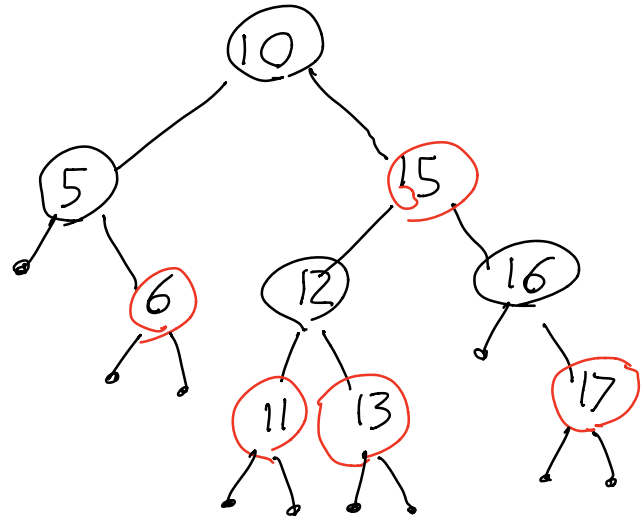
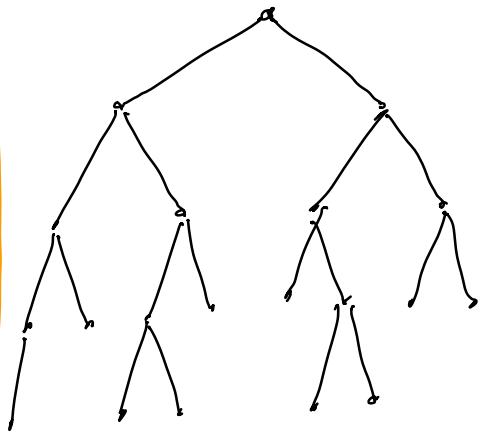
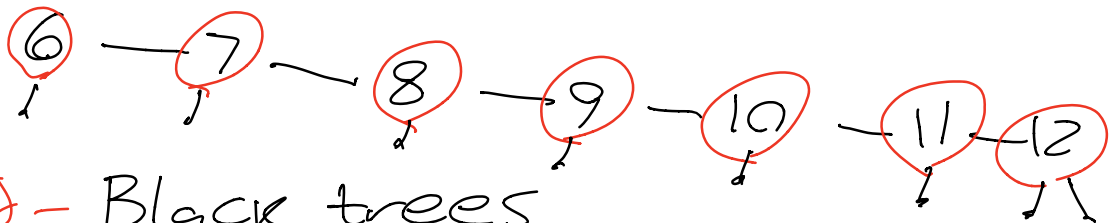


## Final Review: Balanced Trees



$n$  nodes

$$d \leq \log_2(n) + 1$$



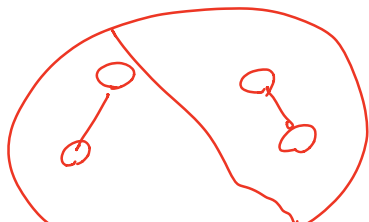
## Red-Black trees

Global Invariant:

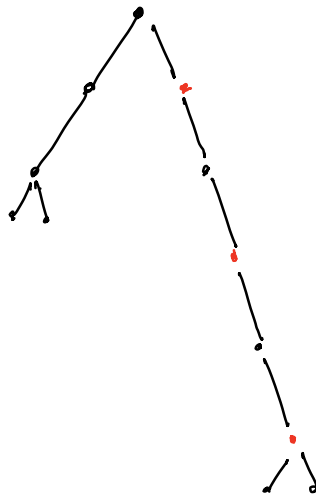
Every root-leaf path has  
same # of black nodes.

Local Invariant:

No two red nodes can have  
parent-child relationship.

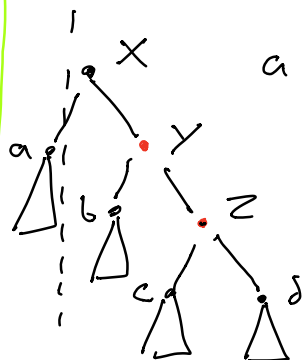


n nodes  
 $d \leq 2 \log_2(n)$



4 black nodes  
 3 red nodes  
 6 black nodes  
 6-1 red nodes  
 $2b-1$

Balance Operation



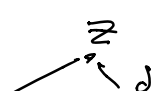
$a < b < c < d$

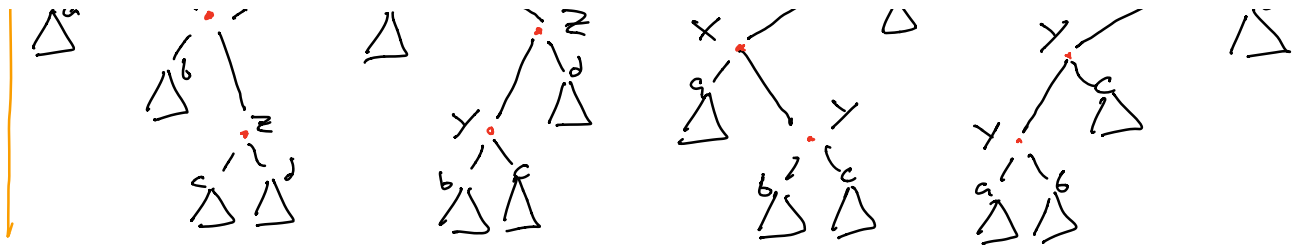


$x < y < z$

$x < y < z$

4 cases





Exercise:

insert 14 into

