## Chapter 3 Assessment

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Directions: Strike-through false statements using ~~strikethrough~~. Bold all true statements and answers. By entering your name on the document you turn in, you are acknowledging that the work in the document is entirely your own unless specified otherwise in the document. Compile your document using Knit PDF and turn in a stapled hardcopy no later than 10am, Friday March 18, 2016. Create a directory named ChapterThreeAssessment inside your private class repository. Store this file inside the ChapterThreeAssessment directory. Use inline R expressions rather than hardcoding your numeric answers. Hand write the eight digit SHA for the document you turn in next to your name.

- 1. Why is linear regression important to understand? Select all that apply:
- The linear model is often correct.
- Linear regression is very extensible and can be used to capture nonlinear effects.
- Simple methods can outperform more complex ones if the data are noisy.
- Understanding simpler methods sheds light on more complex ones.
- 2. You may want to reread the paragraph on confidence intervals on page 66 of the textbook before trying this question (the distinctions are subtle). Which of the following are true statements? Select all that apply:
- A 95% confidence interval formula is a random interval that is expected to contain the true parameter 95% of the time.
- "The true parameter is a random value that has 95% chance of falling in the 95% confidence interval."
- "I perform a linear regression and get a 95% confidence interval from 0.4 to 0.5. There is a 95% probability that the true parameter is between 0.4 and 0.5."
- The true parameter (unknown to me) is 0.5. If I repeatedly sample data and construct 95% confidence intervals, the intervals will contain 0.5 approximately 95% of the time.

- 3. We run a linear regression and the slope estimate is 0.5 with estimated standard error of 0.2. What is the largest value of b for which we would NOT reject the null hypothesis that  $\beta_1 = b$ ?
- a. Assume a normal approximation to the t distribution, and that we are using the 5% significance level for a two-sided test; use two significant digits of accuracy.

```
StdE <- 0.2
b_hat <- 0.5
z <- qnorm(.975) #get z-score
b_lower <- b_hat - z*StdE
b_upper <- b_hat + z*StdE
b_upper <- round(b_upper,digits = 2) #round to 2 digits</pre>
```

The largest value of b for which we would not reject the null hypothesis that  $\beta_1 = b$  is b = 0.89

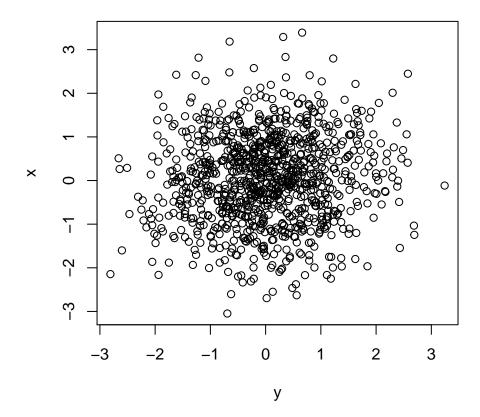
b. Use a t distribution with 10 degrees of freedom, and assume that we are using the 5% significance level for a two-sided test; use two significant digits of accuracy.

```
dfr <- 10
t <- qt(0.95,df=dfr ) #get t-score
b_upper <- b_hat + t*StdE
b_upper <- round(b_upper, digits = 2) #round to 2 digits</pre>
```

The largest value of b for which we would not reject the null hypothesis that  $\beta_1 = b$  is b = 0.86

- 4. Which of the following indicates a fairly strong relationship between X and Y?
- $R^2 = 0.9$
- The p-value for the null hypothesis  $\beta_1 = 0$  is 0.0001.
- The t-statistic for the null hypothesis  $\beta_1 = 0$  is 30.

```
set.seed(123)
y <- rnorm(1000)
x <- rnorm(1000)
plot(x~y)</pre>
```



mod <- lm(y~x)
summary(mod)</pre>

Call:

 $lm(formula = y \sim x)$ 

Residuals:

Min 1Q Median 3Q Max -2.7168 -0.6290 -0.0060 0.6451 3.2383

Coefficients:

Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.01252 0.03129 0.400 0.68909
x 0.08494 0.03097 2.742 0.00621 \*\*

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9885 on 998 degrees of freedom Multiple R-squared: 0.007479, Adjusted R-squared: 0.006484

