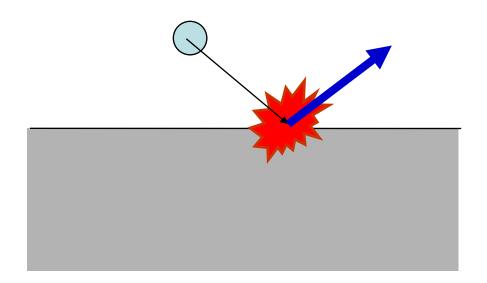
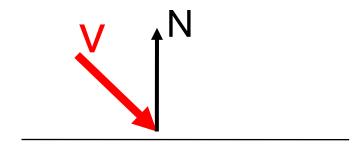


Collisions

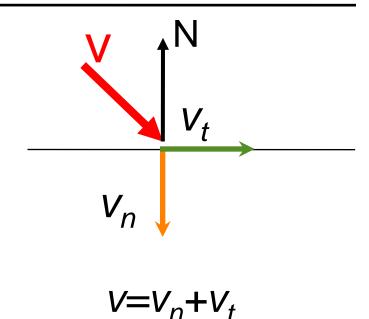
- Detection
- Response
- Overshooting problem (when we enter the solid)



Collision Response for Particles



Collision Response for Particles



normal component tangential component

Collision Response for Particles

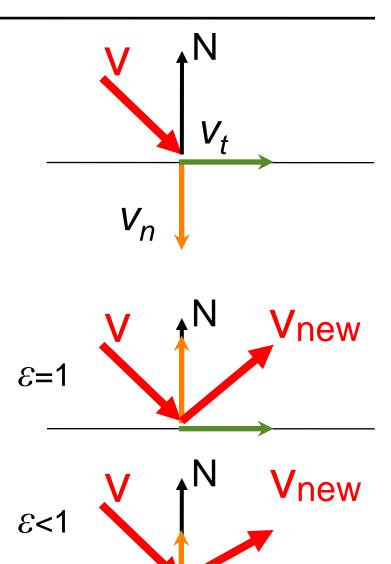
- Tangential velocity v_t often unchanged
- Normal velocity v_n reflects:

$$v = v_t + v_n$$

$$v \leftarrow v_t - \varepsilon v_n$$

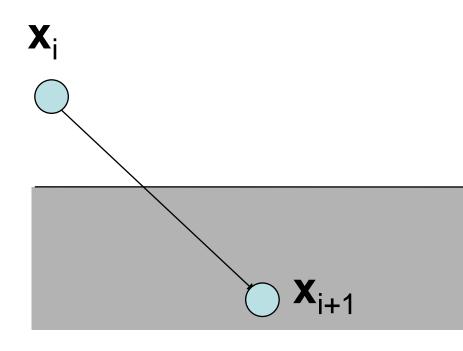
• Coefficient of restitution ε

• When $\varepsilon = 1$, mirror reflection



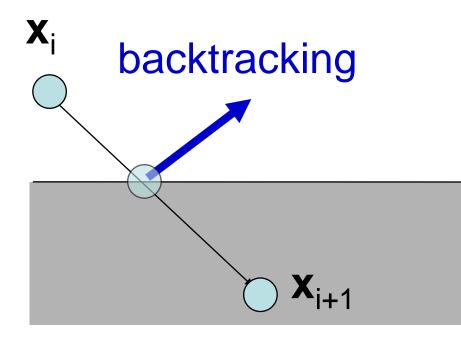
Collisions – Overshooting

• Usually, we detect collision when it is too late: we are already inside



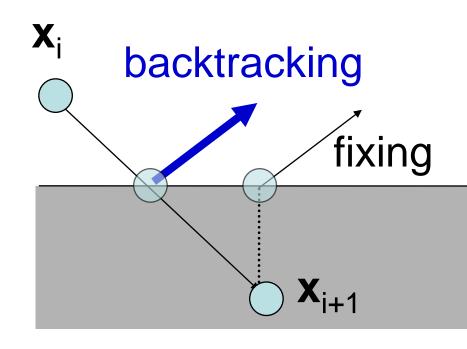
Collisions – Overshooting

- Usually, we detect collision when it is too late: we are already inside
- Solution: Back up
 - Compute intersection point
 - Ray-object intersection!
 - Compute response there
 - Advance for remaining fractional time step



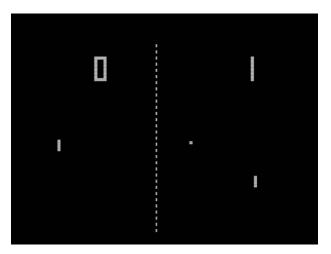
Collisions – Overshooting

- Usually, we detect collision when it is too late: we are already inside
- Solution: Back up
 - Compute intersection point
 - Ray-object intersection!
 - Compute response there
 - Advance for remaining fractional time step
- Other solution:Quick and dirty hack
 - Just project back to object closest point



Questions?

