

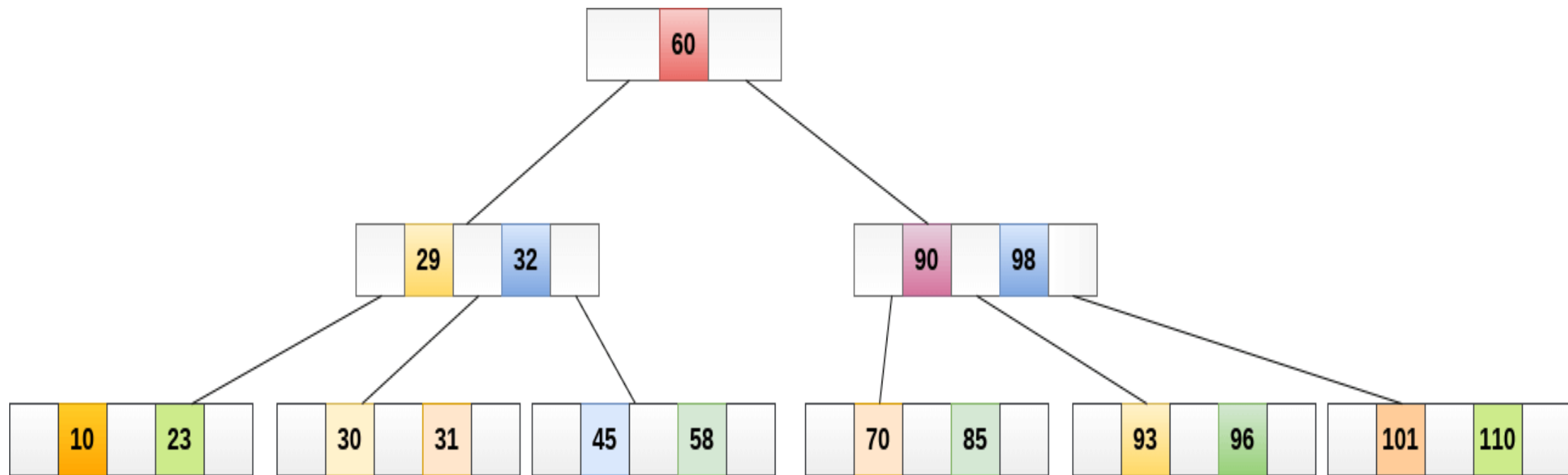
B-Trees

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Introduction of B-Tree

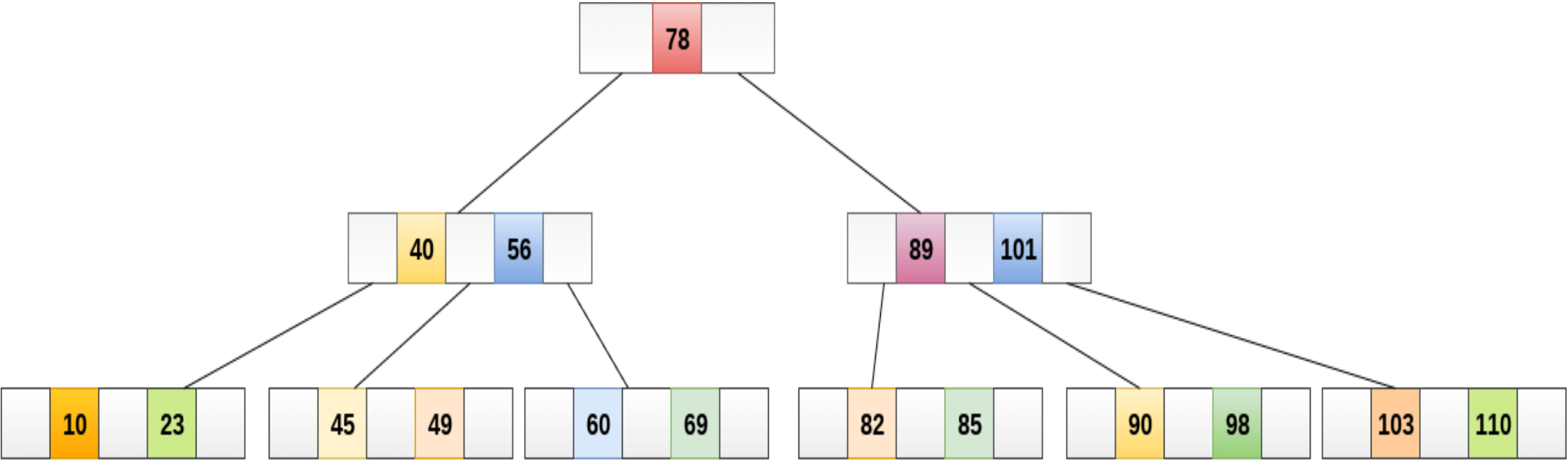
- B Tree is a specialized m-way tree that can be widely used for disk access. A B-Tree of order m can have at most $m-1$ keys and m children. One of the main reasons of using B tree is its capability to store large number of keys in a single node and large key values by keeping the height of the tree relatively small.
- A B tree of order m contains all the properties of an M way tree. In addition, it contains the following properties.

