Logistic Regression in UCLA Data

Hunter Grigsby

Data Preperation

Resources: "https://stats.idre.ucla.edu/stat/data/binary.csv"

```
# packages required
library(aod)
library(ggplot2)

path <- "https://stats.idre.ucla.edu/stat/data/binary.csv"
mydata <- read.csv(path)</pre>
```

• The dataset contains information on applicants, specifically whether they were admitted (admit), their GRE scores (gre), GPAs (gpa), and the rank of their undergraduate institution (rank).

Data Checkup

```
str(mydata)
## 'data.frame':
                    400 obs. of 4 variables:
    $ admit: int
                  0 1 1 1 0 1 1 0 1 0 ...
                  380 660 800 640 520 760 560 400 540 700 ...
                  3.61 3.67 4 3.19 2.93 3 2.98 3.08 3.39 3.92 ...
    $ gpa : num
    $ rank : int
                  3 3 1 4 4 2 1 2 3 2 ...
mydata$rank = as.factor(mydata$rank)
str(mydata)
   'data.frame':
                     400 obs. of 4 variables:
    $ admit: int
                  0 1 1 1 0 1 1 0 1 0 ...
                  380 660 800 640 520 760 560 400 540 700 ...
    $ gre : int
                  3.61 3.67 4 3.19 2.93 3 2.98 3.08 3.39 3.92 ...
    $ rank : Factor w/ 4 levels "1", "2", "3", "4": 3 3 1 4 4 2 1 2 3 2 ...
summary(mydata)
##
        admit
                                           gpa
                                                       rank
##
    Min.
           :0.0000
                     Min.
                             :220.0
                                      Min.
                                             :2.260
                                                       1: 61
   1st Qu.:0.0000
                     1st Qu.:520.0
                                      1st Qu.:3.130
                                                       2:151
## Median :0.0000
                     Median :580.0
                                      Median :3.395
                                                       3:121
                                                       4: 67
## Mean
           :0.3175
                     Mean
                             :587.7
                                      Mean
                                             :3.390
    3rd Qu.:1.0000
                     3rd Qu.:660.0
                                      3rd Qu.:3.670
    Max.
           :1.0000
                     Max.
                             :800.0
                                      Max.
                                             :4.000
```

The summary(mydata) output provides key descriptive statistics for each variable in the dataset, such
as minimum, maximum, median, mean, and the quartiles, which help in understanding the distribution
and central tendencies of GRE scores, GPAs, and undergraduate institution ranks. Additionally, the

conversion of the rank variable to a factor type in R, as shown in the str(mydata) output, facilitates categorical analysis, ensuring that statistical methods appropriate for nominal data are applied in subsequent analyses.

Regression = Estimatation

```
mylogit = glm(admit ~ gre + gpa + rank, data = mydata, family = "binomial")
summary(mylogit)
##
## Call:
## glm(formula = admit ~ gre + gpa + rank, family = "binomial",
##
       data = mydata)
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -3.989979
                          1.139951 -3.500 0.000465 ***
## gre
               0.002264
                           0.001094
                                    2.070 0.038465 *
## gpa
               0.804038
                          0.331819
                                     2.423 0.015388 *
## rank2
               -0.675443
                          0.316490 -2.134 0.032829 *
## rank3
               -1.340204
                           0.345306 -3.881 0.000104 ***
## rank4
               -1.551464
                           0.417832 -3.713 0.000205 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 499.98 on 399 degrees of freedom
## Residual deviance: 458.52 on 394 degrees of freedom
## AIC: 470.52
##
## Number of Fisher Scoring iterations: 4
```

• The output from the logistic regression model shows that GRE scores (p = 0.038465) and GPA (p = 0.015388) are statistically significant predictors of admission, indicating that higher values in these variables increase the likelihood of admission. The negative coefficients for rank2, rank3, and rank4 (all p < 0.05) suggest that applicants from lower-ranked institutions have a reduced chance of admission compared to those from top-ranked institutions, controlling for other factors.

Calculate Odds Ratios

```
coefs = coefficients(mylogit)
ORs = exp(coefs)
CIs = exp(confint(mylogit))

## Waiting for profiling to be done...
CIs

## 2.5 % 97.5 %
## (Intercept) 0.001889165 0.1665354
## gre 1.000137602 1.0044457
## gpa 1.173858216 4.3238349
## rank2 0.272289674 0.9448343
```

```
## rank3
               0.131641717 0.5115181
## rank4
               0.090715546 0.4706961
cbind(round(ORs,2), round(CIs,2))
                    2.5 % 97.5 %
##
## (Intercept) 0.02 0.00
                             0.17
## gre
               1.00
                     1.00
                             1.00
## gpa
               2.23
                     1.17
                             4.32
## rank2
               0.51
                     0.27
                             0.94
## rank3
               0.26
                     0.13
                             0.51
## rank4
               0.21
                     0.09
                             0.47
```

- GRE Scores (gre): The odds ratio of 1.00 indicates negligible impact on admission odds per unit increase in GRE scores.
- GPA (gpa): With an odds ratio of 2.23, each unit increase in GPA significantly boosts admission odds, suggesting GPA is a strong predictor.
- Rank 2 (rank2): Applicants from institutions ranked '2' have roughly half the admission odds compared to top-ranked schools.
- Rank 3 (rank3) and Rank 4 (rank4): These ranks significantly lower the admission odds to 0.26 and 0.21, respectively, indicating much lower chances of admission for applicants from these institutions.

