

OPTIMIZERS

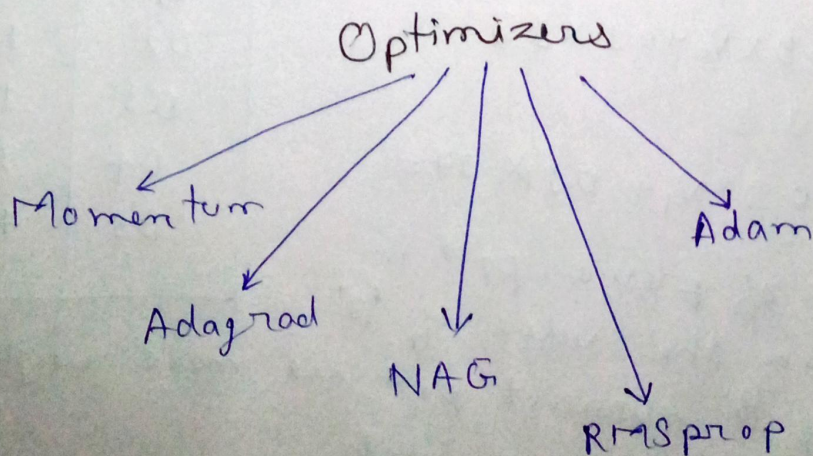
Types of Optimizers:

- Batch Gradient Descent
- Stochastic Gradient Descent
- Mini Batch Gradient Descent

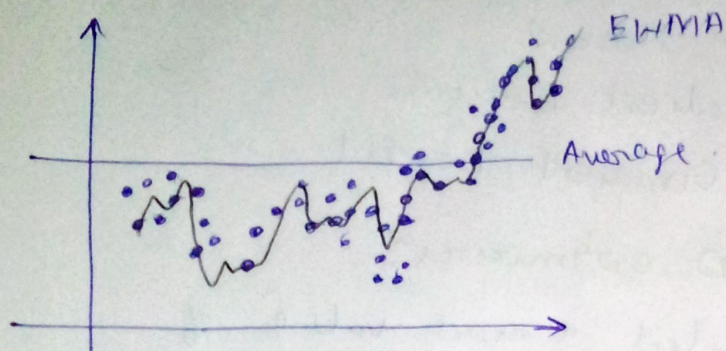
challenges with GD optimizers:

- challenges to select a exact value of learning rate.
- learning rate scheduling (pre defined value)
- finding the optimal value of many weights.
- local minima (may be possible. loss function trapped in local minima)
- saddle point (where slope value are same on all directions)

$$\frac{dL}{dW} = 0 \quad \text{hence no update of weights.}$$



Exponential weighted moving Average (EWMA):
 It is a technique that is used to find the trends in the time series data.



where it used:

- time series.
- financial.
- signal process.
- used in DL to build optimizers

the upcoming point are most preferable or more weightage. and in the flow of time the previous point's weight reduces.

mathematical formula:

$$V_t = \beta V_{t-1} + (1-\beta) \theta_t$$

Here β is constant ranging $[0, 1]$

$$V_0 = \theta_0$$

$$V_1 = 0.9 \times V_0 + 0.1 \times 13 = 1.3$$

$$V_2 = 0.9 \times V_1 + 0.1 \times 17 =$$

index	temp ($^{\circ}$)
D1	25
D2	13
D3	17
D4	31
D5	43

the weightage of previous point is depends on the value of ' β '.
 low value of ' β ' current point are more weightage.
 mostly $\beta = 0.9$ used

Mathematical Intuition:

$$V_t = \beta V_{t-1} + (1-\beta) \theta_t$$

where $V_0 = 0$

$$V_1 = (1-\beta) \theta_1$$

$$\begin{aligned} V_2 &= \beta V_1 + (1-\beta) \theta_2 \\ &= \beta (1-\beta) \theta_1 + (1-\beta) \theta_2 \end{aligned}$$

$$\begin{aligned} V_3 &= \beta V_2 + (1-\beta) \theta_3 \\ &= \beta^2 (1-\beta) \theta_1 + \beta (1-\beta) \theta_2 + (1-\beta) \theta_3 \end{aligned}$$

$$\begin{aligned} V_4 &= \beta V_3 + (1-\beta) \theta_4 \\ &= \beta^3 (1-\beta) \theta_1 + \beta^2 (1-\beta) \theta_2 + \beta (1-\beta) \theta_3 + (1-\beta) \theta_4 \\ &= (1-\beta) [\beta^3 \theta_1 + \beta^2 \theta_2 + \beta \theta_3 + \theta_4] \end{aligned}$$

in the above equation we see that
because β is in range $[0, 1]$

$$\beta^3 \geq \beta^2 > \beta$$

the coefficients of θ_1 , θ_2 and θ_3 respectively