Compilers

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Overview

Any program written in any programming language must be translated before it can be executed on a certain piece of hardware. This translation is typically accomplished by a software system called compiler. This module aims to introduce students to the principles and techniques used to perform this translation and the key issues that arise in the construction of modern compilers.

Syllabus

Introduction What is a compiler? A high-level view of compilation. General structure of a compiler. An overview of compilation technology.

Lexical Analysis (Scanning) Regular languages/expressions, finite state machines, building regular expressions from a finite automaton.

Syntax Analysis (Parsing) Expressing Syntax, Context Free Grammars, Top-Down Parsing, Bottom-Up parsing.

Semantic Analysis Context-sensitive analysis, Attribute

Grammars, Symbol Tables, Type Checking.

Intermediate Representations Properties, taxonomy, Graphical IRs, Linear IRs.

Storage Management The Procedure Abstraction, Linkage convention, Run-time storage organisation.

Code Generation Code Shape, Instruction Selection, Register Allocation, Instruction Scheduling.

Topics in Compiler Construction Code Optimisation, JIT Compilation.

Attribution

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Contribution

Pull requests are very welcome: https://github.com/Todd-Davies/third-year-notes

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1 Intro

A compiler is a program that reads another program written in one language and translates it into an equivalent program written in another language.

An interpreter reads the source code of a program and produces the results of executing the source. Many issues related to compilers are also present in the construction and execution of interpreters.

A good compiler exhibits the following qualities:

- It generates correct code
- It generates code that runs fast
- It confirms to the specification of the input language
- It copes with any input size, number of variables, line length etc
- The time taken to compile source code is linear in its size
- It has good diagnostics
- It has *consistent* optimisation's
- It works will with a debugger

An example of a compiler that optimises code is if we had a for-loop such as:

```
A = []
for i = 0 to N:
   A[i] = i
endfor
```

If N was always equal to 1, then the compiler should optimise this to:

$$A = [1]$$

There are two things that any sensible compiler *must* do:

- Preserve the meaning of the program being compiled
- Improve the source code in some way

In addition, it could do some (it's pretty much impossible to do all) of these things:

- Make the output code run fast
- Make the size of the output code small
- Provide good feedback to the programmer; error messages, warnings etc
- Provide good debugging information (this is hard since transforming the program from one language into another often obscures the relationship between an instance of a program at runtime and the source code it was derived from).
- Compile the code quickly

2 Parts of the compiler

In this section, we'll give a brief overview of all the bits inside a compiler. Most compilers can be roughly split into two parts; the front end and the back end:

The front end is concerned with analysis of the source language, making sure that the input is legal and producing an intermediate representation.

The back end translates the intermediate representation into the target code. This usually involves choosing appropriate instructions for each operation in the intermediate representation.

Usually, the front end can run in linear time, while the back end is NP-Complete. We can automate much of the front end of the compiler.

Having an intermediate representation (IR) of the program is so helpful since it means we can completely separate the front and back ends of a compiler. Consequently, we can have multiple front ends all compiling different languages into the same IR, and multiple back ends producing instructions for different architectures.

If we have n languages and m architectures, then we'd need to write $n \times m$ monolithic compilers, but can instead write n front ends and m back ends (n+m). This is almost as good as it sounds; in practice, you need to choose your IR very carefully, since its hard to make it encapsulate everything all the features of a language (a good example of this is compiling Scala onto code that runs on the JVM, where type erasure is a big limitation for Scala).

In more detail, we code goes through the following steps inside the compiler:

Lexical Analysis (front end):

Here, the source language is read in and tokenized (grouped into tokens for later). If the input was a = b + x, you might get (id,a)(=)(id,b)(+)(id,c) out of the other end. Whitespace is usually ignored (or, depending on the language, Incorporated into the parsing), and a symbol table is generated, containing the words that are not reserved words in the language (e.g. variable names).

Syntax Analysis (front end):

Here, the tokens are given a hierarchical structure, often using recursive rules such as Context Free Grammars. The output might be an **Abstract Syntax Tree** (AST), which is an abstract representation of the program (basically an IR).

Semantic Analysis (front end):

Here, we check for semantic errors (such as type checking, flow control checks etc). The AST is annotated with the results of the checks which can be used for optimisation later.

Intermediate code generation (front end):

The AST is now translated into the IR. If the AST is constructed well, and IR is well chosen, then this should be fairly straightforward. Three address code might be an example of an IR.

Optimisation (back end):

The IR is now optimised to increase how quickly it runs, or decrease how much space it uses etc. Some optimisation are easier than others, and some are very complex! Often, the optimisation stage is so complex, that it could be a whole separate part of the compiler (a middle stage in-between the front and back ends).

Code generation (back end):

This phase is concerned with things such as register allocation (NP-Complete), instruction selection (pattern matching), instruction scheduling (NP-Complete) and more. Architecture specific information may be used for further optimisation here, and machine code is the output.

3 Lexical Analysis

So, lexical analysis is where we read the characters in the input and produce a sequence of tokens (i.e. tokenize the input). We want to do this in an automatic manner.

When translating from a programming language or a natural language, we need to map words to parts of speech. In programming languages, this is syntactic (as opposed to being idiosyncratic in natural languages), and is based on notation. Things like reserved words are very important in tagging a programming language.

To talk about lexical analysis, we should make some definitions:

See my computation notes (COMP11212) for more on CFG's

- A vocabulary (or alphabet) is some finite set of symbols.
- A String is a finite sequence of symbols from the vocabulary.
- A Context Free Grammar (CFG) is a 4-tuple; (S, N, T, P):
 - S: The starting symbol.
 - -N: The non-terminal symbols.
 - -T: The set of terminal symbols.
 - -P: A set of production rules.
- A Language is any set of strings over a fixed vocabulary, or the set of terminal productions of a CFG.

