

Performance

We say that a computer has better performance than another if the **response time/execution time** is smaller than the other. The **response time** is the time which a computer needs in order to finish a task.

We also say that a computer has better performance if a computer has more **throughput/bandwidth** which refers to the total amount of work done in a given time.

So, we can define performance as: $Performance = \frac{1}{Execution\ time}$

So, if we have two computers X and Y we say that "X is **n** times faster than Y" with this formula: $\frac{Performance_X}{Performance_Y} = n$.

How do we measure performance in computers? First, we need to know the execution time of a program. The CPU does a lot of tasks at the same time, so if we want to measure a specific time, we need to check the **CPU time**, which is the time that the CPU spends in that task.

We measure this time with the next formulas:

$$\text{CPU execution time for a program} = \frac{\text{CPU clock cycles for a program}}{\text{Clock cycle time}} \times \text{Clock cycle time}$$

$$\text{CPU execution time for a program} = \frac{\text{CPU clock cycles for a program}}{\text{Clock rate}}$$

These formulas say how much time spends a computer with a task, but we can be more specific trying to know the **instructions** it does per clock cycle, the **clock cycles per instruction CPI**.

$$\text{CPU clock cycles} = \text{Instructions for a program} \times \frac{\text{Average clock cycles}}{\text{per instruction}}$$

Having the CPI, we can take the CPU time with the next formula:

$$\text{CPU time} = \text{Instruction count} \times \text{CPI} \times \text{Clock cycle time}$$

Instruction count refers to the number of instructions done.

$$\text{CPU time} = \frac{\text{Instruction count} \times \text{CPI}}{\text{Clock rate}}$$

Amdahl's law

With the amdahl's law we can see the overall improvement in a given machine:

$$Speedup_{Overall} = \frac{Execution\ time_{old}}{Execution\ time_{new}}$$

$$Speedup_{Overall} = \frac{1}{(1 - Fraction_{enhanced}) + \frac{Fraction_{enhanced}}{Speedup_{enhanced}}}$$

The amdahl's law states that the performance enhancement possible with a given improvement is limited by the amount that the improved feature is used.

There are more metrics used in order to measure the performance of a computer.

MIPS, millions of instructions per seconds:

$$\begin{aligned} \text{MIPS} &= \frac{\text{Instruction count}}{\text{Execution time} \times 10^6} \\ &= \frac{\text{Instruction count}}{\frac{\text{Instruction count} \times \text{CPI}}{\text{Clock rate}} \times 10^6} = \frac{\text{Clock rate}}{\text{CPI} \times 10^6} \end{aligned}$$

MFLOPS, millions of floating-point operations per second.

$$\text{MFLOPS} = \frac{\text{Floating point instruction count}}{\text{Execution time} \times 10^6}$$

Info Adicional: Fórmulas y relaciones útiles para los ejercicios

$$\begin{aligned} T_{\text{CPU}} &= \text{NI} \times \text{CPI} \times T_{\text{CICLO}} = \\ &= \text{NroCiclosReloj} / \text{FreqReloj} \end{aligned}$$

X es n veces más rápido que Y significa:

Una mejora en el sistema se mide con la:

$$\text{Aceleración} = \frac{T_{\text{EJ}}(\text{sin mejora})}{T_{\text{EJ}}(\text{con mejora})} = \frac{R(\text{con m.})}{R(\text{sin m.})}$$

La **ley de Amdahl** mide la mejora del rendimiento global de un sistema. Donde:

F_m : Fracción de tiempo mejorada y Acc_m : Aceleración mejorada

La **ley de Amdahl** para varias mejoras:

$$\text{Acc}_{\text{global}} = \frac{1}{(1 - F_m) + \frac{F_m}{\text{Acc}_m}}$$

$$\text{Acc}_{\text{global}} = \frac{1}{1 - \sum_{i=1}^n F_{m,i} + \sum_{i=1}^n \frac{F_{m,i}}{\text{Acc}_{m,i}}}$$

$$\text{MIPS} = \text{NI} / (T_{\text{CPU}} \times 10^6) = \text{NI} / (\text{NI} \times \text{CPI} \times T_{\text{Ciclo}} \times 10^6) = \text{Freq} / (\text{CPI} \times 10^6)$$