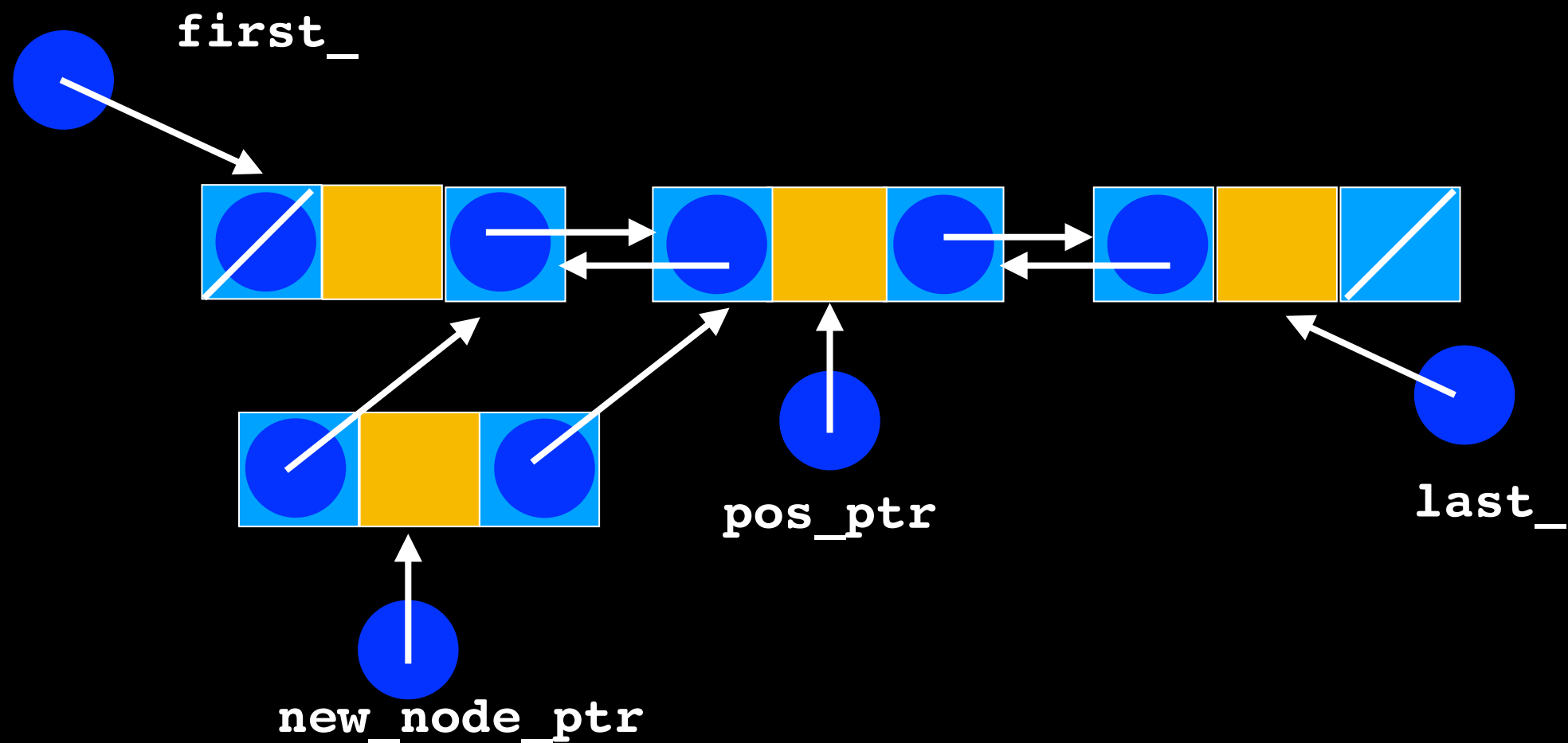
```



```

4 else
{
    // Insert new node before node to which position points
    new_node_ptr->setNext(pos_ptr);
    new_node_ptr->setPrevious(pos_ptr->getPrevious());
    pos_ptr->getPrevious()->setNext(new_node_ptr);
    pos_ptr->setPrevious(new_node_ptr);
}
// end if

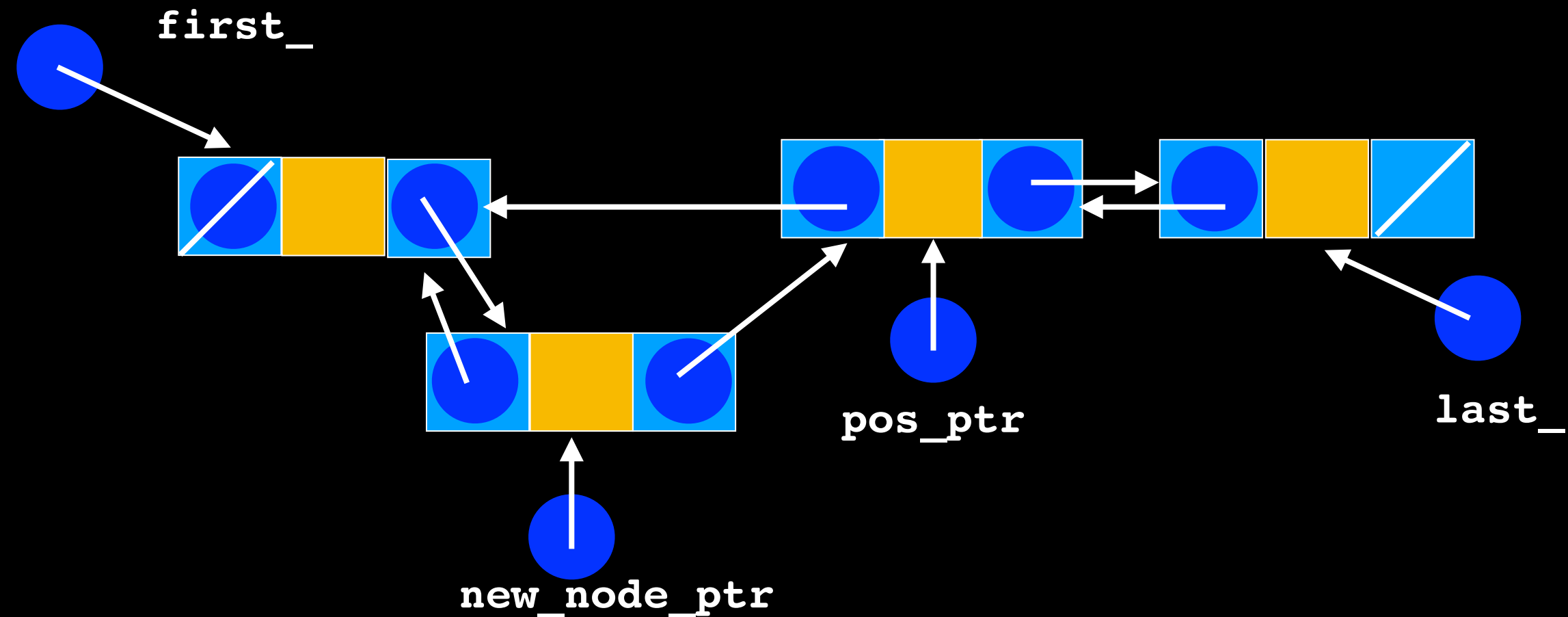
```



```

4 else
{
    // Insert new node before node to which position points
    new_node_ptr->setNext(pos_ptr);
    new_node_ptr->setPrevious(pos_ptr->getPrevious());
    pos_ptr->getPrevious()->setNext(new_node_ptr);
    pos_ptr->setPrevious(new_node_ptr);
} // end if