- Pong: $\varepsilon = ?$
- http://www.youtube.com/watch?v=sWY0Q_IMFfw
- http://www.xnet.se/javaTest/jPong/jPong.html







http://en.wikipedia.org/wiki/Pong

Collision Detection in Big Scenes

- Imagine we have *n* objects. Can we test all pairwise intersections?
 - Quadratic cost $O(n^2)$!

- Simple optimization: separate static objects
 - But still O(static \times dynamic+ dynamic²)

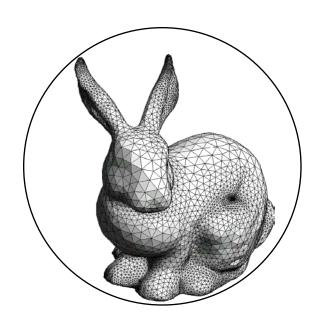
Hierarchical Collision Detection

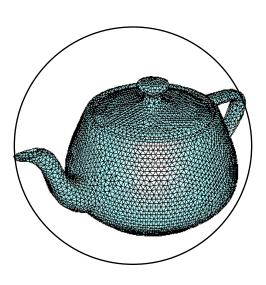
 Use simpler conservative proxies (e.g. bounding spheres)

- Recursive (hierarchical) test
 - Spend time only for parts of the scene that are close
- Many different versions, we will cover only one

Bounding Spheres

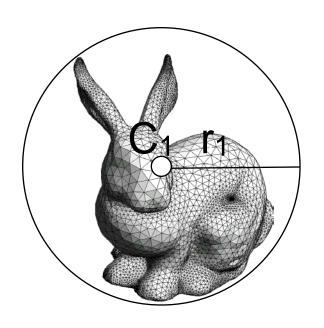
- Place spheres around objects
- If spheres do not intersect, neither do the objects!
- Sphere-sphere collision test is easy.

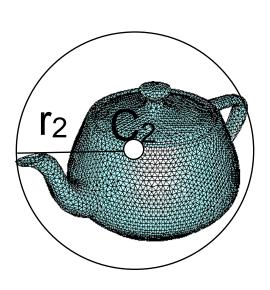




Sphere-Sphere Collision Test

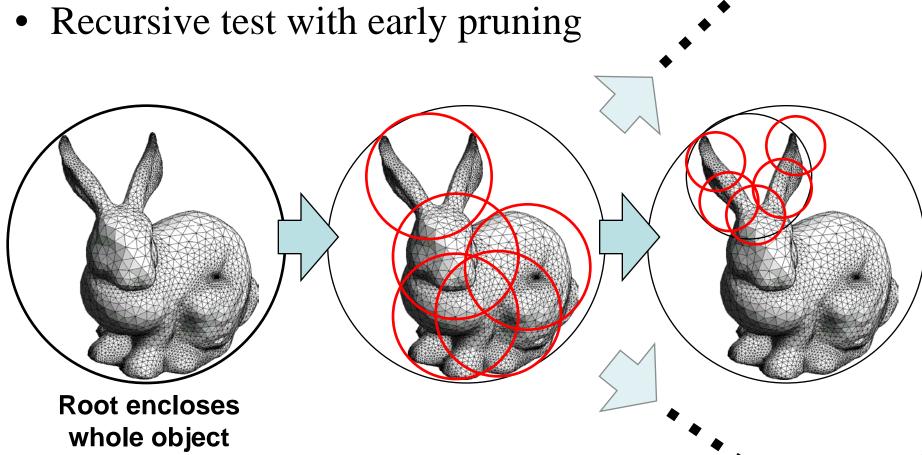
- Two spheres, centers C_1 and C_2 , radii r_1 and r_2
- Intersect only if $|C_1C_2| < r_1 + r_2$