1. Every node in a B-Tree contains at most m children.
 2. Every node in a B-Tree except the root node and the leaf node contain at least $m/2$ children.
 3. The root nodes must have at least 2 child nodes.
 4. All leaf nodes must be at the same level.
- It is not necessary that, all the nodes contain the same number of children but, each node must have $m/2$ number of nodes.
 - A B tree of order 4 is shown in the following image.



- While performing some operations on B Tree, any property of B Tree may violate such as number of minimum children a node can have. To maintain the properties of B Tree, the tree may split or join.
- Operations
 - Searching
 - Insertion
 - Deletion

- Searching:
- Searching in B Trees is similar to that in Binary search tree. For example, if we search for an item 49 in the following B Tree. The process will something like following :
 1. Compare item 49 with root node 78. since $49 < 78$ hence, move to its left sub-tree.
 2. Since, $40 < 49 < 56$, traverse right sub-tree of 40.
 3. $49 > 45$, move to right. Compare 49.
 4. Match found, return.
- Searching in a B tree depends upon the height of the tree. The search algorithm takes $O(\log n)$ time to search any element in a B tree.



•Inserting

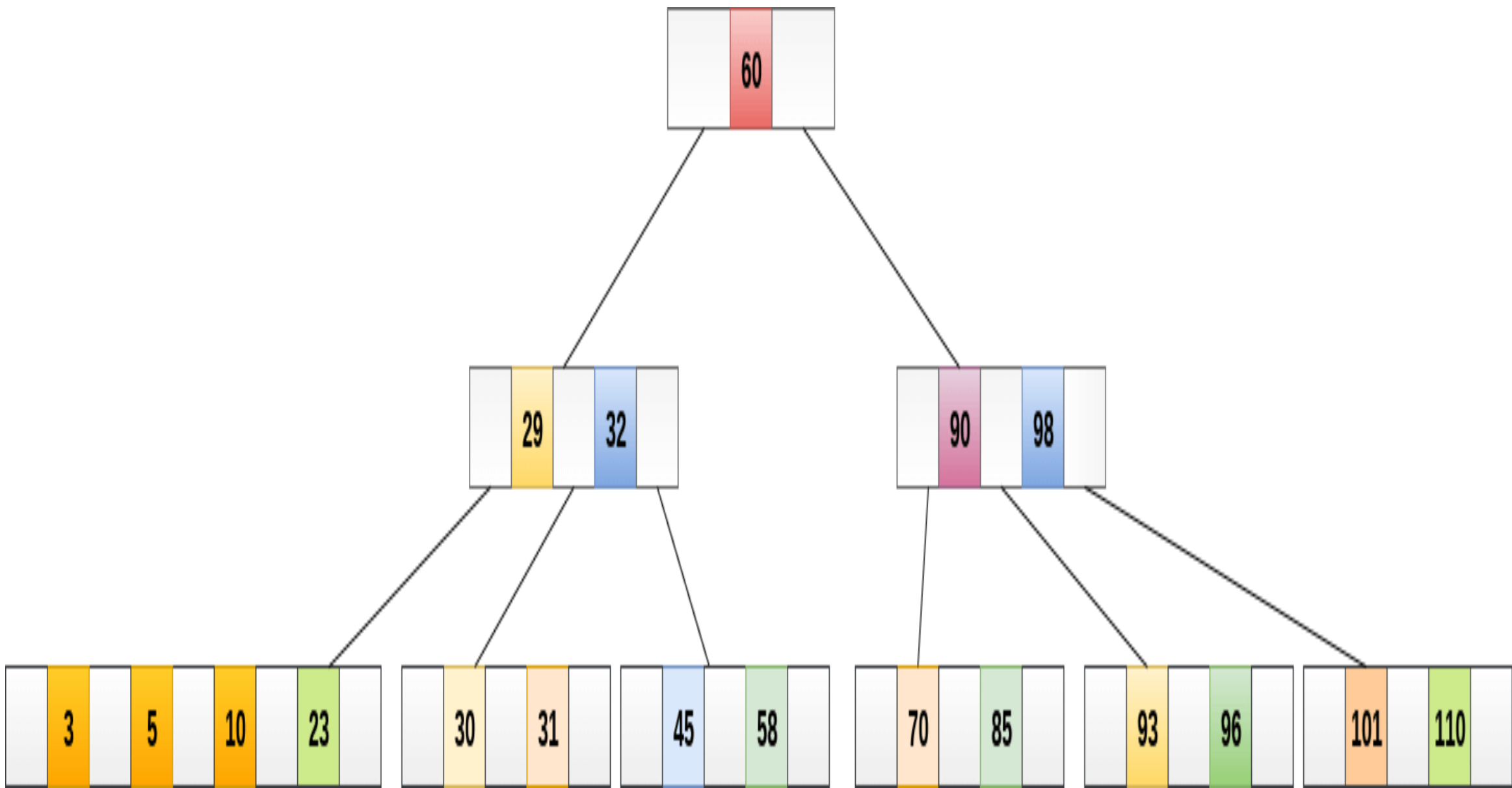
- Insertions are done at the leaf node level. The following algorithm needs to be followed in order to insert an item into B Tree.
 1. Traverse the B Tree in order to find the appropriate leaf node at which the node can be inserted.
 2. If the leaf node contain less than $m-1$ keys then insert the element in the increasing order.