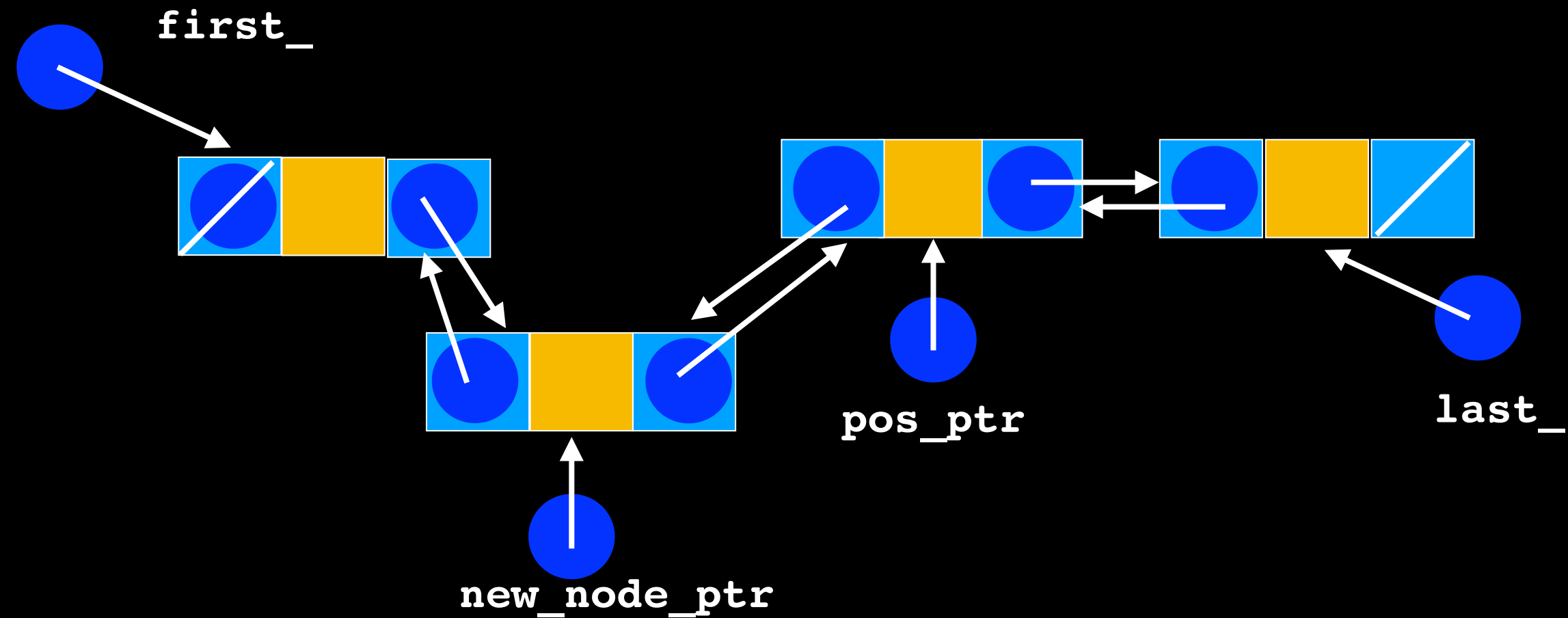
```




```

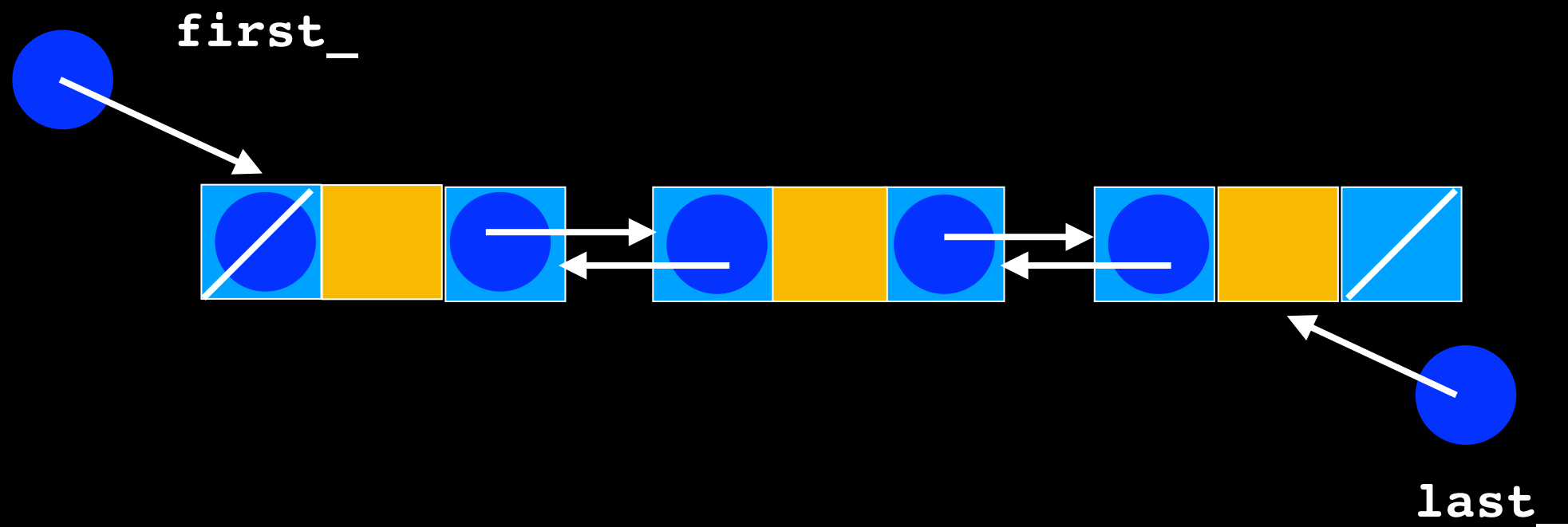
4 else
{
    // Insert new node before node to which position points
    new_node_ptr->setNext(pos_ptr);
    new_node_ptr->setPrevious(pos_ptr->getPrevious());
    pos_ptr->getPrevious()->setNext(new_node_ptr);
    pos_ptr->setPrevious(new_node_ptr);
} // end if

```



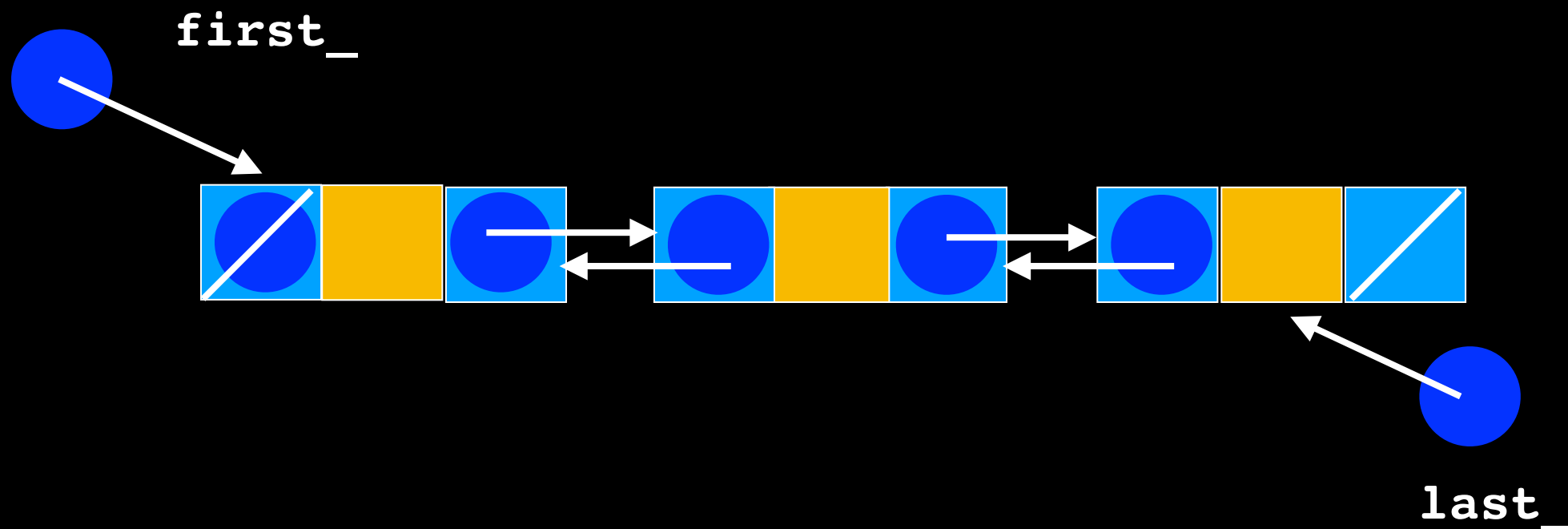
List::remove

What are the different cases that should be considered?



Lecture Activity

Write **Pseudocode** to remove the node at position 1 in a doubly-linked list (assume position follows classic indexing from 0 to item_count - 1, and there is a node at position 2)



List::Remove