F-statistic: 7.52 on 1 and 998 DF, p-value: 0.006211

## 5. Given the following:

```
site <- "http://www-bcf.usc.edu/~gareth/ISL/Credit.csv"</pre>
Credit <- read.csv(file = site)</pre>
str(Credit)
'data.frame': 400 obs. of 12 variables:
$ X
        : int 12345678910...
$ Income : num 14.9 106 104.6 148.9 55.9 ...
$ Limit : int 3606 6645 7075 9504 4897 8047 3388 7114 3300 6819 ...
$ Rating : int 283 483 514 681 357 569 259 512 266 491 ...
$ Cards
           : int 2343242253...
           : int 34 82 71 36 68 77 37 87 66 41 ...
$ Education: int 11 15 11 11 16 10 12 9 13 19 ...
$ Gender : Factor w/ 2 levels "Female", " Male": 2 1 2 1 2 2 1 2 1 1 ...
\ Student \ : Factor \ w/ 2 levels "No", "Yes": 1 2 1 1 1 1 1 1 1 2 ...
\ Married : Factor w/ 2 levels "No", "Yes": 2 2 1 1 2 1 1 1 1 2 ...
 $ Ethnicity: Factor w/ 3 levels "African American",..: 3 2 2 2 3 3 1 2 3 1 ...
$ Balance : int 333 903 580 964 331 1151 203 872 279 1350 ...
ModEthnic <- lm(Balance ~ Ethnicity, data = Credit)</pre>
summary(ModEthnic)
Call:
lm(formula = Balance ~ Ethnicity, data = Credit)
Residuals:
            1Q Median
                            3Q
   Min
                                   Max
-531.00 -457.08 -63.25 339.25 1480.50
Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
(Intercept)
                    531.00
                                46.32 11.464
                                                <2e-16 ***
EthnicityAsian
                    -18.69
                                65.02 -0.287
                                                 0.774
EthnicityCaucasian -12.50
                                56.68 -0.221
                                                 0.826
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 460.9 on 397 degrees of freedom
Multiple R-squared: 0.0002188, Adjusted R-squared: -0.004818
F-statistic: 0.04344 on 2 and 397 DF, p-value: 0.9575
b0 <- coef(summary(ModEthnic))[1, 1]</pre>
b1 <- coef(summary(ModEthnic))[2, 1]</pre>
b2 <- coef(summary(ModEthnic))[3, 1]
c(b0, b1, b2)
```

[1] 531.00000 -18.68627 -12.50251

```
AsianPredB <- b0 + b1 #the predicted balance for an Asian in the data set
AsianPredB <- round(AsianPredB, digits = 2)
AfAmPredB <- round(b0, digits = 2) #the predicted balance for an African American in the data set
```

a. According to the balance vs ethnicity model (ModEthnic), what is the predicted balance for an Asian in the data set? (within 0.01 accuracy)

According to the balance vs ethnicity model (ModEthnic), the predicted balance for an Asian in the data set is \$512.31.

b. What is the predicted balance for an African American? (within .01 accuracy)

According to the balance vs ethnicity model (ModEthnic), the predicted balance for an African American in the data set is \$531.

c. Construct a 90% confidence interval for the average credit card balance for Asians.

```
AsC <- predict(ModEthnic, newdata = data.frame(Ethnicity = "Asian"),
  interval = "confidence", level = 0.9)</pre>
```

A 90% confidence interval for Asians credit card balance is \$437.0794784 to \$587.5479725.

d. Construct a 92% prediction interval for Joe's (who is African American) credit card balance.

```
AfAmC <- predict(ModEthnic, newdata = data.frame(Ethnicity = "African American"),
   interval = "prediction", level = 0.92)</pre>
```

A 92% prediction interval for Joe's (who is African American) credit card balance is \$-281.975745 to \$1343.975745.