Terminal symbols will usually start with a lower case letter, and non-terminal symbols will start with an upper case one.

We can use repeated substitution to derive *sentinel forms*.

Leftmost derivation is when the leftmost non-terminal symbol is expanded at each step. When we're recognising a valid sentence, we reverse this process.

If we have a knowledge about lexical analysis, we can avoid having to write a lexical analyser by hand, and can simplify the specification and implementation of a language. We need to specify a *lexical pattern* to derive tokens, which is essentially a CFG.

Some parts of this are easy, for example:

WhiteSpace \rightarrow blank|tab|WhiteSpace blank|WhiteSpacetab

Things like keywords, operators and comments are easy to use as well. However, some parts of languages are more complicated, such as identifiers and numbers. We want a notation that lets us go easily to an implementation.

Regular expressions are a way of specifying a regular language; they are formulas that represent a possibly infinite set of strings. A Regular Expression (RE) over the vocabulary V is defined as:

- ϵ is a RE denoting the empty set.
- If $a \in V$ then a denotes $\{a\}$.
- If r_1 and r_2 are RE's, then:
 - $-r_1^*$ denotes zero or more occurrences of r_1
 - $-r_1r_2$ denotes concatenation
 - $-r_1|r_2$ denotes either or.
- Short-hands include [a-d] which expands to [a|b|c|d], r^+ for rr^* and r? for $[r|\epsilon]$

Building a lexical analyser by hand may involve a function with lots of if/else statements as we try to classify each character one by one.

A different idea is to try and match the input to different regular expressions and use the one with the longest match. This would be linear in the number of regular expressions we have (we would need to do a fresh search for each).

We could study the regular expressions we have and try to automate the construction of a scanner. Some regular expressions can be converted into transition diagrams. For example, matching a register (r(0-9)+) can be converted to the following:

The regex would accept the string if the transition diagram ends in an accept state after the string has been run through it. We can produce a transition table (one way of encoding automata in computers) and (once we've figured out how to produce the table, which we'll soon find out) run through the input string in linear time.

3.1 Deriving a Deterministic Finite Automata from a Regular Expression

Remember that a DFA is a special case of an NFA.

Every regular expression can be converted to a deterministic finite automaton (DFA), and DFA's can automate lexical analysis.

For example, the regular expression describing CPU registers (0-31) could be:

Register
$$\to r((0|1|2)(\text{Digit}|\epsilon)|([4-9])|(3|30|31))$$

If we generated the DFA shown in Figure ??, we could produce a transition table like:

State	r	0, 1	2	3	$4 \dots 9$
0	1	_	_	_	_
1	_	2	2	5	4
2(fin)	_	3	3	3	3
3(fin)	—	_	_	_	_
4(fin)	_	_	_	_	_
5(fin)	—	6	_	_	_
6(fin)	–	_	_	_	_

This is done by creating an NFA for each thing you can do in a regular expression (concatenation, either operator, star operator etc) and putting them together.

Converting a RE into an NFA is more direct, but its also a lot slower to parse (since NFA's can have many paths through them). Converting to a DFA is slower (and the resulting automata is slower), but lets us parse an input in linear time.

The idea is:

That's Ken Thompson, the guy who wrote unix.

- 1. Write down the RE for the input language
- 2. Convert it to an NFA (Thompson's construction)
- 3. Build a DFA to simulate the NFA (subset construction)
- 4. Shrink the DFA (Hopcroft's algorithm)

We have seen the subset construction algorithm before (in COMP11212), where it was called 'Algorithm One'. There is a rather compact but (I think) working implementation in COMP36512/programs/nfa-dfa.py on Github that you could look at.

Before we look at the algorithm itself, we need to look at two operations:

move(states, a) Returns all the states to which there is a transition from some state in states with the symbol a.

e-closure(states) All the states that are reachable using only epsilon transitions from any state in states.

The algorithm is:

```
dStates = e-closure(startState)
markedStates = []
dTable = {}
// While there are unmarked states
while (dStates - markedStates) is not []:
    t = (dStates - markedStates).get(0)
    markedStates.add(t)
    for symbol in alphabet:
        U = e-closure(move(t, symbol))
        if U in dStates:
            dStates.add(U)
        dTable(t, a) = U
```

This builds up a table (representing a DFA) by creating states representing all the states reachable with a specific symbol from a set of states within the NFA.

3.2 DFA minimisation; Hopcroft's algorithm

The main disadvantage of DFA's is that they can be rather large (when converting from an NFA to a DFA, the DFA could have worst case exponential number of states). As a result, Hopcroft's algorithm for minim sing the number of states in a DFA is good for our memory usage.

The idea behind the algorithm is to find groups of states where for each input symbol, every state in the group will have transitions exclusively within the group.

The algorithm is:

```
while the groups are not stable {
  for each group g {
    for each input symbol I {
      for each state s in g {
        if s(g) not in g {
          put s in its own group
      }
   }
}
```

3.3 Fast scanners

Now it is very easy to build a recogniser for the DFA, we can just get the transition table for the DFA, and read each character of the input, transitioning to the next state every time. Accepting and rejecting depends on whether we get to eof in a finishing state (accept)or we didn't/we made an invalid transition (reject).

However, table recognisers aren't as fast as they could be; each character requires one memory access, which is not very efficient, especially if the transition table is big and won't fit in a cache. Some automatic code generation tools will output a series of goto or case statements instead, since then a transition table isn't needed (the states are hardcoded into the program).