```
template<class T>
bool List<T>::remove(size_t position)
{
```

0 // get pointer to position
Node<T>* pos_ptr = getPointerTo(position); $O(n)$
if (pos_ptr == nullptr) // no node at position
return false;

else
{
// Remove node from chain

3 else if (pos_ptr == last_)
{
//remove last_ node
last_ = pos_ptr->getPrevious();
last_ ->setNext(nullptr);

// Return node to the system
pos_ptr->setPrevious(nullptr);
delete pos_ptr;
pos_ptr = nullptr;

4 } else
{
//Remove from the middle
pos_ptr->getPrevious()->setNext(pos_ptr->getNext());
pos_ptr->getNext()->setPrevious(pos_ptr->getPrevious());

// Return node to the system
pos_ptr->setNext(nullptr);
pos_ptr->setPrevious(nullptr);
delete pos_ptr;
pos_ptr = nullptr;

}
item_count--;
return true;

}
// end remove

1 if ((pos_ptr == first_) && pos_ptr == last_)
{
// Only one node
first_ = nullptr;
last_ = nullptr;

// Return node to the system
pos_ptr->setNext(nullptr);
delete pos_ptr;
pos_ptr = nullptr;
}

2 if (pos_ptr == first_)
{
// Remove first node
first_ = pos_ptr->getNext();
first_->setPrevious(nullptr);

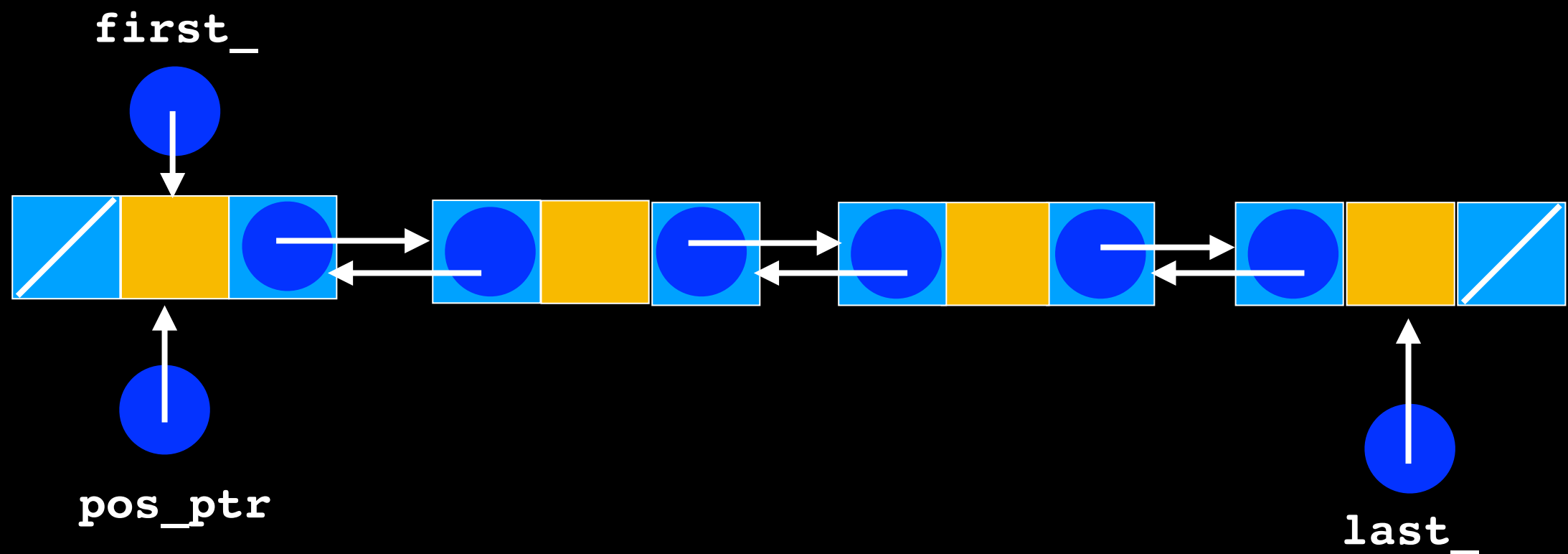
// Return node to the system
pos_ptr->setNext(nullptr);
delete pos_ptr;
pos_ptr = nullptr;
}

5 $O(1)$ cases

2

