CISS350: Data Structures and Advanced Algorithms
Quiz q10202

Name: YOUR EMAIL Score:

Note that `answercode` is for writing code/pseudocode/simple answers and does not require mathematical notation. For `answerlong`, you can enter LaTeX code for mathematical notation. Some incomplete/wrong answers are included in the `answerlong` – you will need make modifications.

Here are some pointers on writing math LaTeX code:

1. For "inline math mode", use `$...$`. Example: `$x = 42 + y$` gives you $x = 42 + y$. (Mathematical expressions have their own spacing, special symbols, and are in italics.)
2. For "display math mode", use `\[...\]`. Example: `\[ x = 42 \]` gives you

$$x = 42$$

   (Display math mode is used for emphasis.)
3. Here's how you do fractions: `$\frac{1}{2}$` gives you $\frac{1}{2}$.
4. Here's how you do subscript: `$t_{123}$` gives you t_{123}.
5. Here's how you do superscript: `$n^{123}$` gives you n^{123}.
6. Here's how you do log: `$\lg n$` gives you $\lg n$.
7. Example: `$T(n) = \frac{1}{2} t_{42} n^3 \lg n = An^3 \lg n = O(n^3 \lg n)$` gives you $T(n) = \frac{1}{2} t_{42} n^3 \lg n = An^3 \lg n = O(n^3 \lg n)$.

The above information should be enough for this quiz. For more information on LaTeX you can go to my website, scroll down to the Tutorials section and click on latex.pdf.

(Turn Page)

Runtime for array swap

The goal is to compute the big-O runtime of the basic array swapping algorithm (i.e., swap the contents between two arrays).

For the next few questions, the goal is to analyze the runtime of this algorithm:

```
for i = 0, ..., n - 1:
    t = x[i]
    x[i] = y[i]
    y[i] = t
```

Q1. Rewrite the above algorithm with goto statements, assign constant times to each statement and compute the time taken as a function of n, t_1, t_2, t_3, ... where $t_1, t_2, t_3, ...$ are runtimes for each statement in your algorithm. Make sure you number these times starting with t_1, then t_2, etc. Include the number of times each statement is executed.

Answer:

```
          i = ??                  t1      ?
LOOP:     if i >= n:              t2      ?
              goto ENDLOOP        t3      ?
```

Q2. Let $T(n)$ be the runtime function of the above algorithm. Write $T(n)$ as a polynomial in descending power of n, i.e., the *highest degree term appearing first.*

Answer:

$T(n) = t_{200}n^{100} + t_{1000}n^{20}$

(Correct the above.)

Q3. Simplify the runtime function $T(n)$ by giving names A, B, C, D, ... to the constants of the function from (a). (The $t_1, t_2, ...$ should disappear.)

Answer:

$T(n) = An^{100} + Bn^{99}$

(Correct the above.)

Q4. Fudge away the constants and write down the simplest $g(n)$ such that the runtime is a big-O of your $g(n)$. Your $g(n)$ should be either n or n^2 or n^3 or $n^{102.25}$ ...

Answer:

$T(n) = O(n^{3.1415} \lg n + 5000)$

(Correct the above.) □

Instructions

In the file `thispreamble.tex` look for

```
\renewcommand\AUTHOR{}
```

and enter your email address:

```
\renewcommand\AUTHOR{jdoe5@cougars.ccis.edu}
```

(This is not really necessary since alex will change that for you when you execute `make`.) In your bash shell, execute "`make`" to recompile `main.pdf`. Execute "`make v`" to view `main.pdf`.

Enter your answers in `main.tex`. In the bash shell, execute "`make`" to recompile `main.pdf`. Execute "`make v`" to view `main.pdf`.

For each question, you'll see boxes for you to fill. For small boxes, if you see

```
1 + 1 = \answerbox{}.
```

you do this:

```
1 + 1 = \answerbox{2}.
```

`answerbox` will also appear in "true/false" and "multiple-choice" questions.

For longer answers that need typewriter font, if you see

```
Write a C++ statement that declares an integer variable name x.
\begin{answercode}
\end{answercode}
```

you do this:

```
Write a C++ statement that declares an integer variable name x.
\begin{answercode}
int x;
\end{answercode}
```

`answercode` will appear in questions asking for code, algorithm, and program output. In this case, indentation and spacing is significant. For program output, I do look at spaces and newlines.

For long answers (not in typewriter font) if you see

```
What is the color of the sky?
\begin{answerlong}
\end{answerlong}
```

you can write

```
What is the color of the sky?
\begin{answerlong}
The color of the sky is blue.
\end{answerlong}
```

A question that begins with "T or F or M" requires you to identify whether it is true or false, or meaningless. "Meaningless" means something's wrong with the question and it is not well-defined. Something like "$1 + 2 = 4$" is either true or false (of course it's false). Something like "$1+_2 = 4$?" does not make sense.

When writing results of computations, make sure it's simplified. For instance write 2 instead of $1 + 1$.

Higher level classes.

For students beyond 245: You can put LaTeX commands in `answerlong`.

More examples of meaningless statements: Questions such as "Is $42 = 1+_2$ true or false?" or "Is $42 = \{2\}^{\{3\}}$ true or false?" does not make sense. "Is $P(42) = \{42\}$ true or false?" is meaningless because $P(X)$ is only defined if X is a set. For "Is $1 + 2 + 3$ true or false?", "$1 + 2 + 3$" is well–defined but as a "numerical expression", not as a "proposition", i.e., it cannot be true or false. Therefore "Is $1 + 2 + 3$ true or false?" is also not a well-defined question.

More examples of simplification: When you write down sets, if the answer is $\{1\}$, do not write $\{1, 1\}$. And when the values can be ordered, write the elements of the set in ascending order. When writing polynomials, begin with the highest degree term.

When writing a counterexample, always write the simplest.