Poor language design can complicate analysis though. For example, in Fortran:

```
D05i=1,25
5
```

Is a for-loop from 1 to 25. However, the following is also valid:

```
D05i=1.25
5
```

The only difference is that there is a comma instead of a period, but now the compiler will have that counts. assigned the token D05i a value of 1.25, and the 5 at the end will be a non-operation.

This may not exactly be what happens, but it's the thought

Similarly, in C++ having types within types can be hard since myType<myType2<int>> includes the symbols >>, which is the operator for writing to an output stream.

lex and flex are tools for generating lexical analysers.

4 Parsing languages

Not all languages can be described by regular expressions (as we have attempted to do so far). They cannot describe things like nested constructs (i.e. is the bracketing legal in a mathematical formula). Also, you can't use a terminal symbol in a regular expression before it has been fully defined (i.e. no recursion).

Chomsky's hierarchy of grammars tells us which grammars can describe other ones:

Phase structured:

Context sensitive:

Context free:

Regular:

Only rules of the form $A \to \epsilon$, $A \to a$, $A \to pB$ are allowed.

Context free syntax is expressed with a context free grammar, which is a 4-tuple $G = \{S, N, T, P\}$, where S is the start symbol, N are the non-terminal symbols, T are the terminal symbols and P are the production rules. We re- write rules (starting from the initial rule) in order to make them closer to a sentence we're trying to obtain. A sequence of re-writes leading to some desired output is called a *derivation*, and the process of finding a derivation for a specific sentence is called *parsing*.

A derivation is a sequence of steps from the initial rule to a parsed representation of the input. Different choices of steps can potentially lead to different derivations of the same input. Two derivations are of particular interest to us:

Leftmost derivation; at each step, replace the leftmost non-terminal.

Rightmost derivation; at each step, replace the rightmost non-terminal.

A parse tree is a graphical representation of a derivation that is independent of the order that the derivation rules were applied in. To construct a parse tree, start with the starting symbol (which is the root of the tree), then for each derivational step, add children nodes for each symbol on the right hand of the production rule to the node for the left side. After you've done this, the leaves of the tree will (should) read from left to right to form the input.

If we're parsing something like a mathematical formula, then we need to build the notion of precedence into our derivational rules so that we get the correct parsing for an input. To do this, we force the parser to recognise the high- precedence subexpressions first.

Grammars are ambiguous if they can possibly produce more than one parse tree for a sentence. This is the case if a grammar has more than one leftmost or rightmost derivation for a single sentinel form. An example is:

```
Stmt = if Expr then Stmt | if Expr then Stmt else Stmt | Expr Expr = W | X | Y | Z
```

This could match the following in two ways:

```
if X then if Y then W else Z
```

In order to eliminate ambiguity (and also deal with precedence), we need to re- write the grammar:

```
Stmt = IfElse | IfNoElse
IfElse = if Expre then IfWithElse else IfWithElse
IfNoElse = if Expr then Stmt | if Expr then IfElse else IfNoElse
Expr = W | X | Y | Z
```

So, if there is ambiguity, then we should try and resolve it in the CFG (after all, we only have to do this once, instead of resolving at runtime every time!). Overloading (when you give multiple things the same name or structure, such as method overloading in Java) can create ambiguity that you can only resolve using context. In general, to solve ambiguity:

If the issue is context free, then re-write the CFG so that there is no ambiguity.

If the issue requires context to solve, then we need more information in order to continue. This is really a problem with the design of the language.

There are two broad classes of parsers; top down parsers and bottom up parsers:

Top-down parsers:

- Construct the root of the tree first, then construct the rest in pre-order, using a depth first search.
- Pick a production, and try to match the input. If you fail then use backtracking.
- Try to find a leftmost derivation for the input string where we scan from left to right.
- Some grammars are backtrack-free (called predictive parsing)

Bottom-up parsers:

- Construct the tree for an input but start at the leaves and work up towards the root.
- Use a left-to-right scan and try to construct a rightmost derivation in reverse.
- Handles a large number of grammars.

4.1 Top Down Recursive Descent Parsing

This is where you:

- Construct the root with the start symbol for the grammar
- While the leaves of the parse tree don't match the input:
 - Select a node in the tree labelled A.
 - Select a production rule for A and construct a child for each symbol on the right hand side of the rule.
 - When a terminal symbol is added to the fringe, but it doesn't match the fringe, then backtrack.

If you choose the right production step at each stage, then this algorithm is fast, if you don't then the runtime will increase due to backtracking.

A grammar is left-recursive if it has a non-terminal symbol A such that there is a derivation $A \to Aa$ for some string a. Such a grammar can cause an infinite look for recursive-descent parsers since they may output an string of infinite a's. To avoid this, we try to eliminate left recursion; i.e. replace $A \to Aa|b$ with $A \to bA$ $A' \to aA'|\epsilon$.

The general algorithm for non-cyclic, non- ϵ -productive grammars is:

- Arrange the non-terminal symbols $A_1 \dots A_n$
- For $i = 1 \dots n$:
 - For $j = 1 \dots i 1$:
 - * Replace each production $A_i \to A_j \gamma$ with $A_I \to \delta_1 \gamma | \dots | \delta_k \gamma$, where $A_j \to \delta_1 | \dots | \delta_k$ are the current A_j productions.
 - * Eliminate the left recursion among A_i .

4.1.1 Predictive parsing

So now we can make a top-down parser which will find the correct matching in finite time, but it employs backtracking when it picks the wrong initial rule (which slows everything down). If we look ahead in the input, we can use context to influence our decisions about what production rules to try next so we can attempt to reduce the amount we have to backtrack.