```
// Remove node from chain
if (pos_ptr == first_)
{
    // Remove first node
    first_ = pos_ptr->getNext();
    first_->setPrevious(nullptr);

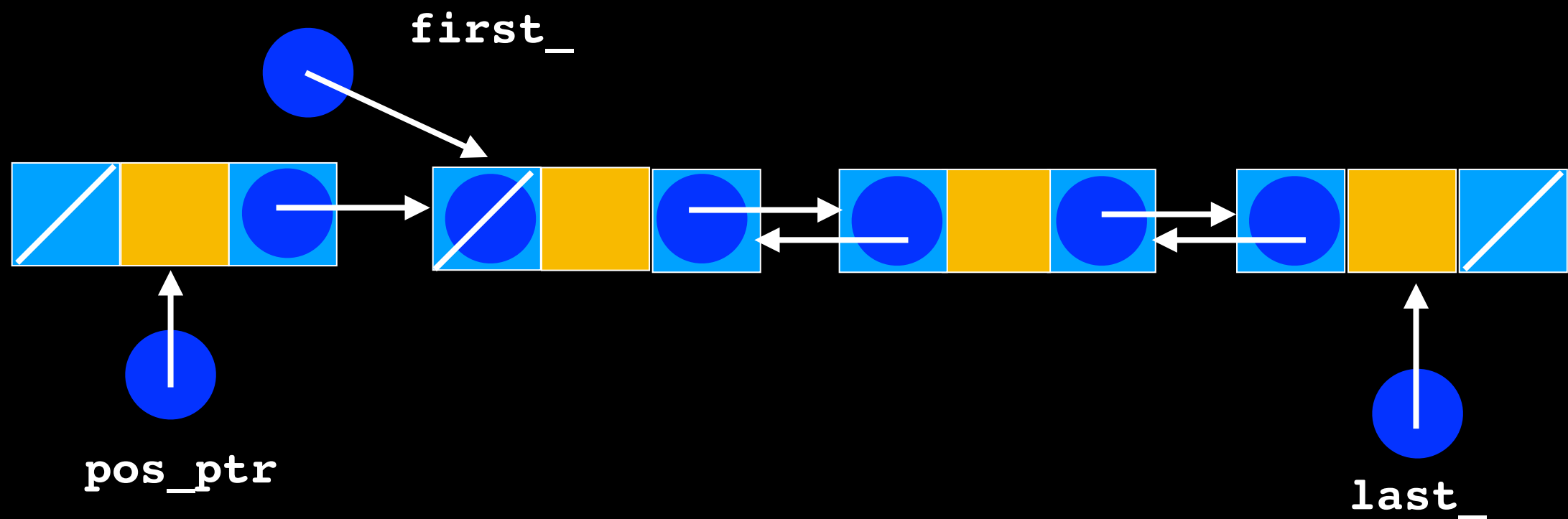
    // Return node to the system
    pos_ptr->setNext(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}
```



2

```
// Remove node from chain
if (pos_ptr == first_)
{
    // Remove first node
    first_ = pos_ptr->getNext();
    first_->setPrevious(nullptr);

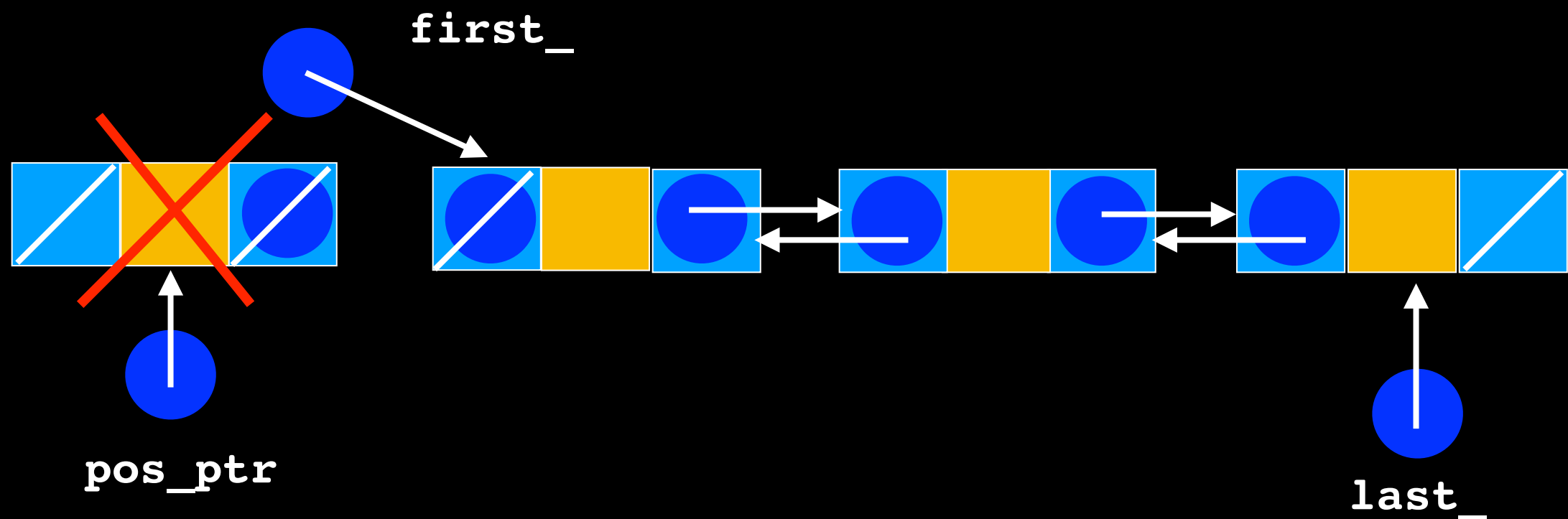
    // Return node to the system
    pos_ptr->setNext(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}
```



2

```
// Remove node from chain
if (pos_ptr == first_)
{
    // Remove first node
    first_ = pos_ptr->getNext();
    first_->setPrevious(nullptr);