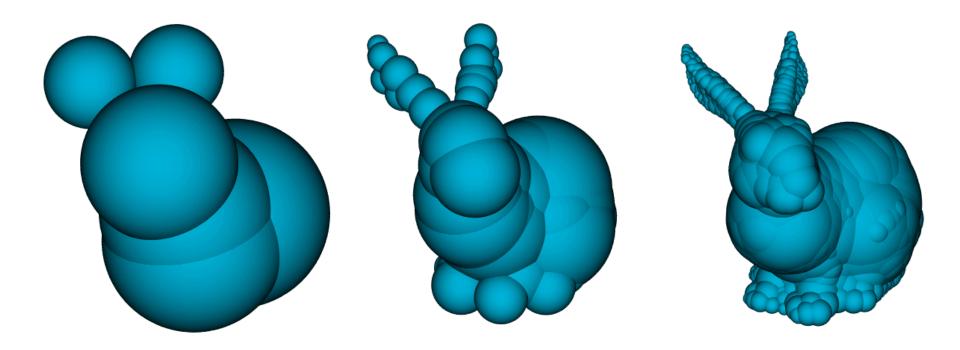
Hierarchical Collision Test

- Hierarchy of bounding spheres
 - Organized in a tree



Examples of Hierarchy

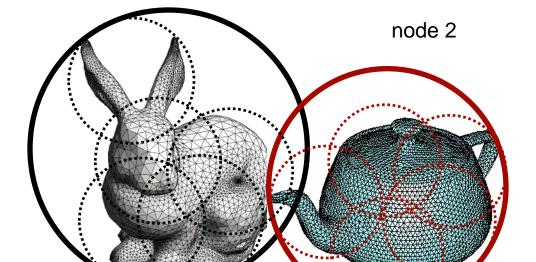
• http://isg.cs.tcd.ie/spheretree/



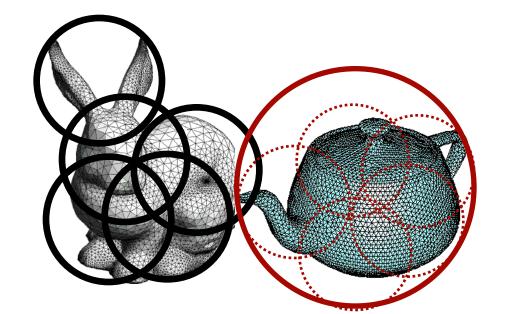
Pseudocode (simplistic version)

```
boolean intersect(node1, node2)
   // no overlap? ==> no intersection!
   if (!overlap(node1->sphere, node2->sphere)
      return false
   // recurse down the larger of the two nodes
   if (node1->radius()>node2->radius())
      for each child c of node1
         if intersect(c, node2) return true
   else
      for each child c f node2
        if intersect(c, node1) return true
   // no intersection in the subtrees? ==> no intersection!
   return false
```

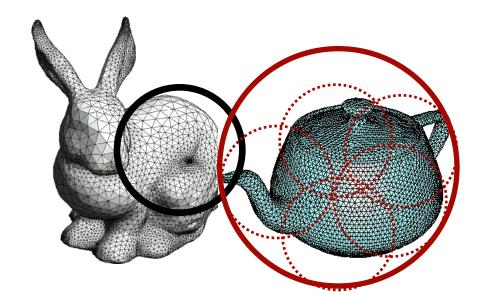
```
boolean intersect(node1, node2)
   if (!overlap(node1->sphere, node2->sphere)
      return false
   if (node1->radius()>node2->radius())
      for each child c of node1
         if intersect(c, node2) return true
   else
      for each child c f node2
        if intersect(c, node1) return true
   return false
                             node 1
```



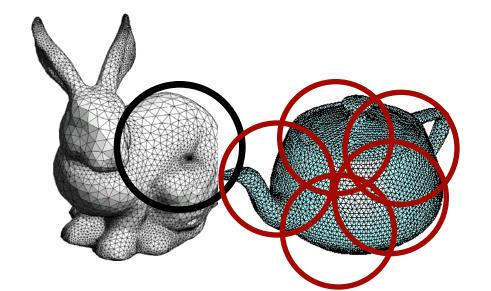
```
boolean intersect(node1, node2)
  if (!overlap(node1->sphere, node2->sphere)
    return false
  if (node1->radius()>node2->radius())
    for each child c of node1
       if intersect(c, node2) return true
  else
    for each child c f node2
       if intersect(c, node1) return true
  return false
```



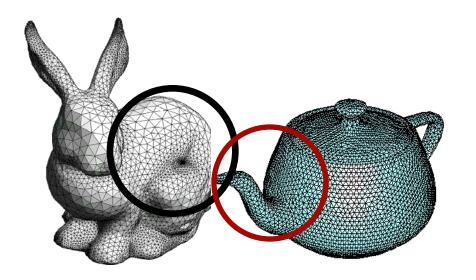
```
boolean intersect(node1, node2)
  if (!overlap(node1->sphere, node2->sphere)
    return false
  if (node1->radius()>node2->radius())
    for each child c of node1
       if intersect(c, node2) return true
  else
    for each child c f node2
       if intersect(c, node1) return true
  return false
```