In general, we need an infinite amount of look-ahead to always make the right decision about what production rule to use next (but this is pretty much the same as parsing the rest of the string, right?). However, most context free grammars can be parsed with a limited look-ahead.

The basic idea is for any production $A \to a|b$, we want to have a distinct way of choosing the correct production to expand (either a or b).

We can do this for some grammars by defining a set called FIRST. This is the set of the first terminal symbols for each string derived from A. A very simple example is:

$$A \to B|C$$

$$B \to x|y$$

$$C \to m|n$$

$$FIRST(B) = \{x, y\}$$

$$FIRST(C) = \{m, n\}$$

If for a production rule $A \to X|Y$, $FIRST(X) \cap FIRST(Y) = \emptyset$, then we can implement the look-ahead with only one symbol. This is the LL property.

If a grammar does not have the LL(1) property, we can sometimes transform it so that it does:

- For each non-terminal A, find the longest prefix a common to two or more of its alternatives (e.g. B and C in $A \to B|C$).
- If $a \neq \epsilon$ then replace all the A productions $A \to ab_1 | \dots | ab_n | \gamma$ (where γ doesn't begin with a) with $A \to aZ | \gamma, Z \to b_1 | \dots b_n$.
- Repeat until we have no common prefixes.

Note that it is undecidable as to whether an LL(1) grammar exists for any CFG. It is also possible to parse non-recursively if we maintain a stack and determine what production rules to apply using a table.

4.2 Bottom up parsing

The goal for bottom-up parsing is the same as that of top-down parsing; construct a parse tree for a string s given some grammar G. Bottom-up parsing starts from the string and works back towards the start symbol of the grammar, whereas top-down goes the other way.

Bottom-up parsing works by applying a sequence of reductions to the input string. A reduction corresponds directly to a rule in the input grammar, and takes the form $A \to b$.

If we defined our grammar G to be:

1.
$$S \to LMR$$

2.
$$L \to c$$

3.
$$M \rightarrow Mo|o$$

4.
$$R \rightarrow mpilers$$

We could parse input like so:

Sentinel Form	Production	Position
cooooompilers	2	1
LMoooompilers	3	2
LMooompilers	3	3
LMoompilers	3	3
LMompilers	3	3
LMmpilers	3	9
LMR	4	3
S	_	_

To do the above, we needed to find some substring s_1 that could match the right side of a production that would occur in the rightmost derivation¹ To be able to reason about this, we define a handle, which is a pair $(A \to b, k)$, where $A \to b \in G$ and k is the position in the input string of the *rightmost* symbol in b.

This is efficient because since we're dealing with a right sentential form, anything to the right of the handle is a terminal symbol, meaning the compiler doesn't have to scan past the handle.

4.2.1 Shift reduce parsers

A basic bottom-up, shift reduce parser is stack based and has four operations:

Shift: The next input is shifted onto the top of the stack.

Reduce: The right end of the handle is on the top of the stack. Locate the left end of the handle within the stack², pop the handle of the stack and push the appropriate non-terminal symbol.

Accept: The string was parsed successfully.

Error: Handle the error somehow (implementation dependent).

Using the 'cooooompilers' example again:

¹As if we started from the start-state of the grammar and always expanded the rightmost non-terminal.

 $^{^2}$ You can just keep popping until you reach the end of the handle

Stack	Input	Handle	Action
\$	coooompilers	None	Shift
\$c	ooooompilers	2, 1	Reduce 2
\$L	ooooompilers	None	Shift
\$Lo	oooompilers	3, 2	Reduce 3
\$LM	oooompilers	None	Shift
\$LMo	ooompilers	3, 3	Reduce 3
\$LM	ooompilers	None	Shift
\$LMo	oompilers	3, 2	Reduce 3
\$LM	oompilers	None	Shift
\$LMo	ompilers	3, 2	Reduce 3
\$LM	ompilers	None	Shift
\$LMo	mpilers	3, 2	Reduce 3
\$LMm	pilers	None	Shift
\$LMmp	ilers	None	Shift
\$LMmpi	lers	None	Shift
\$LMmpil	ers	None	Shift
\$LMmpile	rs	None	Shift
\$LMmpiler	S	None	Shift
\$LMmpilers		4,9	Reduce 4
\$LMR		4,9	Reduce 4
\$G		None	Accept

There are two possible things that can go wrong here:

Shift/Reduce conflict: The parser can't decide whether to do a shift or a reduce. This is usually because of an ambiguous grammar. The solution is to make the grammar unambiguous or just always choose shift.

Reduce/Reduce conflict: The parser can't decide which (of several) reduction to make.

4.2.2 LR parsers

If we want to avoid reduce/reduce conflicts, then we need to have a LR(1) grammar. This is a grammar where we can always choose the next reduction by looking one symbol beyond the end of the current handle, and we can always isolate the handle of any input string (at any stage of the parsing). Most context free programming language definitions can be expressed as an LR(1) grammar, and parsers for such grammars can be implemented in polynomial time (O(|tokens| + |reductions|)).

LR parsing is slightly more complicated than shift reduce parsing in to ways; we need to store state information in the stack, and we need a table consisting of the following:

Action: Either a shift, reduce, accept or error as with the shift-reduce parser. The function of shift is slightly different here, in that the next symbol is pushed to the stack, as well as the current *state*.

Goto: The state that should be pushed onto the stack after a reduction. If no goto is listed, no state should be pushed.