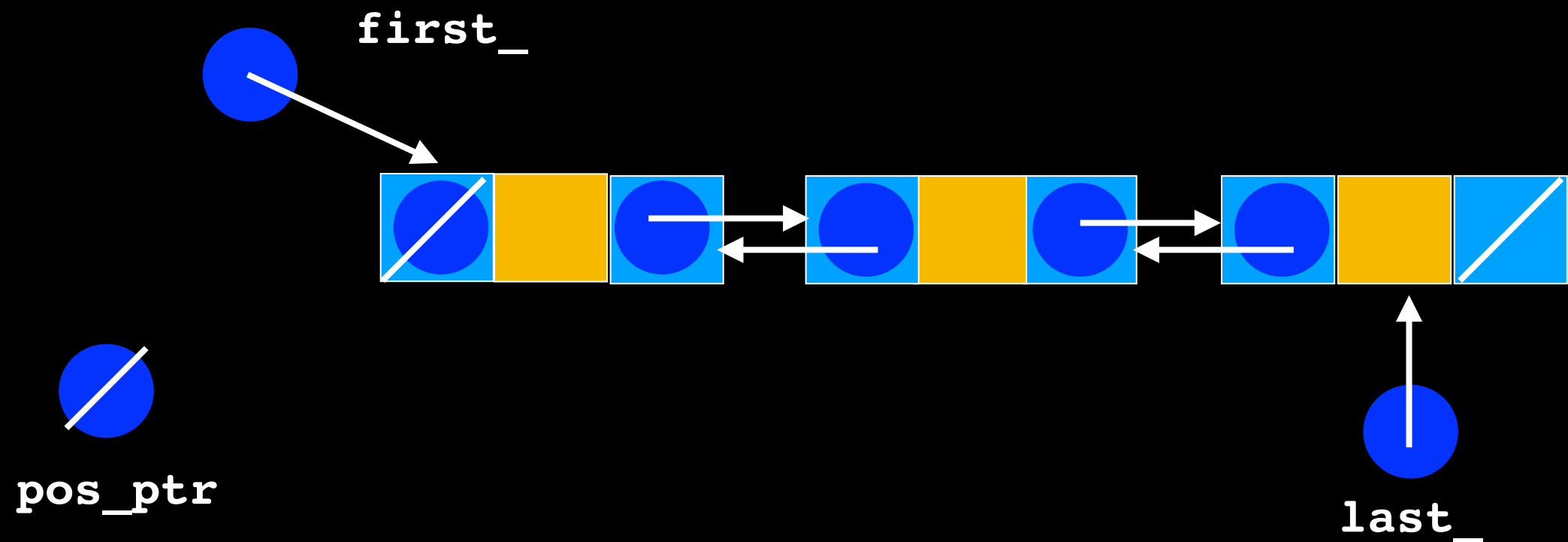
    // Return node to the system
    pos_ptr->setNext(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}
```



2

```
// Remove node from chain
if (pos_ptr == first_)
{
    // Remove first node
    first_ = pos_ptr->getNext();
    first_->setPrevious(nullptr);

    // Return node to the system
    pos_ptr->setNext(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}
```

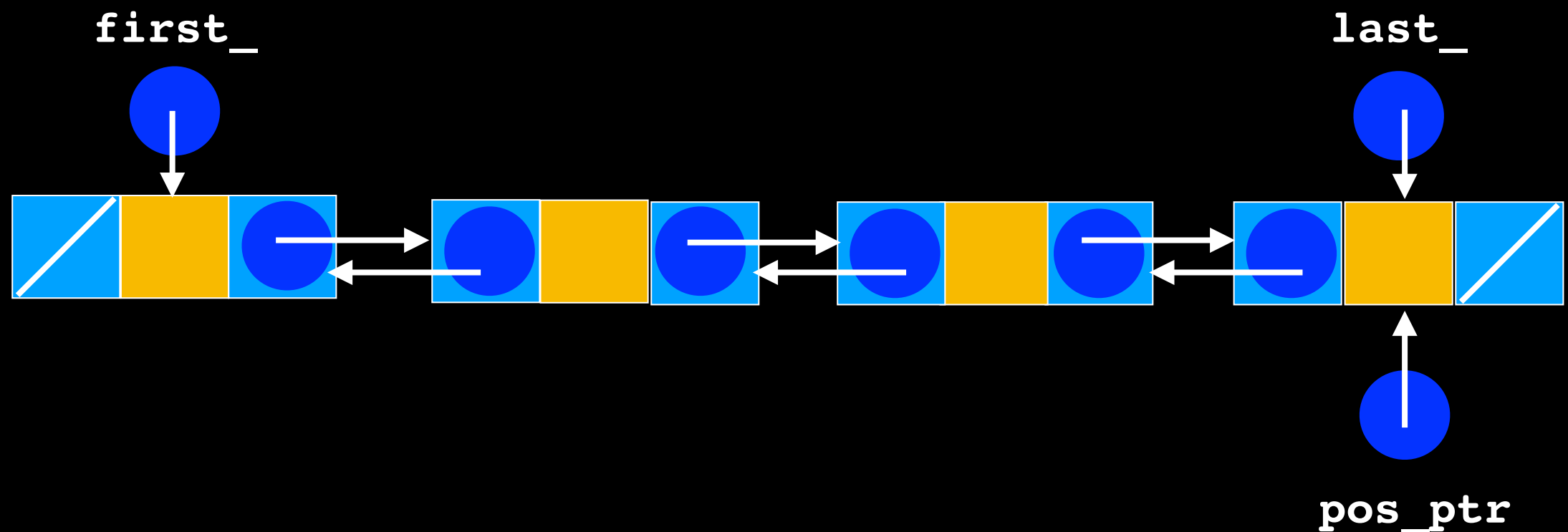



```

3  else if (pos_ptr == last_)
{
    //remove last_ node
    last_ = pos_ptr->getPrevious();
    last_ ->setNext(nullptr);

    // Return node to the system
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}

```

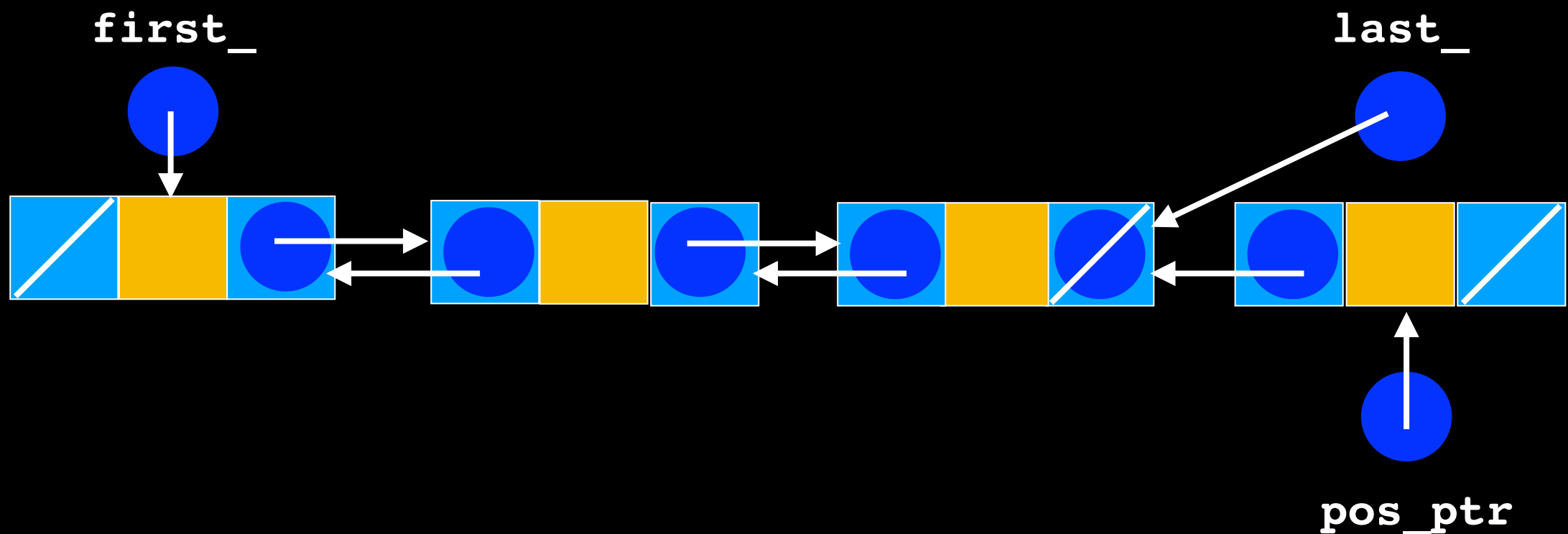