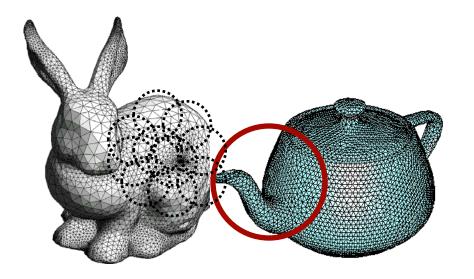
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boolean intersect(node1, node2)
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    return false
  if (node1->radius()>node2->radius())
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```



```
boolean intersect(node1, node2)
  if (!overlap(node1->sphere, node2->sphere)
    return false
  if (node1->radius()>node2->radius())
    for each child c of node1
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  else
    for each child c f node2
       if intersect(c, node1) return true
  return false
```



```
boolean intersect(node1, node2)
  if (!overlap(node1->sphere, node2->sphere)
    return false
  if (node1->radius()>node2->radius())
    for each child c of node1
       if intersect(c, node2) return true
  else
    for each child c f node2
       if intersect(c, node1) return true
  return false
```

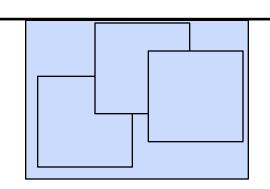


Pseudocode (with leaf case)

```
boolean intersect(node1, node2)
   if (!overlap(nodel->sphere, node2->sphere)
      return false
   // if there is nowhere to go, test everything
   if (node1->isLeaf() && node2->isLeaf())
      perform full test between all primitives within nodes
   // otherwise go down the tree in the non-leaf path
   if ( !node2->isLeaf() && !node1->isLeaf() )
      // pick the larger node to subdivide, then recurse
   else
      // recurse down the node that is not a leaf
   return false
```

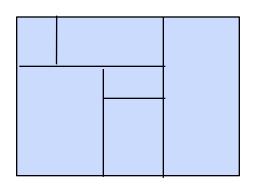
Other Options

- Axis Aligned Bounding Boxes
 - "R-Trees"



- Oriented bounding boxes
 - S. Gottschalk, M. Lin, and D. Manocha. "OBBTree: A hierarchical Structure for rapid interference detection," Proc. Siggraph 96. ACM Press, 1996

• Binary space partitioning trees; kd-trees



Questions?

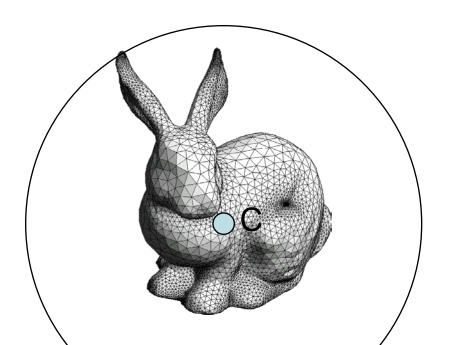
- http://www.youtube.com/watch?v=b_cGXtc-nMg
- http://www.youtube.com/watch?v=nFd9BIcpHX4&f eature=related
- http://www.youtube.com/watch?v=2SXixK7yCGU

Hierarchy Construction

- Top down
 - Divide and conquer
- Bottom up
 - Cluster nearby objects
- Incremental
 - Add objects one by one, binary-tree style.

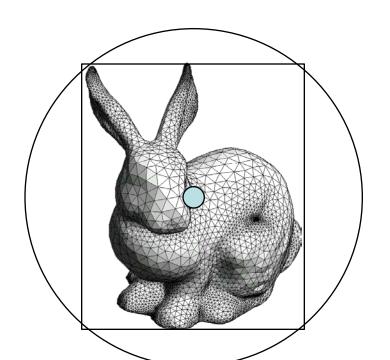
Bounding Sphere of a Set of Points

- Trivial given center C
 - $\text{ radius} = \max_i //C P_i //$



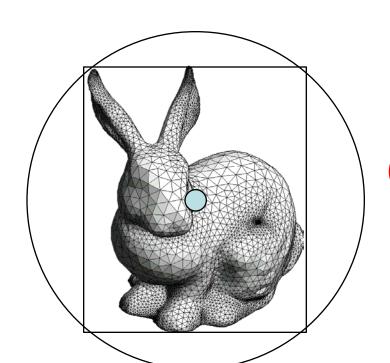
Bounding Sphere of a Set of Points

- Using axis-aligned bounding box
 - center= $((x_{min}+x_{max})/2, (y_{min}+y_{max})/2, (z_{min}, z_{max})/2)$
 - Better than the average of the vertices because does not suffer from non-uniform tessellation