An example of parsing a string with a LR parser will be given here. The grammar is as follows:

- 1. $G \to L$ 2. $L \to LP$
- $3. \qquad L \to P$
- 4. $P \rightarrow (P)$
- 5. $P \rightarrow ()$

Figure 1: A grammar for generating sequences of balanced brackets.

State		Acti	Goto		
State	()	EOF	L	Р
0	S3			1	2
1	S3		accept		4
2	R3		R3		
3	S6	S7			5
4	R2		R2		
5		S8			
6	S6	S10			9
7	R5		R5		
8	R4		R4		
9		S11			
10		R5			
11		R4			

Table 1:	The parse	table for	r the	grammar
shown in	Figure 1.			

Stack	Input	Action
$\$s_0$	(())()\$	Shift 3
$\$s_0(s_3)$	())()\$	Shift 6
$$s_0(s_3(s_6))$))()\$	Shift 10
$$s_0(s_3(s_6)s_{10})$)()\$	Reduce 5
$$s_0(s_3Ps_5)$)()\$	Shift 8
$$s_0(s_3Ps_5)s_8$	()\$	Reduce 4
$\$s_0Ps_2$	()\$	Reduce 3
$s_0 L s_1$	()\$	Shift 3
$s_0 L s_1 (s_3)$)\$	Shift 7
$$s_0 L s_1(s_3) s_7$	\$	Reduce 5
$s_0 L s_1 P s_4$	\$	Reduce 2
$\$s_0L$	\$	Reduce 1
$\$s_0Gs_1$	\$	Accept

Table 2: A parsing of the string '(())()'.

The parsing table and a worked example are shown in Tables 1 and 2 respectively.

4.2.3 Generating LR parser tables

The idea when generating the parser tables is to create a DFA from the grammar, then create the final action/goto table from the DFA. There are three algorithms for building the tables; LR(1), SLR(1) and LALR(1). The first one generates large tables and is slow, the second one generates the smallest tables and is fast, and the third is an in-between solution. SLR(1) used to be most popular when table size was very important, but now computers have lots of memory, LALR(1) is most commonly used.

5 Context sensitive analysis

Lexical and syntactical analysis ensure that the input program is a valid sentence in the source language, yet though we have a parse tree of the input program, there are still classes of errors that could be present in the program. Since syntax analysis is context-free, any semantic errors³ would not have been checked for, and would still exist in the IR.

5.1 Type Systems

We can use a type system to detect many semantic errors in the program. This involves using a *type checker* to assign or infer types for expressions and check that they are legal within context in which they are used.

Type systems consist of a number of built in types (primitives such as int, boolean etc, and language types such as Java's String), and rules to construct new types, determine if types are equivalent, infer⁴ the type of some expression etc. The extent of which type checking is performed varies by language; some languages such as Java employ static type checking at compile time, while others such as Python employ dynamic run-time checking.

A compiler designer must consider that types affect each other; for example, if a double is added to an int, then the result in most programming languages would be a double.

 $^{^3}$ These could include type errors, array index out of bound errors (that can be detected at compile time), undeclared variable errors etc

⁴If a language requires variables to be declared with a type before use (e.g. Java) then inference isn't difficult. It's only when variables can be declared as needed like in Python that it is really hard.

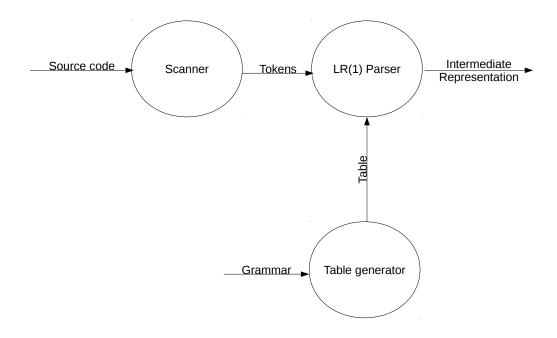


Figure 2: A diagram of the overall compiler system.

In order to perform context-sensitive analysis, formal methods such as grammars can be employed, ad-hoc methods are most effective (symbol tables, syntax directed translation with attribute grammars, etc).

5.1.1 Attribute Grammars

Knuth had the idea to annotate each symbol in a grammar with a set of attributes, and associate semantic rules with each production rule in the CFG to define each attribute in terms of other attributes. We can associate commands/actions with each rule, like so:

$$G \rightarrow E \qquad print(E.val) \\ E \rightarrow E_1 + T \qquad E.val = E_1.val + T.var \\ |T \qquad E.val = T.val \\ T \rightarrow T_1 * F \qquad T.val = T_1.val * F.val \\ |F \qquad T = F.val \\ F \rightarrow integer \qquad F.val = integer.lexval$$

There are two types of dependencies between attributes, synthesised dependencies and inherited dependencies. The former derive their value from constants and their children and grammars consisting of only synthesised dependencies can be parsed in a single bottom up pass. The latter are inherited dependencies, and these derive their value from their parents, siblings and constants.

An example of an inherited dependency would be parsing the expression int i;, since the variable i derives its type from the symbol int, which would be a sibling in the parse tree.

In order to evaluate the attributes of a parse tree, a dependence graph must be created. Nodes represent attributes, and edges represent the flow of the attribute values. The graph can be built as the parse tree is built, so this isn't too expensive (and the graph is proportional to the size of the tree too). A topological sort (nodes are visited such that edges go from earlier to later

nodes) can be used to find independent values and use them to calculate other values, though cyclic graphs mean that this doesn't work.

Generic attribute are rarely used in practice because lots of supporting rules are needed. They have seen use in things like XML editors though. Instead, a simplified idea is used; S-grammars (only use synthesised attributes) or L-grammars (limit the use of inherited attributes).