```

3  else if (pos_ptr == last_)
{
    //remove last_ node
    last_ = pos_ptr->getPrevious();
    last_ ->setNext(nullptr);

    // Return node to the system
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}

```

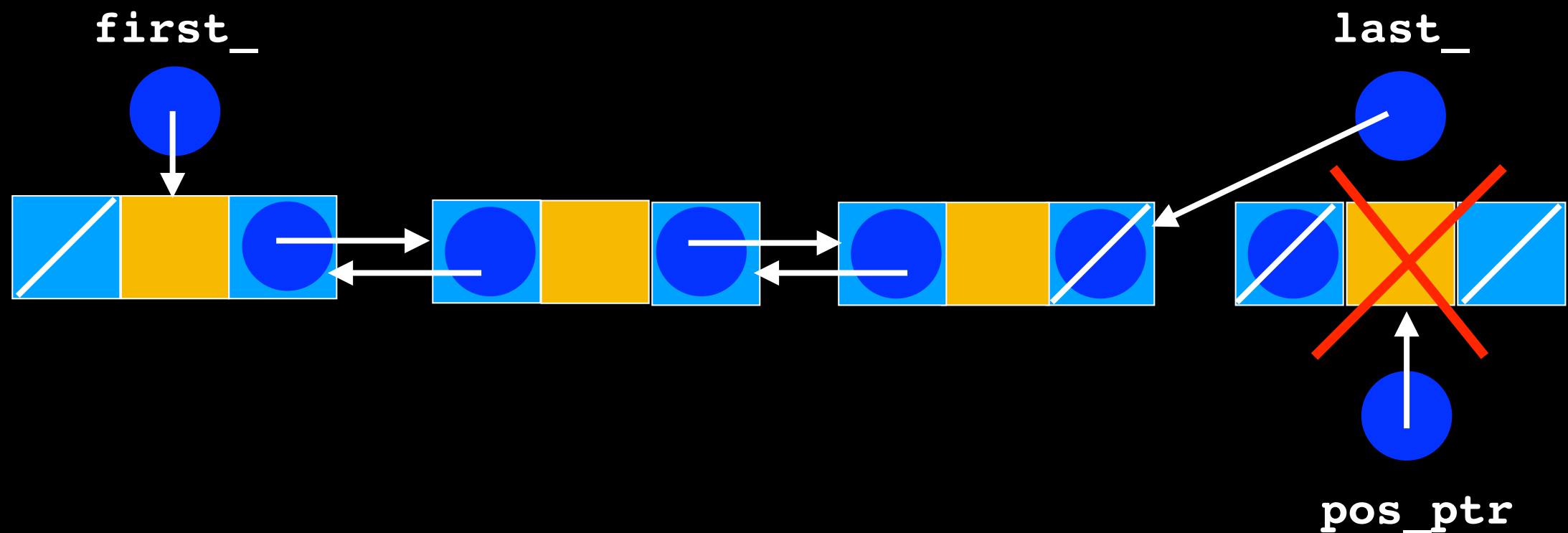


```

3  else if (pos_ptr == last_)
{
    //remove last_ node
    last_ = pos_ptr->getPrevious();
    last_ ->setNext(nullptr);

    // Return node to the system
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}

```

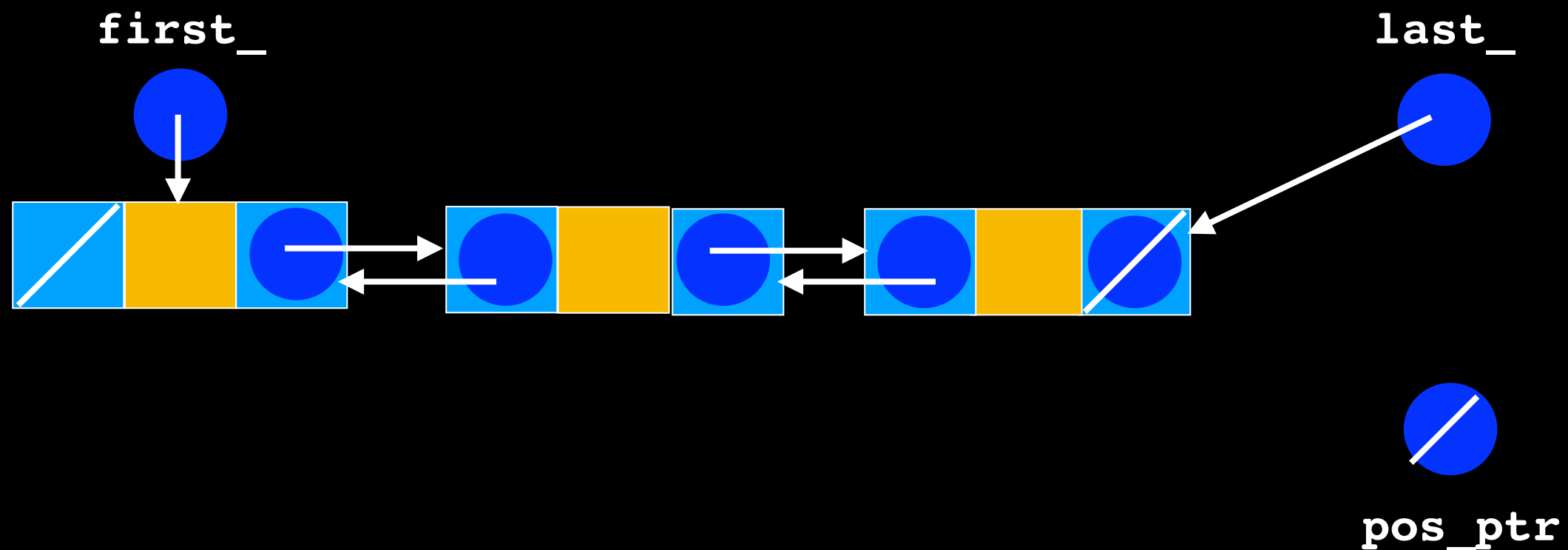


```

3  else if (pos_ptr == last_)
{
    //remove last_ node
    last_ = pos_ptr->getPrevious();
    last_ ->setNext(nullptr);

