

求证: $F = 2 \frac{h-u}{L_1} \cdot \frac{L_0-l_1}{L_0} EA$.

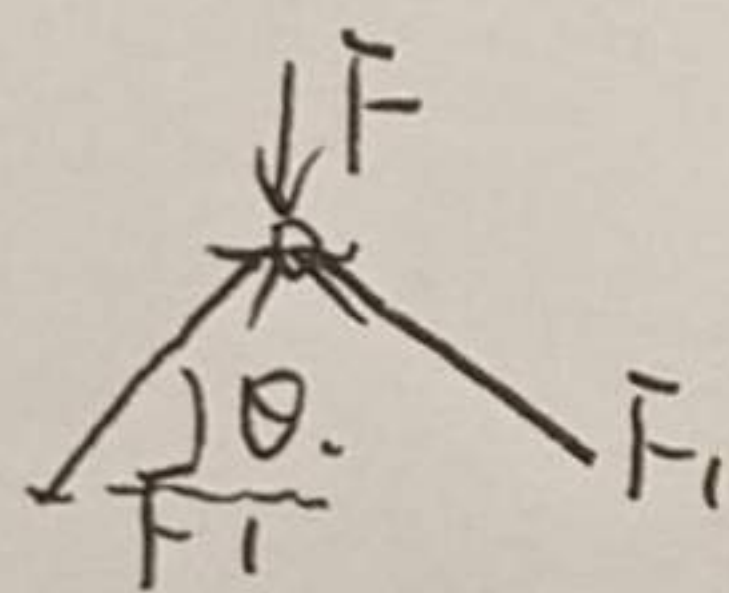
其中 $L_0 = \sqrt{(\frac{L}{2})^2 + h^2}$, $L_1 = \sqrt{(\frac{L}{2})^2 + (h-u)^2}$.

证: 由胡克定律可知
 L_0 即为初始杆长, L_1 为当顶位移移为 u 时杆长.

由于结构对称, 取其中一根分析. 有: (记 F_1 为杆中内力)

$$\varepsilon = \frac{L_0 - L_1}{L_0}, \quad \sigma = E \varepsilon, \quad F_1 = \sigma A = E A \cdot \frac{L_0 - L_1}{L_0} \quad (\text{压力})$$

对结点进行受力分析:



$$\sum F_y = 0, \quad -F + 2F_1 \sin \theta = 0.$$

$$\Rightarrow F = 2F_1 \sin \theta = 2F_1 \cdot \frac{h-u}{L_1} = 2 \cdot EA \cdot \frac{L_0 - L_1}{L_0} \cdot \frac{h-u}{L_1} \quad \text{得证!}$$