6. Given the following:

```
mod <- lm(Rating ~ poly(Limit, 2, raw = TRUE) + poly(Cards, 2, raw = TRUE) +
           Married + Student + Education, data = Credit)
summary(mod)
Call:
lm(formula = Rating ~ poly(Limit, 2, raw = TRUE) + poly(Cards,
   2, raw = TRUE) + Married + Student + Education, data = Credit)
Residuals:
    Min
              1Q
                   Median
                                3Q
                                        Max
-27.8814
        -6.8317 -0.3358
                            6.5136 25.9925
Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
(Intercept)
                            2.579e+01 3.816e+00
                                                 6.760 5.01e-11 ***
poly(Limit, 2, raw = TRUE)1 6.529e-02 7.506e-04 86.984 < 2e-16 ***
poly(Limit, 2, raw = TRUE)2 1.320e-07 6.297e-08
                                                 2.096 0.0368 *
poly(Cards, 2, raw = TRUE)1 7.615e+00 1.301e+00
                                                 5.855 1.01e-08 ***
poly(Cards, 2, raw = TRUE)2 -3.972e-01 1.783e-01 -2.228 0.0264 *
MarriedYes
                            2.295e+00 1.043e+00 2.199 0.0285 *
StudentYes
                            3.159e+00 1.693e+00
                                                1.866
                                                          0.0628 .
                           -2.774e-01 1.627e-01 -1.705 0.0889 .
Education
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 10.09 on 392 degrees of freedom
                               Adjusted R-squared: 0.9957
Multiple R-squared: 0.9958,
F-statistic: 1.334e+04 on 7 and 392 DF, p-value: < 2.2e-16
```

a. Use mod to predict the Rating for an individual that has a credit card limit of \$6,000, has 4 credit cards, is married, and is not a student, and has an undergraduate degree (Education = 16).

```
#necessary variables's values
cN < -4
cLimit <- 6000
edu <- 16
#necessary coefficients and intercept for the variables of the predicted model
C <- coef(summary(mod))[1, 1]</pre>
1C1 <- coef(summary(mod))[2, 1]</pre>
1C2 <- coef(summary(mod))[3, 1]</pre>
CC1 <- coef(summary(mod))[4, 1]</pre>
CC2 <- coef(summary(mod))[5, 1]</pre>
MYC <- coef(summary(mod))[6, 1]
SYC <- coef(summary(mod))[7, 1]
EC <- coef(summary(mod))[8, 1]</pre>
#predict the rating by using the model "mod"
ratingR <- C + cLimit*lC1 + (cLimit^2)*lC2 + cN*CC1 + (cN^2)*CC2 + (1)*MYC + (0)*SYC
ratingR
```

The Rating for an individual that has a credit card limit of \$6,000, has 4 credit cards, is married, and is not a student, and has an undergraduate degree is 448.691642.

b. Use mod to predict the Rating for an individual that has a credit card limit of \$12,000, has 2 credit cards, is married, is not a student, and has an eighth grade education (Education = 8).

```
#necessary variables's values
cN < -2
cLimit <- 12000
edu <- 8
#necessary coefficients and intercepts for the variables of the predicted model
C <- coef(summary(mod))[1, 1]</pre>
1C1 <- coef(summary(mod))[2, 1]</pre>
1C2 <- coef(summary(mod))[3, 1]</pre>
CC1 <- coef(summary(mod))[4, 1]</pre>
CC2 <- coef(summary(mod))[5, 1]</pre>
MYC <- coef(summary(mod))[6, 1]
SYC <- coef(summary(mod))[7, 1]
EC <- coef(summary(mod))[8, 1]</pre>
#predict the rating by using the model "mod"
ratingR <- C + cLimit*lC1 + (cLimit^2)*lC2 + cN*CC1 + (cN^2)*CC2 + (1)*MYC + (0)*SYC
ratingR
```

[1] 844.2286

The Rating for an individual that has a credit card limit of \$12,000, has 2 credit cards, is married, and is not a student, and has an eighth grade education is 844.2286339.

c. Construct and interpret a 90% confidence interval for  $\beta_5$  (a married person).

```
#Stephanie helped me with the code of this one
CreditMY <- subset(Credit, Credit$Married == "Yes")
tval <- t.test(CreditMY$Rating, conf.level = .90, alternative = "two.sided")
lowerMY <- tval$conf.int[1]
upperMY <- tval$conf.int[2]</pre>
```

We are 90% confident that the true parameter of Rating for a married person would fall between 342.801888 and 376.1123977.