    // Return node to the system
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
}

```

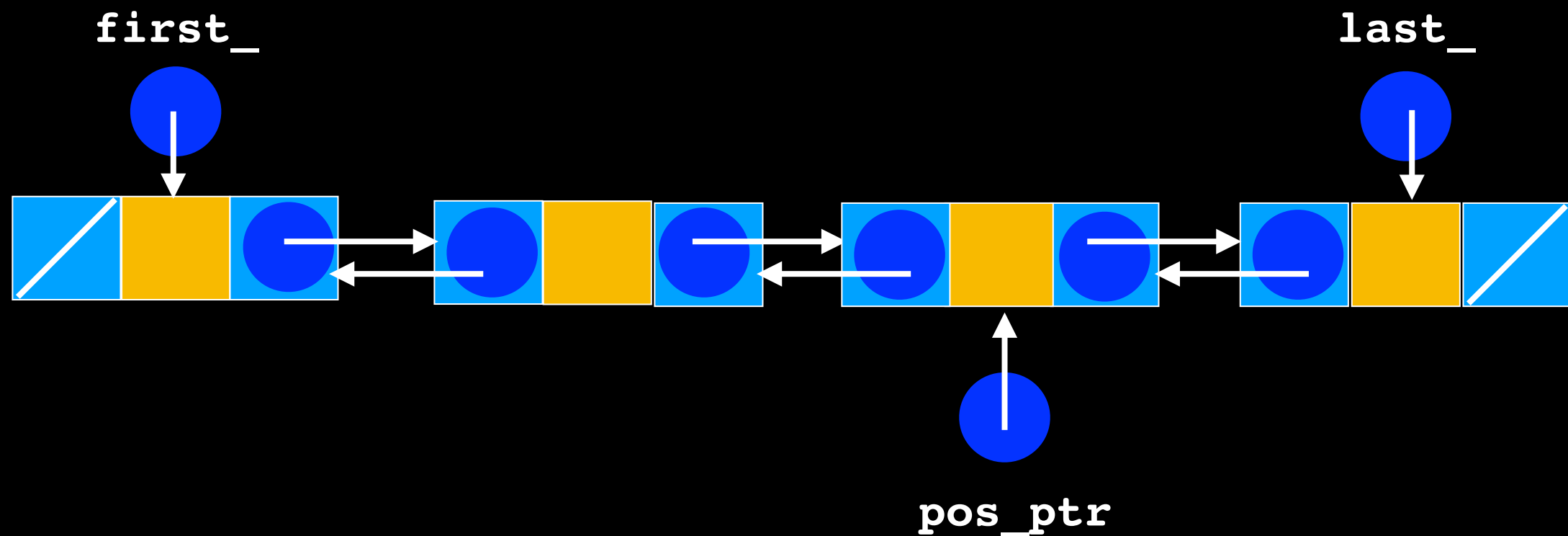


```

4 else if (pos_ptr != nullptr)
{
    //Remove from the middle
    pos_ptr->getPrevious()->setNext(pos_ptr->getNext());
    pos_ptr->getNext()->setPrevious(pos_ptr->getPrevious());

    // Return node to the system
    pos_ptr->setNext(nullptr);
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
} // end if

```

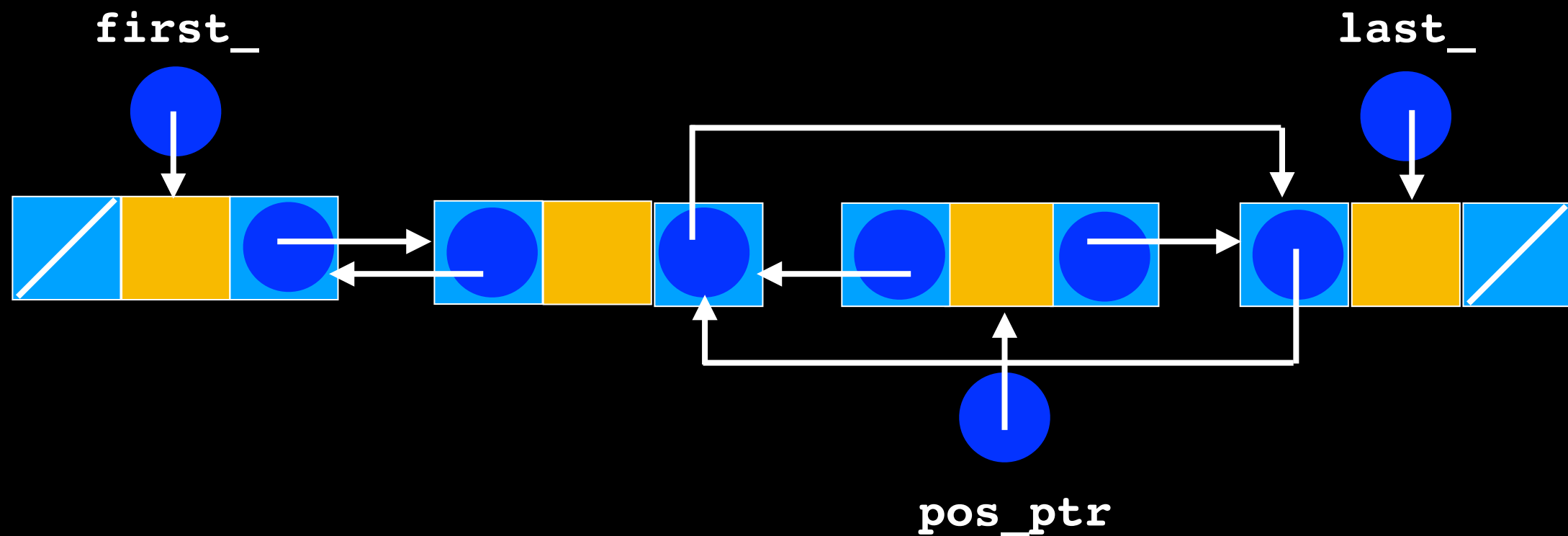


```

4 else if (pos_ptr != nullptr)
{
    //Remove from the middle
    pos_ptr->getPrevious()->setNext(pos_ptr->getNext());
    pos_ptr->getNext()->setPrevious(pos_ptr->getPrevious());

