

LeetCode 33:

Find a target value in a rotated sorted array.

Brute force approach: perform linear search ==> Time complexity: $O(n)$

Binary search: allows us to find a target within a search pool of size n in $O(\log_2(n))$

Predicate: condition: find me an element == target

Predicate for the pivot: find me an element whose successor is smaller

Time complexity: $O(\log_2(n))$

- Recursion:

Recursive method: Method that calls itself to fulfill its purpose. In order for this to be meaningful, the call to itself should be on a smaller version of the problem than the one originally attempted.

Example: Sum(N)

Sum of the values from 1 to $N = N + \text{Sum of the values from 1 to } N-1 =$
 $N + N - 1 + \text{Sum of the values from 1 to } N-2$

Recursive methods have two main parts:

1. Manageable version of the problem: base case

$N = 1 \implies \text{Sum}(1) = 1$

2. Recursive part:

$\text{Sum}(N) = N + \text{Sum}(N-1)$

Example#2: SumRecApp

Iterative solution: Use repetition statements ==> Time complexity: $O(n)$; Space complexity: $O(1)$

Recursive solution: ==> Time complexity: $O(n)$; Space complexity: $O(n)$ (recursive stack)

```
private static long sum_rec(int n) {  
    // Base case  
    if(n == 0) {  
        return 0;  
    }  
    // Recursive part  
    return n + sum_rec(n-1);  
}
```

$\text{sum_rec}(0) \implies \text{return } 0$

```
sum_rec(1) ==> return 1 + 0 ---> 1
n = 0
sum_rec(0)
```

```
sum_rec(2) ==> return 2 + (sum_rec(1) ==> return 1 + sum_rec(0) (recursive path)
```

"Don't complain, just work harder"

- Example#3: FactorialRecApp

$0! = 1$

$N! = N (N-1)!$

BigInteger ==> Array of int values

- Example#4: Fibonacci

0 1 1 2 3 5 ...etc

golden ratio: 1.618

fib(n): Fibonacci function

Time complexity: $O(2^n)$

fib(0) = 0 and fib(1) = 1: base case

fib(n) = fib(n-1) + fib(n-2): recursive part
fib(4)

```

                fib(3)                fib(2)
            fib(2)    fib(1)    fib(0)    fib(1)
fib(0)    fib(1)
```

n = 20 ==> 20 K recursive calls

n = 30 ==> 2 million recursive calls

n = 31 ==> 4 million recursive calls

n = 32 ==> 7 million recursive calls

Recursion + caching (memoization): Dynamic programming

Time complexity: $O(n)$

Space complexity: $O(n)$

Best solution for Fibonacci: Time complexity: $O(\log_2(n))$

0 1 1 2 etc

Time complexity: $O(n)$

Space complexity: $O(n)$

Dynamic programming: bottom-up approach

0, prevprev = 1, prev=1, current = 2

Time complexity: $O(n)$

Space complexity: $O(1)$