6 Intermediate Representation

The intermediate representation (IR) encodes the knowledge about the program that the compiler has derived. The purpose of an IR is to enable retargeting for different machines (you don't have to re-write the front end of the compiler every time), and to let machine independent optimisations be implemented.

Things that are hard to 'get right' with IR's include the level of abstraction that they exist on and how easy they are to manipulate and generate. Common IR choices include a directed acyclic graph (DAG), trees, or linear code (such pseudo code for an abstract machine). It is emphasised in the notes that there is no unversally good choice, and the goals of the compiler dictate what choice is best.

We can use an abstract syntax tree as an IR, and as such we want to convert a parse tree (from the front end of the compiler) to an AST. A parse tree contains lots of information that is not needed by the back end of the compiler, such as that of the terminal symbols from the CFG. The conversion involves traversing the parse tree in a post order manner, and matching each action (in the output) with a grammar rule.

Essensially what we end up with, is the parse tree with all non-terminal symbols removed. This is a near-source-level representation. In fact, to generate something similar to the original source code, then an in-order walk can be performed on the tree. Disadvantages of AST's like this are that they're very pointer intensive and often have multiple ways of being encoded for the same tree.

A DAG can be used instead of an AST. These are often more powerful than AST's, but are also harder to transform and are not useful for showing control flow. To construct a DAG, do the same as you would for an AST (post-order traversal & generate nodes for each action), but nodes can have multiple parents according to what other nodes make use of their result.

Other graph representations include control flow graphs (each node is a block of code, edges transfer control between them), data dependence graphs (nodes are program statements, edges join nodes if they one uses another's results), and call graphs which show the dependencies between different procedures.

6.1 Linear Representations

Three address code is similar to assembly, where each line is an instruction followed by up to three operands. The code is compact, resembles that produced as target code on many machines, and makes intermediate values created within a computation explicit.

Each instruction in two address code only takes two operands is more compact than three address code, but one address code (also called stack machine code, and used by Java bytecode) is the most compact. Each operation takes only one operand, and if more operands are required for an instruction, then they can be popped off a stack.

7 Back-end Datastructures

Representing the source code as a graph/tree/stack machine translation is useful, but we still need to encode much of the contextual information we derived about the program. This usually

includes a symbol table (among other things), which contain a piece of code for every production rule that is ran when the production rule is applied. Examples of code could be to type check an assignment, or check that a variable has been declared before it it used. Symbol tables are retained between multiple compilations (and also during debugging) so that they do not have to be re-constructed each time.

Things that go inside a symbol table include variable names, constants, function names, strings, text labels, and temporary variables for the compiler. The actual information stored about each entity varies according to what the entity actually is. Quick access is important, since the symbol table is frequently accessed by the compiler.

Obviously you could implement a symbol table in a variety of ways, but a hash table is most commonly used due to its O(1) lookup time (linked lists or binary trees are worse alternatives). In the course notes, bucket hashing is mentioned to resolve hash collisions, where a linked list is maintained for each hash value to store items with that hash key. Open addressing is also given, which is where the hash value is recalculated with an added constant each time there is a collision until a free space is found.

8 The Procedure Abstraction

The front end of the compiler is well understood and theoretically sound, while the second half is a more hotch-potch affair; it is here that clever engineering must by used to solve NP-hard problems and choose between diffucult trade offs.

Programming is all about abstraction, and one of the main tools in a programmer's abstraction toolbox is the procedure. Procedures let programmers define entry and exit points to a block of code, work within a set context, and have a clean external interface that can be used to call the code. However, there must be an agreement between different parts of the system as to how procedures are to work; how is memory laid out (and protected), how are arguments passed, where are procedures stored, etc. These concerns transcend those of the compiler, the Operating System, and to an extent, the architecture of the machine must all be designed with this in mind.

Sometimes each procedure is compiled individually, meaning that the compile time can be reduced (less code in each procedure means less complexity for the compiler, and recompilation needs only to concern the procedures that have been edited).

8.1 Linkage

Since procedures have such well defined control flow behaviour, a protocol exists for passing values and control at procedure calls and returns. This is called the linkage convention, and it ensures that procedures inherit a valid run-time environment and that they restore one for their parents.

The code to make a linkage happen is generated at compile time, but generated at runtime. To do this, the compiler must consider that local variables require storage during procedure execution, and it must set asside a region of memory for this (and other things) called an activation record $(AR)^5$. Things stored within the AR include:

- Parameters to the function
- Register save area
- Return value
- Return address
- Access link (helps with non-local access)

⁵They are called activation records in the notes, but are referred to as stack frames in most places I've seen.

- Caller's access link (to return to parent once complete)
- Temporary variables and local variables

This is how the whole process happens, and what each part is responsible for:

- Caller (pre call)
 - Allocate the AR
 - Store the parameters in the AR
 - Store the return address
 - Jump to the child
- Callee (prologue)
 - Save the caller's registers
 - Extend the AR for local data
 - Init local variables
 - Start execution
- Callee (epilogue)
 - Store the return value
 - Restore registers
 - Unextend the AR frame
 - Jump to return address
- Caller (post return)
 - Copy the return value
 - Deallocate the caller's AR
 - Restore the parameters

At runtime, the size of the code and static/global variables are known, but the size of the heap and stack varies. As such, the address space is organised like so:



Figure 3: The memory layout of a program. The heap and stack grow towards each other.

