

CISS350: Data Structures and Advanced Algorithms
Quiz q10303

Name: YOUR EMAIL Score:

All questions below refer to our standard mergesort. For big-O, your answer should be of the form $O(n^k \lg^\ell n)$ for $k = 0, 1, 2, \dots$ $\ell = 0, 1, 2, \dots$. Of course $O(n^0)$ is $O(1)$.

Q1. For array $x = \{5, 3, 1, 4\}$, how many mergesort function calls are there when you perform mergesort on x ?

ANSWER:

Q2. We will number the mergesort function calls 1, 2, 3, etc. On returning from mergesort function call 1, the array is complete sorted. What is the array x on returning from mergesort function call 7?

ANSWER:

Q3. What is the array on returning from mergesort function call 6?

ANSWER:

Q4. What is the array on returning from mergesort function call 5?

ANSWER:

Q5. What is the array on returning from mergesort function call 4?

ANSWER:

Q6. What is the array on returning from mergesort function call 3?

ANSWER:

Q7. What is the array on returning from mergesort function call 2?

ANSWER:

{?, ?, ?, ?}

Q8. What is the array on returning from mergesort function call 1?

ANSWER:

{?, ?, ?, ?}

Q9. Is it stable? Write YES, or write NO and then write down the simplest array of smallest size and using smallest positive integers > 0 which when traced will show that the sorting is not stable.

ANSWER:

YES. ... or ... NO. {?, ?}.

Q10. If it is not stable write down the simplest array (of smallest size and using smallest positive integers) to show that it is so. If it is stable, erase all contents in the answer box and leave it blank.

ANSWER:

{?, ?}

Q11. What is the big-O of the runtime in terms of n where n is the size of the array?

ANSWER:

$O(?)$

Q12. What is the big-O of the best runtime in terms of n where n is the size of the array?

ANSWER:

$O(?)$

Q13. What is the space complexity (i.e., memory usage) in terms of n where n is the size of the array?

ANSWER:

$O(?)$

INSTRUCTIONS

In the file `thispreamble.tex` look for

```
\renewcommand\AUTHOR{}
```

and enter your email address:

```
\renewcommand\AUTHOR{jdoe5@cougars.ccis.edu}
```

(This is not really necessary since alex will change that for you when you execute `make`.) In your bash shell, execute “`make`” to recompile `main.pdf`. Execute “`make v`” to view `main.pdf`.

Enter your answers in `main.tex`. In the bash shell, execute “`make`” to recompile `main.pdf`. Execute “`make v`” to view `main.pdf`.

For each question, you’ll see boxes for you to fill. For small boxes, if you see

```
1 + 1 = \answerbox{}
```

you do this:

```
1 + 1 = \answerbox{2}
```

`answerbox` will also appear in “true/false” and “multiple-choice” questions.

For longer answers that need typewriter font, if you see

```
Write a C++ statement that declares an integer variable name x.  
\begin{answercode}  
\end{answercode}
```

you do this:

```
Write a C++ statement that declares an integer variable name x.  
\begin{answercode}  
int x;  
\end{answercode}
```

`answercode` will appear in questions asking for code, algorithm, and program output. In this case, indentation and spacing is significant. For program output, I do look at spaces and newlines.

For long answers (not in typewriter font) if you see

```
What is the color of the sky?  
\begin{answerlong}  
\end{answerlong}
```

you can write

```
What is the color of the sky?  
\begin{answerlong}  
The color of the sky is blue.  
\end{answerlong}
```

A question that begins with “T or F or M” requires you to identify whether it is true or false, or meaningless. “Meaningless” means something’s wrong with the question and it is not well-defined. Something like “ $1 + 2 = 4$ ” is either true or false (of course it’s false). Something like “ $1+2 = 4?$ ” does not make sense.

When writing results of computations, make sure it’s simplified. For instance write 2 instead of $1 + 1$.

HIGHER LEVEL CLASSES.

For students beyond 245: You can put L^AT_EX commands in `answerlong`.

More examples of meaningless statements: Questions such as “Is $42 = 1+2$ true or false?” or “Is $42 = \{2\}^{\{3\}}$ true or false?” does not make sense. “Is $P(42) = \{42\}$ true or false?” is meaningless because $P(X)$ is only defined if X is a set. For “Is $1 + 2 + 3$ true or false?”, “ $1 + 2 + 3$ ” is well-defined but as a “numerical expression”, not as a “proposition”, i.e., it cannot be true or false. Therefore “Is $1 + 2 + 3$ true or false?” is also not a well-defined question.

More examples of simplification: When you write down sets, if the answer is $\{1\}$, do not write $\{1, 1\}$. And when the values can be ordered, write the elements of the set in ascending order. When writing polynomials, begin with the highest degree term.

When writing a counterexample, always write the simplest.