Bounding Sphere of a Set of Points

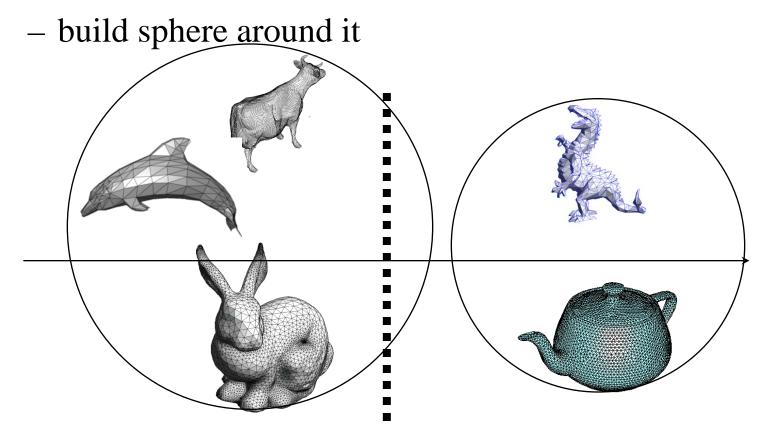
- Using axis-aligned bounding box
 - center= $((x_{min}+x_{max})/2, (y_{min}+y_{max})/2, (z_{min}, z_{max})/2)$
 - Better than the average of the vertices because does not suffer from non-uniform tessellation



Questions?

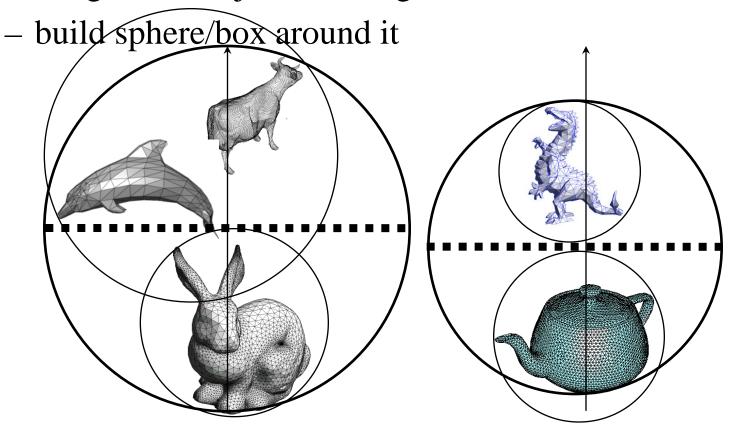
Top-Down Construction

- Take longest scene dimension
- Cut in two in the middle
 - assign each object or triangle to one side



Top-Down Construction - Recurse

- Take longest scene dimension
- Cut in two in the middle
 - assign each object or triangle to one side

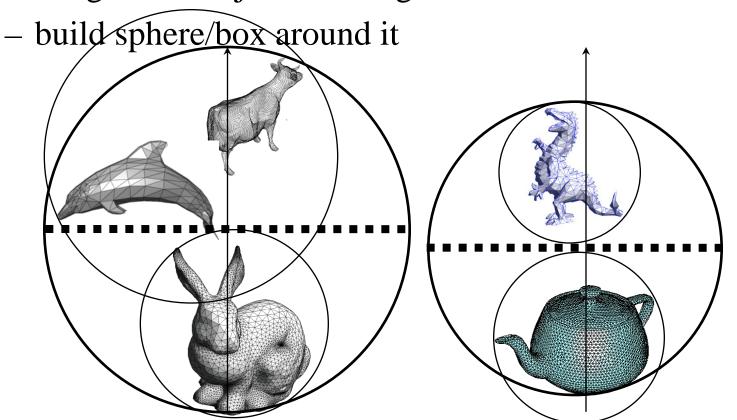


Top-Down Construction - Recurse

- Take longest scene dimension
- Cut in two in the middle

Questions?

assign each object or triangle to one side

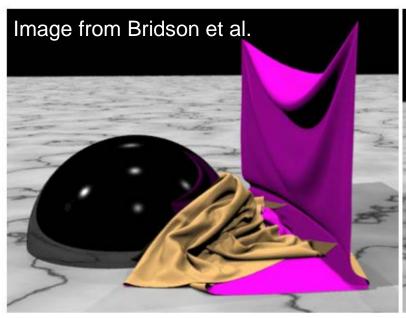


Reference



The Cloth Collision Problem

- A cloth has many points of contact
- Stays in contact
- Requires
 - Efficient collision detection
 - Efficient numerical treatment (stability)





Robust Treatment of Simultaneous Collisions

David Harmon, Etienne Vouga, Rasmus Tamstorf, Eitan Grinspun