Variables are stored in the AR using offsets, but must be put on the heap if the variables themselves are of variable length. The activation records themselves will either be on the heap or the stack; if the procedure makes no calls, then the AR can be allocated statically, if it has a normal return value, then it can simply go on the stack as normal (which is good, because we don't need to worry much about deallocation), but if it may need to be active after exit (e.g. it returns a pointer pointing to a local variable), then it should be on the heap. The heap is least efficient, the stack is more efficient, but static allocation is most efficient.

Most variables are allocated at runtime, but static and global variables are usually allocated at compile time since their memory requirements are known inadvance. Variables can either be put on the stack or on the heap, and are done so according to whether they need to be preserved across procedures and if they have fixed sizes.

The compiler must consider things like storing variables at the start of word boundaries and re-ordering variables to maximise memory usage efficiency. The proximity and ordering of variables can also affect cache performance (they are likely to be fetched in the same cache load).

The compiler can also avoid some problems/overheads relating to procedure calling/linkage by inlining procedures (copying their code into another procedure with no call), though this is not possible in all cases due to register consumption, code size (too many inline functions means lots of repeated code), cache trashing etc.

9 Code generation & instruction selection

Here, we want to map the IR to low level machine instructions. The compiler also needs to make sure that the generated program stays within the resource limits of the CPU; different processors have different amounts of registers for example. Accessing data in registers is of course far more efficient than having to access data in memory, so intelligent use of registers (register allocation) is important for efficiency.

It is here that compilers apply tricks such as instruction reordering, where operations are re-ordered to hide latencies in other operations. Instruction selection, register allocation and instruction scheduling are all NP-complete problems that can be solved independently⁶.

We are using a very simple instruction set; LDR RX, ADDR/RY (with direct & indirect addressing), MOV RX, RY, ADD RX, RY, RZ, SHR RX, RY, VAL, STORE RX. However, instructions have different *latencies*⁷, which the compiler needs to take into account.

9.1 Generating code for arithmetic expressions

We can simply walk the IR in postorder and generate code with a procedure like this:

On most processors, the cost of multiplication might be several cycles, while shifting and adding is typically one or two cycles. In many instances, we can use shifting and addition instead of multiplications, so that we can multiply some constant integer with an unknown integer efficiently⁸.

9.2 Trading register usage with performance

Often, if we load values into registers first and compute after, then we can hide some of the memory latency. However, doing this uses up registers, of which we have a finite limit.

9.3 Array references

The compiler must always use the same storage scheme for arrays; either row-major order, column-major order or indirection orders (each element is a pointer to the actual array value).

9.4 Boolean & relational values

The compiler can use a treewalk generation like with arithmetic expressions...

⁶For example, instruction reordering can happen at a higher level than register allocation, for example whole program statements (that compile down to hundreds of instructions) can be reordered, but there is no equivalent for register allocation.

⁷The time (in cycles) between the instruction being issued and the time that the instruction results can be used

⁸Like in COMP27112

9.5 Control flow statements

10 Register allocation

The compiler must choose what registers to store data in while the program is executing. We assume that a three-address code has been generated, which uses an unlimited abount of *virtual registers*, but we want to map that onto the *physical registers* in the machine.

Henceforth, the task is to produce correct code that uses at most k registers, and minimises the number of loads and stores to memory (i.e. minimise register spilling). Ideally, we don't use backtracking so the compiler is fast.

A basic block is a segment of branch-free, straight line code. Local register allocation is within a basic block, and global allocation is within an entire procedure. Allocation is choosing what values to keep within registers, but assignment is choosing which specific registers get the values.

To determine how many registers we need in a given basic block, we must compute a set of *live ranges*, where the value of a variable is live between its definition and its last use. We must define a value maxlive to be the maximum number of live variables we can have in registers, and if the number of live ranges active at any point is greater than this value, then the registers must spill to memory.

A common top-down method of register allocation is the *frequency count algorithm*, where f registers are reserved for use when loading and saving values to memory, and so k-f registers are used for the program. The compiler looks at the k-f most commonly used values and stores them in registers, while using the f registers to spill the other values to memory.

Bottom up register allocation uses Best's algorithm, which is given as:

```
for (op, vr3, vr2, vr1) in operations
  ensure vr1 in r1
  ensure vr2 in r2
  if r1 not needed after this instruction
    free(r1)
  endif
  if r2 not needed after this instruction
    free(r2)
  endif
  allocate r3 for vr3
  emit op r3, r2, r1
```

This relies on two operations; *ensure* and *allocate*. The former assigns a virtual register to an actual register and ensures all occurances of that virtual register are tied to the real one. The latter allocates a free physical register, or finds the register that is being used farthest in the future, stores its value and returns it.

In practice, we often have multiple basic blocks being executed one after the other, and there are often opportunities for optimisation between them (e.g. some basic blocks use values already in the registers of others). If the control path between the basic blocks is nonlinear, then this may not be easy.

Rather than looking at local blocks of code in isolation, some approaches take the global program into account, and use generalised frequency counts as well as avoiding load and store operations between different basic blocks. Graph colouring can be used to assign registers if each colour is mapped onto a register.

11 Instruction Scheduling

The problem of instruction scheduling is that given some target code, the latencies for each operation on the target machine, we need to reorder operations in order to minimise the execution

It is important to remember that real processors have many different register types, and real compilers must factor this in when allocating. time of the code. This is made more complicated by the fact that modern processors usually have multiple functional units.

More specifically, we want to produce correct code (most importantly), minimise the number of wasted CPU cycles, avoid spilling registers and to operate efficiently (depending on your definition of efficiency).