    // Return node to the system
    pos_ptr->setNext(nullptr);
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
} // end if

```

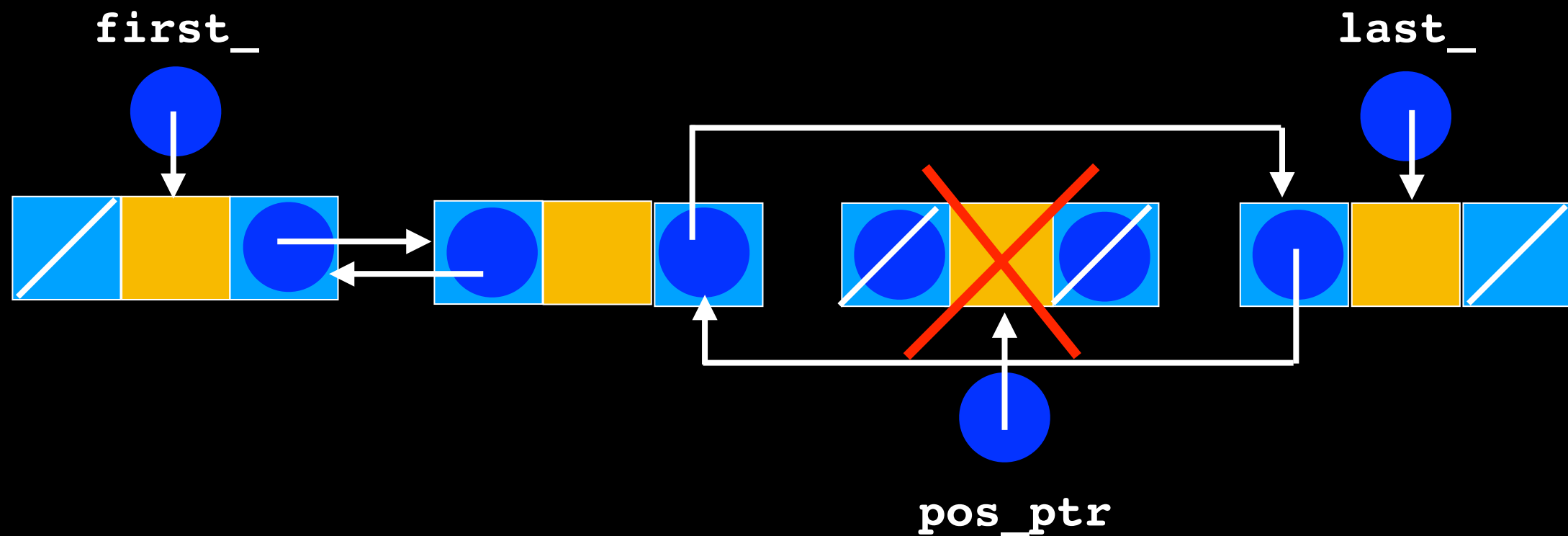


```

4 else if (pos_ptr != nullptr)
{
    //Remove from the middle
    pos_ptr->getPrevious()->setNext(pos_ptr->getNext());
    pos_ptr->getNext()->setPrevious(pos_ptr->getPrevious());

    // Return node to the system
    pos_ptr->setNext(nullptr);
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
} // end if

```

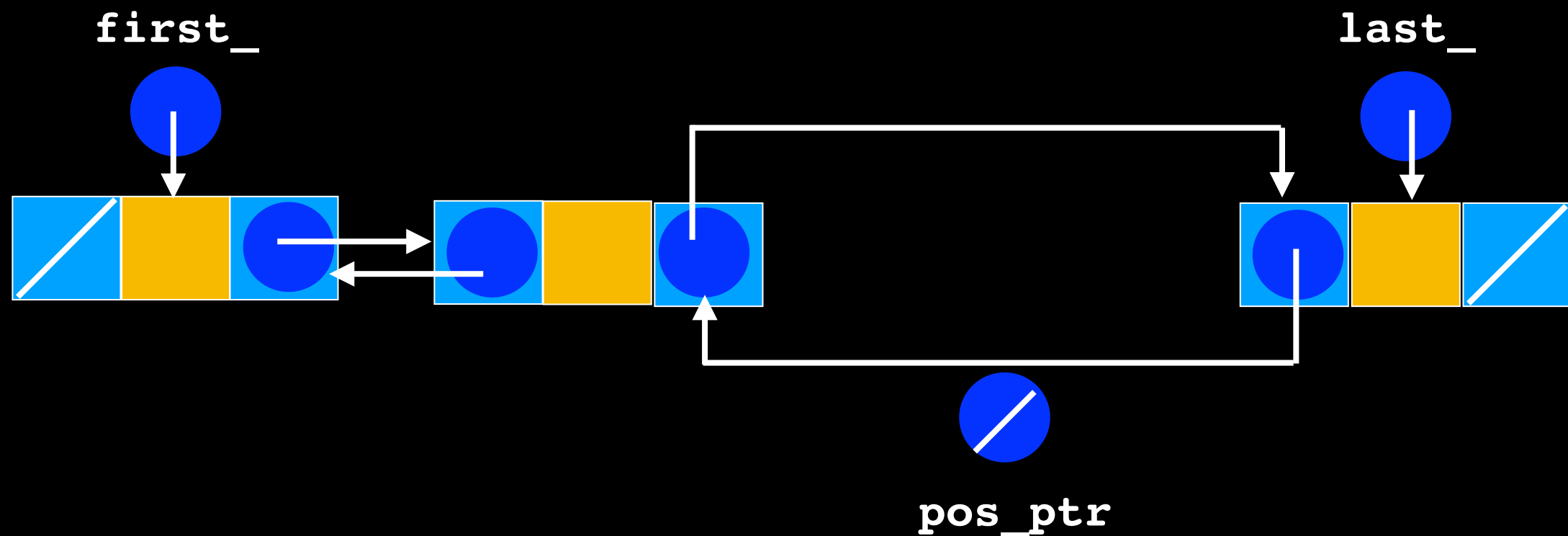


```

4 else if (pos_ptr != nullptr)
{
    //Remove from the middle
    pos_ptr->getPrevious()->setNext(pos_ptr->getNext());
    pos_ptr->getNext()->setPrevious(pos_ptr->getPrevious());

    // Return node to the system
    pos_ptr->setNext(nullptr);
    pos_ptr->setPrevious(nullptr);
    delete pos_ptr;
    pos_ptr = nullptr;
} // end if

```



List::getPointerTo

```
template<class T>
Node<T>* List<T>::getPointerTo(size_t position) const
{
    Node<T>* find_ptr = nullptr;
    // return nullptr if there is no node at position
    if(position < item_count)
    { //there is a node at position
        find_ptr = first_;
        for(size_t i = 0; i < position; ++i)
        {
            find_ptr = find_ptr->getNext();
        }
        //find_ptr points to the node at position
    }

    return find_ptr;
} //end getPointerTo
```

How could you optimize traversal TO POSITION given this implementation?

Still $O(n)$!!!

```
if(position < item_count/2)
{
    find_ptr = first_;
    . . .
}
else
{
    find_ptr = last_;
    . . .
}
```

List::getItem

```
template<class T>
T List<T>::getItem(size_t position) const
{
    Node<T>* pos_ptr = getPointerTo(position);
    if(pos_ptr != nullptr)
        return pos_ptr->getItem();
    else
        ???
}
```

List::getItem

```
template<class T>
T List<T>::getItem(size_t position) const
{
    Node<T>* pos_ptr = getPointerTo(position);
    if(pos_ptr != nullptr)
        return pos_ptr->getItem();
    else
        ???
}
```

Problem: return type is T
There is no “default” or null
value to indicate
uninitialized object

Next time

Exception Handling