## 7. Given the following:

```
site <- "http://www-bcf.usc.edu/~gareth/ISL/Advertising.csv"</pre>
Advertising <- read.csv(file = site)
str(Advertising)
'data.frame':
               200 obs. of 5 variables:
          : int 1 2 3 4 5 6 7 8 9 10 ...
$ X
$ TV
           : num 230.1 44.5 17.2 151.5 180.8 ...
$ Radio
         : num 37.8 39.3 45.9 41.3 10.8 48.9 32.8 19.6 2.1 2.6 ...
$ Newspaper: num 69.2 45.1 69.3 58.5 58.4 75 23.5 11.6 1 21.2 ...
         : num 22.1 10.4 9.3 18.5 12.9 7.2 11.8 13.2 4.8 10.6 ...
$ Sales
modSales <- lm(Sales ~ TV + Radio + TV:Radio, data = Advertising)</pre>
summary(modSales)
Call:
lm(formula = Sales ~ TV + Radio + TV:Radio, data = Advertising)
Residuals:
   Min
            1Q Median
                                   Max
-6.3366 -0.4028 0.1831 0.5948 1.5246
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 6.750e+00 2.479e-01 27.233
                                         <2e-16 ***
TV
           1.910e-02 1.504e-03 12.699
                                          <2e-16 ***
Radio
           2.886e-02 8.905e-03 3.241
                                          0.0014 **
TV:Radio 1.086e-03 5.242e-05 20.727
                                          <2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.9435 on 196 degrees of freedom
Multiple R-squared: 0.9678,
                              Adjusted R-squared: 0.9673
F-statistic: 1963 on 3 and 196 DF, p-value: < 2.2e-16
coef(modSales)
                             Radio
                                      TV:Radio
(Intercept)
                    TV
6.750220203\ 0.019101074\ 0.028860340\ 0.001086495
```

a. According to the model for sales vs TV interacted with radio (modSales), what is the effect of an additional 1 unit of radio advertising if TV = 25? (with 4 decimal accuracy)

```
TVN <- 25
RadioN <- 1
RadioNC <- coef(modSales)[3] #coefficient of Radio variable for the model for sales vs TV interacted w
TVvsRC <- coef(modSales)[4] #coefficient of TV interacted with Radio variable for the model for sales

Effect <- RadioN * RadioNC + TVN * RadioN * TVvsRC

Effect <- round(Effect, digits = 4) #round to 4 digits
```

According to the model for sales vs TV interacted with radio (modSales), the effect of an additional 1 unit of radio advertising if TV = 25 is 0.056.

b. What if TV = 300? (with 4 decimal accuracy)

```
TVN <- 300

RadioN <- 1

RadioNC <- coef(modSales)[3] #coefficient of Radio variable for the model for sales vs TV interacted w

TVvsRC <- coef(modSales)[4] #coefficient of TV interacted with Radio variable for the model for sales

Effect <- RadioN * RadioNC + TVN * RadioN * TVvsRC

Effect <- round(Effect, digits = 4) #round to 4 digits
```

According to the model for sales vs TV interacted with radio (modSales), the effect of an additional 1 unit of radio advertising if TV = 300 is 0.3548.

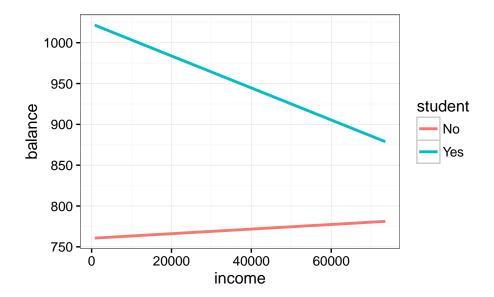
8. What is the difference between  $lm(y \sim x*z)$  and  $lm(y \sim I(x*z))$ , when x and z are both numeric variables?

#Kevin helps me understand the solutions for this problem

- The first one includes an interaction term between x and z, whereas the second uses the product of x and z as a predictor in the model.
- The second one includes an interaction term between **x** and **z**, whereas the first uses the product of **x** and **z** as a predictor in the model.
- The first includes only an interaction term for **x** and **z**, while the second includes both interaction effects and main effects.
- The second includes only an interaction term for x and z, while the first includes both interaction effects and main effects.

9. Given the following model:

```
modBalance <- lm(balance ~ student + income + student:income, data = Default)
library(ggplot2)
ggplot(data = Default, aes(x = income, y = balance, color = student)) +
   geom_smooth(method = "lm", se = FALSE, fullrange = TRUE) +
   theme_bw()</pre>
```



Which of the following statements are true?

- In the modBalance model, the estimate of  $\beta_3$  is negative.
- One advantage of using linear models is that the true regression function is often linear.
- If the F statistic is significant, all of the predictors have statistically significant effects.
- In a linear regression with several variables, a variable has a positive regression coefficient if and only if its correlation with the response is positive.