Many CPU instructions have some delay latencies for execution, memory operations in particular. Modern processors issue several operations per cycle, and the execution time of each is often order dependent. In order to minimise waiting for load operations, we can move them back so that their data becomes available when it is needed, but this increases register pressure. The general idea is to do things that are potentially costly as early as possible so that the result is likely to be ready for when it is needed.

11.1 Instruction Scheduling - How To

Instruction Scheduling is NP-Complete, so we use heuristics to do it as best as we can.

- Build a precedence graph (of data dependencies)
- Compute a priority function for the nod esof the graph
- Use list scheduling to construct a schedule, one cycle at a time:
 - Have a queue of ready operations
 - At each cycle, choose an operation from the queue and execute it (and update the ready queue according to the dependencies in the precedence graph).

This is a greedy heuristic, and can (obviously) be modified. The priority function really determines what instructions are scheduled first among the ready instructions. One example priority function could be $p(node) = latency(node) + max(p(child\#1), p(child\#2), \dots, p(child\#n))$.

11.2 List scheduling

Ready	Scheduled	Active
6,4,1,3	6	6
1,4,3	1	6, 1
2,4,3	2	6, 2
4, 3	4	6,4
3,7	7	7,4

There are two distinct classes of list scheduling, forward list scheduling and backward list scheduling. Forward scheduling starts with the available operations and works forward in time, but backward scheduling starts with the leaves and works backwards in time (using latency to determine what is available). Often both are applied and whichever produces the best result is used.

The priority function has many variations, including prioritising the critical path, prioritising nodes with many immediate successors or total number of descendants, ignoring latency etc

11.3 Multiple functional units

When we have multiple functional units, we just run the list scheduling algorithm as normal, but have it schedule multiple operations (as many as we have functional units) per cycle.

11.4 Further issues

We want to identify highly used sections of code and spend more time optimising that (or schedule it as a single block). We can also schedule multiple loop iterations together (loop unrolling) so that we can reduce the overhead of the loop. Register allocation can restrict the choices for instruction scheduling (not enough registers), so optimising allocation to avoid spilling (loading and storing to memory) is beneficial. We also want to minimise the size of the code and the energy usage of the code.

12 Code optimisation

Code optimisation is very hard and could be a course on its own. The end goal is to improve the performance of the program within some constraints, for example, to reduce the size of the code, improve the performance, reduce memory bandwidth, reduce power consumption etc.

The issues are the legality (the meaning of the program must be preserved), benefit (we need to optimise for the average or common case, but determining what these cases are is often non-trivial) and compile time cost (there are a large number of possible optimisations, applying them all takes a long time).

Optimising transformations can be applied at multiple levels of abstractions; at the source code level (choosing the right algorithm), at the IR level (machine independent) and at the target code level (machine-dependent). Typical transformations include discovering and propagating constant values, removing unreachable code or redundant computations, or encoding a computation in some particularly efficient form.

We can classify optimisations by their scope (local (within a block), peephole (within a few blocks), loop level, global, inter-procedural (across a whole program or between procedures)), by machine information (such as machine dependent or independent operations) or by their effect on the structure of a program (e.g. re-ordering algebraic operations).

Examples of transformations applied for optimisation purposes include:

Name	Before	After
Computing com-	A[i, i * 2 + 10] = B[i, i * 2 +	tmp = i * 2 + 10
mon subexpres-	10] + 5	A[i, tmp] = B[i, tmp] + 5
sions		
Copy propaga-	t = i * 4	t = i * 4
tion	s = t	a[t] = a[t] + 5
	a[s] = a[s] + 5	
Constant propa-	N = 64	N = 64
${f gation}$	c = 2	c = 2
	for (i = 0; i < N; i++)	for $(i = 0; i < 64; i++)$
	a[i] = a[i] + c	a[i] = a[i] + 2
	tmp = 5 * 3 + 8 - 12 / 2	tmp = 17
Dead code elimi-	if(3>7)	// Nothing
nation		
Reduction in	y = x * 2 + x * 1024	y = x + x + (x << 10)
strength		

12.1 Loop optimisation

Loops are an important target for optimisation, mainly because much of the complexity inherent in programs is derived from looping control structures. Three optimisations are mentioned in the course:

Loop-invariant code-motion:

If a constant expression is computed inside a loop, move the computation outside the loop so that it is only done once.

Loop interchange:

Swap the variables that are being altered in two nested loops so that the order of access matches the order that the data items are in memory. The course notes describe the aim as being to achieve 'unit stride' accesses, i.e. so that each access is one sequential array stride from the last.

Strip mining:

Strip mining transforms a singly nested loop into a double nested one. The outer loop steps through the index in blocks of some size, and the inner loop steps through each block. The block size of the outer loop is determined by some characteristic of the target machine, such as the vector register length or the size of one cache line.

Loop unrolling:

The idea behind loop unrolling is to process multiple iterations of the loop inside one iteration to reduce the overhead of looping and perhaps make better use of SIMD instructions or to make scheduling easier. For example:

```
for (int i = 0; i < 12; i++) x[i] += 1;

Could go to:
    for (int i = 0; i < 12; i+=4) {
        x[i] += 1
        x[i+1] += 1
        x[i+2] += 1
        x[i+3] += 1
    }

Or even:
    // Add8 does four 8-bit add operations in one instruction for (int i = 0; i < 12; i+=4) add8(x[i], 1);</pre>
```

If the number of loop items is not divisible by the unroll length (four in our case), then an additional loop may be added after the main loop to complete the last few iterations.

Asserting that these optimisations are legal is a hard problem. A model is often used to represent the loop control logic, by which logical conclusions can be drawn. The main issue is data dependence; in order to do things like switching an inner and outer loop, we need to ensure that the end result is the same if the loops interact with each other.