3. Else, if the leaf node contains $m-1$ keys, then follow the following steps.

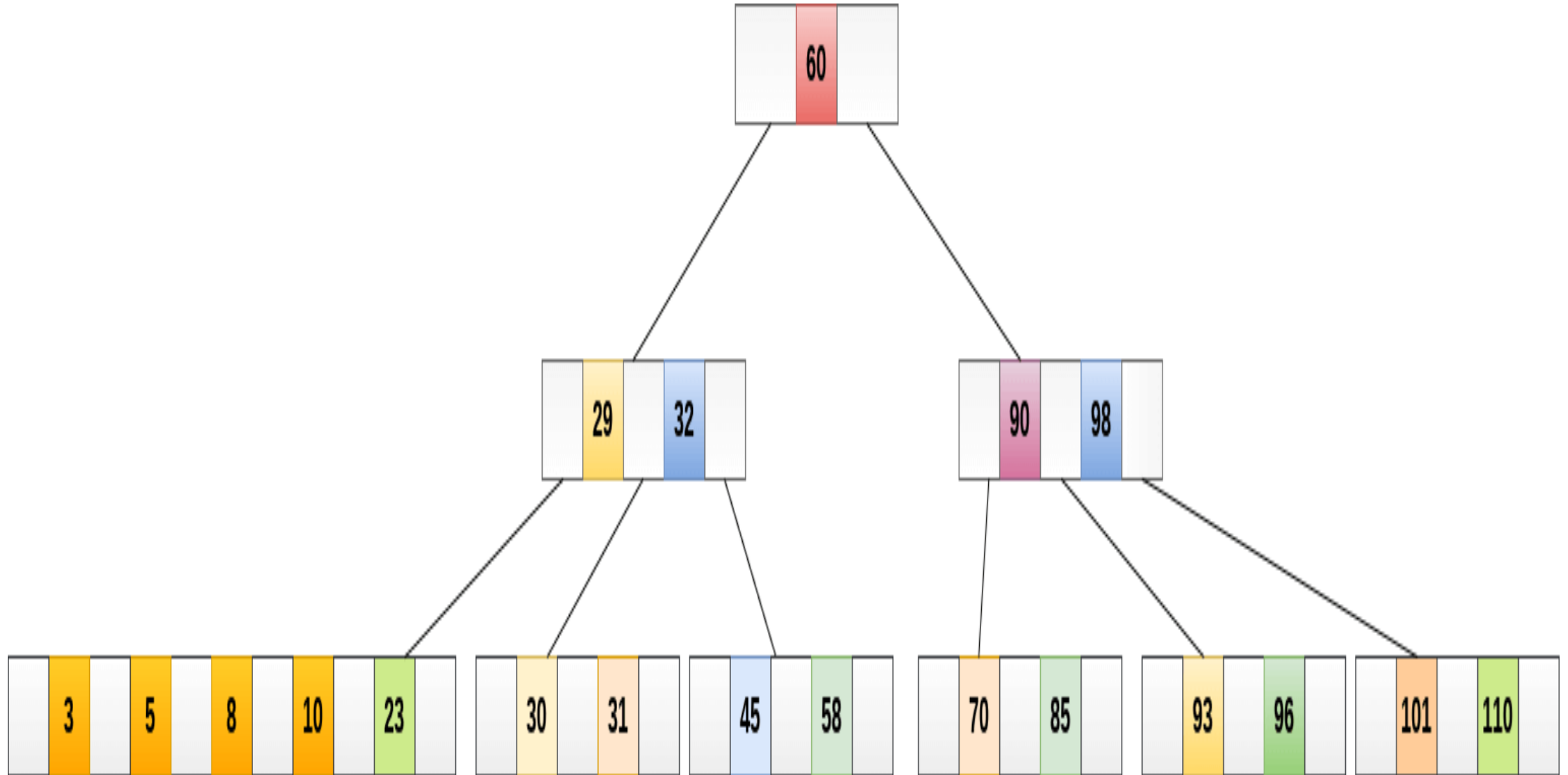
- Insert the new element in the increasing order of elements.
- Split the node into the two nodes at the median.
- Push the median element up to its parent node.
- If the parent node also contains $m-1$ number of keys, then split it too by following the same steps.

• **Example:**

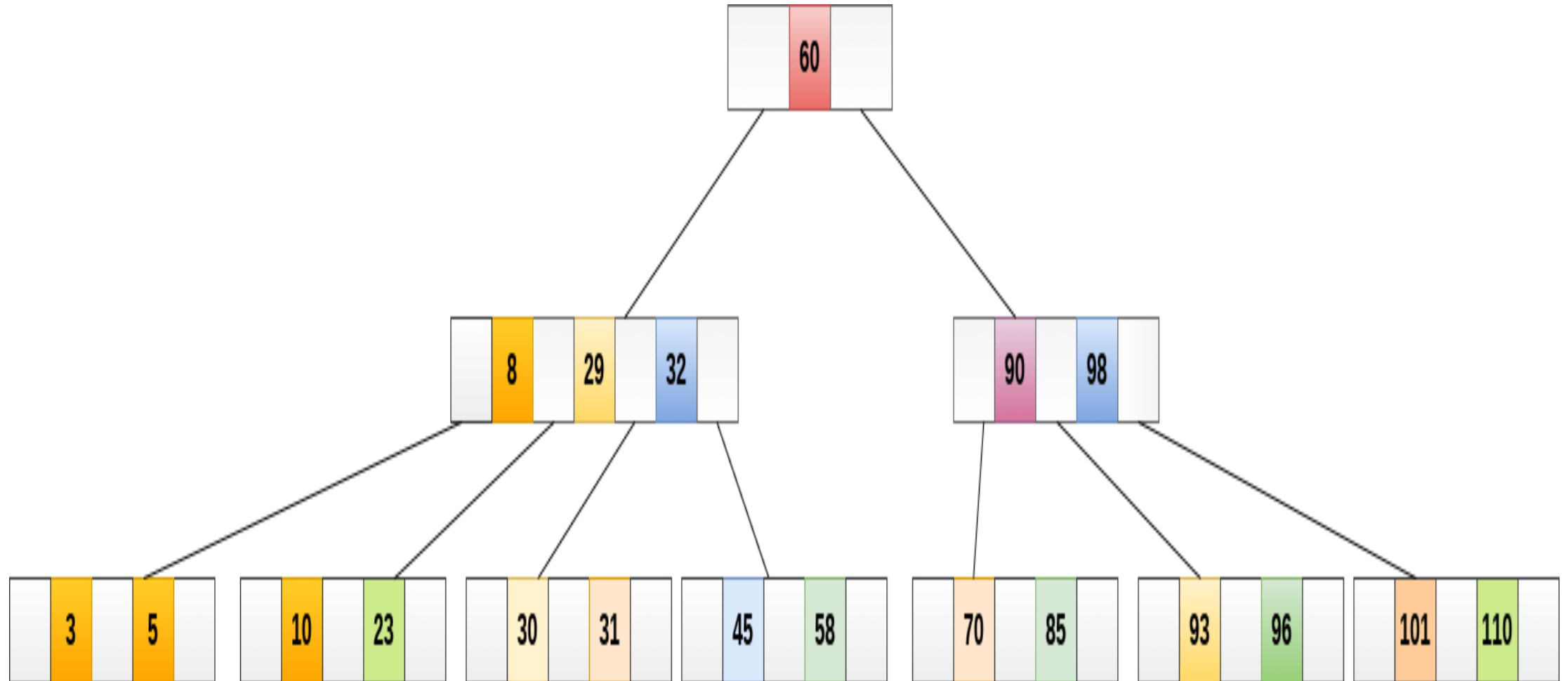
- Insert the node 8 into the B Tree of order 5 shown in the following image.



8 will be inserted to the right of 5, therefore insert 8.



The node, now contain 5 keys which is greater than $(5 - 1 = 4)$ keys. Therefore split the node from the median i.e. 8 and push it up to its parent node shown as follows.



- THANK YOU